### **Exploratory Analysis**

#### Libraries

```
In [1]: import pandas as pd
   import matplotlib.pyplot as plt
   import seaborn as sns
   from statsmodels.tsa.seasonal import seasonal_decompose
   from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
   from statsmodels.tsa.stattools import acf, pacf, adfuller, kpss
In [2]: import warnings
   warnings.filterwarnings('ignore')
```

#### **Data Overview**

```
In [3]: data = pd.read_csv("daily_data.csv")
In [4]: data.head()
                 date daily_avg_benzene
Out[4]:
                                                      datetime
        0 2004-03-10
                                8.460790 2004-03-10T00:00:00Z
         1 2004-03-11
                                7.989058 2004-03-11T00:00:00Z
         2 2004-03-12
                               12.129509 2004-03-12T00:00:00Z
         3 2004-03-13
                               10.922887 2004-03-13T00:00:00Z
        4 2004-03-14
                                9.631442 2004-03-14T00:00:00Z
In [5]: df = data.drop("datetime", axis='columns')
In [6]:
        df.head()
Out[6]:
                 date daily_avg_benzene
        0 2004-03-10
                                8.460790
         1 2004-03-11
                                7.989058
         2 2004-03-12
                               12.129509
         3 2004-03-13
                               10.922887
        4 2004-03-14
                                9.631442
```

```
In [7]: # Statistics
         df.describe()
 Out[7]:
                daily_avg_benzene
          count
                       391.000000
          mean
                         10.173870
                         4.308602
            std
           min
                          1.431244
           25%
                         6.921344
           50%
                         9.984321
           75%
                         13.112391
           max
                        24.395876
 In [8]: # Missing Values
         df.isnull().sum()
 Out[8]: date
                                0
          daily_avg_benzene
          dtype: int64
 In [9]: # Data Types
         df.dtypes
 Out[9]: date
                                 object
          daily_avg_benzene
                                float64
          dtype: object
In [10]: # Length of Dataset
          len(df)
Out[10]: 391
```

# **Pre-Processing**

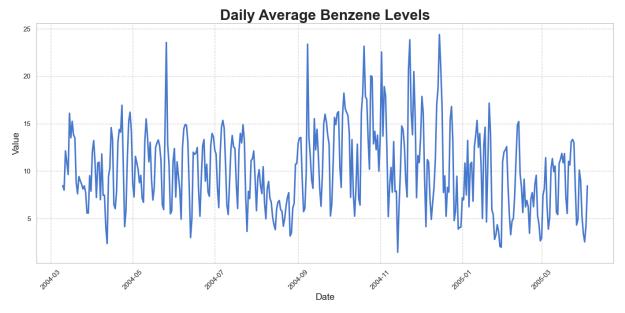
```
In [11]: df['date'] = pd.to_datetime(df['date'])
```

#### **Exploratory Data Analysis**

```
In [12]: # Time Series Plot
sns.set(style="whitegrid", palette="muted")
plt.figure(figsize=(14, 7))
sns.lineplot(x='date', y='daily_avg_benzene', data=df, linewidth=2.5)

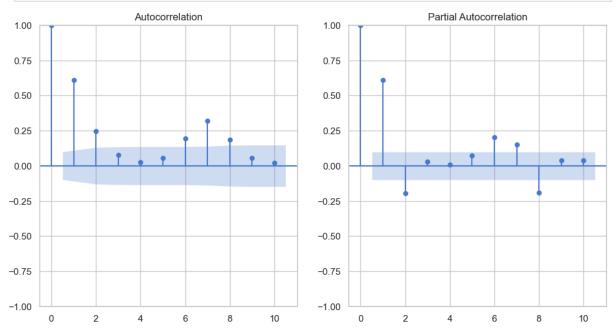
plt.title('Daily Average Benzene Levels', fontsize=24, fontweight='bold')
plt.xlabel('Date', fontsize=15)
```

```
plt.ylabel('Value', fontsize=15)
plt.xticks(rotation=45)
plt.grid(True, linestyle='--', alpha=0.7)
plt.tight_layout()
```



### **Statistical Analysis**

```
In [13]: # ACF and PACF
plt.figure(figsize=(12, 6))
plt.subplot(121)
plot_acf(df['daily_avg_benzene'], lags=10, ax=plt.gca())
plt.subplot(122)
plot_pacf(df['daily_avg_benzene'], lags=10, ax=plt.gca())
plt.show()
```



```
In [14]: # ADF Test
         adf_result = adfuller(df['daily_avg_benzene'].dropna())
         print('ADF Statistic:', adf result[0].round(4))
         print('p-value:', adf_result[1].round(4))
         print("Number of Observations Used: {}".format(adf_result[3]))
         print("Critical Values:")
         for key, value in adf result[4].items():
             print(" {}: {:.4f}".format(key, value))
        ADF Statistic: -4.0217
        p-value: 0.0013
        Number of Observations Used: 375
        Critical Values:
          1%: -3.4479
          5%: -2.8693
          10%: -2.5709
In [15]: # KPSS Test
         kpss_result = kpss(df['daily_avg_benzene'].dropna(), regression='c')
         print('KPSS Statistic:', kpss_result[0].round(4))
         print('p-value:', kpss_result[1].round(4))
         print("Critical Values:")
         for key, value in kpss_result[3].items():
             print(" {}: {:.4f}".format(key, value))
        KPSS Statistic: 0.357
        p-value: 0.0957
        Critical Values:
          10%: 0.3470
          5%: 0.4630
          2.5%: 0.5740
          1%: 0.7390
```

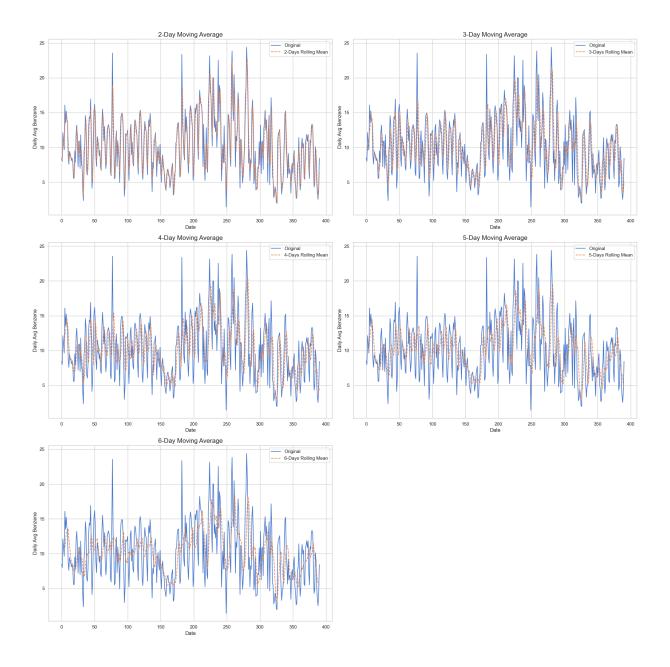
#### **Moving Average**

```
In [16]: plt.figure(figsize=(20, 20))

for i, window in enumerate([2, 3, 4, 5, 6]):
    moving_average = df['daily_avg_benzene'].rolling(window=window).mean()

    plt.subplot(3, 2, i + 1)
    plt.plot(df.index, df['daily_avg_benzene'], label='Original', linestyle=
    plt.plot(df.index, moving_average, label='{}-Days Rolling Mean'.format(w
    plt.xlabel("Date")
    plt.ylabel("Daily Avg Benzene")
    plt.title("{}-Day Moving Average".format(window), fontsize=15)
    plt.grid(True)
    plt.legend(loc='best')

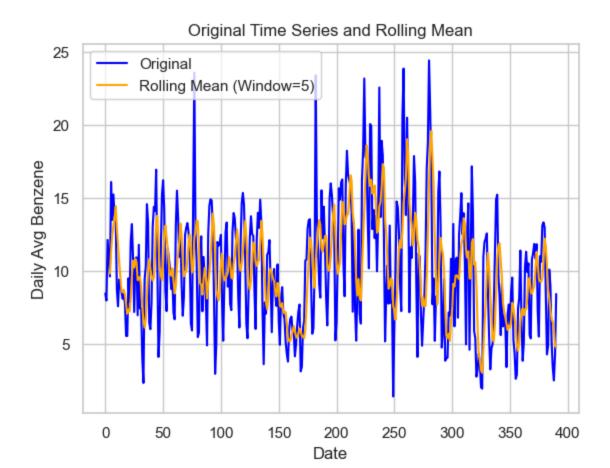
plt.tight_layout()
plt.show()
```



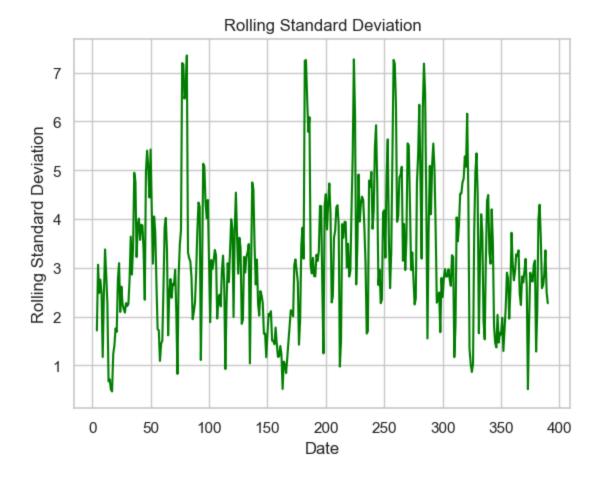
### **Rolling Statistics**

```
In [17]: rolling_mean = df['daily_avg_benzene'].rolling(window=5).mean()
    rolling_std = df['daily_avg_benzene'].rolling(window=5).std()

In [18]: # Original Time Series and Rolling Mean
    plt.plot(df.index, df['daily_avg_benzene'], label='Original', color='blue')
    plt.plot(df.index, rolling_mean, label='Rolling Mean (Window=5)', color='ora
    plt.title('Original Time Series and Rolling Mean')
    plt.xlabel('Date')
    plt.ylabel('Daily Avg Benzene')
    plt.legend(loc='best')
    plt.grid(True)
    plt.show()
```

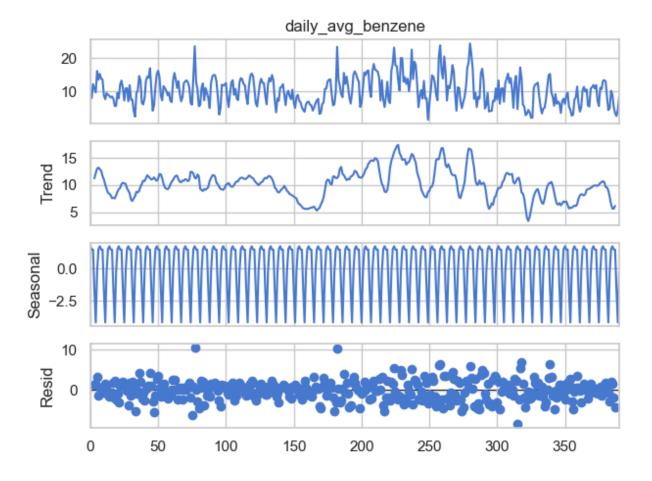


```
In [19]: # Rolling Standard Deviation
plt.plot(df.index, rolling_std, label='Rolling Std Dev (Window=5)', color='g
plt.title('Rolling Standard Deviation')
plt.xlabel('Date')
plt.ylabel('Rolling Standard Deviation')
plt.show()
```



## Decomposition

```
In [20]: # Additive Decomposition
   additive_decomposition = seasonal_decompose(df['daily_avg_benzene'], model='
   additive_decomposition.plot()
   plt.show()
```



#### **Residuals of Decomposition**

```
residuals = additive_decomposition.resid
In [21]:
In [22]: # Dickey-Fuller Test
         adf_test = adfuller(residuals.dropna(), autolag='AIC')
         print("ADF Statistic: {:.4f}".format(adf_test[0]))
         print("p-value: {:.4f}".format(adf_test[1]))
         print("Number of Lags Used: {}".format(adf_test[2]))
         print("Number of Observations Used: {}".format(adf test[3]))
         print("Critical Values:")
         for key, value in adf_test[4].items():
             print(" {}: {:.4f}".format(key, value))
        ADF Statistic: -8.5327
        p-value: 0.0000
        Number of Lags Used: 17
        Number of Observations Used: 367
        Critical Values:
          1%: -3.4483
          5%: -2.8694
          10%: -2.5710
In [23]: # KPPS Test
         kpss_test = kpss(residuals.dropna(), nlags='auto')
```

```
print("KPSS Statistic: {:.4f}".format(kpss_test[0]))
print("p-value: {:.4f}".format(kpss_test[1]))
print("Lags Used: {}".format(kpss_test[2]))
print("Critical Values:")
for key, value in kpss_test[3].items():
    print(" {}: {:.4f}".format(key, value))
```

KPSS Statistic: 0.3624

p-value: 0.0934 Lags Used: 209 Critical Values: 10%: 0.3470 5%: 0.4630 2.5%: 0.5740

1%: 0.7390