# CSE 537 Assignment 3 Report: Sudoku

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Remy Oukaour Jian Yang
SBU ID: 107122849 SBU ID: 110168771
remy.oukaour@gmail.com jian.yang.1@stonybrook.edu
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## 1 Introduction

This report describes our submission for assignment 3 in the CSE 537 course on artificial intelligence. Assignment 3 requires us to implement some different algorithms to solve Sudoku games: variations on backtracking (simple, MRV, MRV with forwarding checking, and MRV with constraint propagation), and min-conflicts. In this report, we discuss the implementation details and performance of our solutions.

## 2 Implementation

#### 2.1 Data structures

We implemented one class named gameNode in gameNode.py to contain the state of a Sudoku board in the search tree used by our algorithms.

The gameNode data structure supports operations such as setting a value, rolling back a value, and checking if the board is solved. (The solved method for performing that check also increments the node's  $num_checks$  counter.) It also supports the constraint-related operations for different algorithms.

Two important methods of the gameNode class are get\_neighbors and get\_valid\_moves:

```
def get_neighbors(self, pos):
    i, j = pos
    bi = i // self.M * self.M
    bj = j // self.K * self.K
    neighbors = set()
    for k in xrange(self.N):
        neighbors.add((i, k))
        neighbors.add((k, j))
        neighbors.add((bi + k // self.K, bj + k % self.K))
    neighbors.remove(pos)
    return list(neighbors)
```

```
def get_valid_moves(self, pos):
    if self[pos].value():
        return []
    invalid_moves = {self[n].value() for n in self.get_neighbors(pos)}
    return [m for m in self.get_values() if m not in invalid_moves]
```

## 2.2 Backtracking

For backtracking, the algorithm chooses one arbitrary unassigned position and uses the edge constraints to get valid values. It traverses all these valid values, and using a backtracking depth-first search, it tries to find a solution if one exists.

The implementation of simple backtracking search in csp.py is:

```
def backtracking(filename):
    node = gameNode.gameNode()
    if not node.load_game(filename):
        return ("Error: Fail Load", 0)
    if backtracking_helper(node):
        return node.solution()
    return ("Error: No Solution", node.num_checks)
def backtracking_helper(node):
   if node.solved():
        return True
   unassigned = node.get_unassigned_positions()
    if not unassigned:
        return False
   pos = unassigned[0]
    for move in node.get_valid_moves(pos):
        domain = node[pos].domain
        node[pos] = move
        if backtracking_helper(node):
            return True
        node[pos] = domain
    return False
```

## 2.3 Backtracking + MRV

We added the *count\_contraints* method to the *gameNode* class:

```
def count_constraints(self, pos, value=None):
    if value is None:
       value = self[pos].value()
    return len([n for n in self.get_neighbors(pos)
       if not self[n].value() and value in self.get_valid_moves(n)])
```

The implementation of backtracking + MRV in csp.py is:

```
def backtrackingMRV(filename):
    node = gameNode.gameNode()
    if not node.load_game(filename):
        return ("Error: Fail Load", 0)
    if backtrackingMRV_helper(node):
        return node.solution()
    return ("Error: No Solution", node.num_checks)

def backtrackingMRV_helper(node):
    # Based on Figure 6.5 from page 215 of the textbook
    if node.solved():
        return True
    unassigned = node.get_unassigned_positions()
    if not unassigned:
```

```
return False
mrv_pos = min(unassigned, key=lambda p: len(node.get_valid_moves(p)))
lcv_moves = sorted(node.get_valid_moves(mrv_pos),
    key=lambda m: node.count_constraints(mrv_pos, m))
for move in lcv_moves:
    domain = node[mrv_pos].domain
    node[mrv_pos] = move
    if backtrackingMRV_helper(node):
        return True
    node[mrv_pos] = domain
return False
```

## 2.4 Backtracking + MRV + FC

We added the forward\_checking method to the gameNode class:

```
def forward_checking(self, pos):
    # Use AC-3 with limited queue
    queue = [(n, pos) for n in self.get_neighbors(pos)
        if not self[n].value()]
    return self._ac3(queue)
def _ac3(self, queue):
    # Based on Figure 6.3 from page 209 of the textbook
    while queue:
        pos1, pos2 = queue.pop()
        if self[pos2].value() in self[pos1].domain:
            self[pos1].domain -= self[pos2].domain
            if not self[pos1].domain:
                return False
            for pos3 in set(self.get_neighbors(pos1)) - {pos2}:
                queue.append((pos3, pos1))
    return True
```

The implementation of backtracking + MRV + forward checking in csp.py is:

```
def backtrackingMRVfwd(filename):
   node = gameNode.gameNode()
    if not node.load_game(filename):
        return ("Error: Fail Load", 0)
    if backtrackingMRVfwd_helper(node):
        return node.solution()
    return ("Error: No Solution", node.num_checks)
def backtrackingMRVfwd_helper(node):
    # Based on Figure 6.5 from page 215 of the textbook
    if node.solved():
        return True
   unassigned = node.get_unassigned_positions()
    if not unassigned:
        return False
   mrv_pos = min(unassigned, key=lambda p: len(node.get_valid_moves(p)))
    lcv_moves = sorted(node.get_valid_moves(mrv_pos),
        key=lambda m: node.count_constraints(mrv_pos, m))
    for move in lcv_moves:
```

```
backup_board = copy.deepcopy(node.board)
node[mrv_pos] = move
if (node.forward_checking(mrv_pos) and
          backtrackingMRVfwd_helper(node)):
        return True
node.board = backup_board
return False
```

### 2.5 Backtracking + MRV + CP

We added the *propagate\_constraints* method to the *gameNode* class:

```
def propagate_constraints(self):
    # Use AC-3 with all constrained pairs
    queue = []
    for pos1 in self.get_positions():
        for pos2 in self.get_neighbors(pos1):
            if (pos2, pos1) not in queue:
                 queue.append((pos1, pos2))
    return self._ac3(queue)
```

The implementation of backtracking + MRV + constraint propagation in csp.py is:

```
def backtrackingMRVcp(filename):
   node = gameNode.gameNode()
    if not node.load_game(filename):
        return ("Error: Fail Load", 0)
    if backtrackingMRVcp_helper(node):
        return node.solution()
   return ("Error: No Solution", node.num_checks)
def backtrackingMRVcp_helper(node):
    # Based on Figure 6.5 from page 215 of the textbook
    if node.solved():
        return True
    unassigned = node.get_unassigned_positions()
    if not unassigned:
        return False
   mrv_pos = min(unassigned, key=lambda p: len(node.get_valid_moves(p)))
    lcv_moves = sorted(node.get_valid_moves(mrv_pos),
        key=lambda m: node.count_constraints(mrv_pos, m))
    for move in lcv_moves:
        backup_board = copy.deepcopy(node.board)
        node[mrv_pos] = move
        if node.propagate_constraints() and backtrackingMRVcp_helper(node):
            return True
        node.board = backup_board
    return False
```

#### 2.6 Min-conflicts

We added the *count\_conflicts* method to the *gameNode* class:

```
def count_conflicts(self, pos, value=None):
    if value is None:
      value = self[pos].value()
```

```
return len([n for n in self.get_neighbors(pos)
   if self[n].value() == value])
```

The implementation of min-conflicts in csp.py is:

```
def minConflict(filename):
   node = gameNode.gameNode()
    if not node.load_game(filename):
        return ("Error: Fail Load", 0)
    if minConflict_helper(node):
        return node.solution()
    return ("Error: No Solution", node.num_checks)
def minConflict_helper(node, max_steps=10000):
    # Based on Figure 6.8 from page 221 of the textbook
    # initial complete assignment
    # greedy minimal-conflict values for each variable
    for pos in node.get_positions():
        if not node[pos].given:
            node[pos] = min(node.get_values(),
                key=lambda m: node.count_conflicts(pos, m))
   for _ in xrange(max_steps):
        if node.solved():
            return True
        con_pos = random.choice(node.get_conflicted_positions())
        lcv_move = min(node.get_values(),
            key=lambda m: node.count_conflicts(con_pos, m))
        node[con_pos] = lcv_move
    return False
```

#### 3 Results

#### 3.1 Test cases

#### 3.1.1 Empty Input

As a given input in the assignment, we use an empty board to test our algorithms. The result is shown in table 1.

#### 3.1.2 Manual Cases

We added several manual test cases (including the ones provided by Caleb on Piazza) to compare the results.

#### 3.2 Benchmarks

## 4 Conclusion

#### 4.1 Optimizations in backtracking

In the test result, we could see that with different extra optimization methods to choose the next backtracking node worked much better than the simple backtracking with arbitrary node sequence. The methods really chose "better" nodes to expand in the progress as we expected and we learnt from the lectures.

	BT	BT+MRV	BT+MRV+FC	BT+MRV+CP	Min-conflicts
Empty $(9 \times 9)$	392	82	49	82	>10K
Empty $(12 \times 12)$	7426	145	95	145	40
board1	210	77	74	75	>10K
board2	46019	2482	2458	N/A	N/A
board3	N/A	248	244	239	>10K
board4	N/A	N/A	N/A	N/A	N/A
board5	N/A	N/A	N/A	N/A	N/A

Table 1: Expanded node counts for all algorithms in different test cases

## 4.2 Hanging

The min-conflicts algorithm sometimes does not solve a board, even with a high iteration limit. We suspect that this is because it uses random choices to solve the board, and sometimes those choices are not useful ones.

## 4.3 Best algorithm

We recommend using backtracking search with the MRV heuristic and forward checking. This algorithm made the fewest consistency checks in our testing. MRV + constraint propagation performed roughly the same as MRV by itself, but was much slower. (This may be due to an inefficient implementation of constraint propagation.) Min-heuristics sometimes made even fewer consistency checks than BT+MRV+FC, but other times it would fail to solve the board.