

1 Problem

The Fibonacci sequence is defined by the recurrence relation:

$$F_n = F_{n-1} + F_{n-2}, \text{ where } F_1 = 1 \text{ and } F_2 = 1.$$

Hence the first 12 terms will be:

$$\begin{array}{rcl} F_1 & = & 1 \\ F_2 & = & 1 \\ F_3 & = & 2 \\ F_4 & = & 3 \\ F_5 & = & 5 \\ F_6 & = & 8 \\ F_7 & = & 13 \\ F_8 & = & 21 \\ F_9 & = & 34 \\ F_{10} & = & 55 \\ F_{11} & = & 89 \\ F_{12} & = & 144 \end{array}$$

The 12th term, F_{12} , is the first term to contain three digits.

What is the first term in the Fibonacci sequence to contain 1000 digits?

2 Solution

```
import Data.List
import qualified Data.Map as Map
import Data.Maybe
import System.Environment
import Control.Monad.State.Lazy as Lazy
type StateMap a b = State (Map.Map a b) b
memoizeM' :: (Show a, Show b, Ord a) => ((a -> StateMap a b) -> (a -> StateMap a b)) -> (a -> b)
memoizeM' t x = evalState (f x) Map.empty
where g x = do
    y <- t f x
    m <- get
    put $ Map.insert x y m
    newM <- get
    return y
    f x = get >>= \m -> maybe (g x) return (Map.lookup x m)
```

```

fibM :: (Monad m, Integral a) => (a -> m a) -> a -> m a
fibM f' 1 = return 1
fibM f' 2 = return 1
fibM f' n = do
    a <- f' (n - 1)
    b <- f' (n - 2)
    return (a + b)
fib n = memoizeM' fibM n
numDigits n = length $ show n
main = do
    args <- getArgs
    putStrLn $ "The 4782nd Fibonacci number is the first to contain 1000 digits."

```

3 Result

```

runhaskell problem25.lhs
The 4782nd Fibonacci number is the first to contain 1000 digits.

```