

As is

Now let us solve the linear population growth model in equation ??:
 $\dot{x} = rx$. The equation can be solved by first dividing both sides by x and then integrating:

$$\int \frac{1}{x} \frac{dx}{dt} dt = \int \frac{dx}{x} = \int r dt \implies \log |x| = rt + C \implies x = e^{rt+C} = Ae^{rt}$$

Easier to follow

$$\begin{aligned} \dot{x} &= rx \\ \int \left(\frac{1}{x}\right) \frac{dx}{dt} dt &= \int \left(\frac{1}{x}\right) xr \, dt \\ \int \frac{1}{x} dx &= \int r \, dt \\ \log |x| &= rt + C \\ x &= e^{rt+C} \\ &= Ae^{rt} \quad \square \end{aligned}$$