

Python list of list

$$a = \begin{bmatrix} [1, 2] & [3, 4] \end{bmatrix}$$

$$a[0] = [1, 2] \quad \begin{cases} a[0][0] = 1 \\ a[0][1] = 2 \end{cases}$$

$$a[1] = [3, 4] \quad \begin{cases} a[1][0] = 3 \\ a[1][1] = 4 \end{cases}$$

$$A = \begin{bmatrix} [1, 2] & , & [3, 4] \end{bmatrix}$$

Seen as matrix

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$\phi = \left[\begin{array}{l} [1, 2, 3], [4, 5, 6], [7, 8, 9], \\ [10, 11, 12] \end{array} \right]$$

$$= \left[\begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \end{array} \right]$$

Many matrix operation will fail if we use
default list of list Python

$a = \begin{bmatrix} 1, 2 \\ 3, 4 \end{bmatrix}$

instead we use numpy array

$a = \text{numpy.array} \begin{bmatrix} 1, 2 \\ 3, 4 \end{bmatrix}$

to represent matrix

$$a = [[1, 2], [3, 4]]$$

$$a = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$a[0, 1] = \begin{matrix} \text{0th row} \\ \text{1st column} \end{matrix} = 2$$

$$\begin{matrix} \text{0th row} \\ \vdots \\ a[0, \vdots] \end{matrix}$$

$$\begin{matrix} \text{from 0th column} \\ \text{to last column} \\ \vdots \\ \end{matrix}$$

$z[1]$

| | | | | | | |
|---|---|---|---|---|---|---|
| | 0 | 1 | 2 | 3 | 4 | 5 |
| 0 | a | b | c | d | e | f |
| 1 | g | h | i | j | k | l |
| 2 | m | n | o | p | q | r |

$z[:, 2]$

row = 0 to last column

$= ["c", "i", "o"]$

2nd row
1st column
 $z[2, 1] = "n"$

1st row
1st to 3rd column
 $z[1, 1:3] = ["h", "i"]$

Object Oriented

class Student

~~int age~~

~~String name~~

setAge (self, num)

self.age = num

setNation (self, country_name)

nation = country_name

Instance

Student A

name: Aody

age: 19

Student B

name: Bob

age: 20

StudentA.nation

→ "Germany"

Student

→ nation = "Germany"

| | 0 | 1 | 2 | 3 | 4 |
|---|----|----|----|----|----|
| 0 | 0 | 1 | 2 | 3 | 4 |
| 1 | 10 | 11 | 12 | 13 | 14 |
| 2 | 20 | 21 | 22 | 23 | 24 |
| 3 | 30 | 31 | 32 | 33 | 34 |
| 4 | 40 | 41 | 42 | 43 | 44 |

`A[1:4, 1:4]`

row = from $i=1$ to $i=3$

col = from $i=1$ to $i=3$

`A[::2, ::2]`

row from $i=0$ to last
step every 2 element

column from $i=0$ to last
step every 2 element

array as index

| | 0 | 1 | 2 | 3 | 4 |
|---|----|----|----|----|----|
| 0 | 0 | 1 | 2 | 3 | 4 |
| 1 | 10 | 11 | 12 | 13 | 14 |
| 2 | 20 | 21 | 22 | 23 | 24 |
| 3 | 30 | 31 | 32 | 33 | 34 |
| 4 | 40 | 41 | 42 | 43 | 44 |

row_idx = [3, 2, 3]

$A[[0, 2]]$

row 0 row 2

$\begin{bmatrix} 0 & 1 & 2 & 3 & 4 \\ 20 & 21 & 22 & 23 & 24 \end{bmatrix}$

$A[\text{row_idx}]$

row 3 $\begin{bmatrix} 30 & 31 & 32 & 33 & 34 \end{bmatrix}$
row 2 $\begin{bmatrix} 20 & 21 & 22 & 23 & 24 \end{bmatrix}$
row 3 $\begin{bmatrix} 30 & 31 & 32 & 33 & 34 \end{bmatrix}$

$= A[[3, 2, 3]]$

row 3 row 2 row 3

```
[[ 0,  1,  2,  3,  4],  
 [10, 11, 12, 13, 14],  
 [20, 21, 22, 23, 24],  
 [30, 31, 32, 33, 34],  
 [40, 41, 42, 43, 44]]
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$A[[1, 2], [3, 3]]$

row 1 column 3

row 2 column 3

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

$$B = \begin{bmatrix} 11 & 12 & 13 \\ 14 & 15 & 16 \\ 17 & 18 & 19 \end{bmatrix}$$

$$\rightarrow A + 2 = \cancel{A} = \begin{bmatrix} 1+2 & 2+2 & 3+2 \\ 4+2 & 5+2 & 6+2 \\ 7+2 & 8+2 & 9+2 \end{bmatrix} = \begin{bmatrix} 3 & 4 & 5 \\ 6 & 7 & 8 \\ 9 & 10 & 11 \end{bmatrix}$$

$$\rightarrow A * B = \cancel{A} = \begin{bmatrix} 1 \times 11 & 2 \times 12 & 3 \times 13 \\ 4 \times 14 & 5 \times 15 & 6 \times 16 \\ 7 \times 17 & 8 \times 18 & 9 \times 19 \end{bmatrix} = \begin{bmatrix} 11 & 24 & 39 \end{bmatrix}$$

$$\langle w, x \rangle = \sum w_i x_i \quad \|x\| = \sqrt{\langle x, x \rangle} = \sqrt{\sum x_i^2}$$

$$w = [1, 2, 3] \quad x = [4, 4, 5]$$

$$\begin{aligned} \text{np.dot}(w, x) &= 1 \cdot 4 + 2 \cdot 4 + 3 \cdot 5 \\ &= 27 \end{aligned}$$

$$\begin{aligned} w * x &= [1 \times 4 \quad 2 \times 4 \quad 3 \times 5] \\ &= [4 \quad 8 \quad 8] \end{aligned}$$

