Digital Image Processing

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Purpose of Digital Image Processing

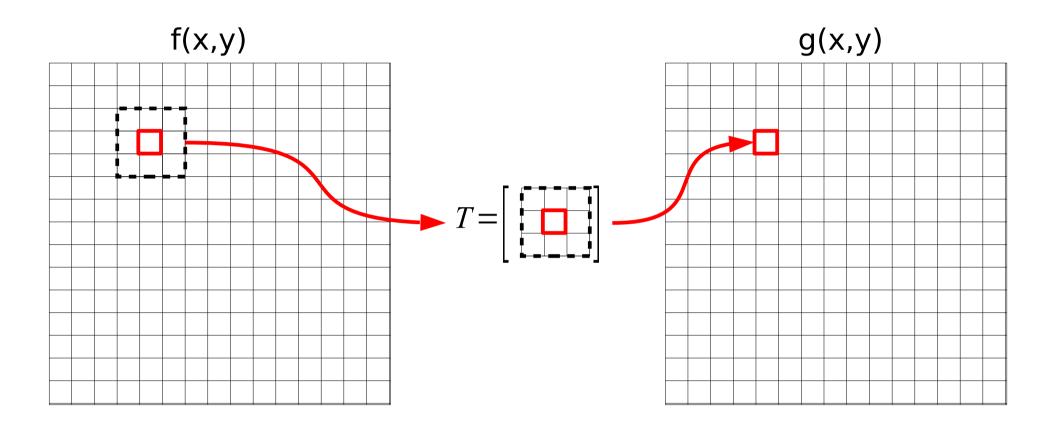
Image restoration: Improving *objective* image quality e.g. noise suppression







Sliding Window



- Operator T takes into account only local information
- Result in g is based on pixel intensity and intensities of neighbours
 - → 'Filter size' refers to size of neighbourhood (e.g. 3x3 pixels)

Convolution

$$g(\alpha, \beta) = \sum_{x=1}^{N} \sum_{y=1}^{M} f(x, y) \cdot h(x - \alpha, y - \beta)$$

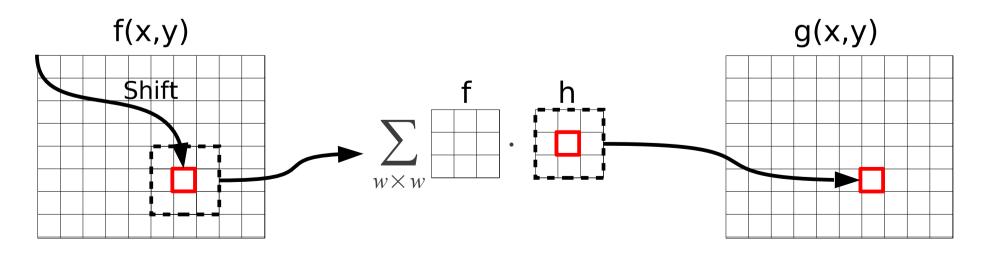
1. Flip filter kernel (about the filter centre)







2. Shift (re-centre), Multiply and Integrate



Convolution

Filter consists of coefficients and has a centre:

$$h(r,s) = \begin{pmatrix} h(-1,-1) & h(0,-1) & h(1,-1) \\ h(-1,0) & h(0,0) & h(1,0) \\ h(-1,1) & h(0,1) & h(1,1) \end{pmatrix}$$

Linear filters are applied by convolution:

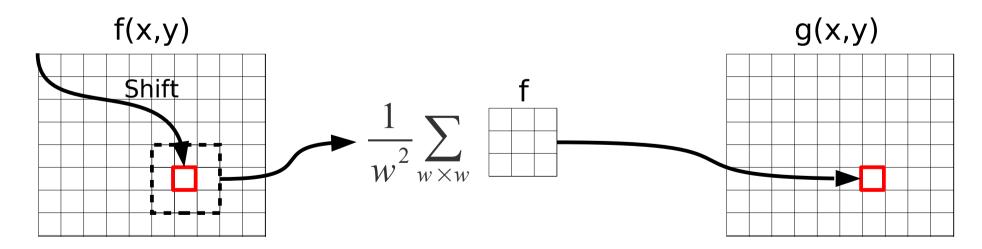
$$g(x,y) = (f*h)(x,y) =$$

$$\sum_{3\times3} \begin{cases} f(x-1,y-1)h(1,1) & f(x,y-1)h(0,1) & f(x+1,y-1)h(-1,1) \\ f(x-1,y)h(1,0) & f(x,y)h(0,0) & f(x+1,y)h(-1,0) \\ f(x-1,y+1)h(1,-1) & f(x,y+1)h(0,-1) & f(x+1,y+1)h(-1,-1) \end{cases}$$

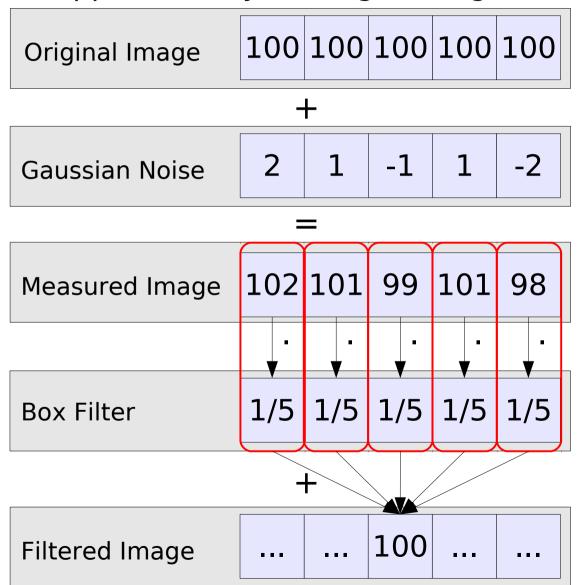
Example: Noise Suppression by Moving Average Filter

$$h(x,y) = \frac{1}{w^2} \begin{pmatrix} 1 & 1 & 1 & \dots \\ 1 & 1 & 1 & \dots \\ 1 & 1 & 1 & \dots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix}$$
 (w x w Filter Kernel)

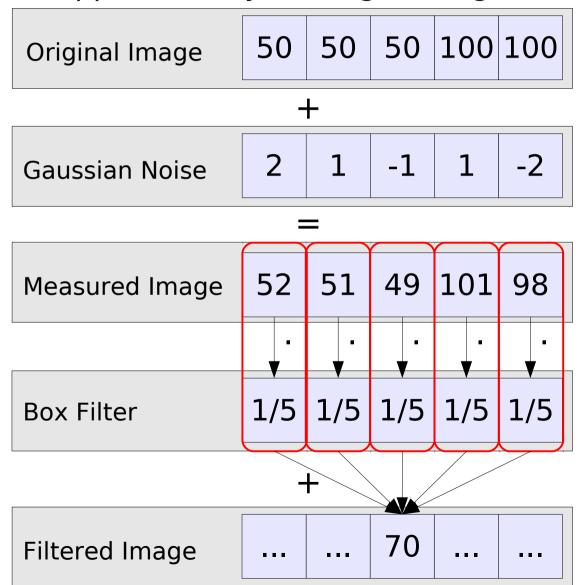
Each pixel intensity is replaced by the local average...



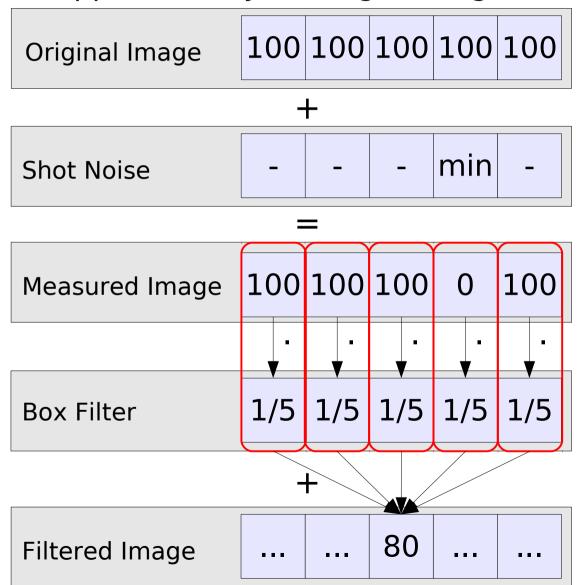
Example: Noise Suppression by Moving Average Filter



Example: Noise Suppression by Moving Average Filter



Example: Noise Suppression by Moving Average Filter

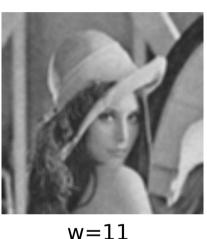


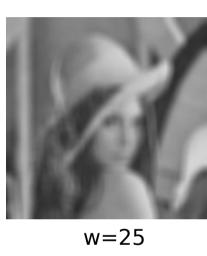
Example: Noise Suppression by Moving Average Filter

Gaussian Noise

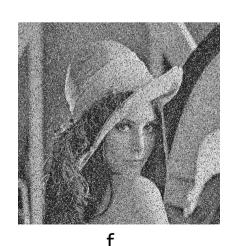








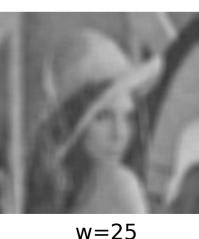
Shot Noise







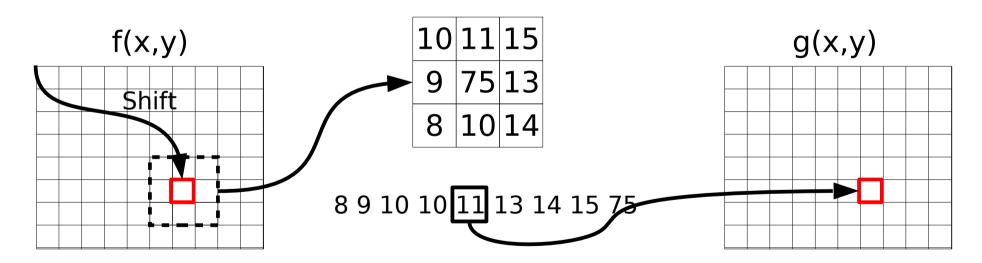
w = 11





Example: Noise Suppression by Median Filter (NOTE: No convolution)

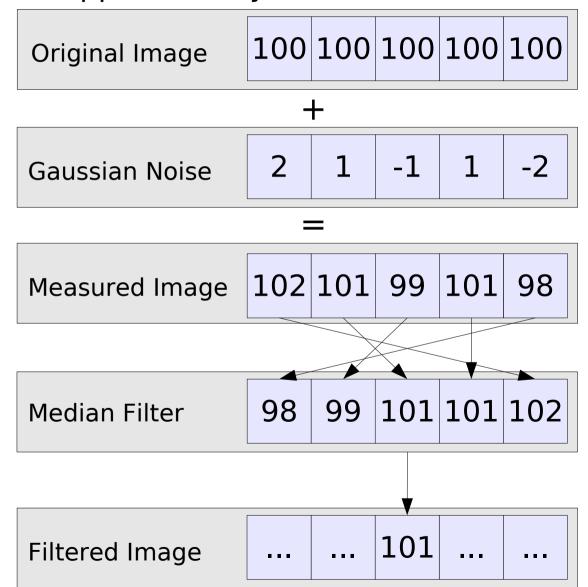
- 1. Consider intensities in a local NxN window
- 2. Sort intensities
- 3. Select middle value (median) as result
- Each pixel intensity is replaced by the local median...



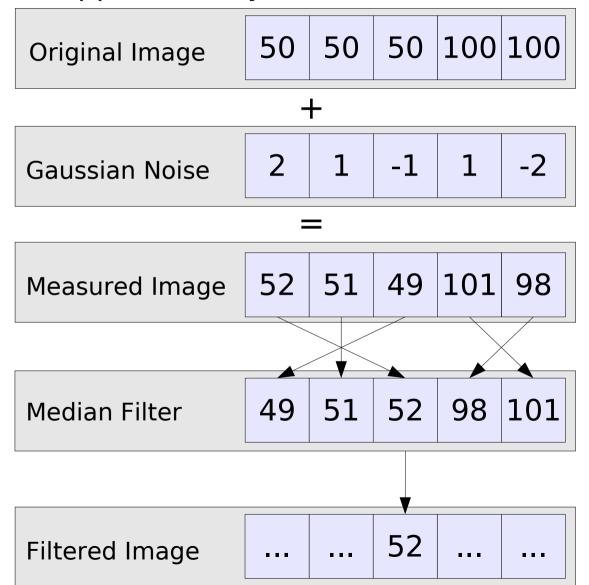
- Effectively removes outliers
- Preserves sufficiently large (>> wxw) image structures



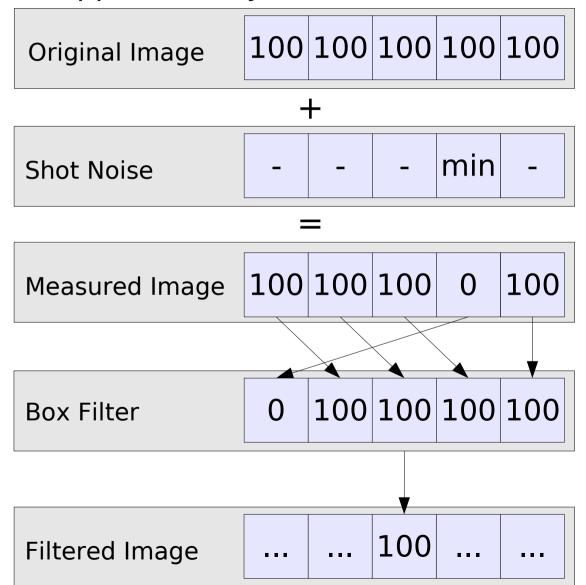
Example: Noise Suppression by Median Filter



Example: Noise Suppression by Median Filter



Example: Noise Suppression by Median Filter



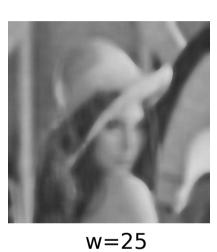
Example: Noise Suppression by Median Filter

Gaussian Noise

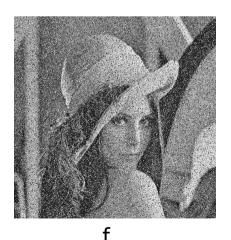








Shot Noise





w=5

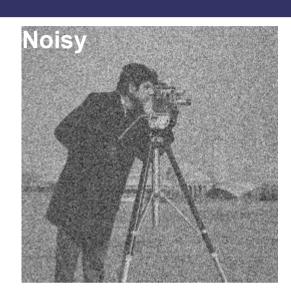






Noise Suppression vs. Resolution

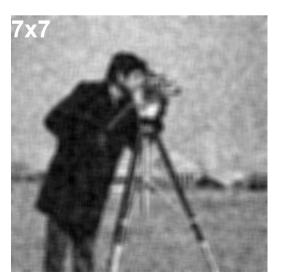




Moving average filtering









Adaptive Smoothing

Moving Average Filter:
$$m_k(x, y) = \begin{cases} 1/k^2 & -k/2 \le x, y < k/2 \\ 0 & \text{otherwise} \end{cases}$$

Modified Filtering:

$$g_n(x,y) = \begin{cases} (f * m_n)(x,y) & |(f * m_3)(x,y) - (f * m_n)(x,y)| \le T \\ (f * m_3)(x,y) & \text{otherwise} \end{cases}$$

- Average unless filtered version departs too far from original
 - → Largest discrepancies expected near strong edges
 - → Threshold T and size *n* must be specified by the user!

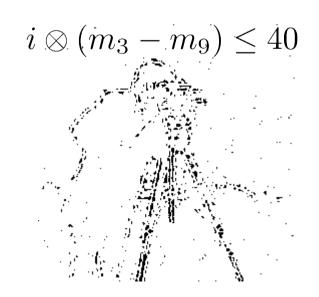


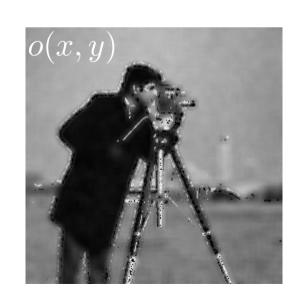
Edge Preservation















Excursus: Bilateral Filter

Spatial Weight:

$$h_{spat}(r, s) = \frac{1}{2 \pi \sigma^2} \exp \left(-\frac{(r - \mu)^2 + (s - \mu)^2}{2 \sigma^2} \right)$$

Radiometric Weight:

$$h_{rad}(p,q) = \frac{1}{2\pi\sigma_p^2} \exp\left(-\frac{(p-q)^2}{2\sigma_p^2}\right)$$

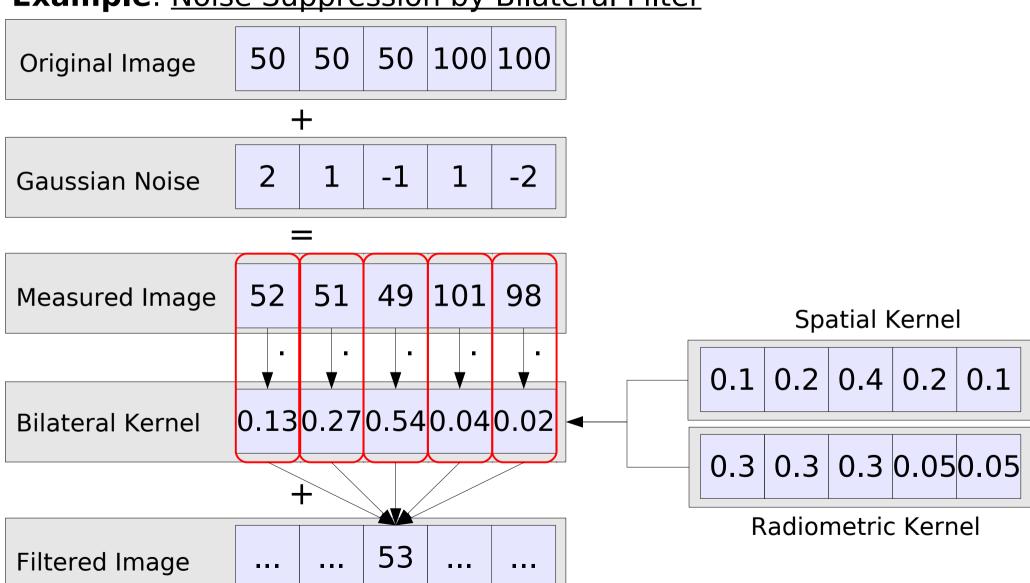
Combined:

$$h(r, s, f(x, y)) = h_{spat}(r, s) \cdot h_{rad}(f(x, y))$$

Output:

$$g(\vec{x}) = \frac{1}{Z(\vec{x})} \sum_{\vec{x}' \in N(\vec{x})} \exp\left(-\frac{(\vec{x}' - \vec{x})^2}{2 \cdot \sigma_1^2}\right) \cdot \exp\left(-\frac{(f(\vec{x}') - f(\vec{x}))^2}{2 \cdot \sigma_2^2}\right) \cdot f(\vec{x}')$$

Example: Noise Suppression by Bilateral Filter





Excursus: Bilateral Filter

$$g(\vec{x}) = \frac{1}{Z(\vec{x})} \sum_{\vec{x}' \in \partial \vec{x}} \exp\left(-\frac{(\vec{x}' - \vec{x})^2}{2 \cdot \sigma_1^2}\right) \cdot \exp\left(-\frac{(f(\vec{x}') - f(\vec{x}))^2}{2 \cdot \sigma_2^2}\right) \cdot f(\vec{x})$$

Excursus: Bilateral Filter



Original

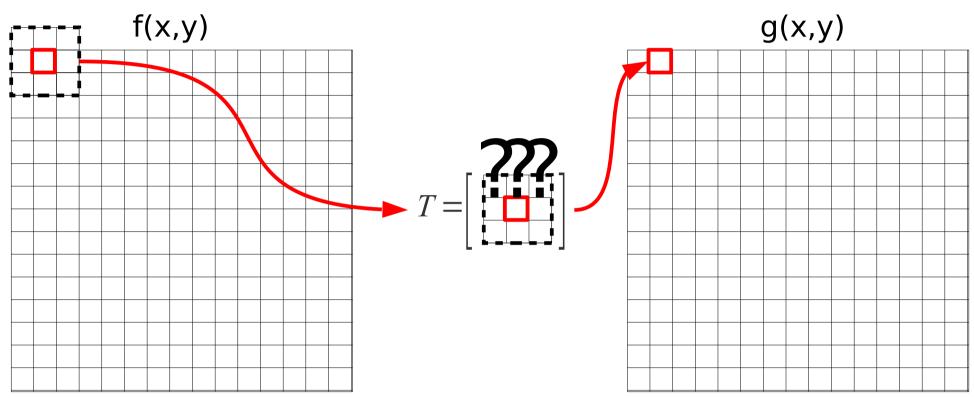


Filter Result

C. Tomasi and R. Manduchi, "Bilateral Filtering for Gray and Color Images", Proceedings of the 1998 IEEE International Conference on Computer Vision, Bombay, India



Border handling



- Problem: Unknown image values beyond image borders
- Possible solution
 - "Shrink" output image using only available information
 - Adapt kernel shape
 - Use "default" values (0, 255)
 - Use other image information (e.g. mirroring, wrapping)



2. Exercise - Noise Suppression

- → Part I Theoretical
- → Part II Practical
 - Moving Average Filter
 - Median Filter
 - Adaptive Smoothing
 - → OPTIONAL:
 - Bilateral Filtering

2. Exercise - Theory

1. When should the median filter be applied to an image and when the moving average filter?

2. Explain your answer to question 1.

3. Is there a **general** better choice than the moving average filter?

4. Explain your answer to question 3.

2. Exercise - Given Functions

```
FILE: Dip2.cpp/h
void Dip2::generateNoisyImages(string fname)
```

- → Applies two noise models to original image
- → Saves both images (noiseType_1.jpg and noiseType_2.jpg)



2. Exercise - Given Functions

```
FILE: Dip2.cpp
void Dip2::run(void) {
    ...
    Mat noise1 = imread("noiseType_1.jpg", 0);
    Mat noise2 = imread("noiseType_2.jpg", 0);
    ...
    Mat restorated1 = noiseReduction(noise1, "", 1);
    Mat restorated2 = noiseReduction(noise2, "", 1);
    ...
}
```

2. Exercise - Given Functions

Parameter:

→ src : noisy source image

→ method : defines method to be used

→ median, average, adaptive, bilateral

→ kSize : Kernel size

→ param : adaptive smoothing: threshold

bilateral filter: std-dev of radiometric kernel

→ return : noised reduced output image

Calls

→ averageFilter(...), medianFilter(...), adaptiveFilter(...), or bilateralFilter(...)

2. Exercise - To Do

Mat Dip2::spatialConvolution(Mat& src, Mat& kernel)

- Parameter:
 - → **src** : source image
 - → kernel : kernel of the convolution
 - → return : output image
- Applies convolution in spatial domain
- One method of border handling: size(src) == size(return)
- Do NOT use convolution functions of OpenCV

2. Exercise - To Do

```
Mat Dip2::averageFilter(Mat& src, int kSize)
```

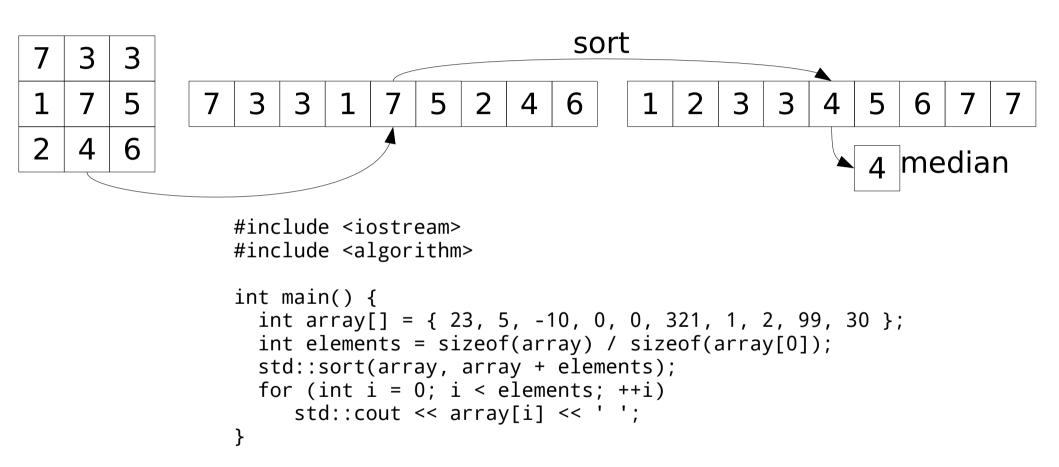
- Parameter:
 - → src : noisy source image
 - → kSize : Kernel size
 - → return : output image
- Uses convolution to calculate local average
- Calls spatialConvolution(...)

```
Mat Dip2::medianFilter(Mat& src, int kSize)
```

- Parameter:
 - → src : noisy source image
 - → kSize : Kernel size
 - → return : output image
- Applies local median filtering



2. Exercise - Median



2. Exercise - To Do

Mat adaptiveFilter (Mat& src, int kSize, double threshold)

- Parameter:
 - → src : noisy source image
 - → kSize : kernel size
 - → threshold : smooth only if difference is below this value
 - → return : output image
- Uses moving average filter, but preserves edges
- Calls averageFilter(...)

2. Exercise - Optional

Mat bilateralFilter(Mat& src, int kSize, double sigma)

Parameter:

→ **src** : noisy source image

→ kSize : size of spatial kernel

→ Calculate standard-deviation accordingly

→ sigma : Standard-Deviation of radiometric kernel

→ return : output image

Implements bilateral filter

Deadline: 22nd May