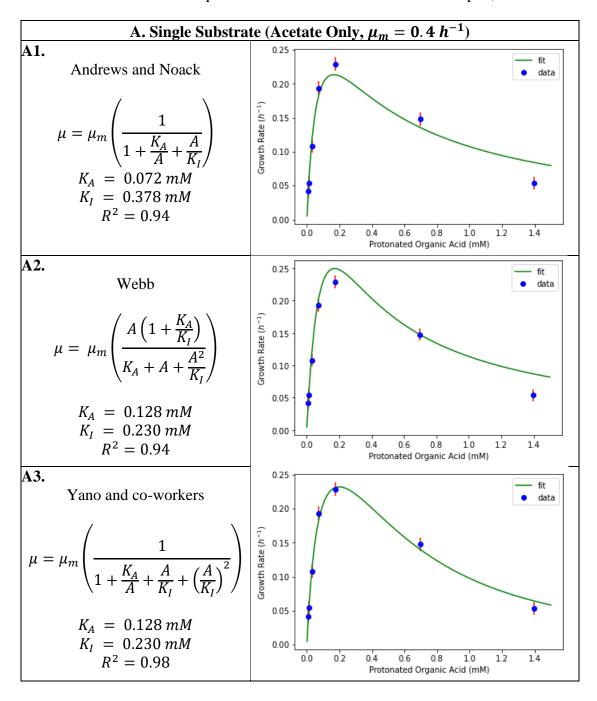
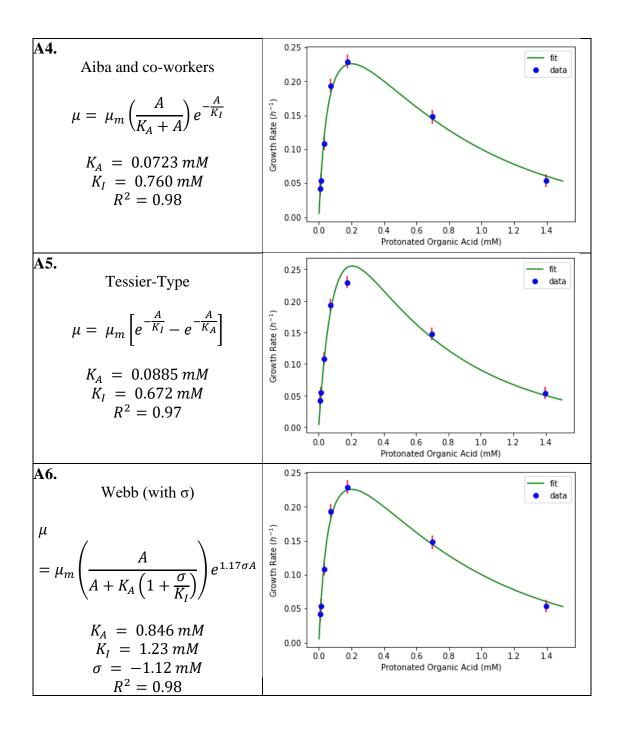
Supplemental Table S1. (A) Parameterized inhibition model fits for acetate as sole substrate.

(B) Parameterized inhibition model fits for acetate as a product with glucose as the main substrate. References for model equations can be found in Han and Levenspiel, 1988.







Wayman and Tseng

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right), A < A'$$

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right), A < A'$$

$$\mu = \mu_m \left(\frac{A}{K_A + A} \right) - K_I (A - A'),$$

$$A > A'$$

$$A' = 0.139 \, mM$$

$$K_A = 0.124 \, mM$$

$$K_A = 0.124 \, mM$$

 $K_I = 0.659 \, mM$
 $R^2 = 0.88$

A8.

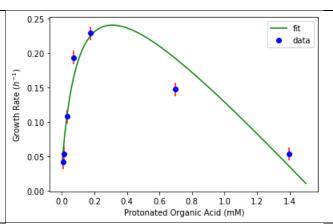


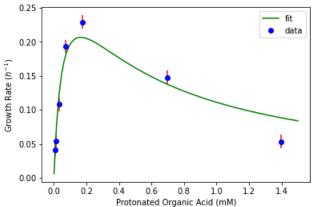
$$\mu = \mu_m \left(\frac{A}{K_A + A} \right) \left(\frac{K_I}{K_I + A} \right)$$

$$K_A = 0.0644 \, mM$$

$$K_A = 0.0644 \, mM$$

 $K_I = 0.421 \, mM$
 $R^2 = 0.92$





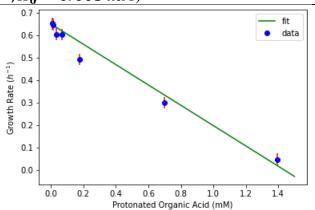
B. Multiple Substrate (Acetate and Glucose, $\mu_m = \mu_G = 0.65 \ h^{-1}$, $\mu_A =$ $0.4 h^{-1}, K_G = 0.005 mM$

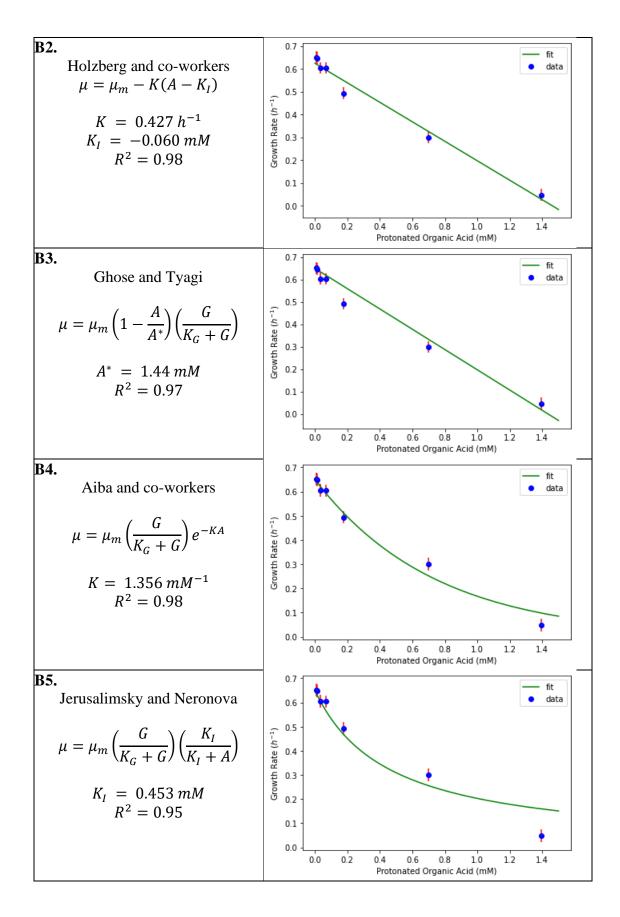
B1.

Dagley and Hinshelwood

$$\mu = \mu_m \left(\frac{G}{K_G + G} \right) (1 - KA)$$

$$K = 0.696 \, mM^{-1}$$
$$R^2 = 0.97$$





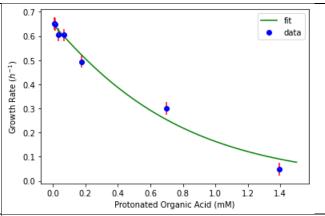
B6.

Aiba and co-workers dual substrate derivative

$$\mu = \left[\mu_G \left(\frac{G}{K_G + G}\right) + \mu_A \left(\frac{A}{K_A + A}\right)\right] e^{-\alpha A}$$

$$K_A = 1.54 \, mM$$

 $\alpha = 1.60 \, mM^{-1}$
 $R^2 = 0.98$



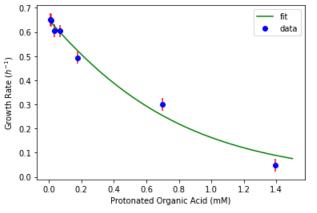
B7.

Aiba and co-workers dual substrate derivative (single μ)

$$\mu = \mu_m \left[\left(\frac{G}{K_G + G} \right) + \left(\frac{A}{K_A + A} \right) \right] e^{-\alpha A}$$

$$K_A = 2.06 \, mM$$

 $\alpha = 1.67 \, mM^{-1}$
 $R^2 = 0.98$



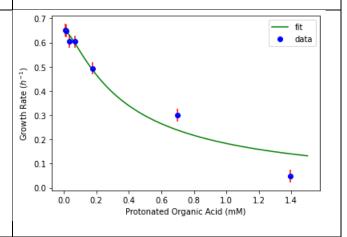
B8.

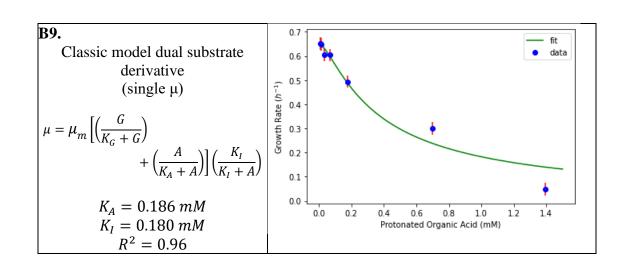
Classic model dual substrate derivative

$$\begin{split} & \mu \\ & = \left[\mu_G \left(\frac{G}{K_G + G} \right) \right. \\ & + \left. \mu_A \left(\frac{A}{K_A + A} \right) \right] \left(\frac{K_I}{K_I + A} \right) \end{split}$$

$$K_A = 0.145 \ mM$$

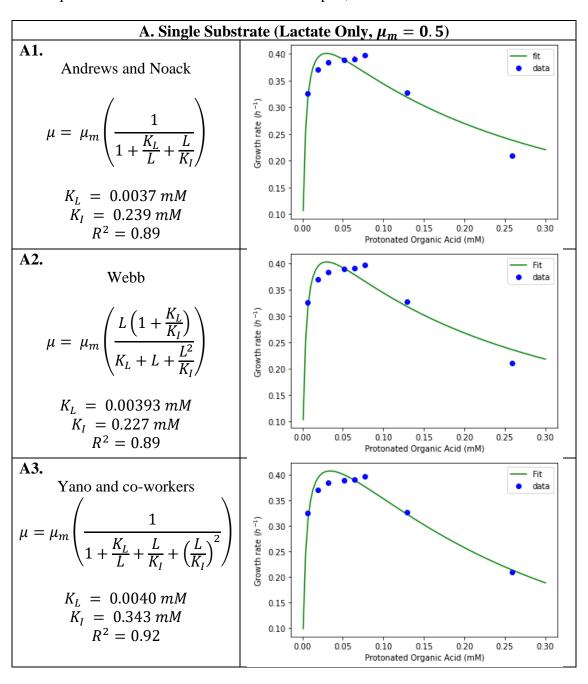
 $K_I = 0.224 \ mM$
 $R^2 = 0.96$

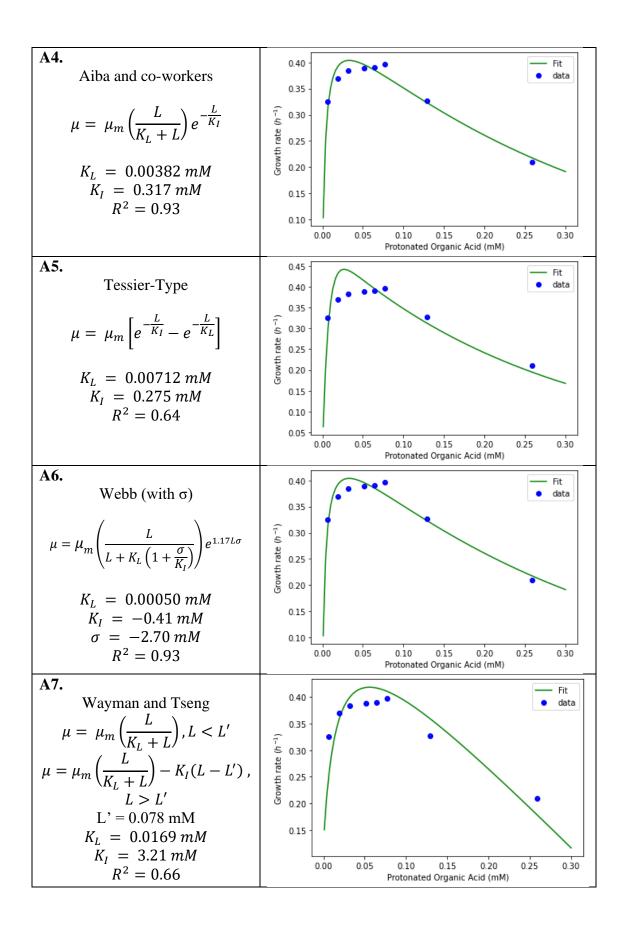




Supplemental Table S2. (A) Parameterized inhibition model fits for lactate as sole substrate.

(B) Parameterized inhibition model fits for lactate as a dual substrate with glucose. References for model equations can be found in Han and Levenspiel, 1988.





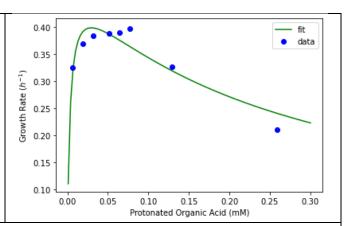
A8.

Classic Model

$$\mu = \mu_m \left(\frac{L}{L + K_L}\right) \left(\frac{K_I}{K_I + L}\right)$$

$$K_L = 0.0035 \ mM$$

 $K_I = 0.246 \ mM$
 $R^2 = 0.89$



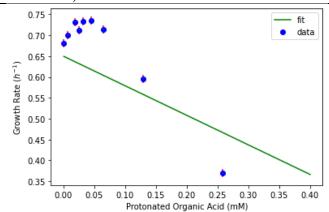
B. Multiple Substrate (Lactate and Glucose, $\mu_m = \mu_G = 0.65$, $\mu_L = 0.5$, $K_G = 0.005$)

B1.

Dagley and Hinshelwood

$$\mu = \mu_m \left(\frac{G}{K_G + G} \right) (1 - KL)$$

$$K = 1.092 \, mM$$
$$R^2 = 0.4$$



B2.

Holzberg and co-workers

$$\mu = \mu_m - K(L - K_I)$$

$$K = 1.347 \, mM$$

 $K_I = 0.075 \, mM$
 $R^2 = 0.88$

