

Class: 10  
Time : 3hrs

F.M.: 75

Subject: O.Math

Attempt all the questions

Group 'A'

[5 × 2 = 10]

1. a) What is the y-intercept of  $y = \sin x$  ?

b) Which range of the functions between  $f$  and  $g$  is equal to the range of the functions  $\text{gof}(x)$  ?

2.a) Define composite function with an example .

b) If a polynomial  $q(x)$  is divided by  $(x-b)$ , what will be its remainder?

3.a) If  $f(x) = q(x) \times d(x) + r(x)$ , write the meaning of each term.

b) Define factor theorem.

4.a) State the meaning of each term in the formula :  $t_n = a + (n-1)d$ .

b) Write the sum of  $n$  terms of arithmetic sequence whose first term 'P' and the last term 'q' .

5.a) What is the geometric mean between two positive numbers  $m$  and  $n$  ?  
Write it .

b) Write the meaning of each term in the formula  $s_n = \frac{a(r^n - 1)}{r - 1}$

Group B (4x4= 16)

6. a) If  $f = \{(3,4), (4,5), (5,6)\}$  and  $g = \{(2,3), (3,4), (4,5)\}$  express  $\text{fog}$  in an ordered pair form.

b) If  $f(x) = 3x+7$ , Find the value of  $\text{ff}(2)$  .

7. a) If  $f: x \rightarrow 3x+p$  and  $\text{ff}(2)=12$ , find the value of  $P$ .

b) If  $2x^3 - 6x^2 + 3 = (-2)xQ(x) + R$ , Find  $Q(x)$  and  $R$  using synthetic division method.

8.a) If  $(x-7)$  is a factor of polynomial  $f(x) = x^3 - 9x^2 + (k+1)x - 7$ , find the value of  $k$ .

b) How many terms are there in the series  $5+9+13+\dots+77$ ? find .

9.a) If  $5, p, q, 11$  is an arithmetic sequence .Find the values of  $x$  and  $y$  .

b) If  $a+2$ ,  $a+8$  and  $17+a$  are in geometric sequence, find the value of  $a$ .

Group C 11x3=33

10 . If  $f(x) = 3x+4$  and  $g(x) = 2x+2$  then prove that  $(\text{fog})(x) = (\text{gof})(x)$

11. If  $f(x) = 3x-2$  and  $\text{fog}(x) = 6x-2$  then find value of  $x$  such that  $\text{gof}(x) = 8$ .

12. If  $f(x) = 2x-5$ ,  $g(x) = 3x+1$  are two functions, find  $gf^{-1}(5)$

13. If  $f(x) = 2x-5$ ,  $g(x) = \frac{3x+5}{2}$  and  $\text{ff}(x) = g^{-1}(x)$ , then find the value of  $x$  .

14. Solve :  $x^3 - 4x^2 - 7x + 10 = 0$

15. Find the value of  $n$  where  $y = x^3 - 4x^2 + x + 8$  and  $y=2$

16. The third term and the 13th term of an arithmetic sequence are  $-40$  and  $0$  respectively , what is the 28th term of the sequence?

17. If the fourth term of an AP is  $1$  and the sum of its first eight terms is  $18$ , find the tenth term of the series.

18. A person pays a loan of Rs.975 in monthly installments , each installment being less than the former by Rs 5 . The amount of first installment is Rs .100 . In how many installment will the entire amount be paid ?

19. Some geometric means are inserted between  $2$  and  $32$ . Find the number of means between the numbers if second mean is  $8$ .

20. If the third and seventh terms of a geometric series are  $8$  and  $128$  respectively , Find the sum of its first 1 terms.

Group D 4x4=16

21. If  $f(x) = 3x + a$  and  $\text{fof}(6) = 10$  find the values of  $a$  and  $f^{-1}(4)$ .

22. If  $2x^3 - 5x + a$  and  $x^3 - x^2 + ax + 5$  leave equal remainder when divided by  $(x+2)$ , find the value of  $a$ .

23. There are  $n$  arithmetic means between 4 and 24. if the ratio of third mean to the last mean is 4:5 then find the number of terms in the series.

24. The sum of three terms in an arithmetic series is 24. If 1, 6 and 18 are added to them respectively, the result are in geometrical series, Find the terms.

The End