

Assignment 9

Problem 1:

a. How many bits are there in the logical address?

To calculate the number of bits in the logical address, we need to consider both the page number and the offset:

1. Number of pages = $1024 = 2^{10}$, so we need 10 bits for the page number
2. Page size = 4 KB = 4096 bytes = 2^{12} bytes, so we need 12 bits for the offset

Total bits in logical address = bits for page number + bits for offset
= $10 + 12 = \mathbf{22 \text{ bits}}$

b. How many bits are there in the physical address?

For the physical address, we need to consider the frame number and the offset:

1. Number of frames = $256 = 2^8$, so we need 8 bits for the frame number
2. The offset remains the same as in the logical address: 12 bits

Total bits in physical address = bits for frame number + bits for offset
= $8 + 12 = \mathbf{20 \text{ bits}}$

c. What is the maximum amount of physical memory in this system?

To calculate the maximum amount of physical memory:

1. Number of frames = 256
2. Size of each frame = 4 KB = 4096 bytes

Maximum physical memory = Number of frames \times Size of each frame
= $256 \times 4096 \text{ bytes} = 1,048,576 \text{ bytes} = 1,024 \text{ KB} = \mathbf{1 \text{ MB}}$

Therefore, the maximum amount of physical memory in this system is 1 MB.

Problem 2:

Assuming a 2-KB page size (address 0.. 2047), we need to determine the page numbers and offsets for the given address references. To solve this, we'll use the following formula:

- Page number = Address / Page size
- Offset = Address % Page size

a. 3085

Page number = $3085 / 2048 = 1$, Offset = $3085 \% 2048 = 1037$

b. 42095

Page number = $42095 / 2048 = 20$, Offset = $42095 \% 2048 = 1135$

c. 215201

Page number = $215201 / 2048 = 105$, Offset = $215201 \% 2048 = 161$

d. 650000

Page number = $650000 / 2048 = 317$, Offset = $650000 \% 2048 = 784$

e. 2000001

Page number = $2000001 / 2048 = 976$, Offset = $2000001 \% 2048 = 1153$

f. 16479315

Page number = $16479315 / 2048 = 8046$, Offset = $16479315 \% 2048 = 1107$

Problem 3:

specifications:

- 21-bit virtual/logical address
- 16-bit physical address
- 2-KB page size

a. Conventional, single-level page table

1. Calculate the number of bits for page offset: 2 KB = 2048 bytes = 2^{11} bytes
So, we need 11 bits for the page offset
2. Calculate the number of bits for page number: Total bits in virtual address - Bits for page offset = $21 - 11 = 10$ bits
3. Calculate the number of entries: Number of entries = $2^{(\text{number of bits for page number})} = 2^{10} = 1024$ entries

Therefore, a conventional, single-level page table would have **1024 entries**.

b. Inverted page table

1. Calculate the number of bits for frame number: Total bits in physical address
- Bits for page offset = $16 - 11 = 5$ bits
2. Calculate the number of frames: Number of frames = $2^{(\text{number of bits for frame number})} = 2^5 = 32$ frames

Therefore, an inverted page table would have **32 entries**.

Problem 4:

a. If a memory reference takes 50 nanoseconds, how long does a paged memory reference take?

In a paging system with the page table stored in memory, each memory access requires two memory references:

1. One to access the page table
2. One to access the actual data

Therefore, the time for a paged memory reference is: Time = $2 \times$ Memory reference time

$$= 2 \times 50 = \mathbf{100 \text{ ns.}}$$

b. If we add TLBs, and if 75 percent of all page-table references are found in the TLBs, what is the effective memory reference time? (Assume that finding a page-table entry in the TLBs takes 2 nanoseconds if the entry is present.)

To calculate the effective memory reference time with TLBs, we need to consider two scenarios:

1. TLB hit (75% of the time): Time = TLB access + Memory access = $2 + 50 = 52$
2. TLB miss (25% of the time): Time = TLB access + Page table access + Memory access = $2 + 50 + 50 = 102$

Now, we can calculate the weighted average: Effective time = $(0.75 \times 52) + (0.25 \times 102)$

$$= 39 + 25.5 = \mathbf{64.5\ ns}$$