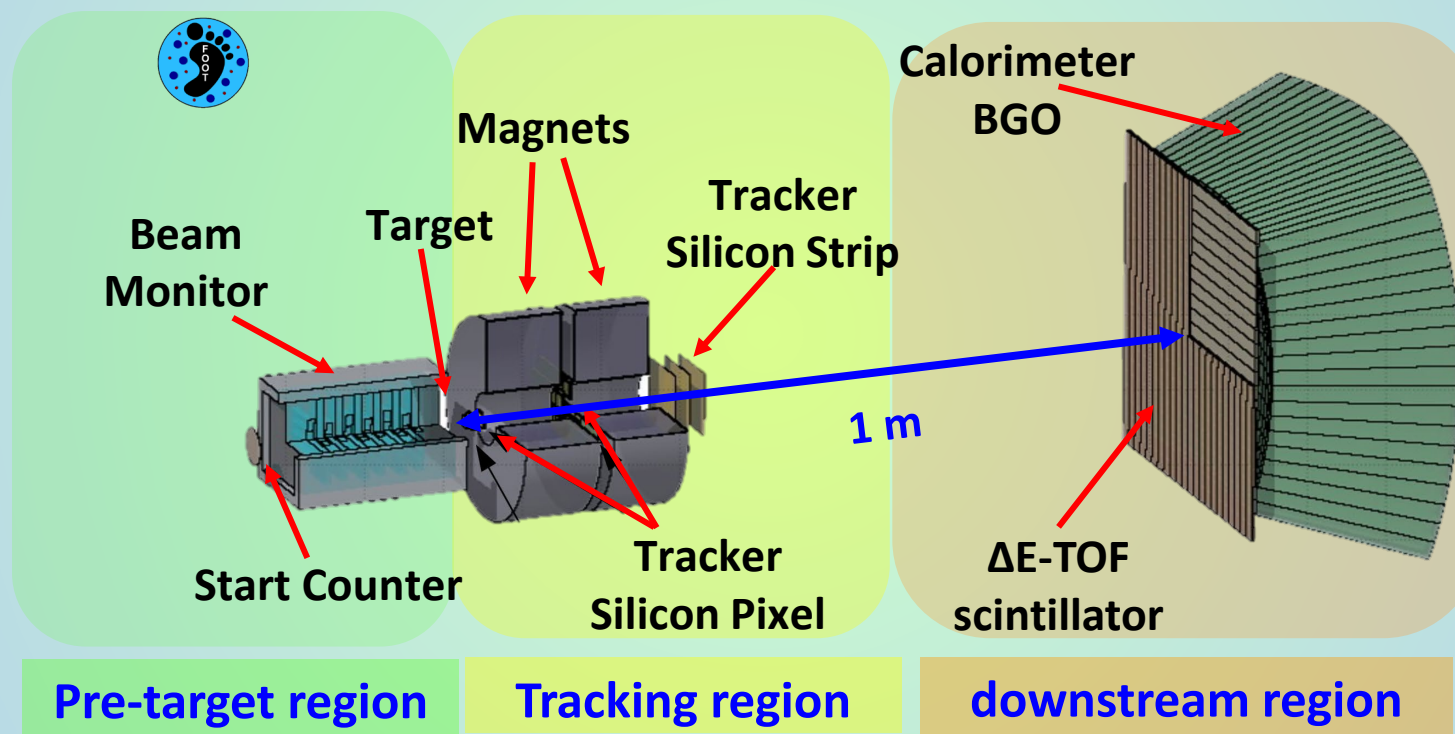


FOOT: FragmentatiOn Of Target Experiment



Hadrontherapy

FOOT goals

Radioprotection in space

Target fragmentation

- ❑ $d\sigma/dE$ and $d\sigma/d\omega$ with 5% precision of the fragment production X sections in inverse kinematics
- ❑ p, C, O beams
- ❑ Hadrontherapy energies (200-400 MeV/u)

Projectile fragmentation

- ❑ same but in direct kinematics



detailed knowledge of the fragmentation processes to optimize the spacecraft shielding (long term mission)



- ❑ $d\sigma/dE$ and $d\sigma/d\omega$ with 5% precision of the fragment production X sections in direct and inverse kinematics
- ❑ p, He, Li, C, O beams (the most common in space)
- ❑ Radioprotection energies (around 700 MeV/u)

Radiobiology request: to have a more precise **TPS** Treatment Planning System

FOOT approved by the INFN on September 2017 (CSN3)

INFN sections/labs:



92 members (60% staff):

- ❑ 10 INFN Sections
- ❑ 5 laboratories: Frascati, CNAO, Trento, GSI, IPHC (Strasbourg)
- ❑ 12 Italian Universities
- ❑ 2 foreign Universities: Aachen, Nagoya
- ❑ Centro Fermi

Physics program:

- ❑ Hadrontherapy:
 - ❑ Nuclear fragmentation @ 200 MeV/u
- ❑ Radioprotection in Space:
 - ❑ Nuclear fragmentation @ 700 MeV/u

Hadrontherapy vs Radiotherapy

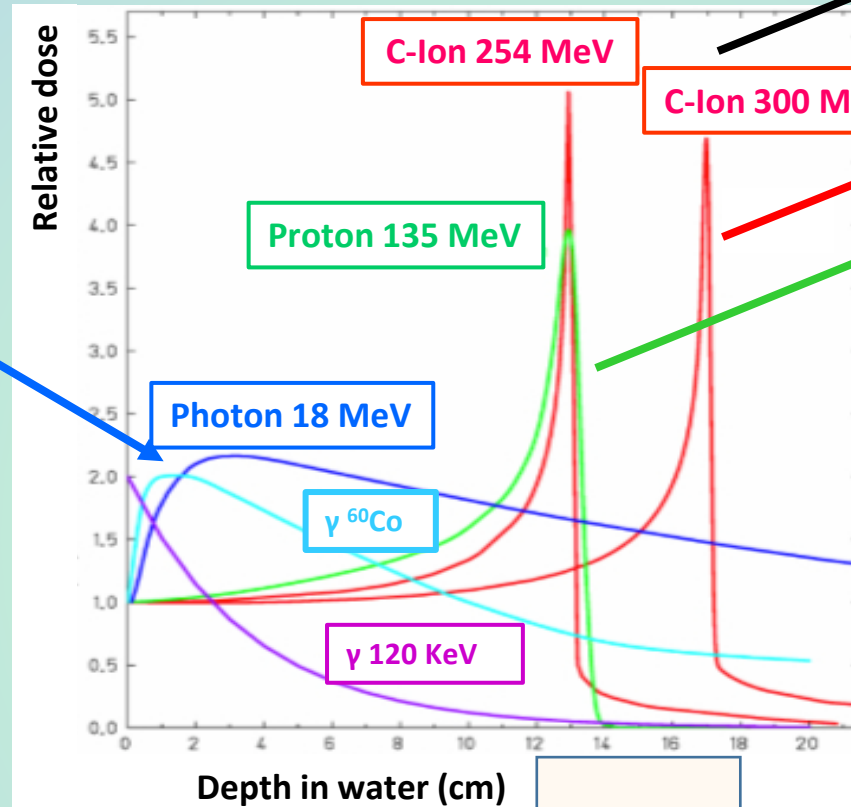
Gamma

- ☐ Photoelectric ($\sim Z^4/E^3$)
- ☐ Compton ($\sim Z/E$)
- ☐ Pair prod ($\sim Z^2/\ln E$)

Pros and cons

- ☐ dose release maximum at the end
- ☐ Penetration depends on energy
- ☐ Hadron > efficient than γ
- ☐ Hadron < damage outside tumor
- ☐ MORE expensive than γ

R. Spighi: FOOT experiment

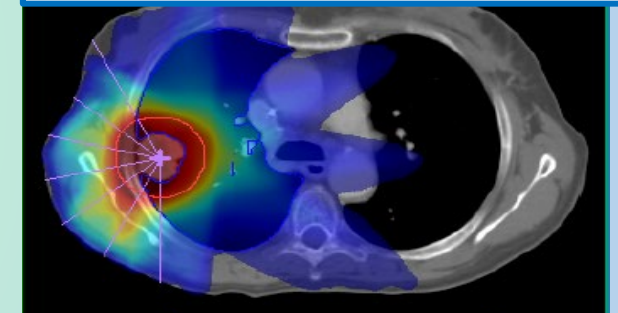


Bragg Peak

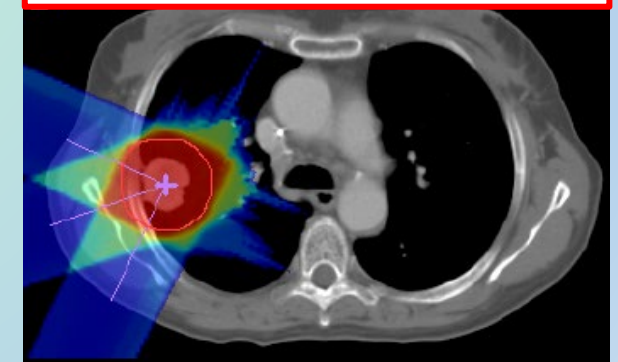
Proton/charged ion

- ☐ Ionization
- ☐ Excitation
- ☐ Bremsstrahlung
- ☐ Fragmentation

Radiotherapy, IMRT 7 fields

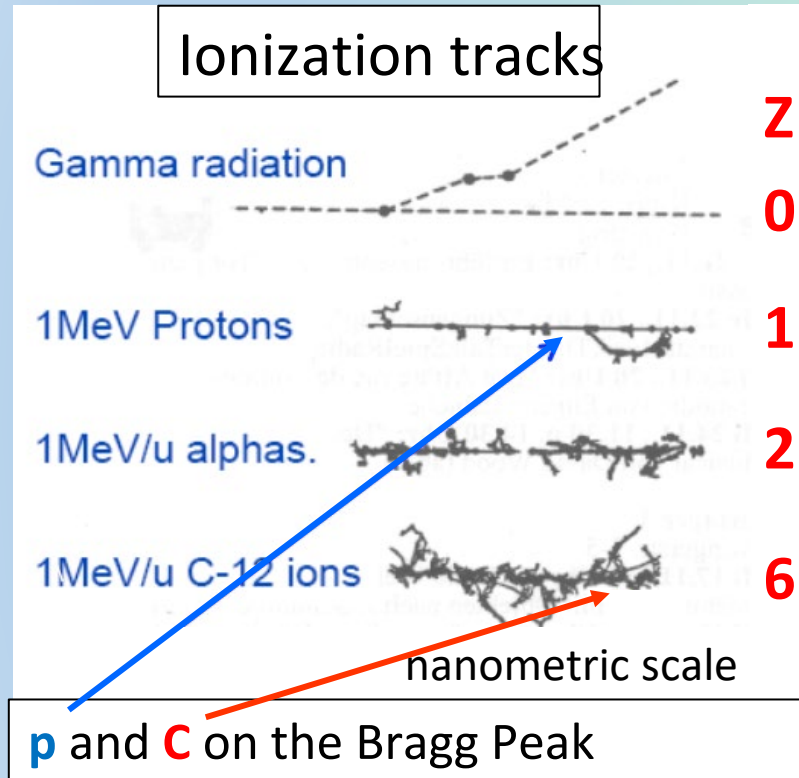


Hadrontherapy, proton



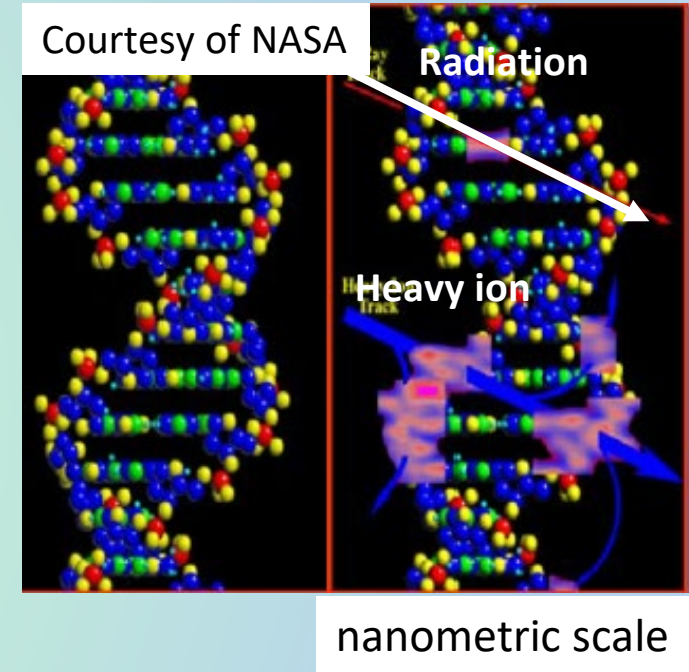
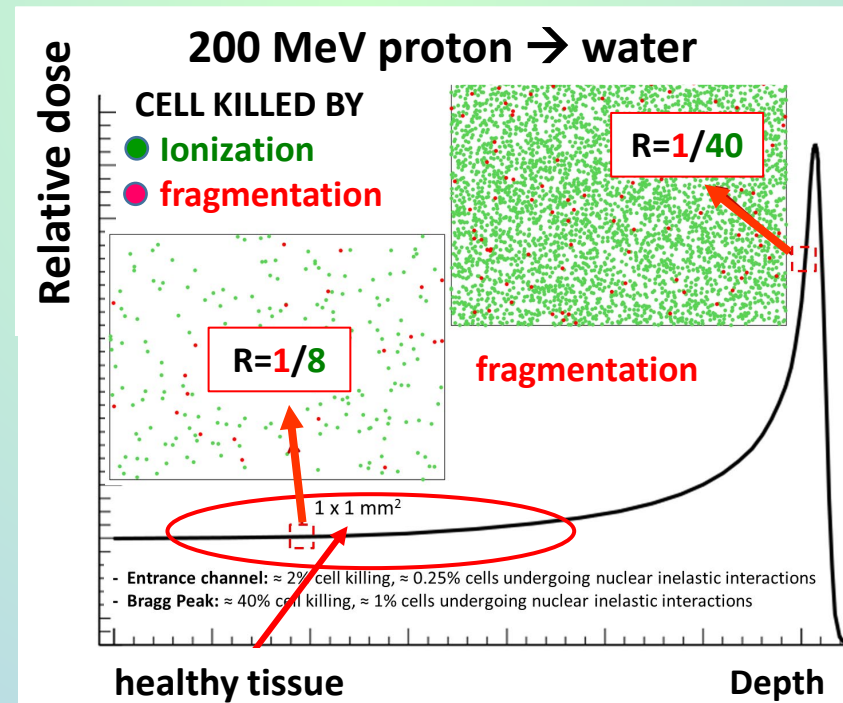
Damage on DNA

Tumor is a cellular alteration → not controlled proliferation → stop the proliferation → damage on DNA



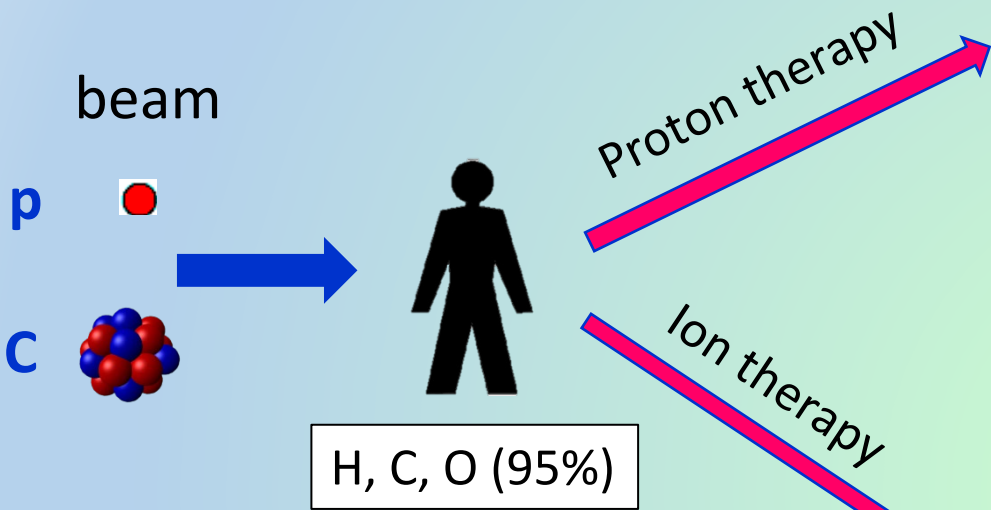
Higher Z → Higher damage

but, necessary to know the
Nuclear fragmentation cross sections



Double strand break →
irreparable damage

Target-Projectile fragmentation



- $p + H$
- $p + C,O \rightarrow$ target fragments
low Energy \rightarrow **low range**

No fragmentation

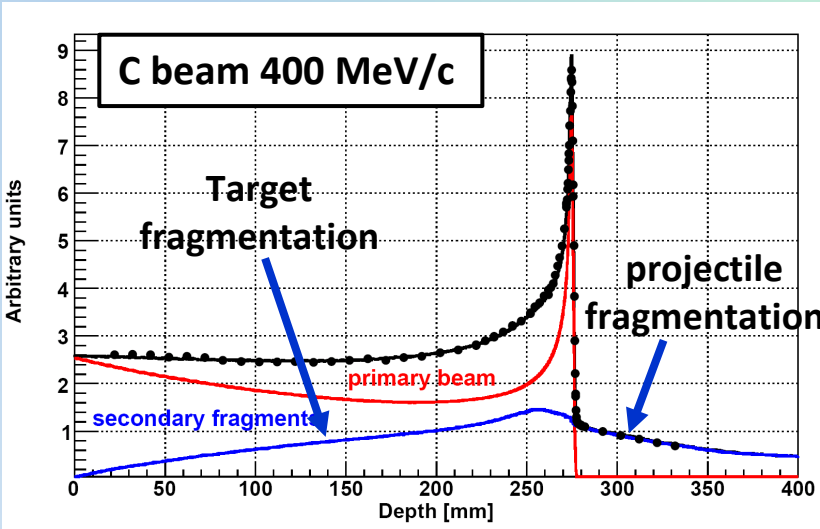
Target fragmentation

Fragment	E (MeV)	LET (keV/μm)	Range (μm)
¹⁵ O	1.0	983	2.3
¹⁵ N	1.0	925	2.5
¹⁴ N	2.0	1137	3.6
¹³ C	3.0	951	5.4
¹² C	3.8	912	6.2
¹¹ C	4.6	878	7.0
¹⁰ B	5.4	643	9.9
⁸ Be	6.4	400	15.7
⁶ Li	6.8	215	26.7
⁴ He	6.0	77	48.5
³ He	4.7	89	38.8
² H	2.5	14	68.9

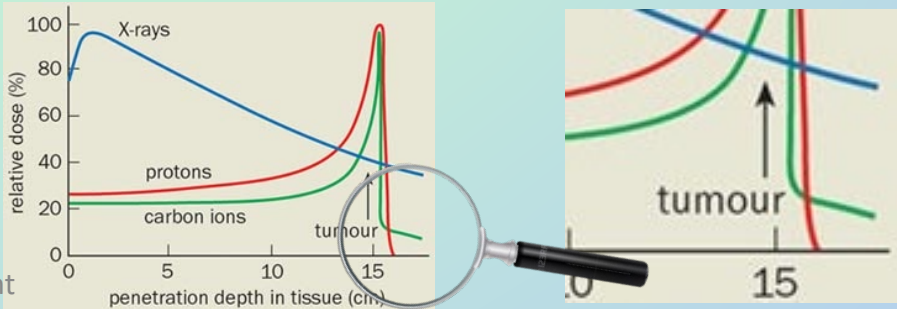
- $C + H \rightarrow$ projectile fragments
High Energy \rightarrow **Long range**
- $C + C,O \rightarrow$ target/projectile fragments

Projectile fragmentation

both



R. Spighi: FOOT experiment



Tail present only when using Carbon

FOOT MAIN GOAL: Target fragmentation in proton therapy



Target fragments remain in the target



Impossible to detect fragments

DIRECT KINEMATIC

proton
200 MeV



C, O at rest



INVERSE KINEMATIC



C, O 200 MeV/A



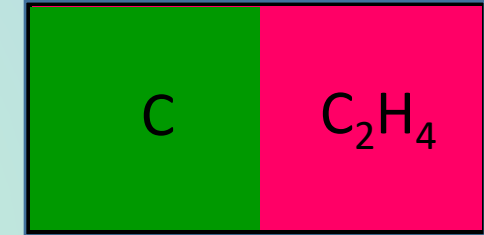
Proton (H)
at rest



A the end
Lorentz boost

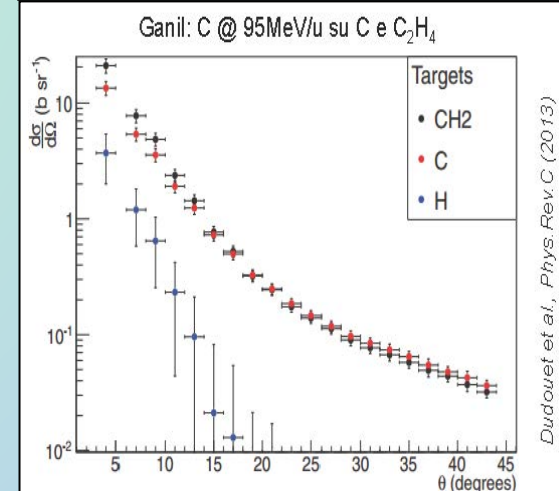


Target (2mm)



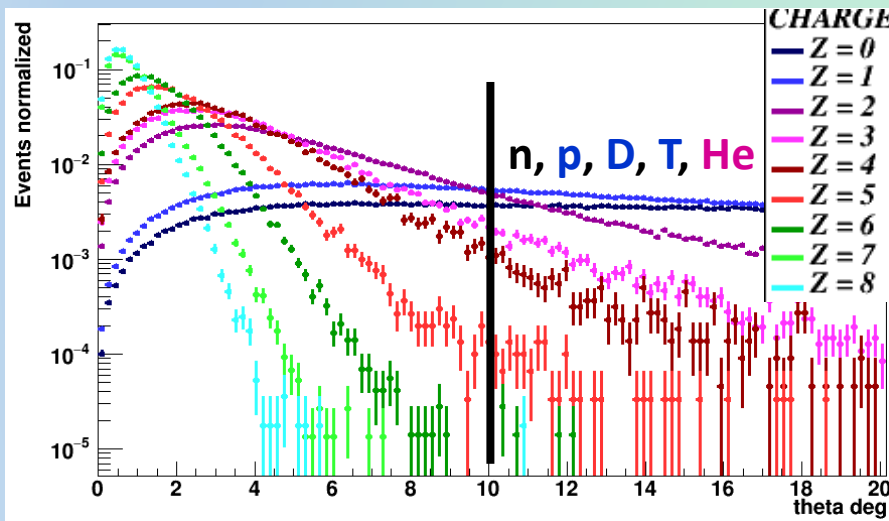
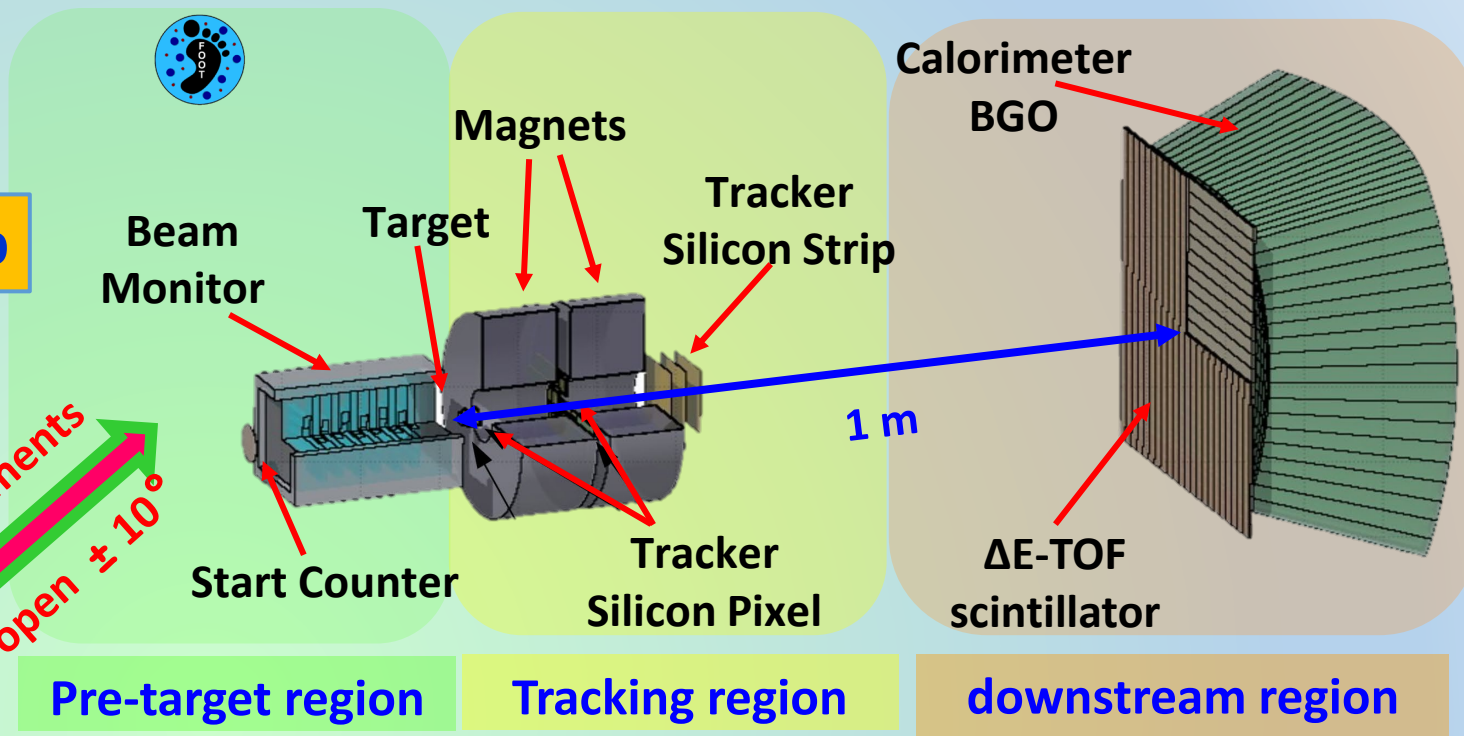
$$\frac{d\sigma}{dE_{kin}}(H) = \frac{1}{4} \left(\frac{d\sigma}{dE_{kin}}(C_2H_4) - 2 \frac{d\sigma}{dE_{kin}}(C) \right)$$

Ganil experimental data



FOOT Detector (in construction)

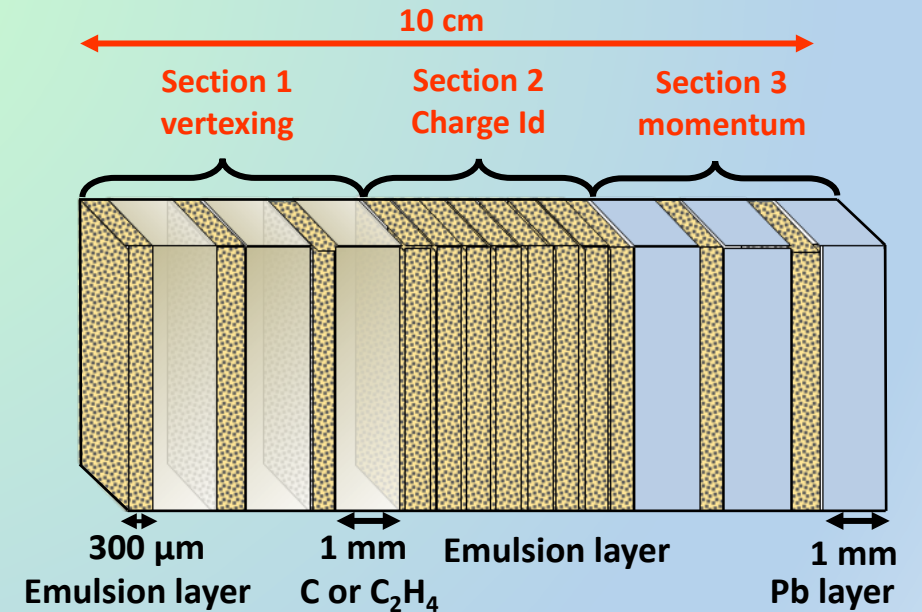
Electronic Setup



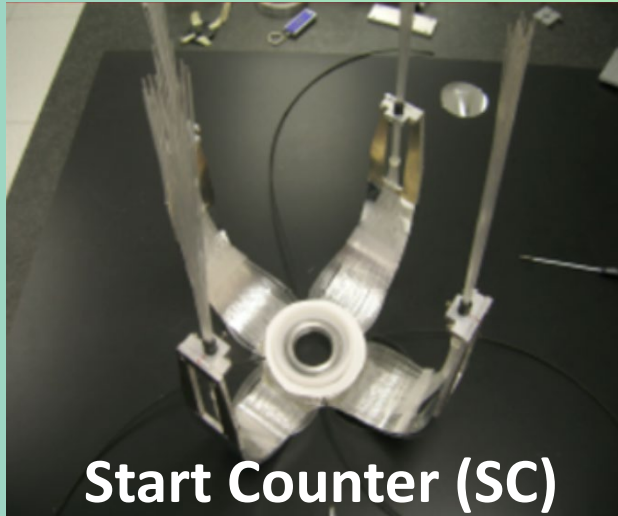
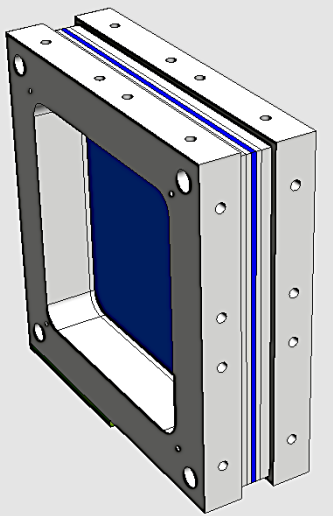
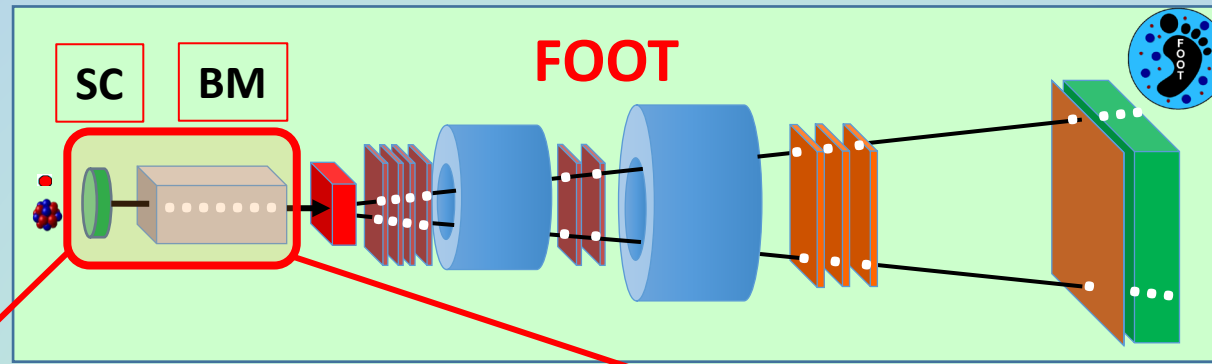
Heavy fragments
Angular open $\pm 10^\circ$

Light fragments
Angular open $\pm 70^\circ$

Emulsion Chamber Setup



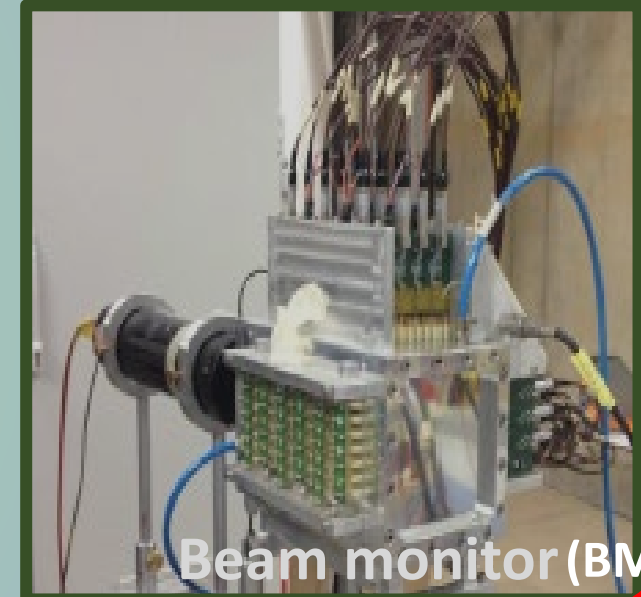
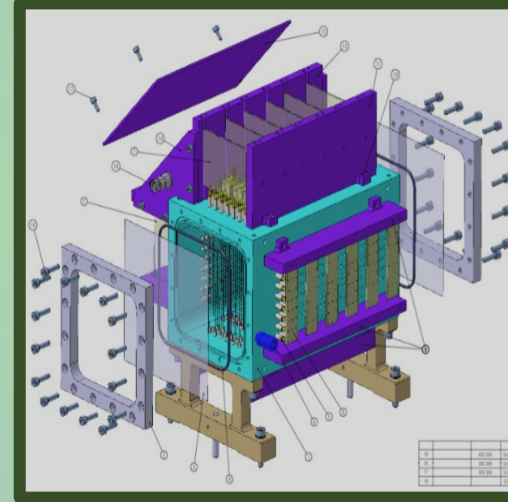
Pre target region



Start Counter (SC)

Trigger and ToF start

250 μm –1 mm thick plastic scintillator (depending on E beam)
50 mm radius
~ 400 optical fibers \rightarrow 4 bundles to 4 PMTs
Test beam in september in Trento



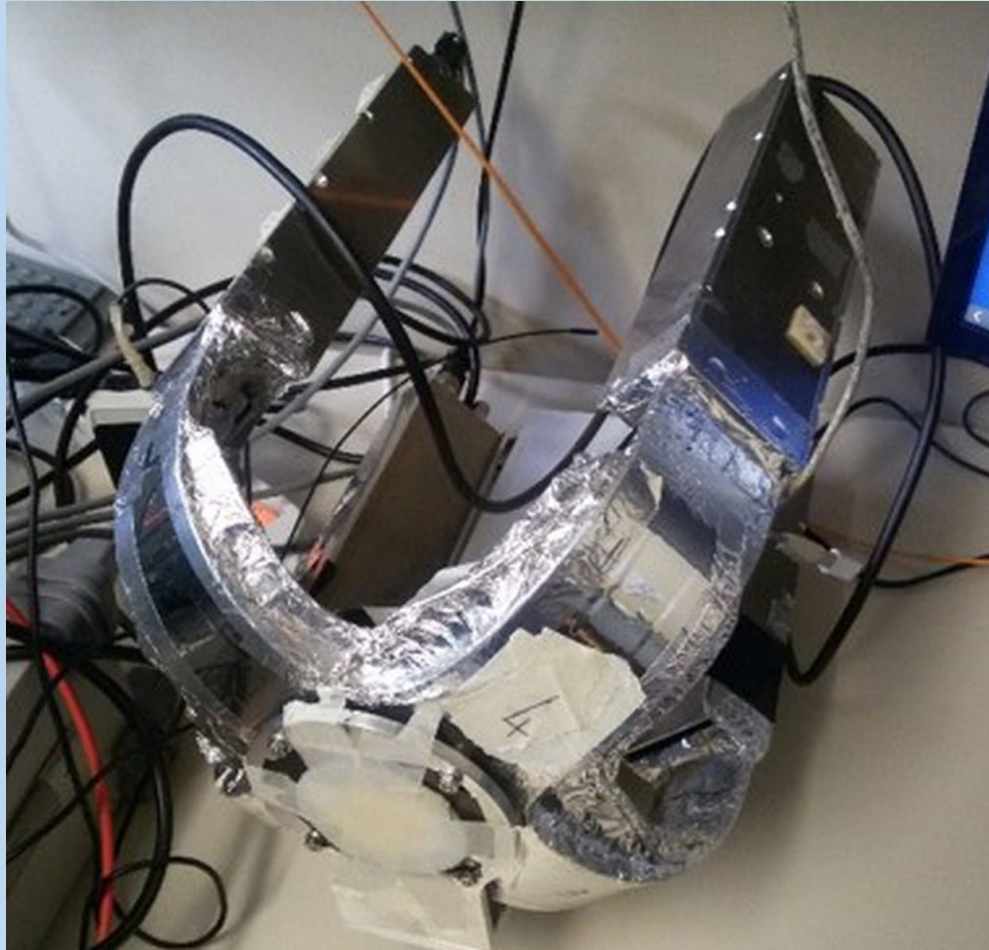
Beam monitor (BM)

Beam momentum/direction & fragmentation in SC

Drift chamber
Gas: Ar/Co₂ (80/20%)
Test beam in september in Trento

Start Counter

Margherita

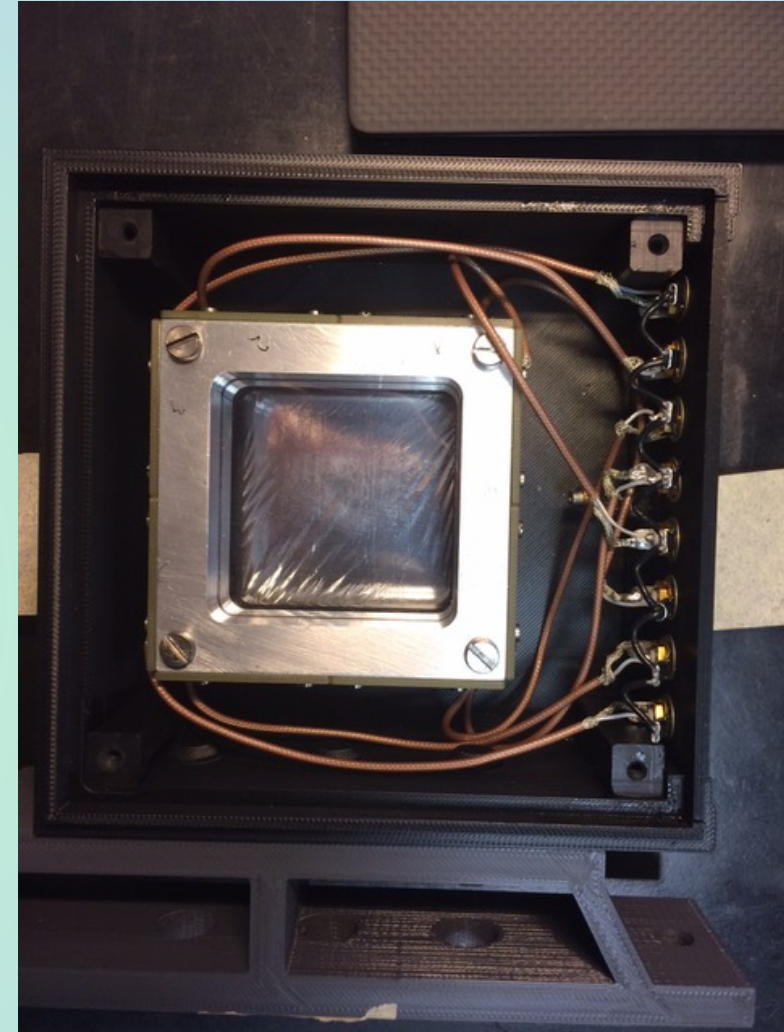


R. Spighi: FOOT experiment

SiPM



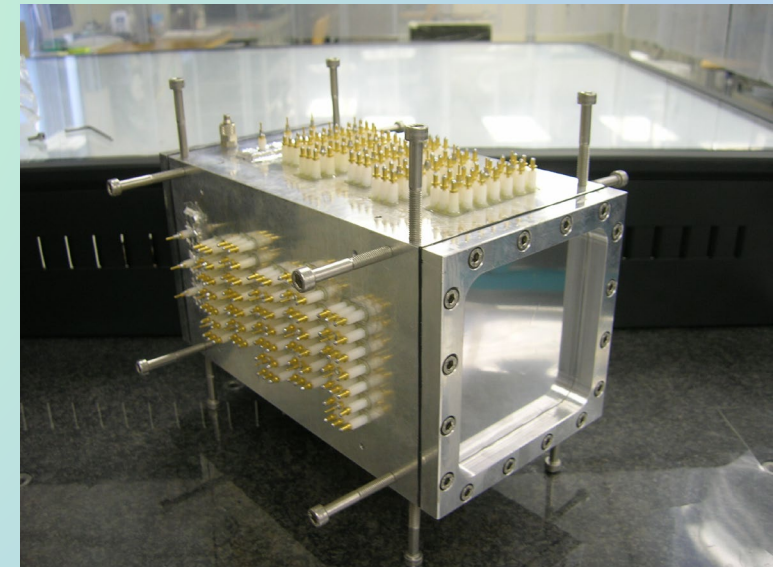
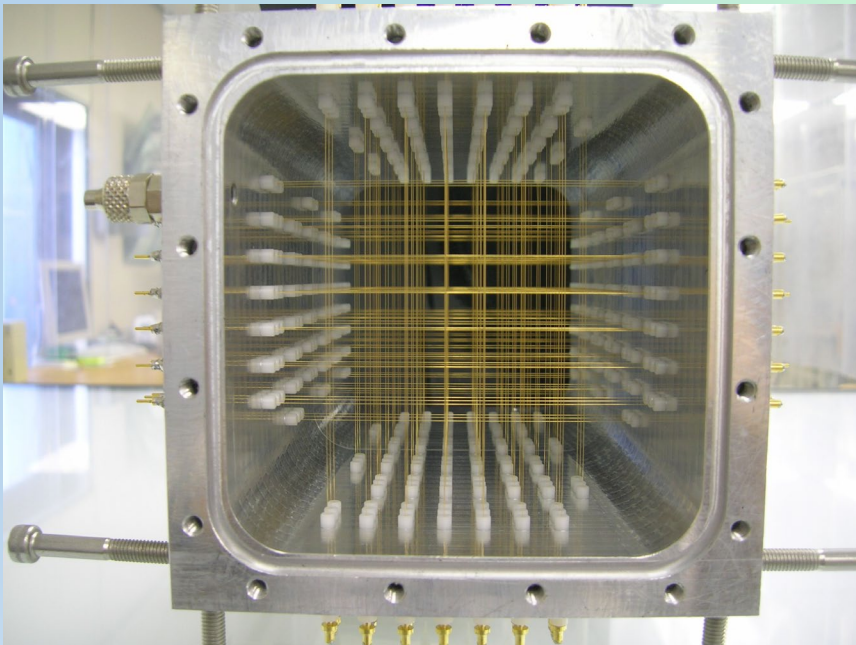
Margarita



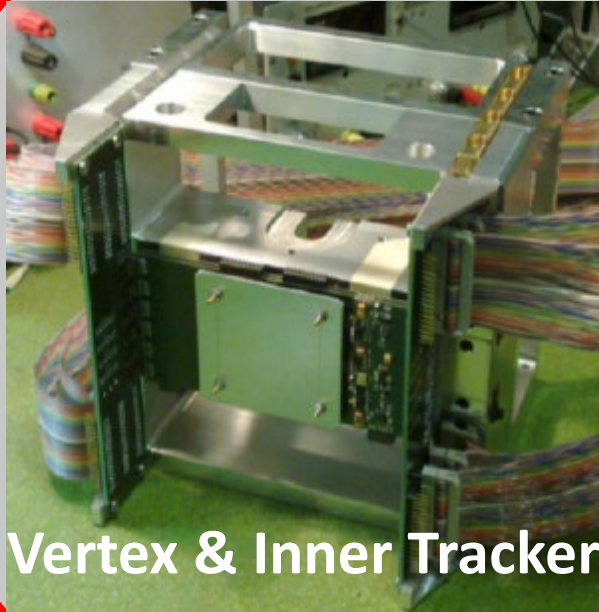
Beam monitor

Direzione beam dopo aver passato lo start counter

$$\begin{pmatrix} ct' \\ x' \\ y' \\ z' \end{pmatrix} = \begin{pmatrix} \gamma & 0 & 0 & -\beta\gamma \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -\beta\gamma & 0 & 0 & \gamma \end{pmatrix} \cdot \begin{pmatrix} ct \\ x \\ y \\ z \end{pmatrix} = \begin{pmatrix} \gamma ct - \beta\gamma z \\ x \\ y \\ -\beta\gamma ct + \gamma z \end{pmatrix}$$



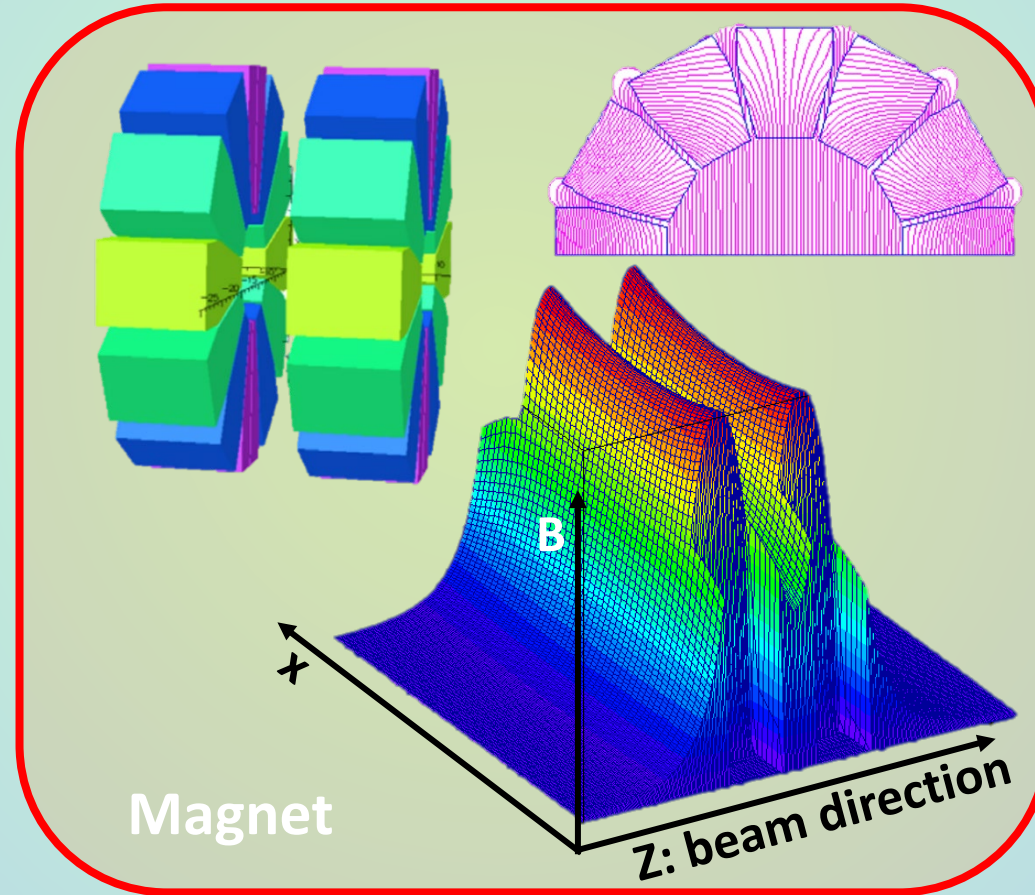
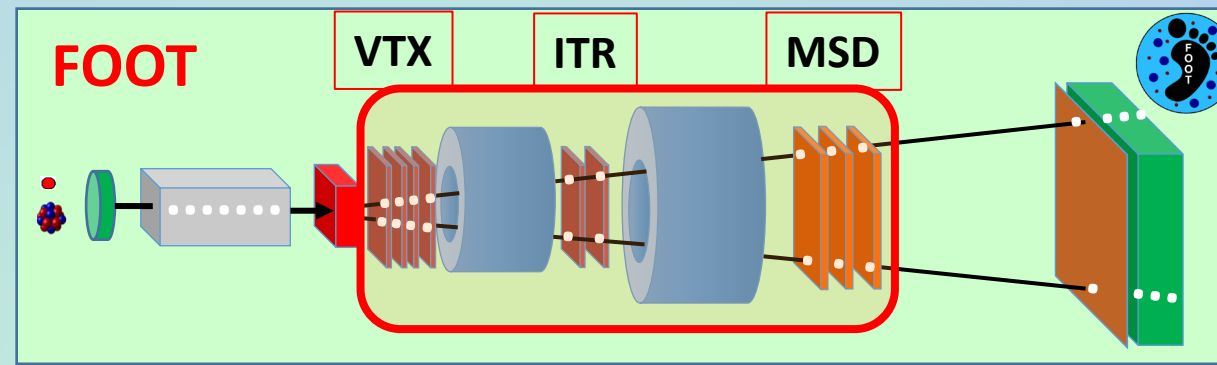
Tracking region



Vertex & Inner Tracker

VTX: 4 layers of Si pixel ($20 \times 20 \mu\text{m}$)

ITR: 2 layers of Si pixel ($20 \times 20 \mu\text{m}$)

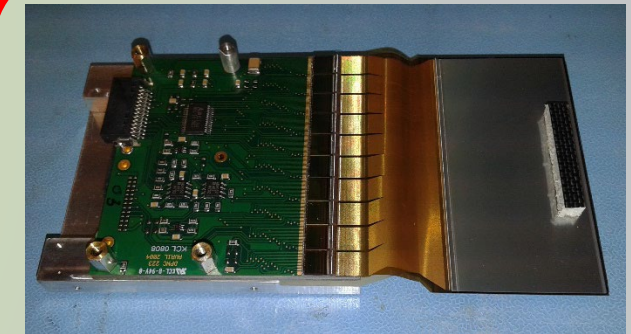


Magnet

2 permanent magnets

Hallbach geometry

B field in y direction (max 0.8 T)



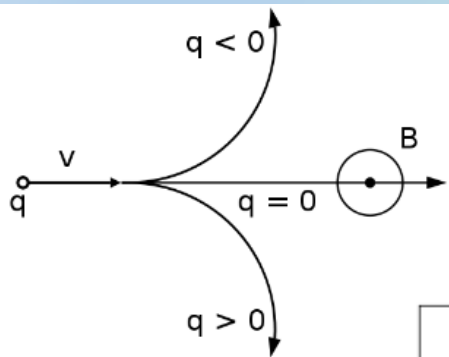
Micro Strip Detector (MSD)

MSD:

3 layers of Si strips ($120 \mu\text{m} \times 9 \text{ cm}$)

Momentum reconstruction

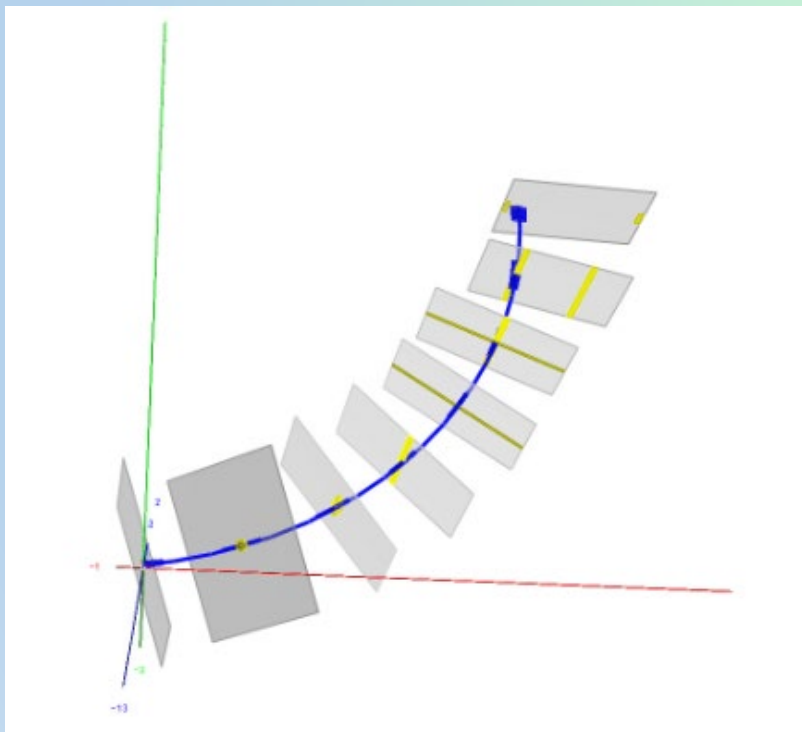
tracker



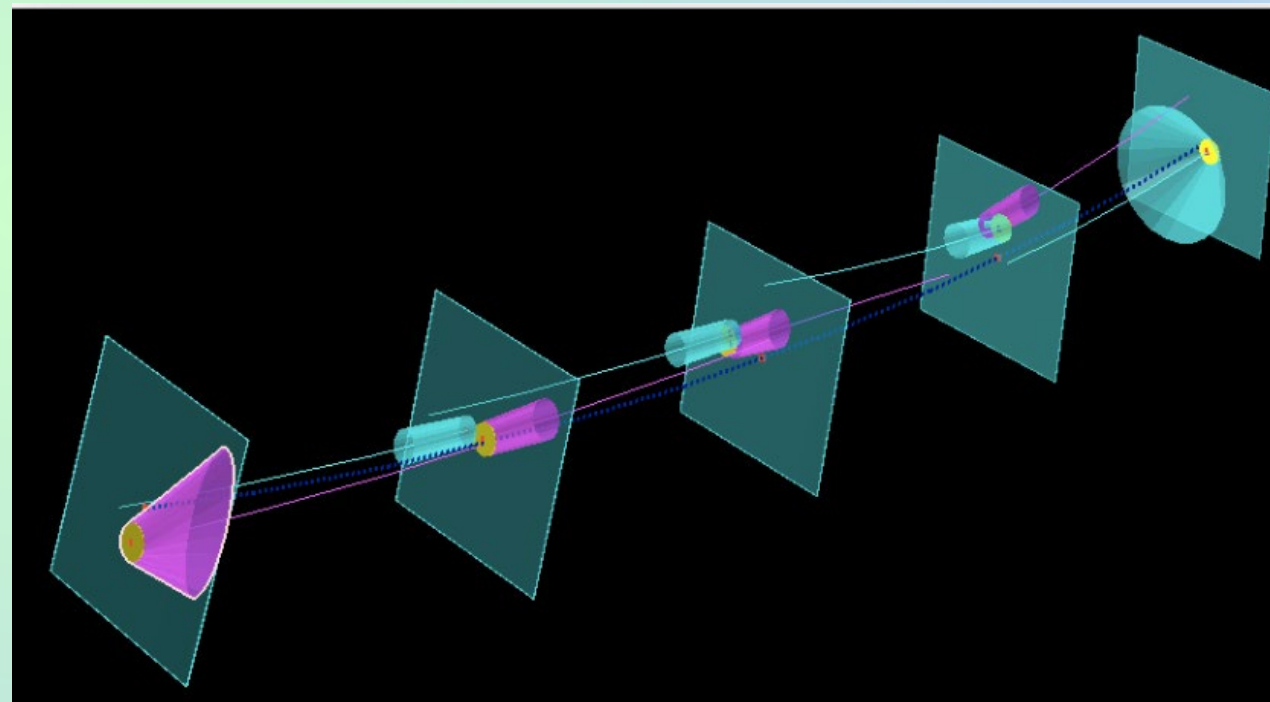
$$\vec{F} = q\vec{v} \times \vec{B}$$

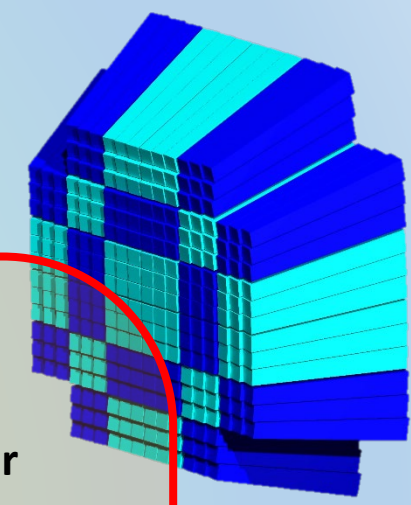
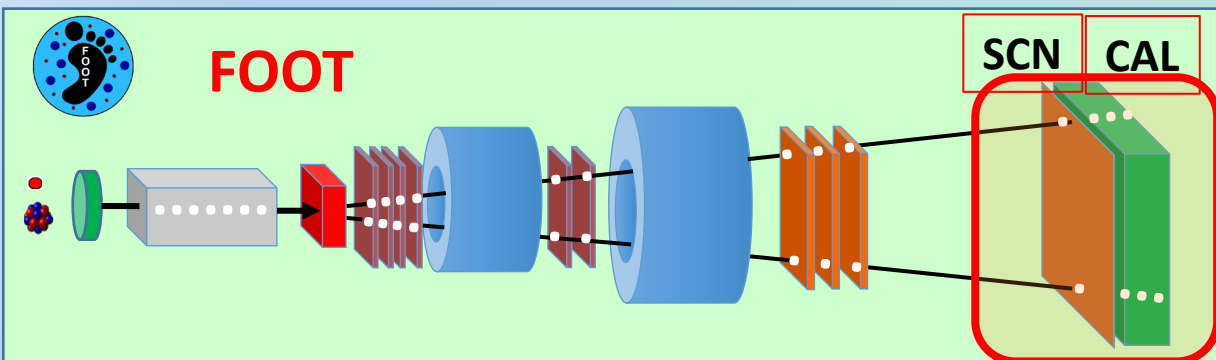
$$\frac{mv^2}{r} = qvB$$

$$p \left[\frac{\text{GeV}}{c} \right] = 0.3 B[\text{T}] R[\text{m}]$$



Trajectory reconstruction





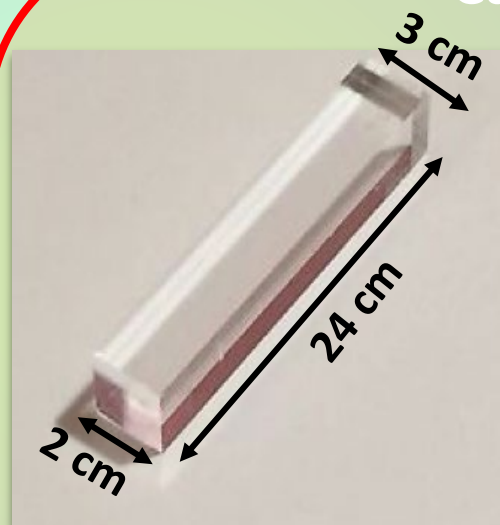
Scintillator (SCN)



40 x 2 cm plastic scintillator bars
3 mm thickness
2 layers of 20 bars
Silicon PhotoMultiplier (SiPM)

ΔE -Tof

Calorimeter (CAL)



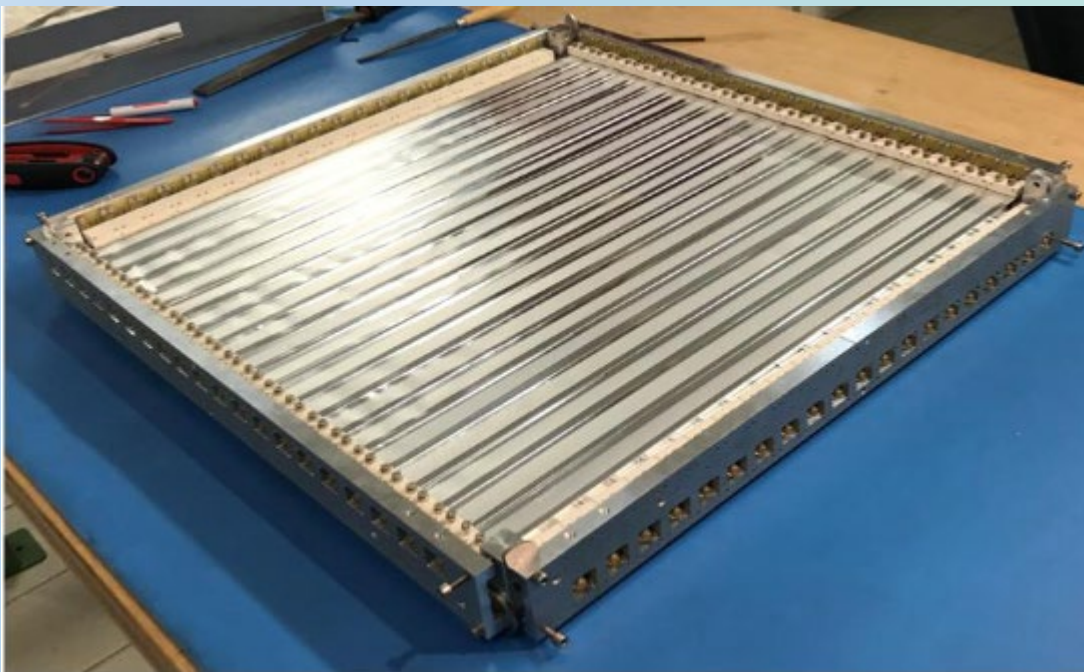
BGO – ($\text{Bi}_4\text{Ge}_3\text{O}_{12}$)
Inorganic scintillator

$Z_{\text{Bi}} = 83$
 $P_{\text{BGO}} = 7.13 \text{ g/cm}^3$
Weight = 1.027 kg
Total weight 330 Kg

SiPM

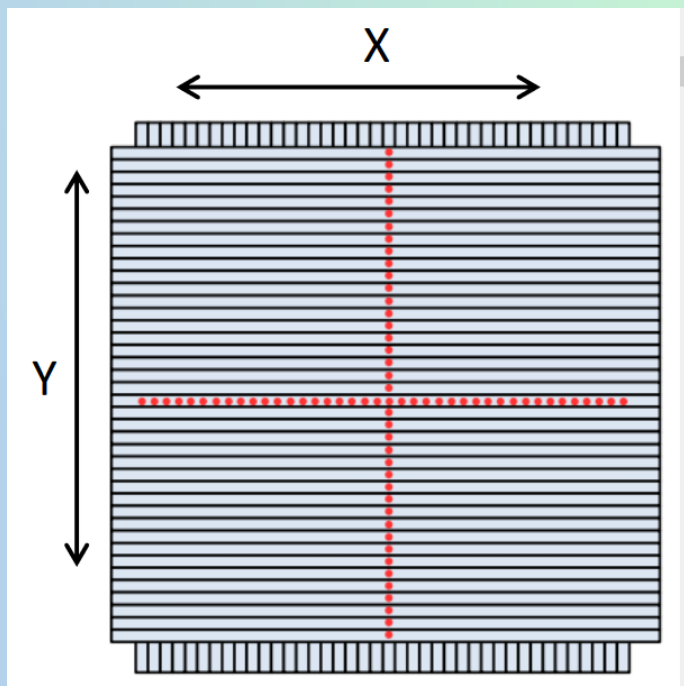
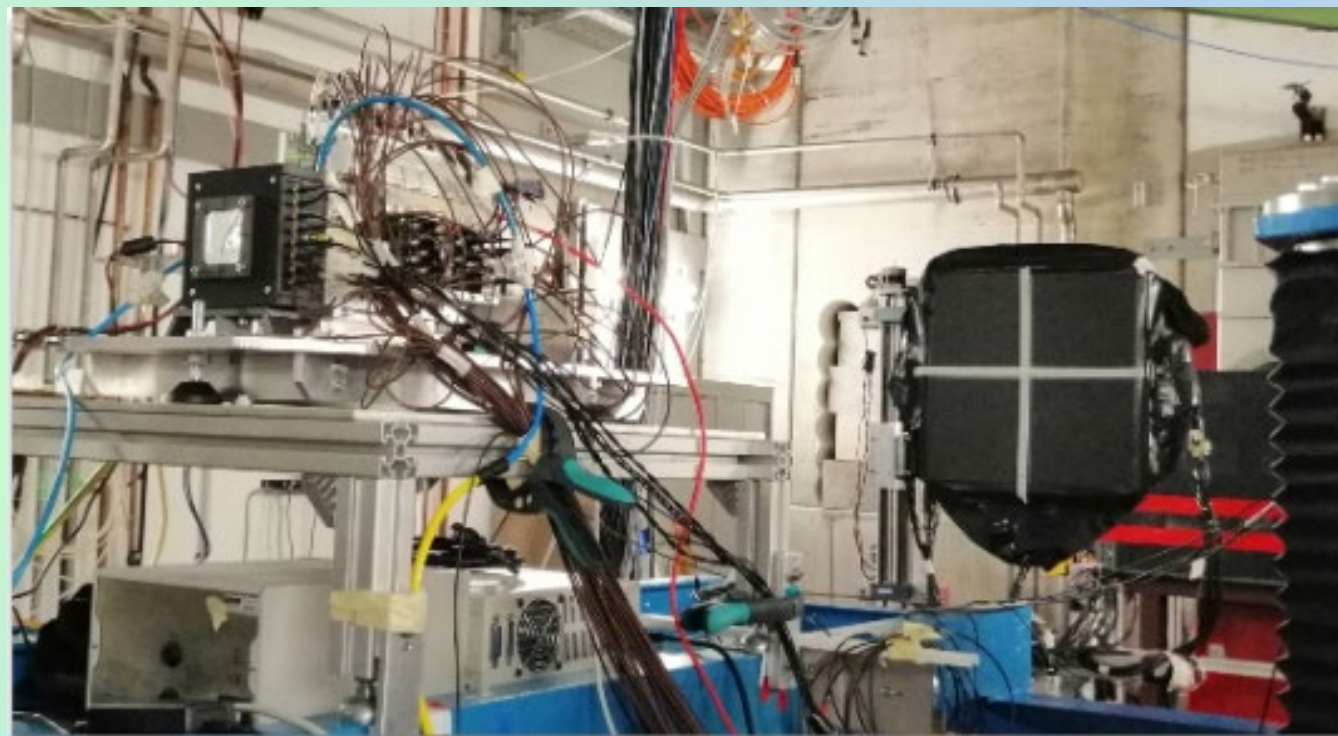
Pitch 50 μm
Voltage breakdown 53 V





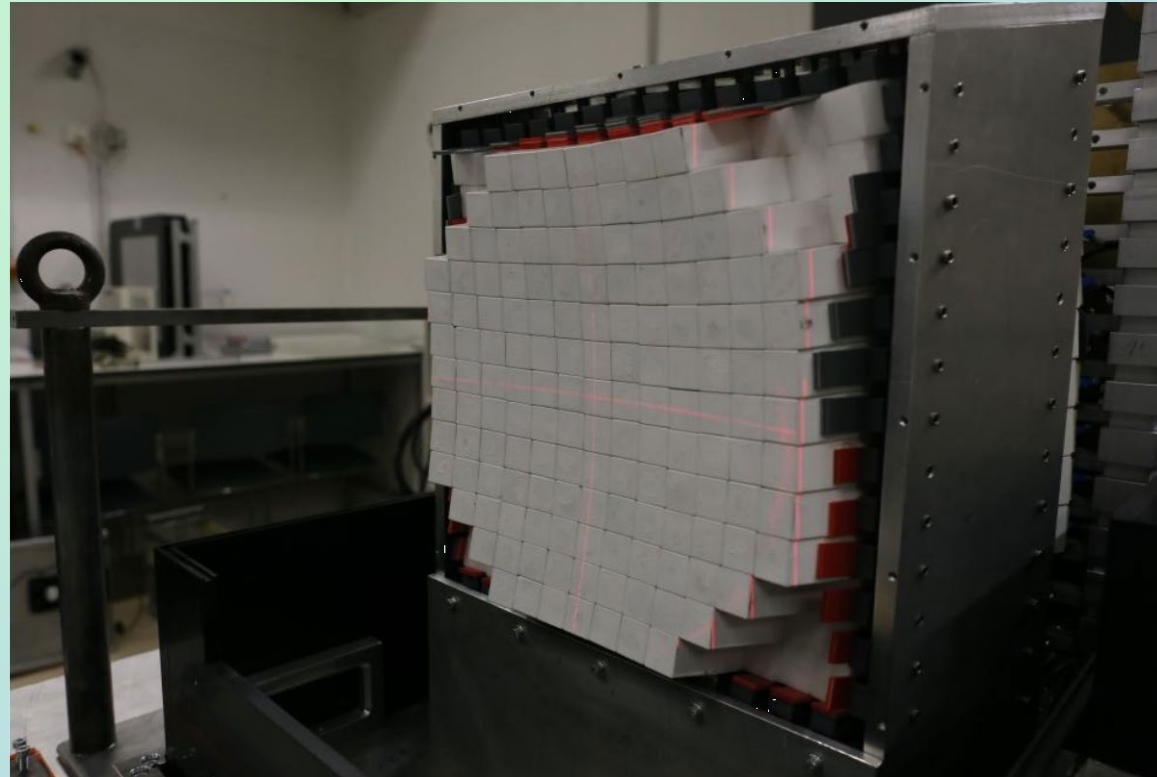
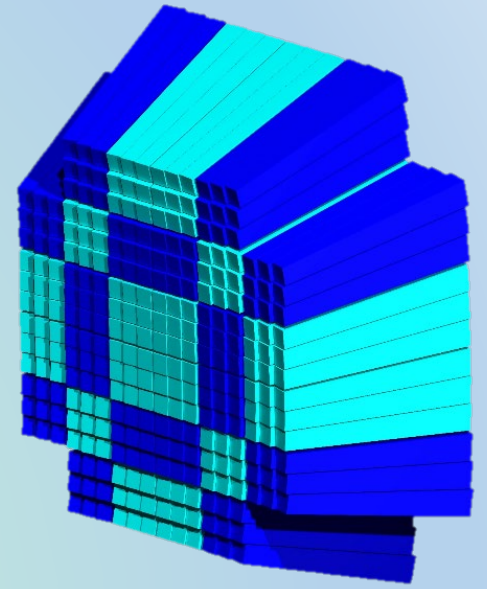
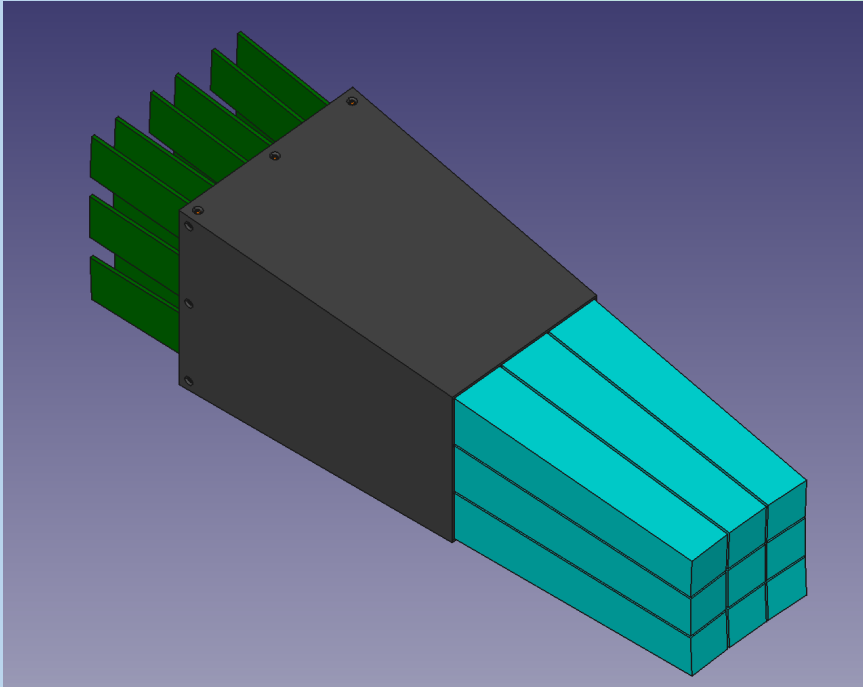
Tof Wall

Measure de/dx and tof



Calorimeter

Measure kinetic energy

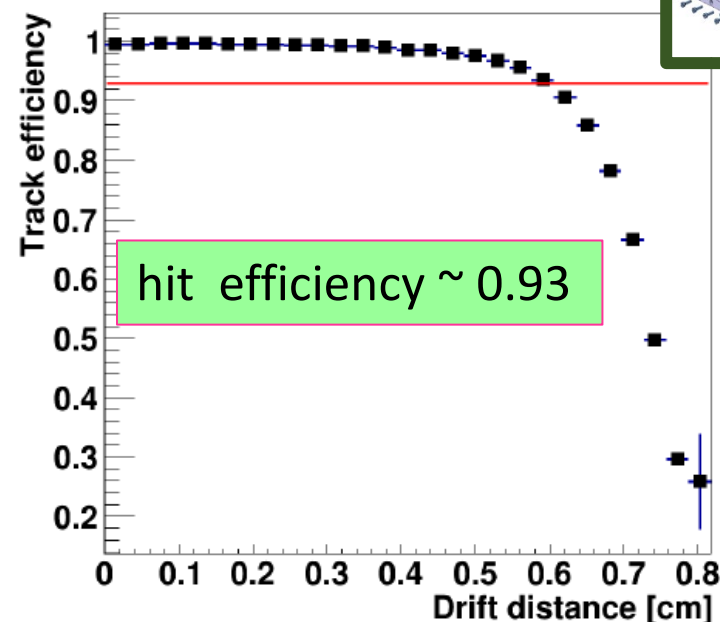
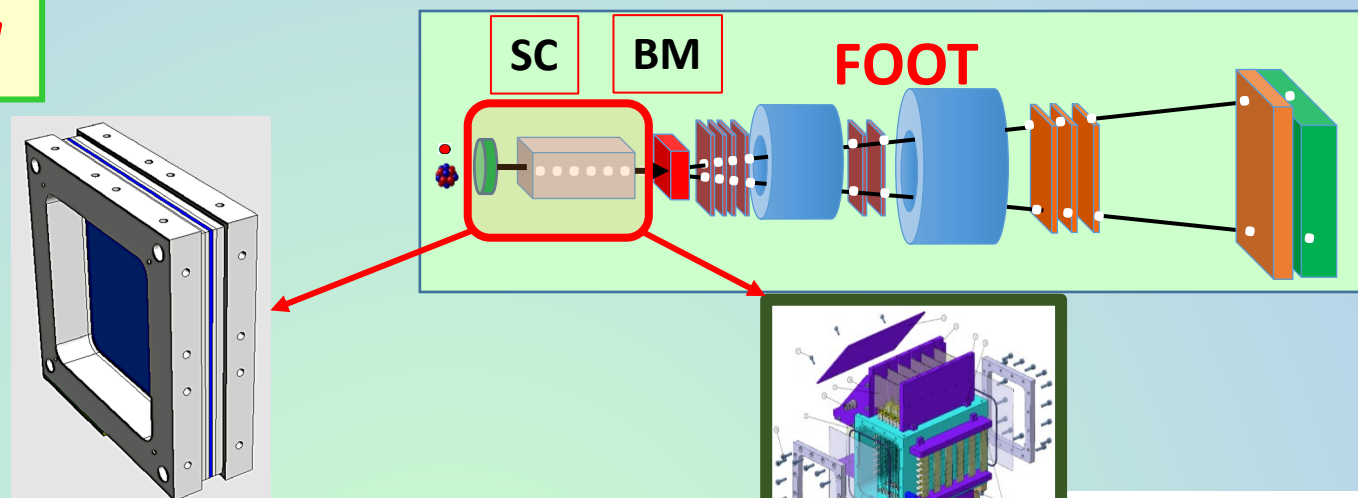
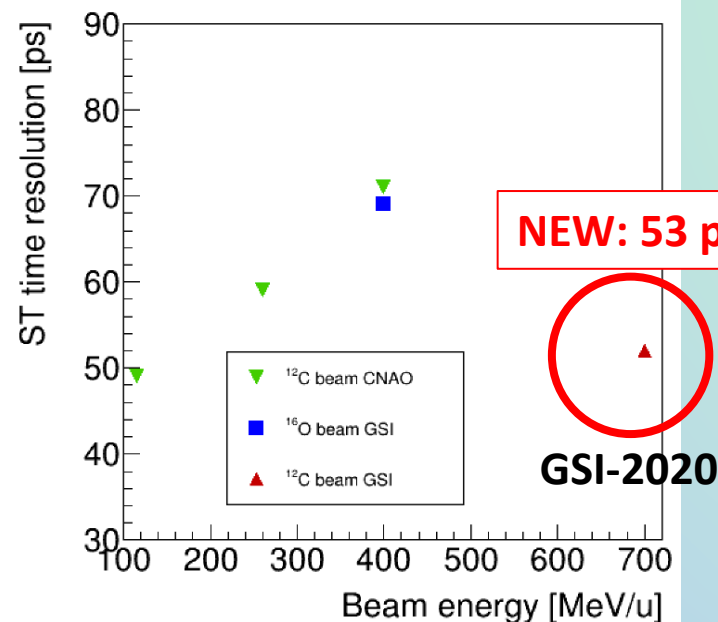


Performance

Beam definition: SC + BM

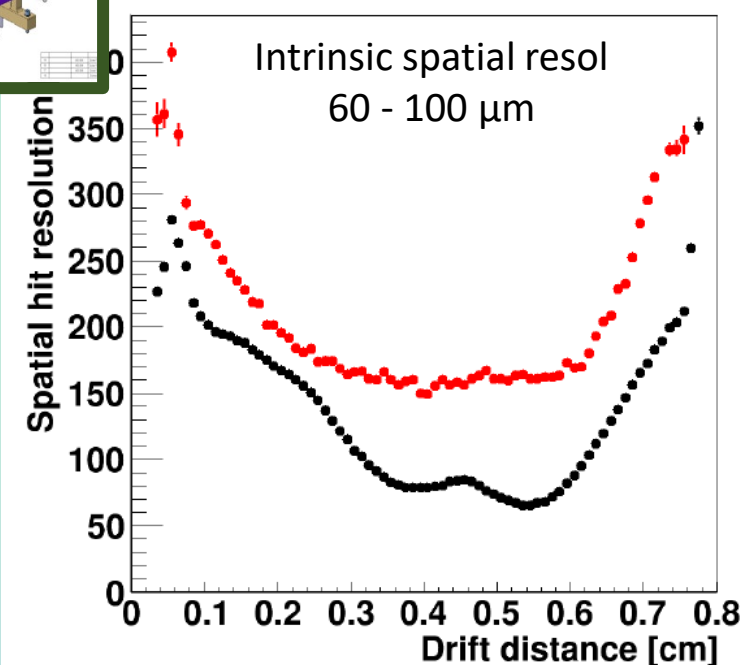
$$\frac{d\sigma_f}{dE_{kin}} = \frac{(Y_f - Bkg_f)^U}{N_{Prim} \cdot N_t \cdot \Omega_{Ekin} \epsilon_f}$$

- Count n° of particles
- Initial Trigger
- Time start
- Discard SC fragmentation
- Extrapolate vertex direction
- Evaluate beam direction



Angular resolution:

- 1.6 mrad p@228 MeV/u
- 2.1 mrad p @ 80 MeV/u



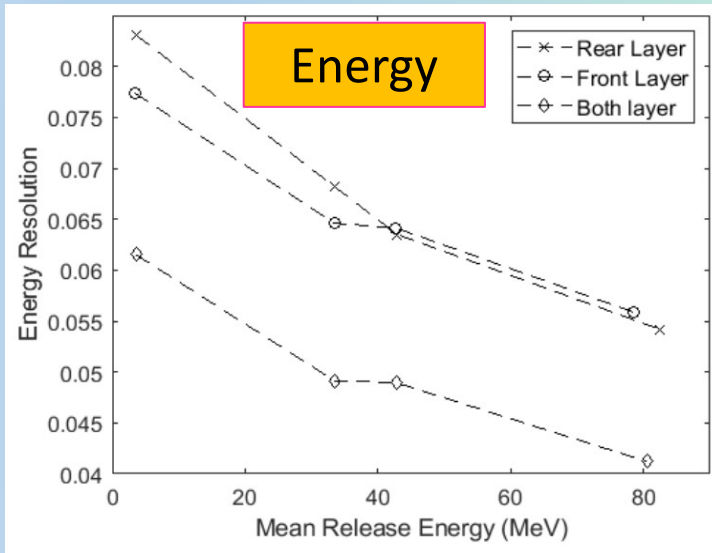
Spatial resolution:

- $150 \pm 10 \mu\text{m}$ p@228 MeV/u
- $300 \pm 10 \mu\text{m}$ p@ 80 MeV/u

Tof Wall

Detector is complete

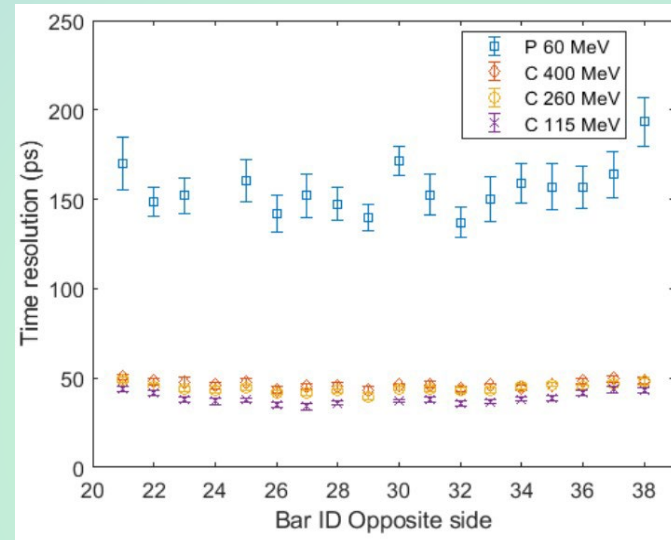
Data taking at CNAO-GSI (march-april 2019) and CNAO (dec 2019)



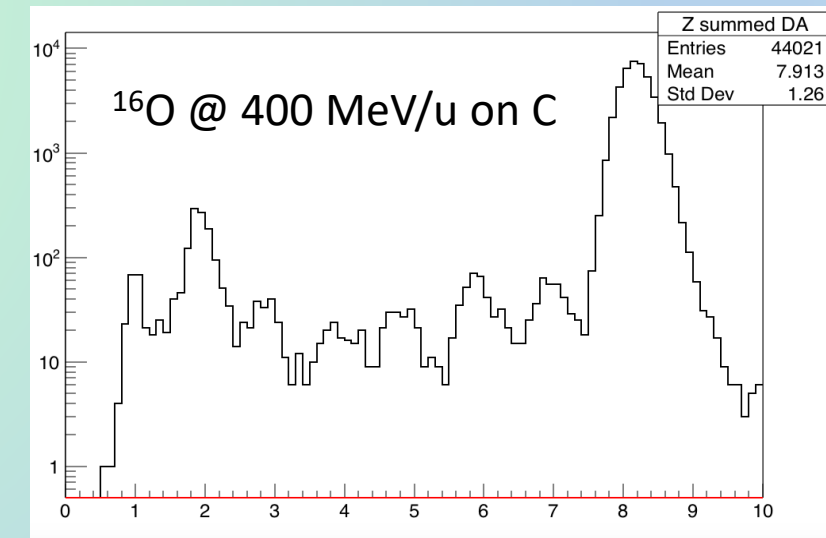
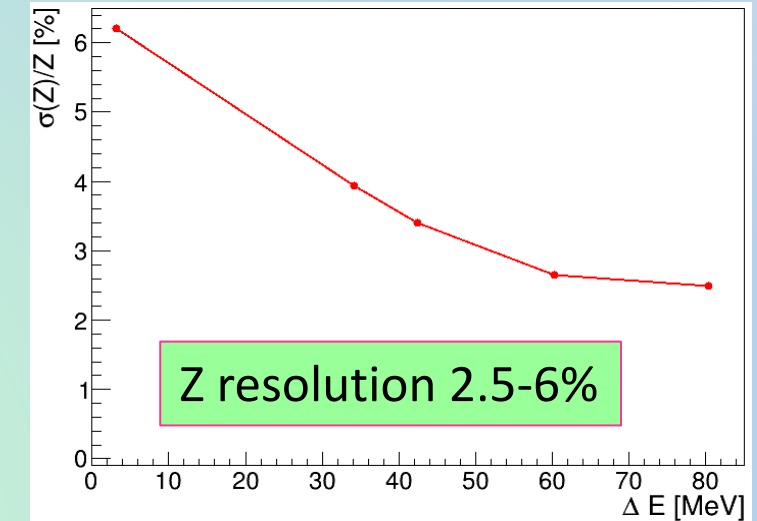
Resolution:

- Energy: 4-6 %
- Time SCN: 40-50 ps for ^{12}C and 150-190 ps for p
- Tof (SC+TofW): 50-75 ps for $^{12}\text{C} - ^{16}\text{O}$
250 ps for p
- Position: 7 mm for ^{12}C and 15 mm for p

Tof



CNAO + GSI

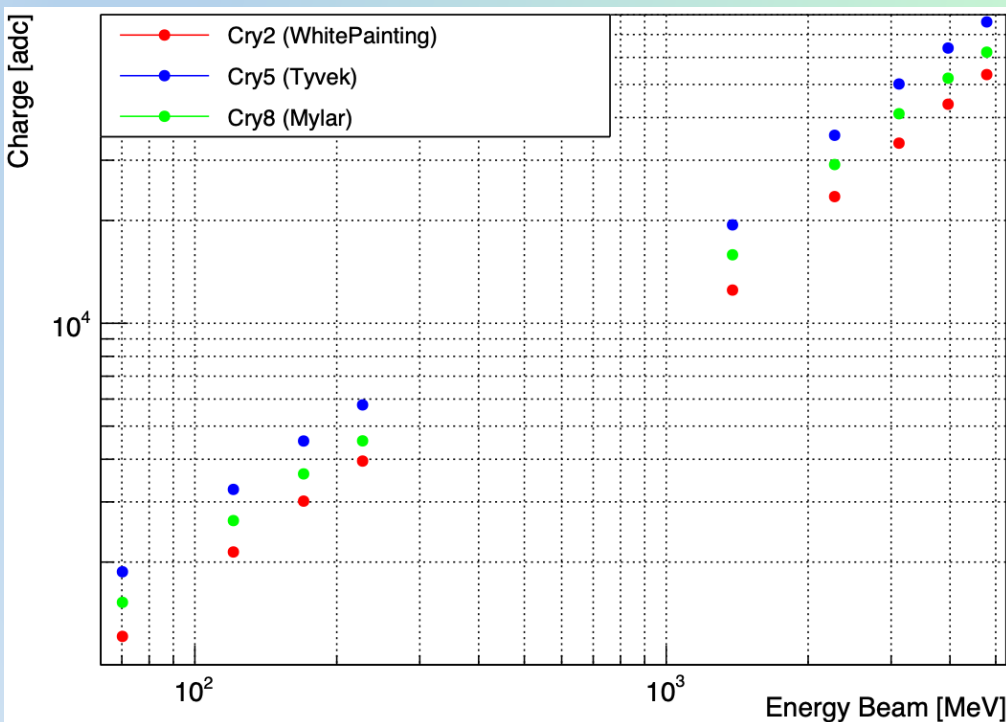


Paper circulates inside collaboration

Calorimeter, 1

TEST BEAM OVERVIEW:

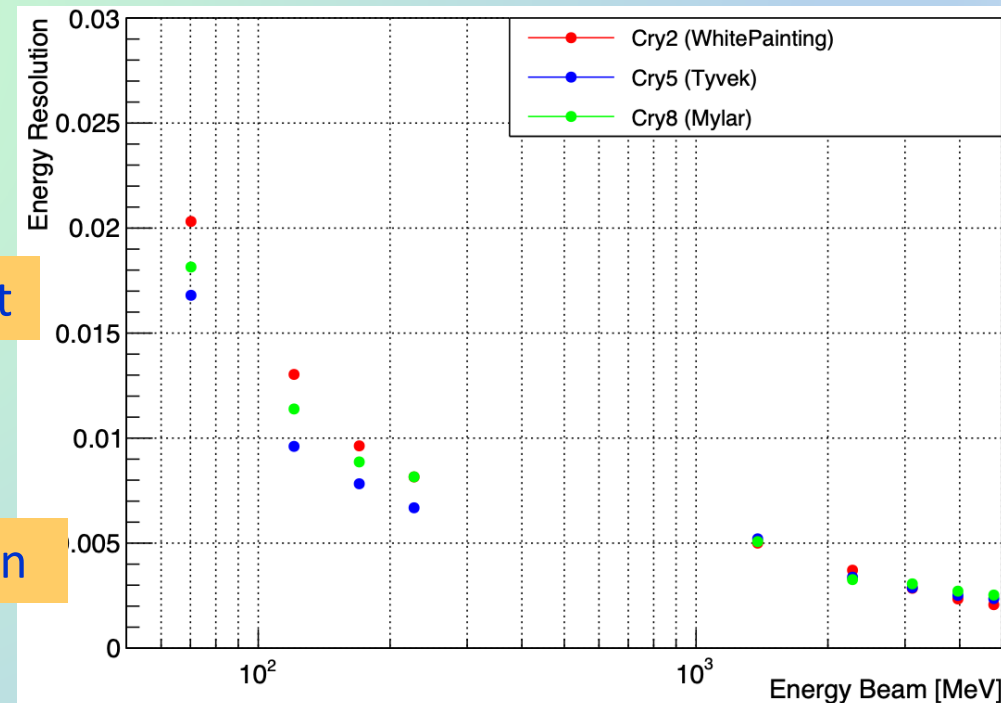
- 9 crystals
- 15 μm SiPM arrays
- 3 reflective wrappings: White Painting, Mylar and Tyvek
- Proton Energy: 70, 120, 170, 227 MeV
- Carbon Energy: 115, 190, 260, 330, 399 MeV/A
- Temperature part:
 - ⊙ For each energy 4 different temperature



Tyvek reflects more light



Better Energy Resolution



Performances: charge Z reconstruction

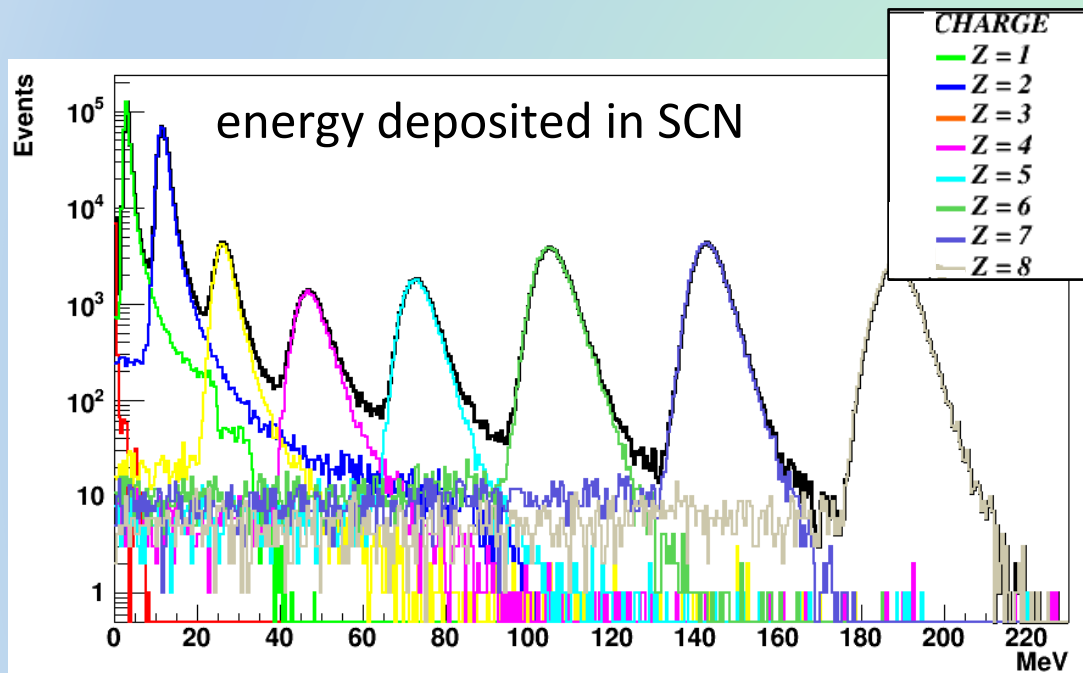
^{16}O (200 MeV/u) \rightarrow C_2H_4

Fragment univocally defined by Z and A

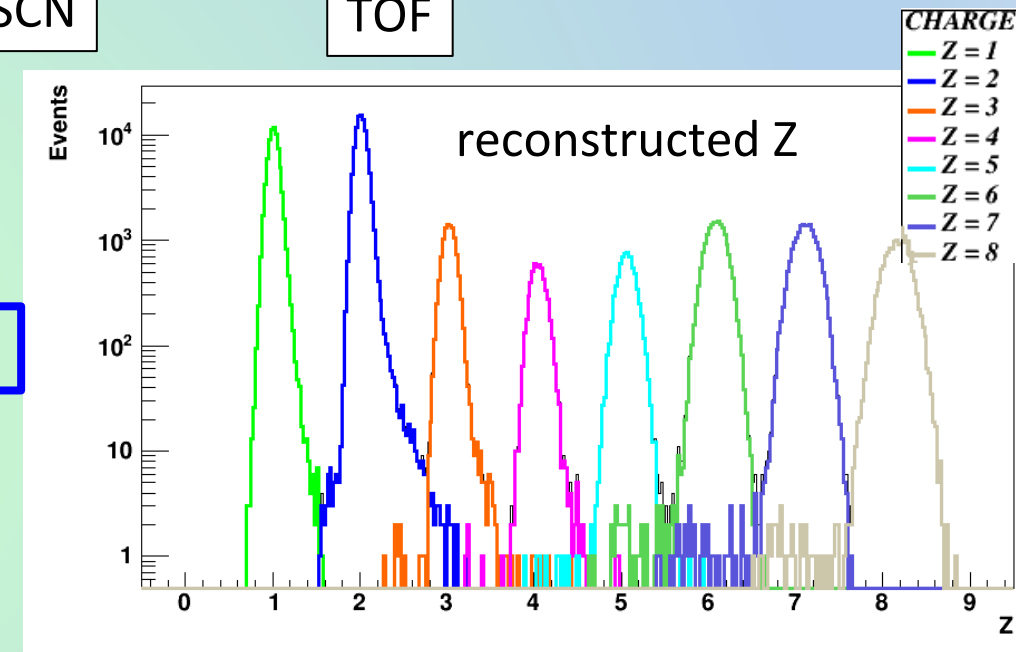
$$-\frac{dE}{dx} = \frac{\rho \cdot Z}{A} \frac{4\pi N_A m_e c^2}{M_U} \left(\frac{e^2}{4\pi\epsilon_0 m_e c^2} \right)^2 \frac{z^2}{\beta^2} \left[\ln \left(\frac{2m_e c^2 \beta^2}{I \cdot (1 - \beta^2)} \right) - \beta^2 \right]$$

SCN

TOF



Fluka simulation



^1H	^4He	^7Li	^9Be	^{11}B	^{12}C	^{14}N	^{16}O
1	2	3	4	5	6	7	8
1.01 ± 0.09	2.01 ± 0.06	3.03 ± 0.08	4.05 ± 0.09	5.06 ± 0.10	6.09 ± 0.12	7.11 ± 0.14	8.15 ± 0.15

Z Resolution : 9% 3%

2.0%

wrong charge assignment < 1%

FOOT Performances: Number of mass reconstruction

Reconstruction

$$A_1 = \frac{m}{U} = \frac{p}{U \beta \gamma}$$

Diagram showing TOF pointing to U and TRACKER pointing to p .

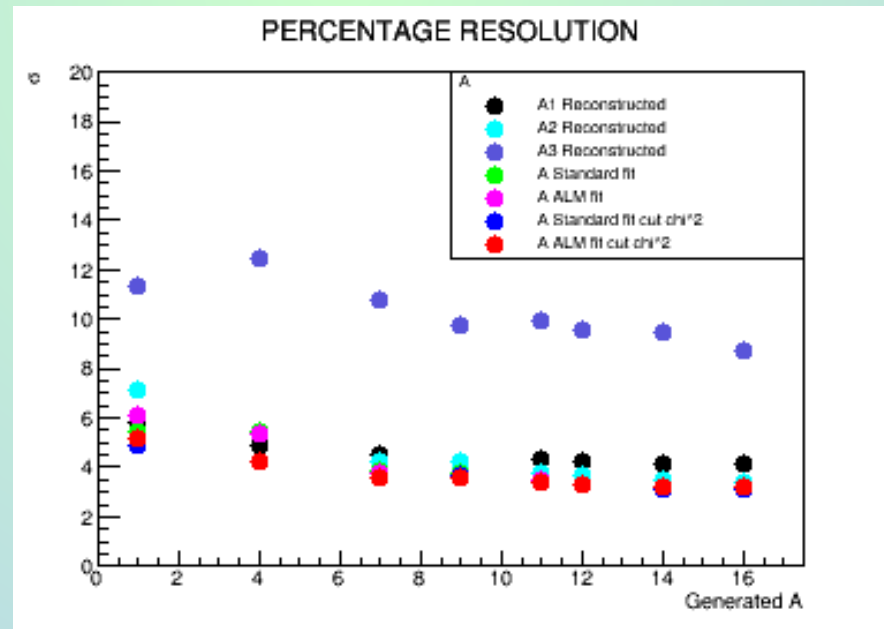
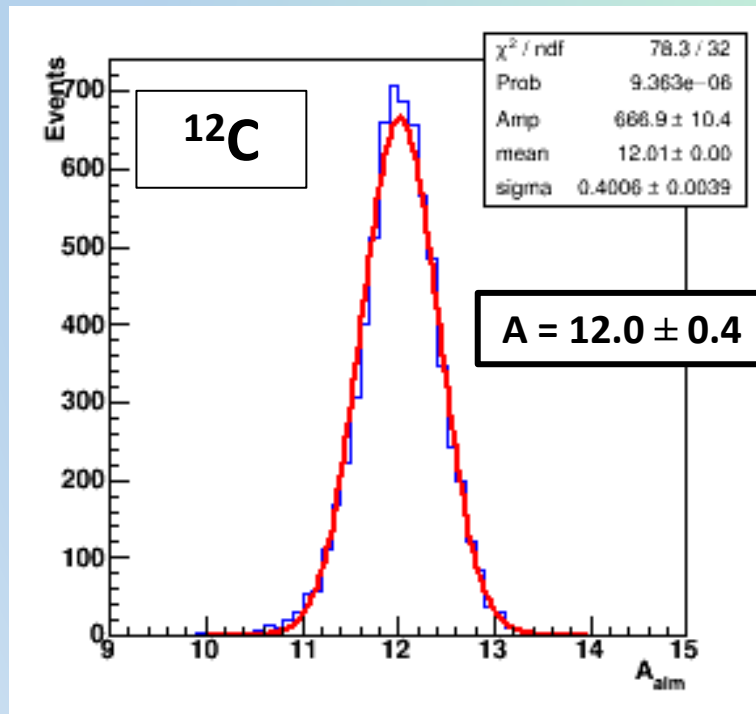
$$A_2 = \frac{m}{U} = \frac{E_{kin}}{U(\gamma - 1)}$$

Diagram showing TOF pointing to U and CALO pointing to E_{kin} .

$$A_3 = \frac{m}{U} = \frac{p^2 - E_{kin}^2}{2E_{kin}U}$$

Diagram showing TRACKER pointing to p and CALO pointing to E_{kin} .

Fit Methods: STANDARD χ^2 and ALM



^{16}O (200 MeV/u) \rightarrow C_2H_4

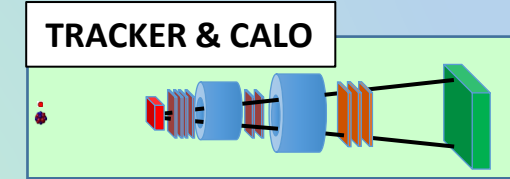
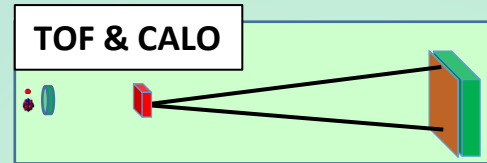
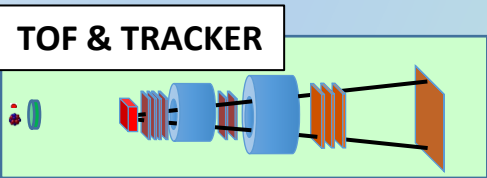
Data simulated by Fluka

Resolution for heavy fragments $\sim 3\text{-}4\%$

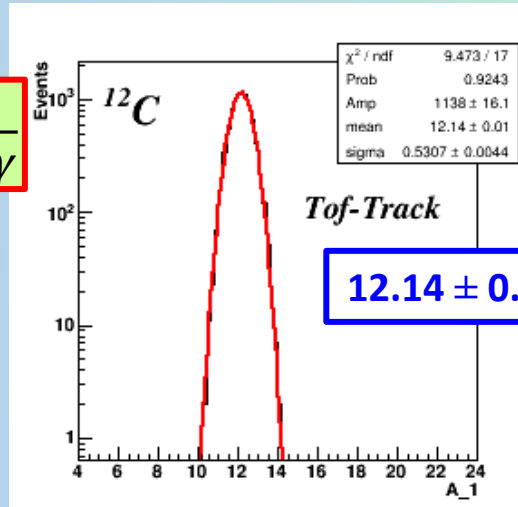
Performances: Number of mass A (ex of ^{12}C)

Fluka simul ^{16}O (200 MeV/u) \rightarrow C_2H_4

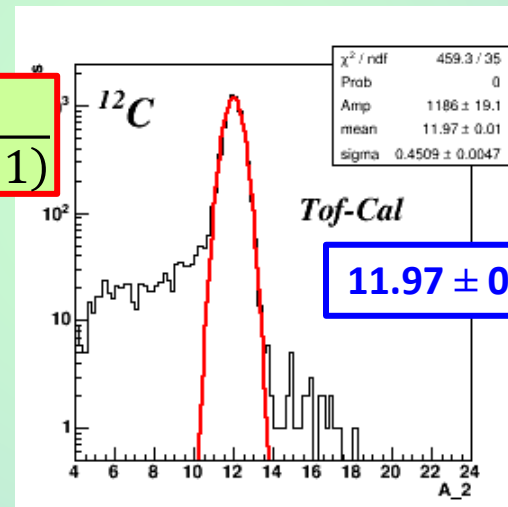
REDUNDANT Detector \rightarrow different ways to determine A



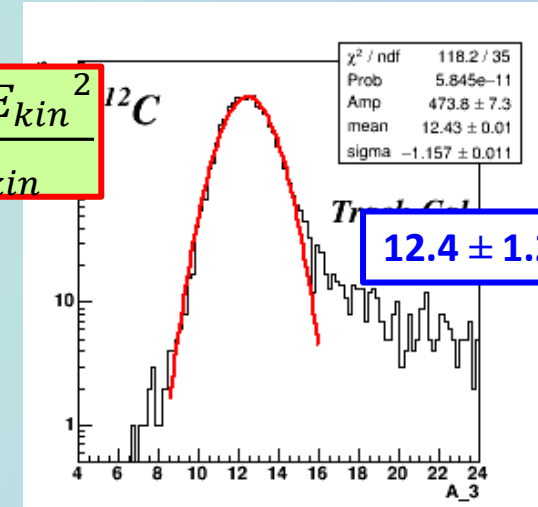
$$A_1 = \frac{p}{U \beta \gamma}$$



$$A_2 = \frac{E_{kin}}{U(\gamma - 1)}$$



$$A_3 = \frac{p^2 - E_{kin}^2}{2E_{kin}}$$



TOF (β) – TRACKER (p)

$$A_1 = \frac{m}{U} = \frac{p}{U \beta \gamma}$$

TOF (β)– CALO (E_{kin})

$$A_2 = \frac{m}{U} = \frac{E_{kin}}{U(\gamma - 1)}$$

TRACKER (p) – CALO (E_{kin})

$$A_3 = \frac{m}{U} = \frac{p^2 - E_{kin}^2}{2E_{kin}}$$

Standard χ^2 Fit

- Taking into account the correlation between A_1 , A_2 and A_3

$$f = \left(\frac{(tof_{reco} - t)}{\sigma_{tof_{reco}}} \right)^2 + \left(\frac{(p_{reco} - p)}{\sigma_{p_{reco}}} \right)^2 + \left(\frac{(E_{kin, reco} - E_{kin})}{\sigma_{E_{kin, reco}}} \right)^2 + (A_1 - A \quad A_2 - A \quad A_3 - A) \begin{pmatrix} C_{00} & C_{01} & C_{02} \\ C_{10} & C_{11} & C_{12} \\ C_{20} & C_{21} & C_{22} \end{pmatrix} \begin{pmatrix} A_1 - A \\ A_2 - A \\ A_3 - A \end{pmatrix}$$

$$C = (A \cdot A^T)^{-1} \quad A = \begin{pmatrix} \frac{\partial A_1}{\partial t} dt & \frac{\partial A_1}{\partial p} dp & 0 \\ \frac{\partial A_2}{\partial t} dt & 0 & \frac{\partial A_2}{\partial E_{kin}} dE_{kin} \\ 0 & \frac{\partial A_3}{\partial p} dp & \frac{\partial A_3}{\partial E_{kin}} dE_{kin} \end{pmatrix}$$

Augmented LagrangianFit (ALM)

$$\tilde{\mathcal{L}}(\vec{x}; \lambda, \mu) \equiv f(\vec{x}) - \sum_a \lambda_a c_a(\vec{x}) + \frac{1}{2\mu} \sum_a c_a^2(\vec{x}).$$

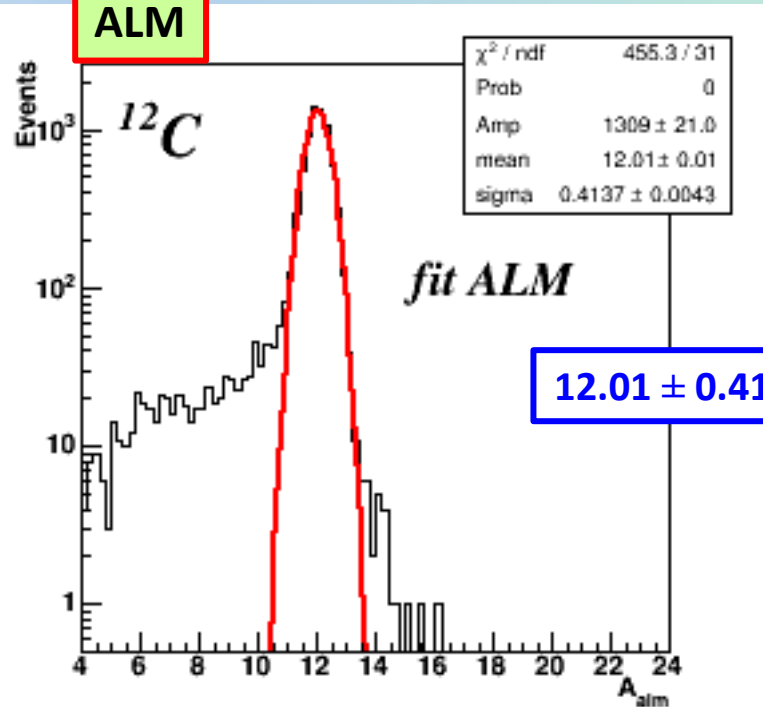
Performances: Number of mass A (ex of ^{12}C)

Fluka simul ^{16}O (200 MeV/u) \rightarrow C_2H_4

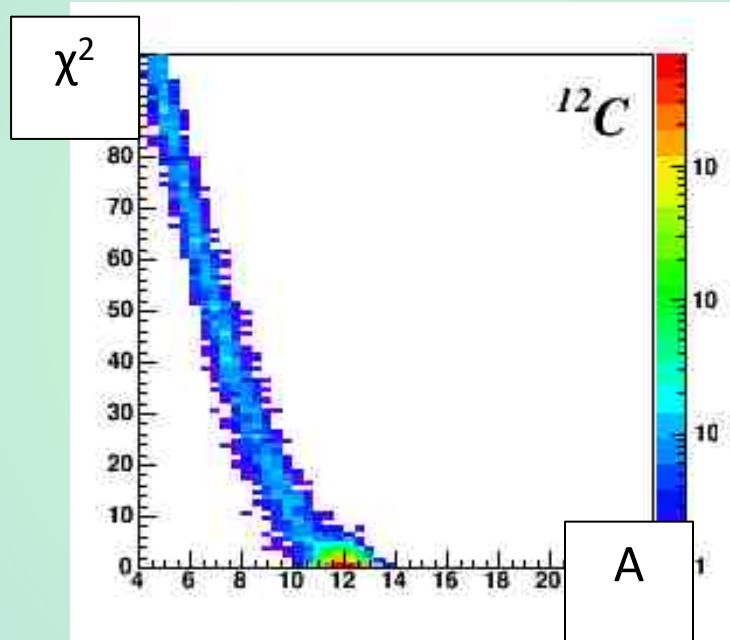
FIT Methods:

- Standard χ^2
- Augmented Lagrangian (ALM)

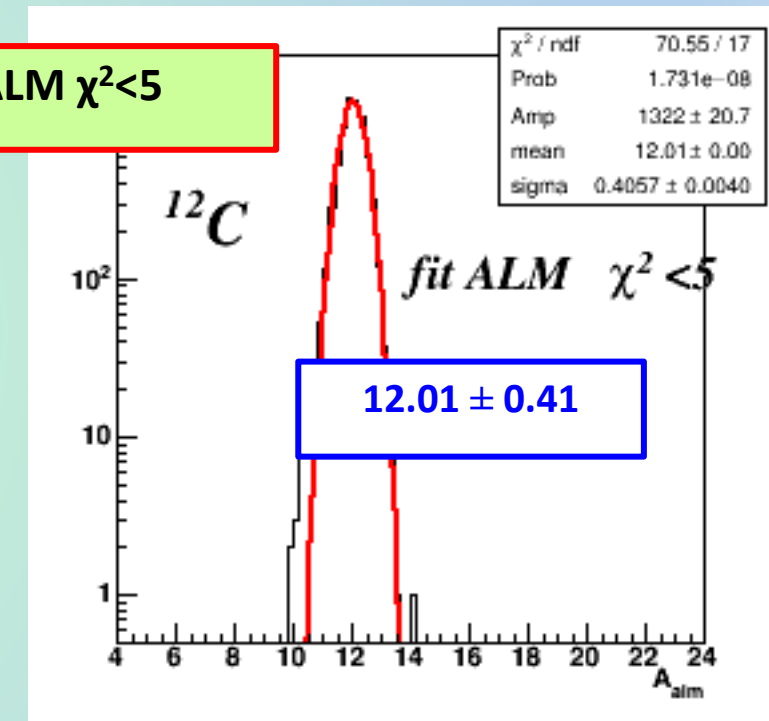
ALM



χ^2



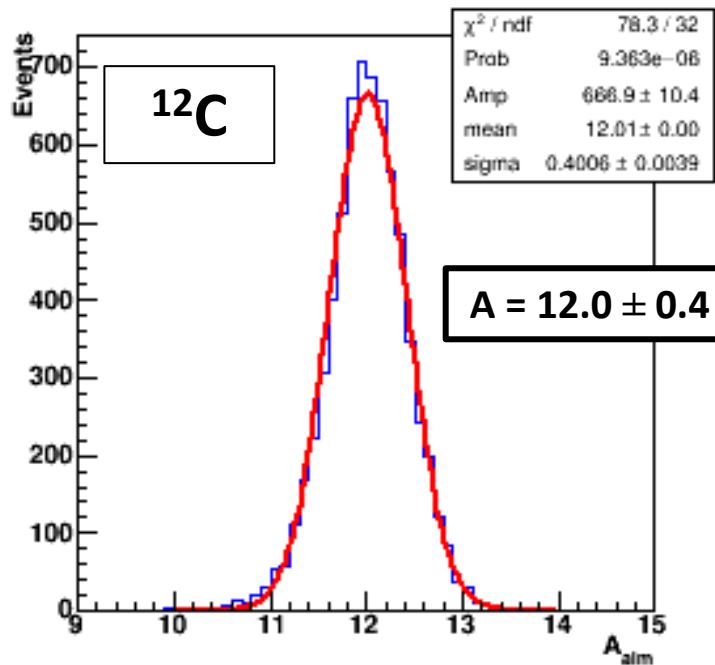
ALM $\chi^2 < 5$



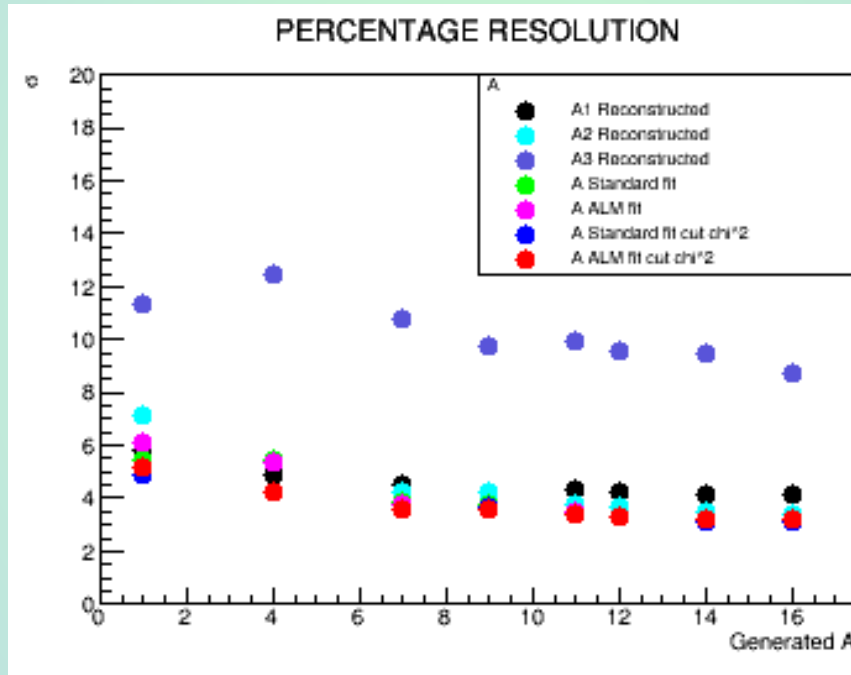
Fit cut the wrong reconstructed fragments

FOOT Performances: Number of mass reconstruction

Simulation by Fluka



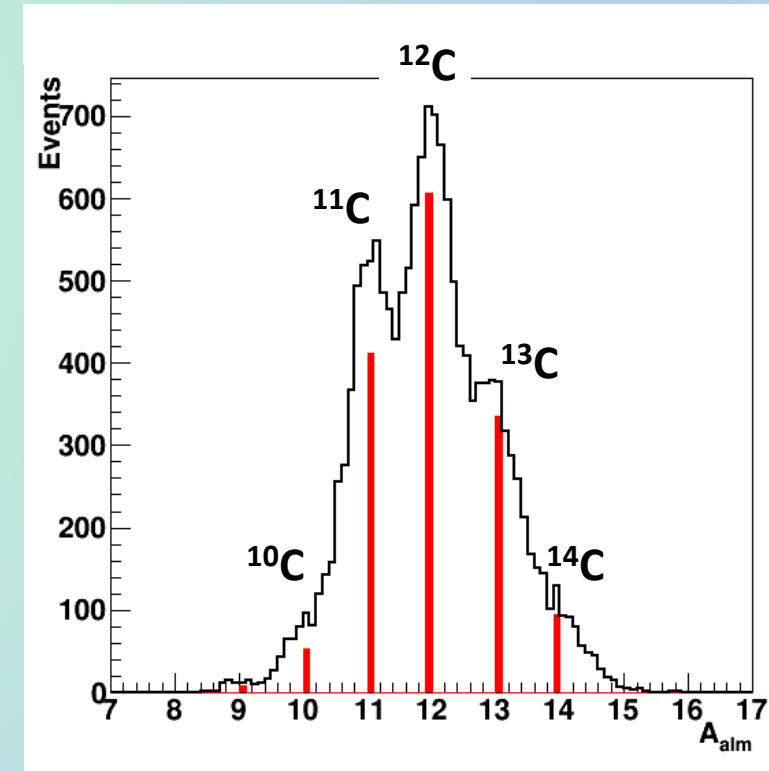
^{16}O (200 MeV/u) \rightarrow C_2H_4



Resolution for heavy fragments $\sim 3\text{-}4\%$

Conservative Resolutions

- $\Delta p/p \rightarrow 4\%$
- $\Delta E_{\text{kin}}/E_{\text{kin}} \rightarrow 1.5\%$
- $\Delta \text{tof} \rightarrow 70 - 140 \text{ ps}$
- $\Delta(dE)/dE \rightarrow 3 - 10\%$



Possibility to disentangle isotopes

FOOT Performances: Isotopes separation (example of C)

Data simulated by Fluka

Conservative Resolutions

- $\Delta p/p \rightarrow 4\%$
- $\Delta E_{\text{kin}}/E_{\text{kin}} \rightarrow 1.5\%$
- $\Delta \text{tof} \rightarrow 70 - 140 \text{ ps}$
- $\Delta(dE)/dE \rightarrow 3-10 \%$

$^{16}\text{O} \text{ (200 MeV/u)} \rightarrow \text{C}_2\text{H}_4$

Resolutions from Test Beam

- $\Delta p/p \rightarrow 4\%$
- $\Delta E_{\text{kin}}/E_{\text{kin}} \rightarrow 1.0\%$
- $\Delta \text{tof} \rightarrow 50 - 100 \text{ ps}$
- $\Delta(dE)/dE \rightarrow 3-10\%$

