

1 Problem

The arithmetic sequence, 1487, 4817, 8147, in which each of the terms increases by 3330, is unusual in two ways:

1. each of the three terms are prime, and,
2. each of the 4-digit numbers are permutations of one another.

There are no arithmetic sequences made up of three 1-, 2-, or 3-digit primes, exhibiting this property, but there is one other 4-digit increasing sequence.

What 12-digit number do you form by concatenating the three terms in this sequence?

2 Solution

```
import Data.List
import qualified Data.Map as Map
import Data.Maybe
import System.Environment
import Data.Numbers
import Data.Numbers.Primes
import qualified Data.Set as Set

sPrimes = filter (≥ 1000) $ takeWhile (<10000) primes

permPrimes x =
  let perms = map (λz → read z :: Integer) (permutations $ show x)
  in sort $ filter isPrime perms

isArithSeq xs = and (map (λz → z ≡ (diffs !! 0)) diffs)
  where diffs = [(xs !! k) - (xs !! (k - 1)) | k ← [1..(length xs)]]

arithSeqs xs =
  let rots = rotations xs
      pairs = map (λz → (head z, filter (λzzz → zzz ∈ xs) $ map (λzz → 0 - (head z) + 2 * zz) (filter (≥ (head z)) (tail z)))) rots
      solns = filter (λz → (snd z ≠ [])) pairs
      osols = (Set.toList ∘ Set.fromList) $ map (λz → sort ([fst z, head (snd z)])) solns
      fsols = map (λz → (head z, (head z) + ((last z) - (head z) `div` 2), last z)) osols
  in fsols

rotations x = map (λz → rotate z x) [0..(length x - 1)]
  where rotate n x = concat [drop n x, take n x]

main = do
  let ssprimes = sortBy (λx y → compare (sort $ show x) (sort $ show y)) sPrimes
      gprimes = groupBy (λx y → (sort $ show x) ≡ (sort $ show y)) ssprimes
      lgprimes = filter (λz → length z ≥ 3) gprimes
      triplets = concat $ map (λz → [sort [x, y, 2 * y - x] | x ← z, y ← z, y > x]) lgprimes
      p1 = filter (λz → ((z !! 2) ∈ sPrimes)) triplets
      p2 = filter (λz → (sort $ show $ head z) ≡ (sort $ show $ last z)) p1
      p3 = filter (λz → 1487 ∉ z) p2
      soln = concat (map show (p3 !! 0))
  putStrLn $ soln
```

3 Result

```
runhaskell problem49.lhs
296962999629
```