Statistics : Final Exam

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If nothing is mentioned, I will use a 5% confidence interval.

Exercise 1

Question 1

The population is the cones in the eye. The variable is the number of the L type of cone. In this case, the sample is the N cones observed.

Question 2

The population is the humans, the variable is the percentage of cone, and the sample here is the 10 people we observe.
The correlation test show, for $M_{\%}$ and $L_{\%}$ (Figure 1), a correlation coefficient of -0.96 with a p-value of $1.0620 \cdot 10^{-5}$. As the correlation coefficient is near from -1 and the p-value far under 0.05, this shows that there is actually a correlation between $M_{\%}$ and $L_{\%}$, as the p-value is far lower than 0.05.
For $M_{\%} - L_{\%}$ and $S_{\%}$ (Figure 2), the correlation coefficient is 0.192 and the p-value 0.5951. As the correlation coefficient is near to 0 and the p-value is above 0.05, this test does not show a correlation between $M_{\%} - L_{\%}$ and $S_{\%}$ for this sample.
We can be pretty confident in the first correlation test, as the p-value is really low. Though, for the second test, it seems pretty unlikely that the test could show a correlation, as the p-value is above 0.5. This sample should be repeated to check this.

Exercise 2

Question 1

Here, we want to see if one of the sample is not equal to the other (i.e the brand put less powder than the other). Thus, our null hypothesis H_0 will be :
H_0 : the two brands tuned the machine to put different weights of powder.
We then perform a two sample Student analysis with R to see if the two means are equal, and we get a p-value of 0.03481. We can see here that we do not refute the null hypothesis. Thus, we can say that the brand A and B tuned the machine in differrent ways.
We perform an other two sample Student analysis with the null hypothesis being H_0 : the brand A put more powder than B. We then get a p-value from the t-test of 0.0174, which means that A puts significantly more powder than B.

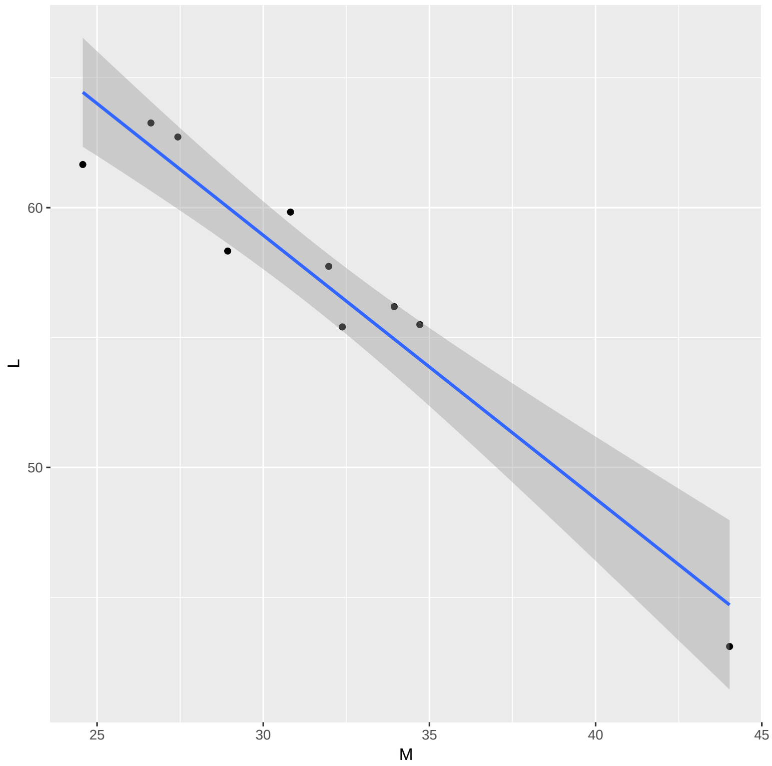

Figure 1: Plot of $M_{\%}$ against $L_{\%}$

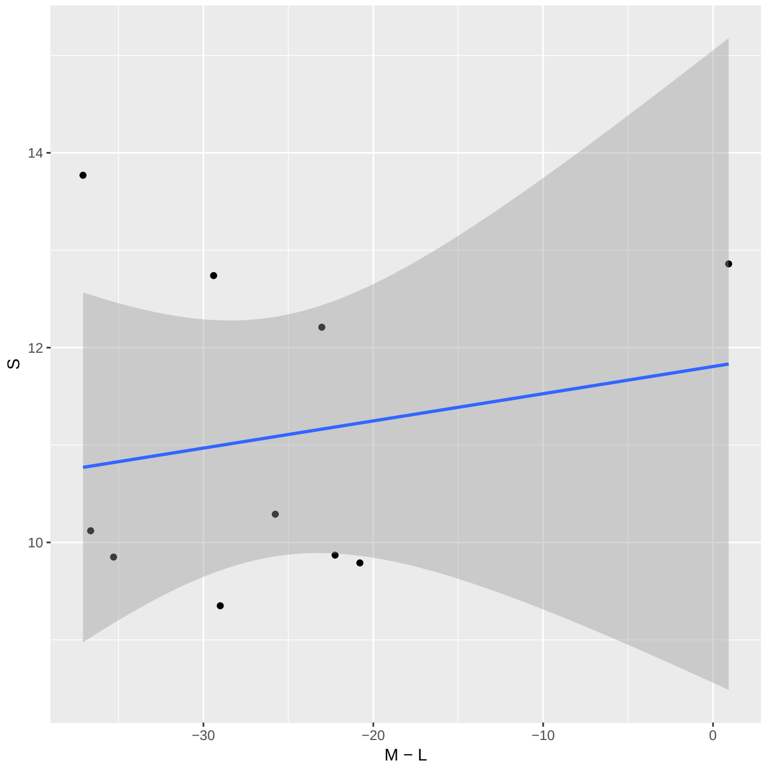

Figure 2: Plot of $M_{\%} - L_{\%}$ against $S_{\%}$

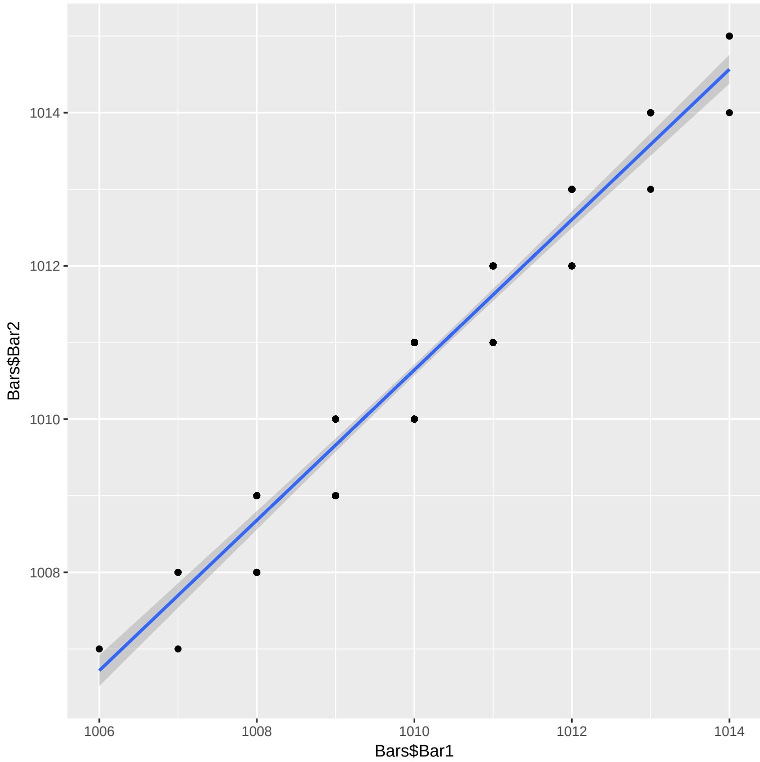

Figure 3: Plot of the data of the second barometer against the first one

Question 2

We want to check if the two brands actually sell 100mg of powder. For both brands, our null hypothesis will then be :
H_0 : the brand sell doses of 100mg.
We perform a one sample Student analysis for both brand samples. We get for the brand A a p-value of 0.06565. This shows us that we refute the null hypothesis, and thus can tell that the brand A do not sell, in mean, 100mg of powder.
For the brand B, after performing the same test, we get a p-value of 0.0001213. This p-value is far under 0.05, thus we do not refute the null hypothesis and can say that the brand B actually sells, in mean, 100mg of powder.

I then wanted to know if A was selling more or less than 100mg, as they do not sell exactly this weight. I used a one sample T-test with H_0 being $\mu_A < 100mg$. I got a p-value of 0.03282, meaning that we do not reject the null hypothesis. We can then determine that A is cheating and sells less powder than B.

Exercise 3

Question 1

Using visual inspection first (FIGURE 3), we observe a pretty good correlation between the two barometers. As we can see in FIGURE, all the points are around a line (here the linear model regression in blue, with confidence interval of 95%).

We then use the correlation function of R to see if this correlation exists. We obtain a correlation coefficient of 0.95 wich is close to 1, and a p-value of 0 (it is unlikely that the actual value is higher, but it is the value returned in the matrix by R. It seems this value is under $1 \cdot 10^{-3}$.). We can conclude that there is a significant correlation between the two barometers.

Question 2

Using the built-in lm R function, we find a equation of the linear model such as $y = 0.9812x + 19.6503$. We then use the summary function on the linear model, and see that the signification level is $< 2 \cdot 10^{-16}$. Thus, we can say that our linear model is significant.