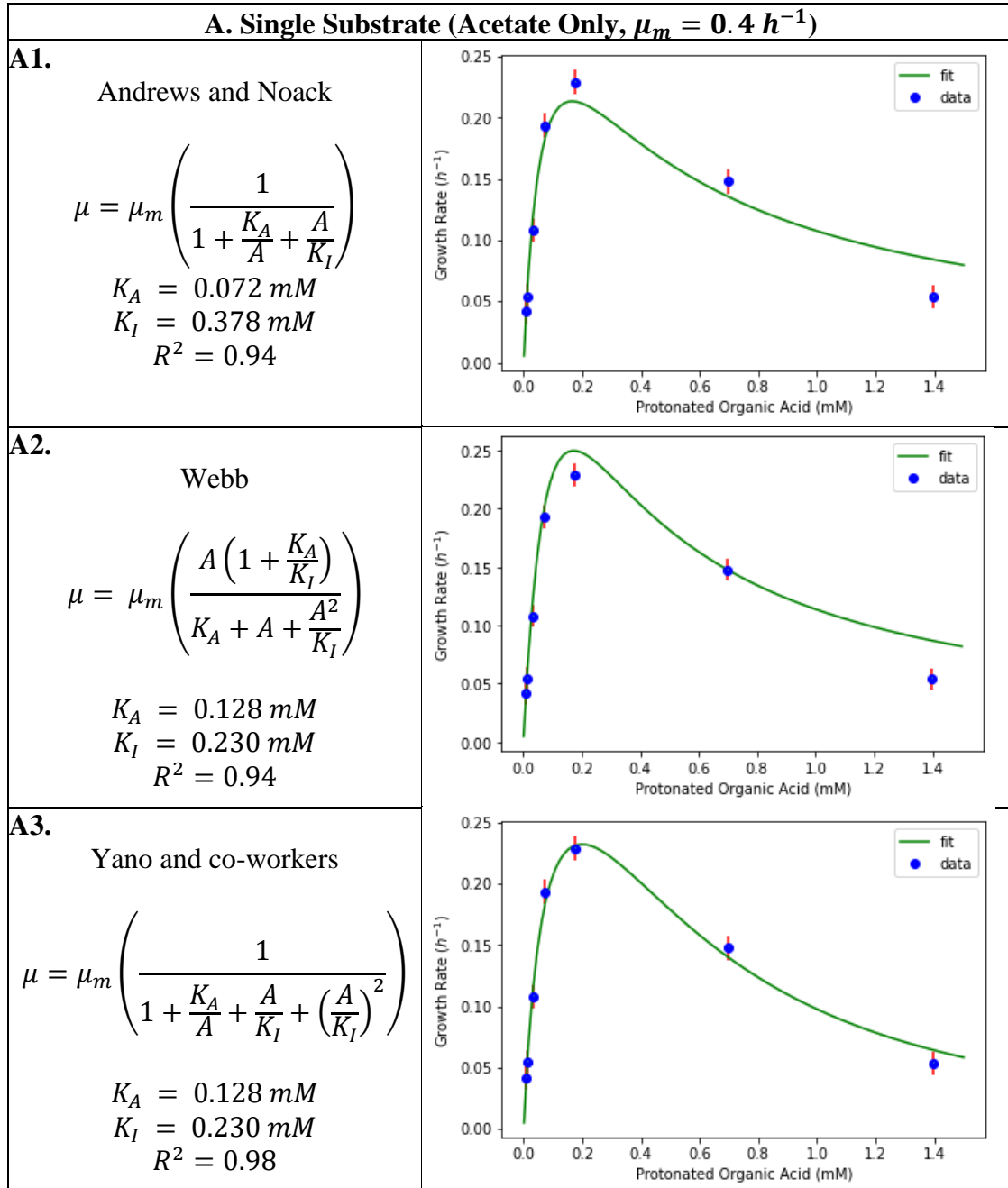


Supplementary material sheet 1. (A) Parameterized inhibition model fits for acetate as sole substrate. **(B)** Parameterized inhibition model fits for acetate as a product with glucose as the main substrate. References for model equations can be found in Han and Levenspiel, 1988.

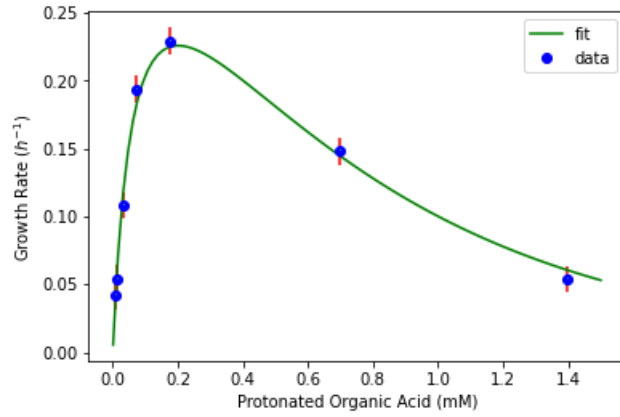


A4.

Aiba and co-workers

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right) e^{-\frac{A}{K_I}}$$

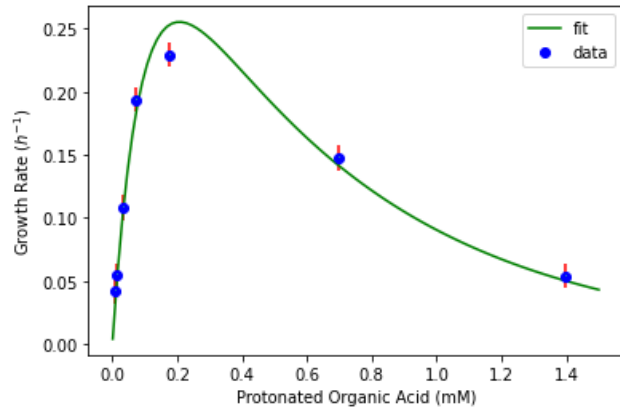
$$\begin{aligned} K_A &= 0.0723 \text{ mM} \\ K_I &= 0.760 \text{ mM} \\ R^2 &= 0.98 \end{aligned}$$

**A5.**

Tessier-Type

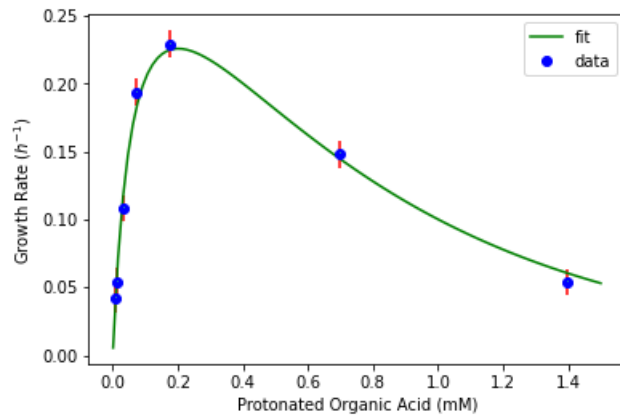
$$\mu = \mu_m \left[e^{-\frac{A}{K_I}} - e^{-\frac{A}{K_A}} \right]$$

$$\begin{aligned} K_A &= 0.0885 \text{ mM} \\ K_I &= 0.672 \text{ mM} \\ R^2 &= 0.97 \end{aligned}$$

**A6.**Webb (with σ)

$$\mu = \mu_m \left(\frac{A}{A + K_A \left(1 + \frac{\sigma}{K_I} \right)} \right) e^{1.17\sigma A}$$

$$\begin{aligned} K_A &= 0.846 \text{ mM} \\ K_I &= 1.23 \text{ mM} \\ \sigma &= -1.12 \text{ mM} \\ R^2 &= 0.98 \end{aligned}$$



A7.

Wayman and Tseng

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right), A < A'$$

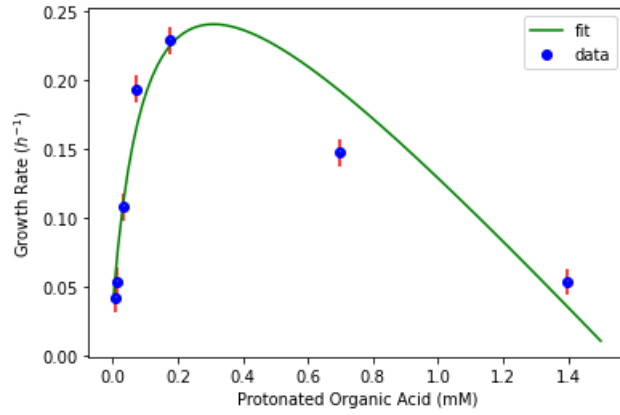
$$\mu = \mu_m \left(\frac{A}{K_A + A} \right) - K_I(A - A'), A > A'$$

$$A' = 0.139 \text{ mM}$$

$$K_A = 0.124 \text{ mM}$$

$$K_I = 0.659 \text{ mM}$$

$$R^2 = 0.88$$

**A8.**

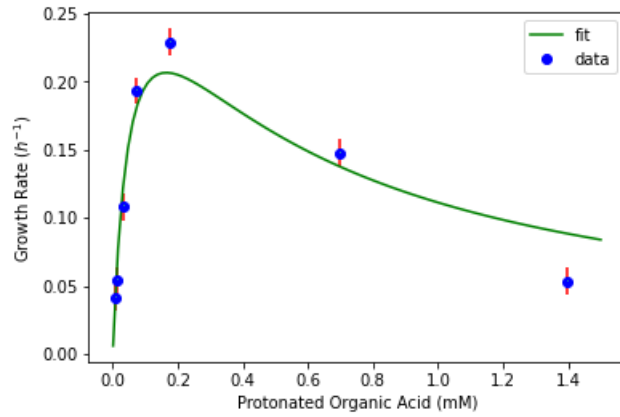
Classic model

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right) \left(\frac{K_I}{K_I + A} \right)$$

$$K_A = 0.0644 \text{ mM}$$

$$K_I = 0.421 \text{ mM}$$

$$R^2 = 0.92$$



B. Multiple Substrate (Acetate and Glucose, $\mu_m = \mu_G = 0.65 \text{ h}^{-1}$, $\mu_A = 0.4 \text{ h}^{-1}$, $K_G = 0.005 \text{ mM}$)

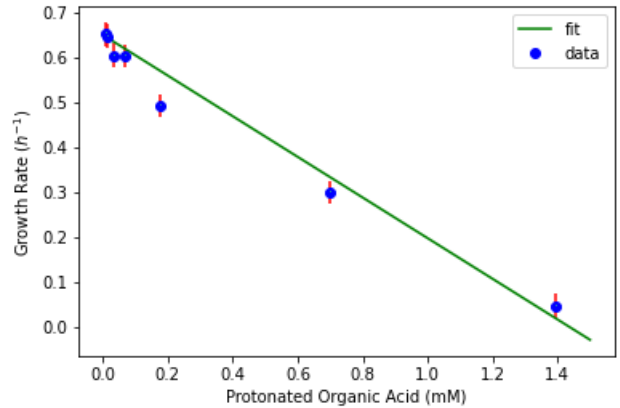
B1.

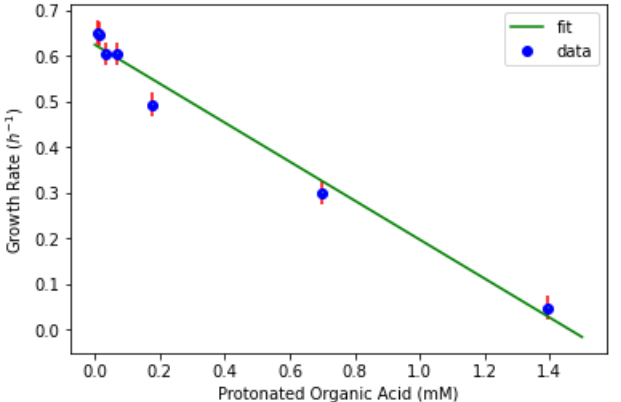
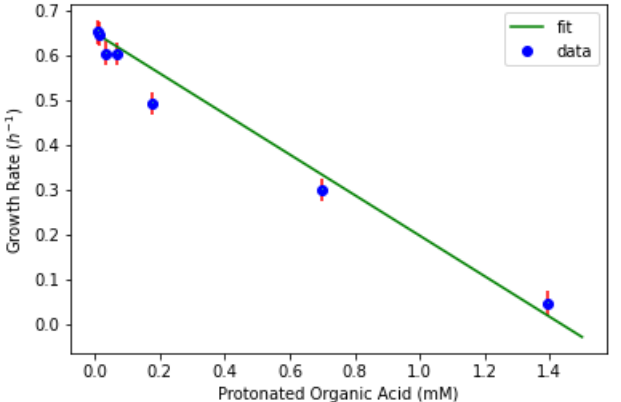
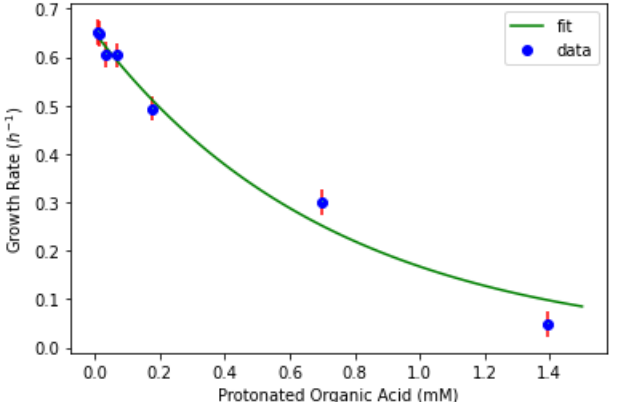
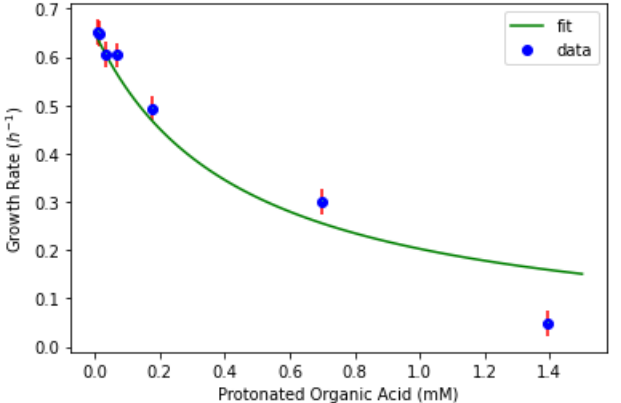
Dagley and Hinshelwood

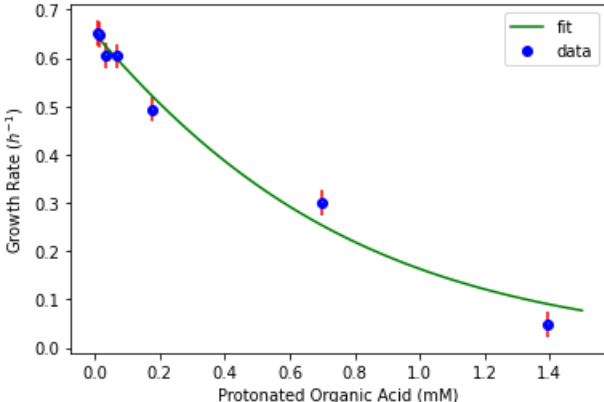
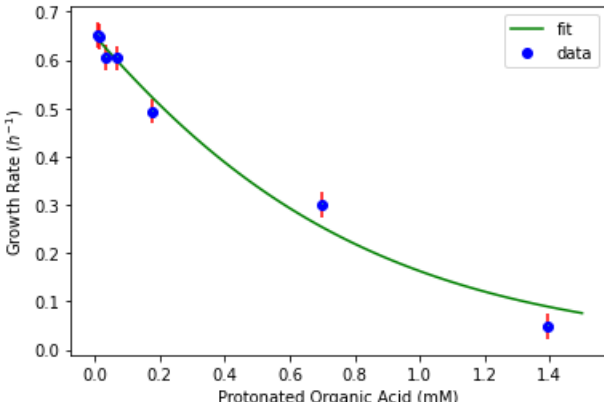
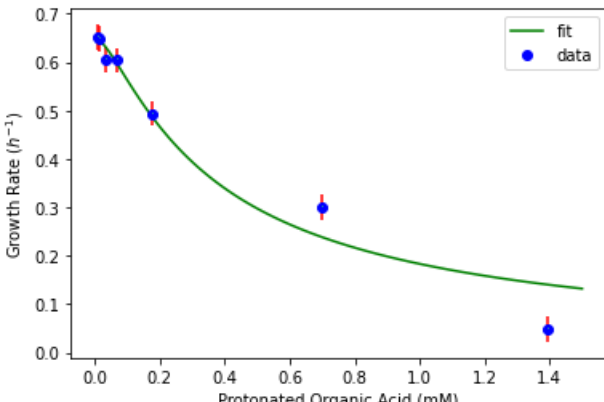
$$\mu = \mu_m \left(\frac{G}{K_G + G} \right) (1 - KA)$$

$$K = 0.696 \text{ mM}^{-1}$$

$$R^2 = 0.97$$



<p>B2. Holzberg and co-workers</p> $\mu = \mu_m - K(A - K_I)$ $K = 0.427 \text{ h}^{-1}$ $K_I = -0.060 \text{ mM}$ $R^2 = 0.98$	 <p>Graph showing Growth Rate (h^{-1}) versus Protonated Organic Acid (mM). The data points (blue circles with error bars) show a linear decrease in growth rate as the concentration of protonated organic acid increases. A green line represents the fit to the data.</p>
<p>B3. Ghose and Tyagi</p> $\mu = \mu_m \left(1 - \frac{A}{A^*}\right) \left(\frac{G}{K_G + G}\right)$ $A^* = 1.44 \text{ mM}$ $R^2 = 0.97$	 <p>Graph showing Growth Rate (h^{-1}) versus Protonated Organic Acid (mM). The data points (blue circles with error bars) show a linear decrease in growth rate as the concentration of protonated organic acid increases. A green line represents the fit to the data.</p>
<p>B4. Aiba and co-workers</p> $\mu = \mu_m \left(\frac{G}{K_G + G}\right) e^{-KA}$ $K = 1.356 \text{ mM}^{-1}$ $R^2 = 0.98$	 <p>Graph showing Growth Rate (h^{-1}) versus Protonated Organic Acid (mM). The data points (blue circles with error bars) show a non-linear decrease in growth rate as the concentration of protonated organic acid increases. A green line represents the fit to the data.</p>
<p>B5. Jerusalimsky and Neronova</p> $\mu = \mu_m \left(\frac{G}{K_G + G}\right) \left(\frac{K_I}{K_I + A}\right)$ $K_I = 0.453 \text{ mM}$ $R^2 = 0.95$	 <p>Graph showing Growth Rate (h^{-1}) versus Protonated Organic Acid (mM). The data points (blue circles with error bars) show a non-linear decrease in growth rate as the concentration of protonated organic acid increases. A green line represents the fit to the data.</p>

<p>B6. Aiba and co-workers dual substrate derivative</p> $\mu = \left[\mu_G \left(\frac{G}{K_G + G} \right) + \mu_A \left(\frac{A}{K_A + A} \right) \right] e^{-\alpha A}$ $K_A = 1.54 \text{ mM}$ $\alpha = 1.60 \text{ mM}^{-1}$ $R^2 = 0.98$	
<p>B7. Aiba and co-workers dual substrate derivative (single μ)</p> $\mu = \mu_m \left[\left(\frac{G}{K_G + G} \right) + \left(\frac{A}{K_A + A} \right) \right] e^{-\alpha A}$ $K_A = 2.06 \text{ mM}$ $\alpha = 1.67 \text{ mM}^{-1}$ $R^2 = 0.98$	
<p>B8. Classic model dual substrate derivative</p> $\mu = \left[\mu_G \left(\frac{G}{K_G + G} \right) + \mu_A \left(\frac{A}{K_A + A} \right) \right] \left(\frac{K_I}{K_I + A} \right)$ $K_A = 0.145 \text{ mM}$ $K_I = 0.224 \text{ mM}$ $R^2 = 0.96$	

B9.

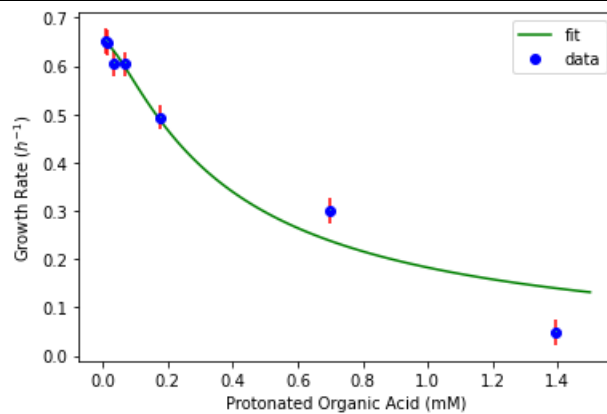
Classic model dual substrate
derivative
(single μ)

$$\mu = \mu_m \left[\left(\frac{G}{K_G + G} \right) + \left(\frac{A}{K_A + A} \right) \right] \left(\frac{K_I}{K_I + A} \right)$$

$$K_A = 0.186 \text{ mM}$$

$$K_I = 0.180 \text{ mM}$$

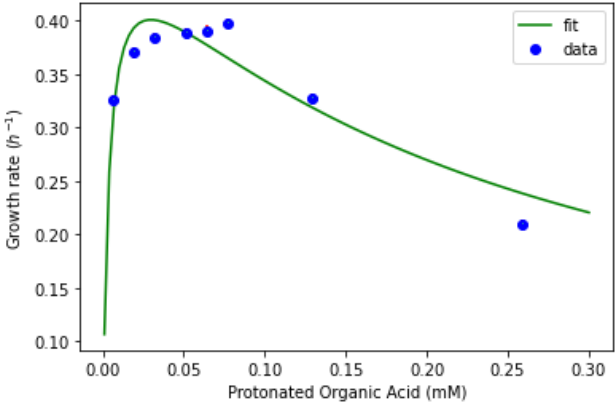
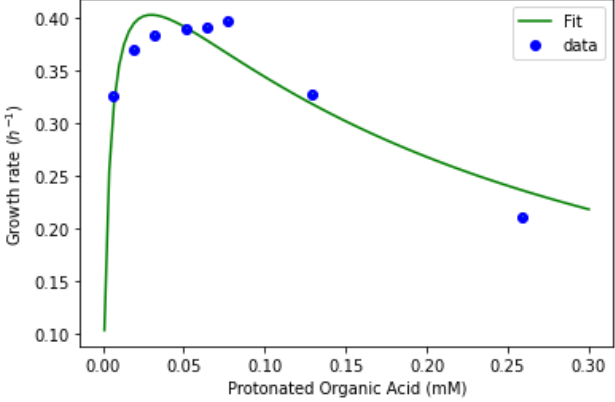
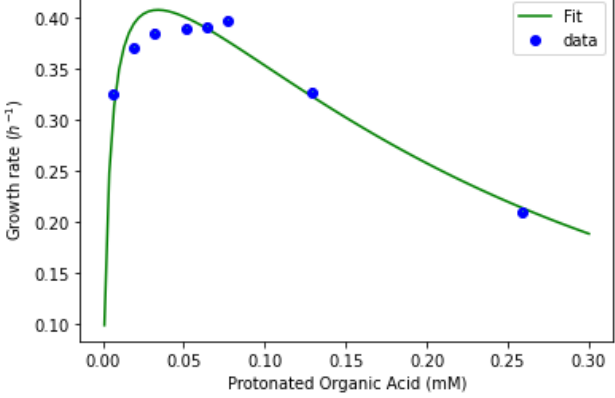
$$R^2 = 0.96$$

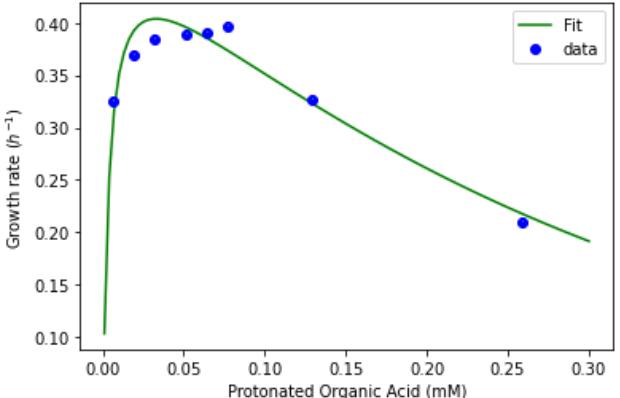
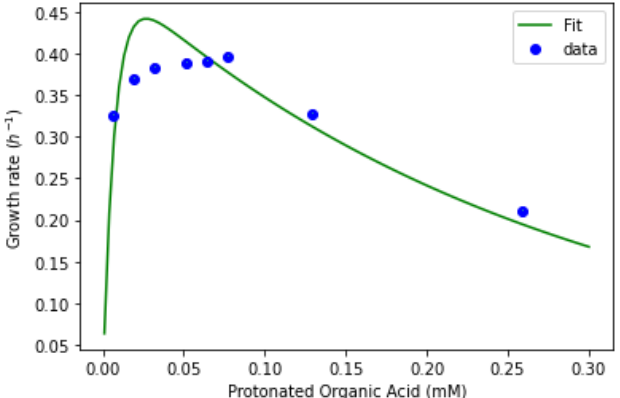
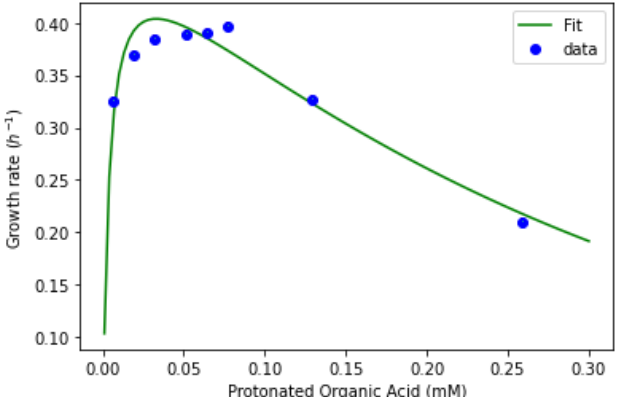
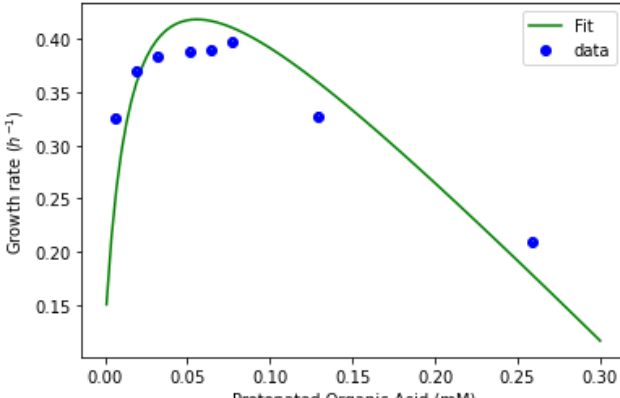


Supplemental Table S2. (A) Parameterized inhibition model fits for lactate as sole substrate.

(B) Parameterized inhibition model fits for lactate as a dual substrate with glucose. References

for model equations can be found in Han and Levenspiel, 1988.

A. Single Substrate (Lactate Only, $\mu_m = 0.5$)	
<p>A1.</p> <p>Andrews and Noack</p> $\mu = \mu_m \left(\frac{1}{1 + \frac{K_L}{L} + \frac{L}{K_I}} \right)$ <p> $K_L = 0.0037 \text{ mM}$ $K_I = 0.239 \text{ mM}$ $R^2 = 0.89$ </p>	
<p>A2.</p> <p>Webb</p> $\mu = \mu_m \left(\frac{L \left(1 + \frac{K_L}{K_I} \right)}{K_L + L + \frac{L^2}{K_I}} \right)$ <p> $K_L = 0.00393 \text{ mM}$ $K_I = 0.227 \text{ mM}$ $R^2 = 0.89$ </p>	
<p>A3.</p> <p>Yano and co-workers</p> $\mu = \mu_m \left(\frac{1}{1 + \frac{K_L}{L} + \frac{L}{K_I} + \left(\frac{L}{K_I} \right)^2} \right)$ <p> $K_L = 0.0040 \text{ mM}$ $K_I = 0.343 \text{ mM}$ $R^2 = 0.92$ </p>	

<p>A4. Aiba and co-workers</p> $\mu = \mu_m \left(\frac{L}{K_L + L} \right) e^{-\frac{L}{K_I}}$ $K_L = 0.00382 \text{ mM}$ $K_I = 0.317 \text{ mM}$ $R^2 = 0.93$	
<p>A5. Tessier-Type</p> $\mu = \mu_m \left[e^{-\frac{L}{K_I}} - e^{-\frac{L}{K_L}} \right]$ $K_L = 0.00712 \text{ mM}$ $K_I = 0.275 \text{ mM}$ $R^2 = 0.64$	
<p>A6. Webb (with σ)</p> $\mu = \mu_m \left(\frac{L}{L + K_L \left(1 + \frac{\sigma}{K_I} \right)} \right) e^{1.17L\sigma}$ $K_L = 0.00050 \text{ mM}$ $K_I = -0.41 \text{ mM}$ $\sigma = -2.70 \text{ mM}$ $R^2 = 0.93$	
<p>A7. Wayman and Tseng</p> $\mu = \mu_m \left(\frac{L}{K_L + L} \right), L < L'$ $\mu = \mu_m \left(\frac{L}{K_L + L} \right) - K_I(L - L'), L > L'$ $L' = 0.078 \text{ mM}$ $K_L = 0.0169 \text{ mM}$ $K_I = 3.21 \text{ mM}$ $R^2 = 0.66$	

A8.

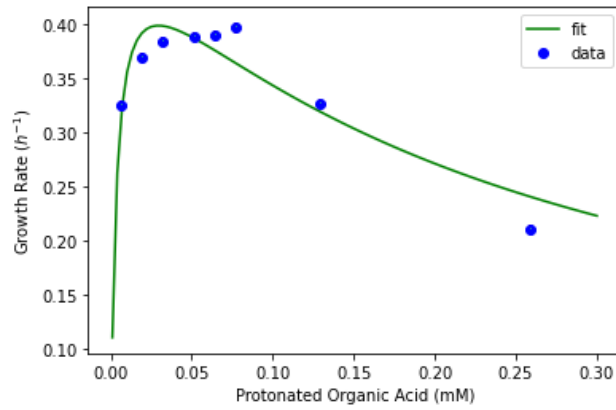
Classic Model

$$\mu = \mu_m \left(\frac{L}{L + K_L} \right) \left(\frac{K_I}{K_I + L} \right)$$

$$K_L = 0.0035 \text{ mM}$$

$$K_I = 0.246 \text{ mM}$$

$$R^2 = 0.89$$



B. Multiple Substrate (Lactate and Glucose, $\mu_m = \mu_G = 0.65$, $\mu_L = 0.5$, $K_G = 0.005$)

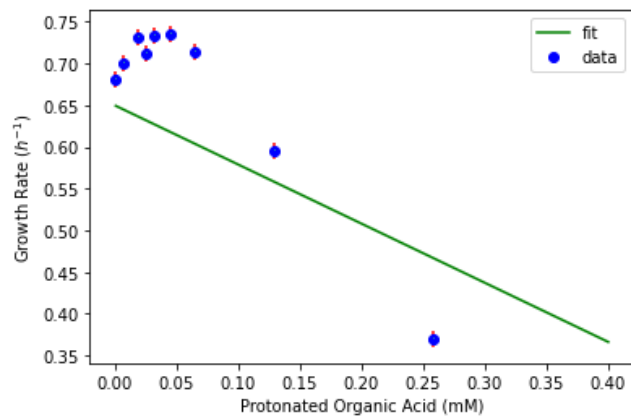
B1.

Dagley and Hinshelwood

$$\mu = \mu_m \left(\frac{G}{K_G + G} \right) (1 - KL)$$

$$K = 1.092 \text{ mM}$$

$$R^2 = 0.4$$

**B2.**

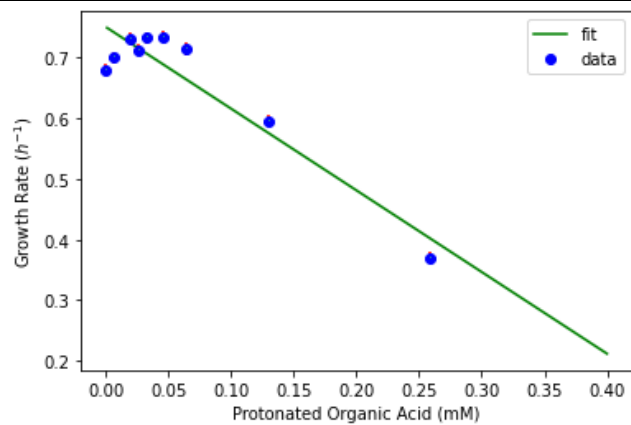
Holzberg and co-workers

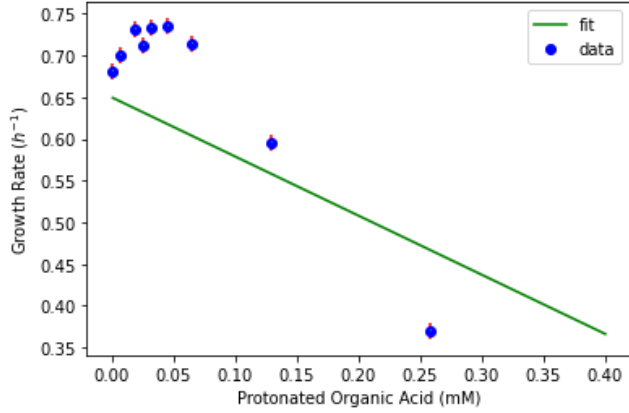
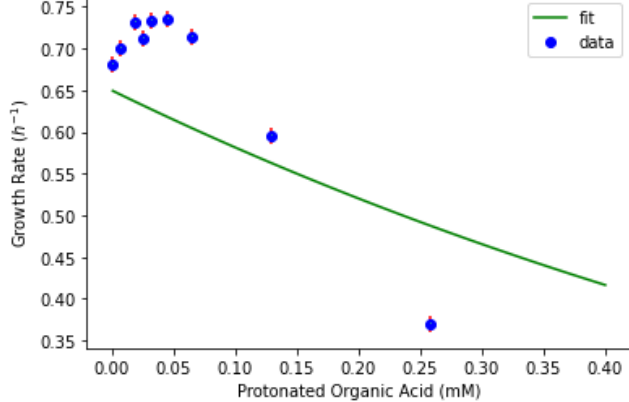
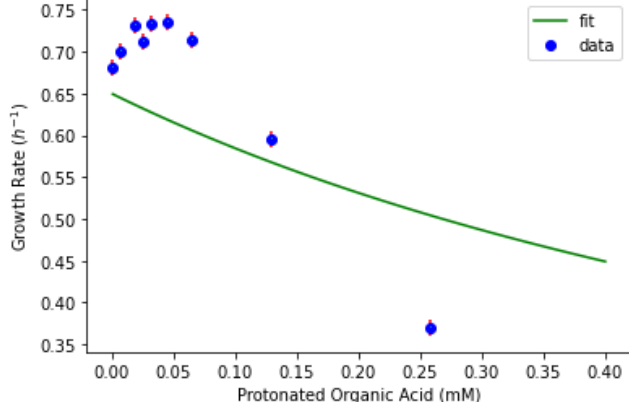
$$\mu = \mu_m - K(L - K_I)$$

$$K = 1.347 \text{ mM}$$

$$K_I = 0.075 \text{ mM}$$

$$R^2 = 0.88$$



<p>B3.</p> <p>Ghose and Tyagi</p> $\mu = \mu_m \left(1 - \frac{L}{L^*}\right) \left(\frac{G}{K_G + G}\right)$ $L^* = 0.916 \text{ mM}$ $R^2 = 0.40$	
<p>B4.</p> <p>Aiba and co-workers</p> $\mu = \mu_m \left(\frac{G}{K_G + G}\right) e^{-KL}$ $K = 1.11 \text{ mM}^{-1}$ $R^2 = 0.36$	
<p>B5.</p> <p>Jerusalimsky and Neronova</p> $\mu = \mu_m \left(\frac{G}{K_G + G}\right) \left(\frac{K_I}{K_I + L}\right)$ $K_I = 0.894 \text{ mM}$ $R^2 = 0.33$	
<p>B6.</p> <p>Aiba and co-workers dual substrate derivative (single μ)</p> $\mu = \mu_m \left[\left(\frac{G}{K_G + G}\right) + \left(\frac{L}{K_L + L}\right) \right] e^{-\alpha L}$ $K_L = 0.0743 \text{ mM}$ $\alpha = 4.44 \text{ mM}^{-1}$	