## Probability, Combinatorics, and Overlapping Sets

	For questions in the Quantitative Comparison format ("Quantity A" and "Quantity B" given), the answer choices are always as follows:
	(A) Quantity A is greater.
	(B) Quantity B is greater.
	(C) The two quantities are equal.
	(D) The relationship cannot be determined from the information given.
	For questions followed by a numeric entry box, you are to enter your own answer in the
	box. For questions followed by fraction-style numeric entry boxes, you are to enter your answer in the form of a fraction. You are not required to reduce fractions. For example, if the answer is 1/4, you may enter 25/100 or any equivalent fraction.
	All numbers used are real numbers. All figures are assumed to lie in a plane unless otherwise indicated. Geometric figures are not necessarily drawn to scale. You should assume, however, that lines that appear to be straight are actually straight, points on a line are in the order shown, and all geometric objects are in the relative positions shown. Coordinate systems, such as <i>xy</i> -planes and
	number lines, as well as graphical data presentations such as bar charts, circle graphs, and line graphs, are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.
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4	are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.  number is randomly chosen from a list of 10 consecutive positive integers. What is the probability that the number is greater than the mean?  (A) 3/10
4	are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.  number is randomly chosen from a list of 10 consecutive positive integers. What is the probability that the number is greater than the mean?  (A) 3/10 (B) 2/5
4	are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.  number is randomly chosen from a list of 10 consecutive positive integers. What is the probability that the number is greater than the mean?  (A) 3/10 (B) 2/5 (C) 1/2
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	are drawn to scale. A symbol that appears more than once in a question has the same meaning throughout the question.  number is randomly chosen from a list of 10 consecutive positive integers. What is the probability that the number is greater than the mean?  (A) 3/10 (B) 2/5 (C) 1/2 (D) 7/10 (E) 4/5  number is randomly chosen from the first 100 positive integers. What is the probability that it is a multiple (A) 32/100
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3. A restaurant menu has several options for tacos. There are 3 types of shells, 4 types of meat, 3 types of cheese, and 5 types of salsa. How many distinct tacos can be ordered assuming that any order contains exactly one of each

of the above choices?

4. A history exam features 5 questions. 3 of the questions are multiple-choice with four options each. The other two questions are true or false. If Caroline selects one answer for every question, how many different ways can she answer the exam?
5. A certain company places a six-symbol code on each of their products. The first two symbols are one of the letters A–E and the last four symbols are digits. If repeats are allowed on both letters and numbers, how many such codes are possible?
6. The probability is 1/2 that a coin will turn up heads on any given toss and the probability is 1/6 that a number cube with faces numbered 1 to 6 will turn up any particular number. What is the probability of turning up a heads and a 6?
(A) 1/36 (B) 1/12 (C) 1/6 (D) 1/4 (E) 2/3
7. An integer is randomly chosen from 2 to 20 inclusive. What is the probability that the number is prime?
8. Five students in a classroom are lining up one behind the other for recess. How many different lines are possible?
(A) 5 (B) 10 (C) 24
(D) 25 (E) 120
9. An Italian restaurant boasts 320 distinct pasta dishes. Each dish contains exactly one pasta, one meat, and one sauce. If there are 8 pastas and 4 meats available, how many sauces are there to choose from?

10. A 10-student class is to choose a president, vice president, and secretary from the group can occupy more than one post, in how many ways can this be accomplished?	p. Assuming that no person
11.	
Quantity A	Quantity B
The number of 4-digit positive integers where all 4 digits are less than 5	625
12. BurgerTown offers many options for customizing a burger. There are 3 types of meats a tomatoes, pickles, onions, ketchup, mustard, and special sauce. A burger must include many or as few condiments as the customer wants. How many different burgers are possible.	e meat, but may include as
(A) 8! (B) (3)(7!) (C) (3)(8!) (D) (8)(2 <sup>7</sup> ) (E) (3)(2 <sup>7</sup> )	
13. The probability of rain is 1/6 for any given day next week. What is the chance it rains on Tuesday?	n both Monday and
(A) 1/36 (B) 1/12 (C) 1/6 (D) 1/3 (E) 2/3	
14. How many five-digit numbers can be formed using the digits 5, 6, 7, 8, 9, 0 if no digits of	can be repeated?
(A) 64 (B) 120 (C) 240 (D) 600 (E) 720	
15. A bag contains 3 red, 2 blue, and 7 white marbles. If a marble is randomly chosen from a probability that it is NOT blue?	the bag, what is the

16. A man has 3 different suits, 4 different shirts, 2 different pairs of socks, and 5 different pairs of shoes. In how

17. A state issues automobile license plates using two letters selected from a 26-letter alphabunumerals selected from the digits 0 through 9, inclusive. Repeats are permitted. For exacombination could be GF3352.	
Quantity A	Quantity B
The number of possible unique license plate combinations	6,000,000
18. A small nation issues license plates that consist of just one number (selected from the diginclusive) and four letters, selected from a 20-letter alphabet. Repeats are permitted. He four-letter combination that is not allowed to appear on license plates. How many allow combinations exist?	owever, there is one
(A) 1,599,990 (B) 1,599,999 (C) 1,600,000 (D) 4,569,759 (E) 4,569,760	
19. A bag contains 6 black chips numbered 1–6 respectively and 6 white chips numbered 1–6 reaches into the bag of 12 chips and removes 2 chips, one after the other, without replace probability that he will pick black chip #3 and then white chip #3?	
20. Tarik has a pile of 6 green chips numbered 1–6 respectively and another pile of 6 blue chi respectively. Tarik will randomly pick 1 chip from the green pile and 1 chip from the bl	_
Quantity A	Quantity B
The probability that both chips selected by Tarik will display a number less than 4	1/2

21. A bag contains 6 red chips numbered 1–6 respectively and 6 blue chips numbered 1–6 respectively. If 2 chips are

chip and then a blue chip with the same number?

to be picked sequentially from the bag of 12 chips, without replacement, what is the probability of picking a red

many ways can the man dress himself if he must wear 1 suit, 1 shirt, 1 pair of socks, and 1 pair of shoes?

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22. In a school of 150 str	udents, 75 take Latin, 110 take Spanish, and 11	take neither.
	Quantity A	Quantity B
	The number of students who take only Latin	46
23. How many 10-digit n	numbers can be formed using only the digits 2 ar	nd 5?
(A) 2 <sup>10</sup> (B) (22)(5!) (C) (5!)(5!) (D) 10!/2 (E) 10!		
24. A 6-sided cube has si the two rolls is equ	ides numbered 1 through 6. If the cube is rolled all to 8?	twice, what is the probability that the sum of
(A) 1/9 (B) 1/8 (C) 5/36 (D) 1/6 (E) 7/36		
5 times, how many	one side and tails on the other has a 1/2 probab distinct outcomes are possible if the last flip metly the same results in exactly the same order.	nust be heads? Outcomes are distinct if they
	ents, every student takes either Spanish, Latin, or lages. 9 take Spanish, 7 take Latin and 5 take exa	
	Quantity A	<b>Quantity B</b>
	The number of students who take French	14
27. Bob has a 24-sided d	ie with an integer between 1 and 24 on each face	e. Every number is featured exactly once.

When he rolls, what is the probability that the number showing is a factor of 24?

grandmother, 5 of the toys are stuffe	are stuffed animals, 7 of the toys were given to the baby by its ed animals given to the baby by its grandmother, and 6 of the toys are neither by by its grandmother, what is the value of $x$ ?
29. How many integers between 2,000 and	13,999 have a ones digit that is a prime number?
	see copy there i have done
30. How many integers between 2,000 and	16,999 are even and have a digit that is a prime number in the tens place?
31. A group of 12 people who have never r	met are in a classroom. How many handshakes are exchanged if each pair
(A) 12 (B) 22 (C) 66 (D) 132 (E) 244	whenever there is handshake que do use nC2
	One quarter of the girls in the class have blue eyes. If a child is selected at robability that he/she is a girl who does not have blue eyes?
(A) 3/32 (B) 9/32 (C) 3/8 (D) 23/32 (E) 29/32	
	s on the other has a 1/2 probability of landing on heads. If the coin is flipped of flipping 2 tails and 1 head, in any order?
(A) 1/8 (B) 1/3 (C) 3/8 (D) 5/8	

	(E) $2/3$	
34.	A 6-sided cube has sides numbered 1 through 6. If the cube is rolled twice, what is the p of the rolls will result in a number higher than 4?	robability that at least one
	(A) 2/9 (B) 1/3 (C) 4/9 (D) 5/9 (E) 2/3	
35.	Tiles are labeled with the integers from 1 to 100 inclusive; no numbers are repeated. If a random, replaces it in the group, and chooses another tile at random, what is the probate the two integer values on the tiles is odd?	
	(A) 1/8 (B) 1/4 (C) 1/3 (D) 1/2 (E) 3/4	
36.	If the word "WOW" can be rearranged in exactly 3 ways (WOW, OWW, WWO), in how "MISSISSIPPI" be rearranged?	many ways can the word
37.	If $a$ , $b$ , and $c$ are integers randomly chosen from the set of prime numbers greater than 2 the probability that $ab + c$ is equal to 23?	and less than 30, what is
38.		
	The probability of rain is 1/2 on any given day next week.	
	Quantity A	Quantity B
	The probability that it rains on AT LEAST one out of the 7 days next week	127/128
39.	Two fair dice with sides numbered 1 to 6 are tossed. What is the probability that the sun the dice is a prime number?	n of the exposed faces on

40. Jack has a cube with 6 sides numbered 1 through 6. He rall of his rolls is even, at which time he stops. (Note: probability that Jack will need to roll the cube more that	it is possible to roll the cube just once.) What is the
(A) 1/8	
(B) 1/4	
(C) 3/8	
(D) 1/2 (E) 2/4	
(E) $3/4$	
41. Jan and 5 other children are in a classroom. The principal random. What is the probability that Jan is chosen?	al of the school walks in and chooses two children at
(A) $4/5$	
(B) 1/3	
(C) 2/5	
(D) 7/15	
(E) $1/2$	
42. The probability that Gary will eat eggs for breakfast on a cereal for breakfast on any given day is 4/7. Gary never	any given day is 3/7. The probability that Gary will eat er has both eggs and cereal for breakfast on the same day.
Quantity A	Quantity B
Probability that Gary eats eggs or cereal for	r breakfast on a particular day 1
43. The probability that Maria will eat breakfast on any given on any given day is 0.3. The two probabilities are independent	· · · · · · · · · · · · · · · · · · ·
Quantity A	Quantity B
The probability that Maria eats breakfa	ast or wears a sweater 0.8
44. The probability of rain in Greg's town on Tuesday is 0.3 quiz on Tuesday is 0.2. The events occur independently	
Quantity A	Quantity B
The probability that either or both events occu	ur The probability that neither event occurs
45. The probability of event <i>X</i> occurring is the same as the prindependently of each other.	probability of event Y occurring. The events occur
Quantity A	Quantity B
The probability that both events occur	The probability that neither event occurs.
46. A certain city has a 1/3 chance of rain occurring on any that the city experiences rain?	given day. In any given 3-day period, what is the probability
(A) 1/3 (B) 8/27 (C) 2/3	
(D) 19/27	

(E	5) 1	
	students, Adnan, Beth, Carol, Dan, and Edmund are ssible if Beth is not allowed to stand next to Dan?	to be arranged in a line. How many such arrangements are
(B (C (D	A) 24 B) 48 C) 72 D) 96 E) 120	
to a		does it have? (A diagonal is a line drawn from one vertex must be until touch or cross any of the edges of the shape. For has two.)
(B (C (D	A) 54 B) 66 C) 108 D) 132 E) 144	
	ident council is to be chosen from a class of 12 stummittee members. How many such councils are po	dents consisting of a president, a vice president, and 3 ssible?
(B (C	12! 7!5! 12! 7!3! 12! 5!3! 12! 7! 12! 7!	
50.		
	Quantity A	Quantity B
	The number of possible pairings of 2 colors that can be selected from 5 possible options	The number of possible pairings of 8 colors that can be selected from 9 possible options
51.		
	<b>Quantity A</b>	Quantity B
	The number of possible 4-person teams that can be selected from 6 people	The number of possible 2-person teams that can be selected from 6 people
52.		

**Quantity B** 

**Quantity A** 

The number of ways 1st, 2nd, and 3rd place prizes could be awarded to 3 out of 6 contestants

The number of ways 1st, 2nd, 3rd, 4th, and 5th place prizes could be awarded to 5 contestants

53. An inventory of coins contains 100 different coins.

## Quantity A

**Quantity B** 

The number of possible collections of 56 coins that can be selected where the order of the coins does not matter

The number of possible collections of 44 coins that can be selected where the order of the coins does not matter

54. An office supply store carries an inventory of 1,345 different products, all of which it categorizes as 'business use," 'personal use," or both. 740 products are categorized as 'business use" ONLY and 520 products are categorized as both 'business use" and 'personal use."

## Quantity A

**Quantity B** 

The number of products characterized as "personal use"

600

- 55. How many distinct 4-letter "words" can be made from the name "CHRISTYNA"? (A "word" is any arrangement of 4 letters regardless of whether it can be found in a dictionary.)
  - (A) 9
  - (B) 24
  - (C)36
  - (D) 504
  - (E) 3,024
- 56. Seiko has a 6-sided number cube with sides labeled 1 through 6. If she rolls the cube twice, what is the probability that the product of the two rolls is less than 36?
  - (A) 1/6
  - (B) 1/3
  - (C) 2/3
  - (D) 5/6
  - (E) 35/36
- 57. There is an 80% chance David will eat a healthy breakfast and a 25% chance that it will rain. If these events are independent, what is the probability that David will eat a healthy breakfast OR that it will rain?
  - (A) 20%
  - (B) 80%
  - (C) 85%
  - (D) 95%
  - (E) 105%
- 58. The probability of rain is 1/2 for every day next week. What is the chance that it rains on at least one day during the workweek (Monday through Friday)?
  - (A) 1/2
  - (B) 31/32
  - (C) 63/64
  - (D) 127/128

that the committee includes at least one man?
(A) 1/32
(B) 1/4
(C) 2/5
(D) 7/15
(E) 8/15
60. At Lexington High School, everyone takes at least one language — Spanish, French, or Latin — but no one takes all three languages. If 100 students take Spanish, 80 take French, 40 take Latin, and 22 take exactly two languages, how many students are there?
(A) 198
(B) 220
(C) 242
(D) 264
(E) 286
61.
Of 60 birds found in a certain location 20 are songbirds and 23 are migratory. (It is possible

for a songbird to be migratory, or not.)

**Quantity B** 

16

Quantity A

The number of the 60 birds that are neither migratory nor songbirds

59. Eight women and two men are available to serve on a committee. If three people are picked, what is the probability

(E) 5/2