1 Problem

The first two consecutive numbers to have two distinct prime factors are:

$$14 = 2 \times 7$$
$$15 = 3 \times 5$$

The first three consecutive numbers to have three distinct prime factors are:

$$644 = 2^2 \times 7 \times 23645 = 3 \times 5 \times 43646 = 2 \times 17 \times 19.$$

Find the first four consecutive integers to have four distinct primes factors. What is the first of these numbers?

2 Solution

```
import Data.List
import qualified Data. Map as Map
import Data.Maybe
import System. Environment
import Data.Numbers
{\bf import}\ Data. Numbers. Primes
import qualified Data. Set as Set
dPrimeFactors\ n = Set.fromList\ \$\ primeFactors\ n
dPFList\ n = [(k, dPrimeFactors\ k) \mid k \leftarrow filter\ (\lambda z \rightarrow (\neg \$isPrime\ z))\ [1 ... n]]
nConsec \ n \ s =
  let dpf = dPFList s
     fltrd = filter \ (\lambda z \rightarrow Set.size \ (snd \ z) \equiv n) \ dpf
     qps = [take (fromIntegral \ n) (drop (fromIntegral \ k) fittrd) | k \leftarrow [0 ... (length fittrd - n)]]
     gps2 = filter (\lambda z \rightarrow isConsec (map fst z)) gps
     gps3 = filter (\lambda zz \rightarrow Set.empty \equiv foldl (\lambda acc z \rightarrow Set.intersection acc (snd z)) (snd (head zz)) zz) gps2
  in gps3
isConsec \ xs = (sort \ xs) \equiv [(minimum \ xs) \dots (maximum \ xs)]
main = \mathbf{do}
  let soln = (fst \circ head \circ head) \ nConsec 4 20000
  putStrLn $ show soln
```

3 Result

```
runhaskell problem47.lhs 134043
```