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Performance Metrics Clustering-Silhouetter Coefficient
          from sklearn.datasets import make blobs
          from sklearn.cluster import KMeans
          from sklearn.metrics import silhouette samples, silhouette score
          import matplotlib.pyplot as plt
          import matplotlib.cm as cm
          import numpy as np
          # Generating the sample data from make blobs
          # This particular setting has one distinct cluster and 3 clusters placed close
          # together.
          X, y = make blobs(n samples=500,
                              n features=2,
                              centers=4,
                              cluster std=1,
                               center box=(-10.0, 10.0),
                               shuffle=True,
                               random state=1) # For reproducibility
          range n clusters = [2, 3, 4, 5, 6]
          from sklearn.cluster import KMeans
          wcss=[]
          for i in range(1,11):
              kmeans=KMeans(n clusters=i, init='k-means++',random state=0)
              kmeans.fit(X)
              wcss.append(kmeans.inertia)
          plt.plot(range(1,11),wcss)
          plt.title('The Elbow Method')
          plt.xlabel('Number of Clusters')
          plt.ylabel('WCSS')
          plt.show()
                                 The Elbow Method
            16000
            14000
            12000
            10000
            8000
            6000
            4000
            2000
               0
                                                               10
                                   Number of Clusters
          clusterer = KMeans(n clusters=4, random state=10)
          cluster labels = clusterer.fit predict(X)
          print(cluster labels)
         [1 \ 1 \ 2 \ 0 \ 3 \ 0 \ 3 \ 3 \ 3 \ 1 \ 1 \ 3 \ 0 \ 3 \ 1 \ 3 \ 1 \ 0 \ 3 \ 2 \ 2 \ 3 \ 0 \ 0 \ 2 \ 3 \ 1 \ 0 \ 3 \ 1 \ 3 \ 1 \ 2
          \begin{smallmatrix} 2 & 1 & 2 & 3 & 2 & 0 & 3 & 3 & 1 & 2 & 3 & 0 & 0 & 0 & 2 & 2 & 3 & 1 & 2 & 2 & 2 & 2 & 3 & 0 & 0 & 2 & 3 & 1 & 3 & 2 & 2 & 1 & 2 & 3 & 1 \\ \end{smallmatrix}
          2 \; 3 \; 1 \; 1 \; 3 \; 0 \; 0 \; 1 \; 1 \; 3 \; 0 \; 3 \; 1 \; 1 \; 0 \; 1 \; 2 \; 0 \; 3 \; 3 \; 1 \; 3 \; 2 \; 1 \; 3 \; 2 \; 3 \; 2 \; 1 \; 3 \; 3 \; 3 \; 0 \; 2 \; 0 \; 3 \; 1
          \begin{smallmatrix}2&3&2&2&2&0&2&0&1&2&1&2&0&0&2&1&0&1&3&2&1&1&1&1&3&2&1&2&3&0&0&3&3&0&2&3&2\end{smallmatrix}
          \begin{smallmatrix}0&3&0&2&2&0&3&1&1&2&2&2&3&0&0&3&0&2&1&0&1&0&1&1&0&1&0&0&3&2&2&2&3&3&2&1&0\end{smallmatrix}
          1 \ 1 \ 1 \ 3 \ 2 \ 3 \ 1 \ 2 \ 1 \ 1 \ 2 \ 0 \ 1 \ 3 \ 3 \ 0 \ 0 \ 2 \ 1 \ 0 \ 0 \ 3 \ 1 \ 0 \ 0 \ 3 \ 2 \ 0 \ 2 \ 3 \ 1 \ 1 \ 0 \ 2
          1 \; 3 \; 0 \; 0 \; 3 \; 3 \; 3 \; 1 \; 3 \; 0 \; 0 \; 2 \; 0 \; 0 \; 0 \; 0 \; 1 \; 1 \; 3 \; 0 \; 2 \; 3 \; 1 \; 0 \; 2 \; 0 \; 3 \; 0 \; 2 \; 3 \; 2 \; 0 \; 3 \; 3 \; 1 \; 0 \; 1
          3\ 1\ 2\ 2\ 1\ 2\ 1\ 2\ 0\ 1\ 0\ 2\ 3\ 0\ 2\ 3\ 0\ 1\ 3\ 0\ 0\ 2\ 3\ 2\ 3\ 1\ 0\ 1\ 3\ 0\ 1\ 1\ 1\ 2\ 0\ 3\ 1
          3 3 2 2 1 3 3 3 3 3 3 1 3 2 1 3 0 3 0 3 2 2 0 0 0 2 3 2 1 2 0 3 1 0 1 0 1
          3 0 0 1 2 3 1 2 2 2 1 3 0 2 3 1 1 1 3]
In [3]: for n clusters in range n clusters:
              # Create a subplot with 1 row and 2 columns
              fig, (ax1, ax2) = plt.subplots(1, 2)
              fig.set size inches (18, 7)
               # The 1st subplot is the silhouette plot
               # The silhouette coefficient can range from -1, 1 but in this example all
               # lie within [-0.1, 1]
              ax1.set xlim([-0.1, 1])
               # The (n clusters+1)*10 is for inserting blank space between silhouette
               # plots of individual clusters, to demarcate them clearly.
              ax1.set ylim([0, len(X) + (n clusters + 1) * 10])
               # Initialize the clusterer with n clusters value and a random generator
               # seed of 10 for reproducibility.
              clusterer = KMeans(n clusters=n clusters, random state=10)
              cluster labels = clusterer.fit predict(X)
               # The silhouette score gives the average value for all the samples.
               # This gives a perspective into the density and separation of the formed
              silhouette avg = silhouette score(X, cluster labels)
              print("For n clusters =", n clusters,
                      "The average silhouette score is :", silhouette avg)
               # Compute the silhouette scores for each sample
              sample silhouette values = silhouette samples(X, cluster labels)
              y lower = 10
              for i in range(n clusters):
                   # Aggregate the silhouette scores for samples belonging to
                   # cluster i, and sort them
                   ith cluster silhouette values = \
                        sample silhouette values[cluster labels == i]
                   ith cluster silhouette values.sort()
                   size cluster i = ith cluster silhouette values.shape[0]
                   y upper = y lower + size cluster i
                   color = cm.nipy spectral(float(i) / n clusters)
                   ax1.fill betweenx(np.arange(y lower, y upper),
                                        0, ith cluster silhouette values,
                                        facecolor=color, edgecolor=color, alpha=0.7)
                   # Label the silhouette plots with their cluster numbers at the middle
                   ax1.text(-0.05, y lower + 0.5 * size cluster i, str(i))
                   # Compute the new y lower for next plot
                   y lower = y upper + 10 # 10 for the 0 samples
              ax1.set title("The silhouette plot for the various clusters.")
              ax1.set xlabel("The silhouette coefficient values")
              ax1.set ylabel("Cluster label")
               # The vertical line for average silhouette score of all the values
              ax1.axvline(x=silhouette avg, color="red", linestyle="--")
              ax1.set yticks([]) # Clear the yaxis labels / ticks
              ax1.set xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
               # 2nd Plot showing the actual clusters formed
              colors = cm.nipy spectral(cluster labels.astype(float) / n clusters)
              ax2.scatter(X[:, 0], X[:, 1], marker='.', s=30, lw=0, alpha=0.7,
                            c=colors, edgecolor='k')
               # Labeling the clusters
              centers = clusterer.cluster centers
               # Draw white circles at cluster centers
              ax2.scatter(centers[:, 0], centers[:, 1], marker='o',
                            c="white", alpha=1, s=200, edgecolor='k')
               for i, c in enumerate(centers):
                   ax2.scatter(c[0], c[1], marker='$%d$' % i, alpha=1,
                                 s=50, edgecolor='k')
              ax2.set title("The visualization of the clustered data.")
               ax2.set xlabel("Feature space for the 1st feature")
               ax2.set ylabel("Feature space for the 2nd feature")
              plt.suptitle(("Silhouette analysis for KMeans clustering on sample data "
                               "with n clusters = %d" % n clusters),
                              fontsize=14, fontweight='bold')
          plt.show()
         For n clusters = 2 The average silhouette score is : 0.7049787496083262
         For n clusters = 3 The average silhouette score is : 0.5882004012129721
         For n clusters = 4 The average silhouette score is : 0.6505186632729437
         For n clusters = 5 The average silhouette score is : 0.5745566973301872
         For n clusters = 6 The average silhouette score is : 0.4387644975296138
                                 Silhouette analysis for KMeans clustering on sample data with n_clusters = 2
                                                                                             The visualization of the clustered data
                       The silhouette plot for the various clusters.
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          -0.1
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                                              0.6
                                                                   1.0
                             The silhouette coefficient values
                                                                                                 Feature space for the 1st feature
                                 Silhouette analysis for KMeans clustering on sample data with n_clusters = 3
                       The silhouette plot for the various clusters.
                                                                                             The visualization of the clustered data
                                                                            7.5
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                                                                        Feature space for the 2nd feature
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         Cluster label
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                                                                            -5.0
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                                                        0.8
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                             The silhouette coefficient values
                                                                                                 Feature space for the 1st feature
                                 Silhouette analysis for KMeans clustering on sample data with n_clusters = 4
                       The silhouette plot for the various clusters.
                                                                                             The visualization of the clustered data
                                                                            5.0
                                                                            2.5
                                                                        Feature space for the 2nd feature
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         Cluster labe
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                              The silhouette coefficient values
                                                                                                  Feature space for the 1st feature
                                 Silhouette analysis for KMeans clustering on sample data with n_clusters = 5
                       The silhouette plot for the various clusters.
                                                                                             The visualization of the clustered data
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         Cluster label
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             1
                                                                            -5.0
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-5.0

-7.5

-10.0

-i2

-10

Feature space for the 1st feature

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Cluster labe

1

0

0.2

0.4

The silhouette coefficient values

0.6

0.8