Probability, Combinatorics, and Overlapping Sets

	or questions in the Quantitative Comparison format ("Quantity A" and "Quantity B" given), the aswer choices are always as follows:
	A) Quantity A is greater. B) Quantity B is greater.
	C) The two quantities are equal.D) The relationship cannot be determined from the information given.
F	or questions followed by a numeric entry box, you are to enter your own answer in the
y	ox. For questions followed by fraction-style numeric entry boxes, you are to enter our answer in the form of a fraction. You are not required to reduce fractions. For example, if the aswer is 1/4, you may enter 25/100 or any equivalent fraction.
ir li ge m	Il numbers used are real numbers. All figures are assumed to lie in a plane unless otherwise dicated. Geometric figures are not necessarily drawn to scale. You should assume, however, that nes that appear to be straight are actually straight, points on a line are in the order shown, and all cometric objects are in the relative positions shown. Coordinate systems, such as <i>xy</i> -planes and umber lines, as well as graphical data presentations such as bar charts, circle graphs, and line graphs, are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.
	mber is randomly chosen from a list of 10 consecutive positive integers. What is the probability that the umber is greater than the mean?
	(A) 3/10
	(B) 2/5 (C) 1/2
	(D) 7/10
	E) 4/5
A nu	mber is randomly chosen from the first 100 positive integers. What is the probability that it is a multiple of
((A) 32/100
	(B) 33/100
	(C) 1/3 (D) 34/100
	(D) 34/100 (E) 2/3
,	()

3. A restaurant menu has several options for tacos. There are 3 types of shells, 4 types of meat, 3 types of cheese, and 5 types of salsa. How many distinct tacos can be ordered assuming that any order contains exactly one of each

of the above choices?

4. A history exam features 5 questions. 3 of the questions are multiple-choice with four options each. The other two questions are true or false. If Caroline selects one answer for every question, how many different ways can she answer the exam?
5. A certain company places a six-symbol code on each of their products. The first two symbols are one of the letters A–E and the last four symbols are digits. If repeats are allowed on both letters and numbers, how many such codes are possible?
6. The probability is 1/2 that a coin will turn up heads on any given toss and the probability is 1/6 that a number cube with faces numbered 1 to 6 will turn up any particular number. What is the probability of turning up a heads and a 6?
(A) 1/36 (B) 1/12 (C) 1/6 (D) 1/4 (E) 2/3
7. An integer is randomly chosen from 2 to 20 inclusive. What is the probability that the number is prime?
8. Five students in a classroom are lining up one behind the other for recess. How many different lines are possible?
(A) 5 (B) 10 (C) 24 (D) 25 (E) 120
9. An Italian restaurant boasts 320 distinct pasta dishes. Each dish contains exactly one pasta, one meat, and one sauce. If there are 8 pastas and 4 meats available, how many sauces are there to choose from?

10. A 10-student class is to choose a president, vice president, and secretary from the group can occupy more than one post, in how many ways can this be accomplished?	o. Assuming that no person
11.	
Quantity A	Quantity B
The number of 4-digit positive integers where all 4 digits are less than 5	625
12. BurgerTown offers many options for customizing a burger. There are 3 types of meats a tomatoes, pickles, onions, ketchup, mustard, and special sauce. A burger must include many or as few condiments as the customer wants. How many different burgers are po	meat, but may include as
(A) 8! (B) (3)(7!) (C) (3)(8!) (D) (8)(2 ⁷) (E) (3)(2 ⁷)	
13. The probability of rain is 1/6 for any given day next week. What is the chance it rains on Tuesday?	both Monday and
(A) 1/36 (B) 1/12 (C) 1/6 (D) 1/3 (E) 2/3	
14. How many five-digit numbers can be formed using the digits 5, 6, 7, 8, 9, 0 if no digits c	an be repeated?
(A) 64 (B) 120 (C) 240 (D) 600 (E) 720	
15. A bag contains 3 red, 2 blue, and 7 white marbles. If a marble is randomly chosen from the probability that it is NOT blue?	he bag, what is the

16. A man has 3 different suits, 4 different shirts, 2 different pairs of socks, and 5 different pairs of shoes. In how

17. A state issues automobile license plates using two letters selected from a 26-letter alph numerals selected from the digits 0 through 9, inclusive. Repeats are permitted. For excombination could be GF3352.	
Quantity A	Quantity B
The number of possible unique license plate combinations	6,000,000
18. A small nation issues license plates that consist of just one number (selected from the dinclusive) and four letters, selected from a 20-letter alphabet. Repeats are permitted. I four-letter combination that is not allowed to appear on license plates. How many allo combinations exist?	However, there is one
(A) 1,599,990 (B) 1,599,999 (C) 1,600,000 (D) 4,569,759 (E) 4,569,760	
19. A bag contains 6 black chips numbered 1–6 respectively and 6 white chips numbered 1–reaches into the bag of 12 chips and removes 2 chips, one after the other, without repl probability that he will pick black chip #3 and then white chip #3?	
20. Tarik has a pile of 6 green chips numbered 1–6 respectively and another pile of 6 blue correspectively. Tarik will randomly pick 1 chip from the green pile and 1 chip from the leaders.	-
Quantity A	Quantity B
The probability that both chips selected by Tarik will display a number less than 4	1/2

21. A bag contains 6 red chips numbered 1–6 respectively and 6 blue chips numbered 1–6 respectively. If 2 chips are

chip and then a blue chip with the same number?

to be picked sequentially from the bag of 12 chips, without replacement, what is the probability of picking a red

many ways can the man dress himself if he must wear 1 suit, 1 shirt, 1 pair of socks, and 1 pair of shoes?

22. In a school of 150 students, 75 take Latin, 110 take Spanish, and 11 take r	neither.
Quantity A	Quantity B
The number of students who take only Latin	46
23. How many 10-digit numbers can be formed using only the digits 2 and 5?	
(A) 2 ¹⁰ (B) (22)(5!) (C) (5!)(5!) (D) 10!/2 (E) 10!	
24. A 6-sided cube has sides numbered 1 through 6. If the cube is rolled twice the two rolls is equal to 8?	e, what is the probability that the sum of
(A) 1/9 (B) 1/8 (C) 5/36 (D) 1/6 (E) 7/36	
25. A coin with heads on one side and tails on the other has a 1/2 probability of 5 times, how many distinct outcomes are possible if the last flip must be do not contain exactly the same results in exactly the same order.	-
26. In a class of 25 students, every student takes either Spanish, Latin, or Frentake all three languages. 9 take Spanish, 7 take Latin and 5 take exactly t	
Quantity A	Quantity B
The number of students who take French	14
27. Bob has a 24-sided die with an integer between 1 and 24 on each face. Ever When he rolls, what is the probability that the number showing is a factor	2

28. A baby has x total toys. If 9 of the toys are stuffed animals, 7 of the toys were given to the baby by its grandmother, 5 of the toys are stuffed animals given to the baby by its grandmother, and 6 of the toys are neither stuffed animals nor given to the baby by its grandmother, what is the value of x?
29. How many integers between 2,000 and 3,999 have a ones digit that is a prime number?
30. How many integers between 2,000 and 6,999 are even and have a digit that is a prime number in the tens place?
31. A group of 12 people who have never met are in a classroom. How many handshakes are exchanged if each pair shakes hands exactly once?
(A) 12 (B) 22 (C) 66 (D) 132 (E) 244
32. A classroom has 12 girls and 20 boys. One quarter of the girls in the class have blue eyes. If a child is selected at random from the class, what is the probability that he/she is a girl who does not have blue eyes?
(A) 3/32 (B) 9/32 (C) 3/8 (D) 23/32 (E) 29/32
33. A coin with heads on one side and tails on the other has a 1/2 probability of landing on heads. If the coin is flipped three times, what is the probability of flipping 2 tails and 1 head, in any order?
(A) 1/8 (B) 1/3 (C) 3/8 (D) 5/8

"MISSISSIPPI" be rearranged?	many ways can the word
36. If the word "WOW" can be rearranged in exactly 3 ways (WOW, OWW, WWO), in how in "MISSISSIPPI" be rearranged?	many ways can the word
(E) 3/4	
(B) 1/4 (C) 1/3 (D) 1/2	
(A) 1/8 (B) 1/4	
random, replaces it in the group, and chooses another tile at random, what is the probabthe two integer values on the tiles is odd?	
the two integer values on the tiles is odd?	
(B) 1/4	
(C) 1/3	
(D) 1/2	
(E) 3/4	
(E) 3/4	
(E) 3/4	
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(E) $3/4$	
(E) $3/4$	
(E) 3/4	
(L) S/T	
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36. If the word "WOW" can be rearranged in exactly 3 ways (WOW OWW WWO) in how	many ways can the word
36. If the word "WOW" can be rearranged in exactly 3 ways (WOW, OWW, WWO), in how	many ways can the word
MISSISSIPPT be rearranged?	
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37. If a, b, and c are integers randomly chosen from the set of prime numbers greater than 2.	and less than 30 what is
37. If a , b , and c are integers randomly chosen from the set of prime numbers greater than 2	and less than 30, what is
37. If a , b , and c are integers randomly chosen from the set of prime numbers greater than 2 the probability that $ab + c$ is equal to 23?	and less than 30, what is
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40.	Jack has a cube with 6 sides numbered 1 through 6. He rol all of his rolls is even, at which time he stops. (Note: it is probability that Jack will need to roll the cube more than	is possible to roll the cube jus	st once.) What is the
	(A) 1/8 (B) 1/4 (C) 3/8 (D) 1/2 (E) 3/4		
41.	Jan and 5 other children are in a classroom. The principal or random. What is the probability that Jan is chosen?	of the school walks in and cho	poses two children at
	(A) 4/5 (B) 1/3 (C) 2/5 (D) 7/15 (E) 1/2		
42.	The probability that Gary will eat eggs for breakfast on any cereal for breakfast on any given day is 4/7. Gary never l		
	Quantity A		Quantity B
	Probability that Gary eats eggs or cereal for b	reakfast on a particular day	1
43.	The probability that Maria will eat breakfast on any given on any given day is 0.3. The two probabilities are independent		Maria will wear a sweater
	Quantity A		Quantity B
	The probability that Maria eats breakfast	or wears a sweater	0.8
44.	The probability of rain in Greg's town on Tuesday is 0.3. To quiz on Tuesday is 0.2. The events occur independently of		cher will give him a pop
	Quantity A	Quantity B	
	The probability that either or both events occur	The probability that neithe	r event occurs
45.	The probability of event <i>X</i> occurring is the same as the proindependently of each other.	bability of event Yoccurring.	. The events occur
	Quantity A	Quantity B	
	The probability that both events occur	The probability that neither e	vent occurs.
46.	A certain city has a 1/3 chance of rain occurring on any given that the city experiences rain?	ven day. In any given 3-day pe	riod, what is the probability
	(A) 1/3 (B) 8/27 (C) 2/3 (D) 19/27		

	(E) 1	
47. Fi	Five students, Adnan, Beth, Carol, Dan, and Edmund are possible if Beth is not allowed to stand next to Dan?	to be arranged in a line. How many such arrangements are
	(A) 24 (B) 48 (C) 72 (D) 96 (E) 120	
48. A		does it have? (A diagonal is a line drawn from one vertex annot touch or cross any of the edges of the shape. For has two.)
	(A) 54 (B) 66 (C) 108 (D) 132 (E) 144	
49. A	A student council is to be chosen from a class of 12 student committee members. How many such councils are po	
	12! (A) 7!5! 12! (B) 7!3! 12! (C) 5!3! 12! (D) 7! (E) 12!	
50.		
	Quantity A	Quantity B
	The number of possible pairings of 2 colors that can be selected from 5 possible options	The number of possible pairings of 8 colors that can be selected from 9 possible options
51.		
	Quantity A	Quantity B
	The number of possible 4-person teams that can be selected from 6 people	The number of possible 2-person teams that can be selected from 6 people
52.		

Quantity B

Quantity A

The number of ways 1st, 2nd, and 3rd place prizes could be awarded to 3 out of 6 contestants

The number of ways 1st, 2nd, 3rd, 4th, and 5th place prizes could be awarded to 5 contestants

53. An inventory of coins contains 100 different coins.

Quantity A

Quantity B

The number of possible collections of 56 coins that can be selected where the order of the coins does not matter

The number of possible collections of 44 coins that can be selected where the order of the coins does not matter

54. An office supply store carries an inventory of 1,345 different products, all of which it categorizes as 'business use," 'personal use," or both. 740 products are categorized as 'business use" ONLY and 520 products are categorized as both 'business use" and 'personal use."

Quantity A

Quantity B

The number of products characterized as "personal use"

600

- 55. How many distinct 4-letter "words" can be made from the name "CHRISTYNA"? (A "word" is any arrangement of 4 letters regardless of whether it can be found in a dictionary.)
 - (A) 9
 - (B) 24
 - (C)36
 - (D) 504
 - (E) 3,024
- 56. Seiko has a 6-sided number cube with sides labeled 1 through 6. If she rolls the cube twice, what is the probability that the product of the two rolls is less than 36?
 - (A) 1/6
 - (B) 1/3
 - (C) 2/3
 - (D) 5/6
 - (E) 35/36
- 57. There is an 80% chance David will eat a healthy breakfast and a 25% chance that it will rain. If these events are independent, what is the probability that David will eat a healthy breakfast OR that it will rain?
 - (A) 20%
 - (B) 80%
 - (C) 85%
 - (D) 95%
 - (E) 105%
- 58. The probability of rain is 1/2 for every day next week. What is the chance that it rains on at least one day during the workweek (Monday through Friday)?
 - (A) 1/2
 - (B) 31/32
 - (C) 63/64
 - (D) 127/128

that the committee includes at least one man?
(A) 1/32
(B) 1/4
(C) 2/5
(D) 7/15
(E) 8/15
60. At Lexington High School, everyone takes at least one language — Spanish, French, or Latin — but no one takes all three languages. If 100 students take Spanish, 80 take French, 40 take Latin, and 22 take exactly two languages, how many students are there?
(A) 198
(B) 220
(C) 242
(D) 264
(E) 286
61.
Of 60 birds found in a certain location 20 are songbirds and 23 are migratory. (It is possible

for a songbird to be migratory, or not.)

Quantity B

16

Quantity A

The number of the 60 birds that are neither migratory nor songbirds

59. Eight women and two men are available to serve on a committee. If three people are picked, what is the probability

(E) 5/2