

# A RELIABILITY-AWARE DISTRIBUTED FRAMEWORK TO SCHEDULE RESIDENTIAL CHARGING OF ELECTRIC VEHICLES

Presented by Rounak Meyur

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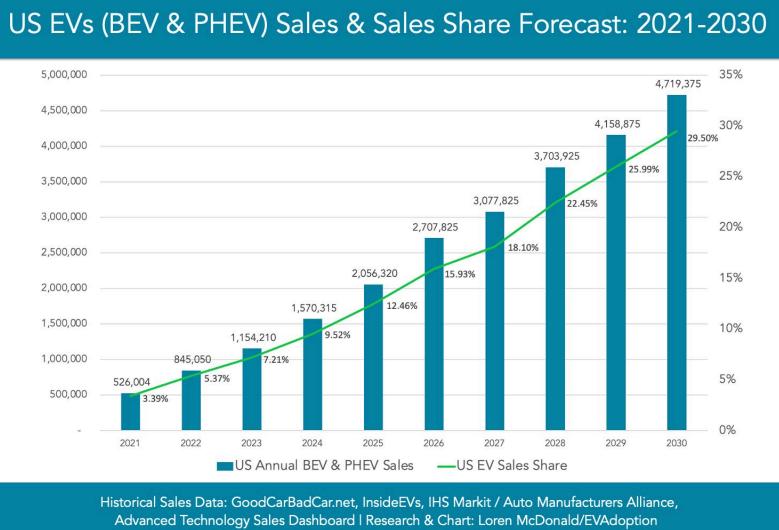


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Henning Mortveit

# MOTIVATION



EV home charging startups on the rise

The number of startup companies offering residential charging services for electric vehicles has risen to more than 100 in Europe and more than 50 in the United States.

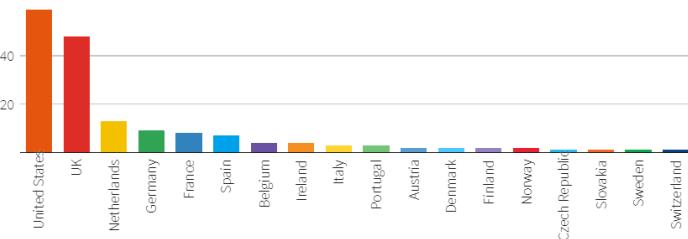
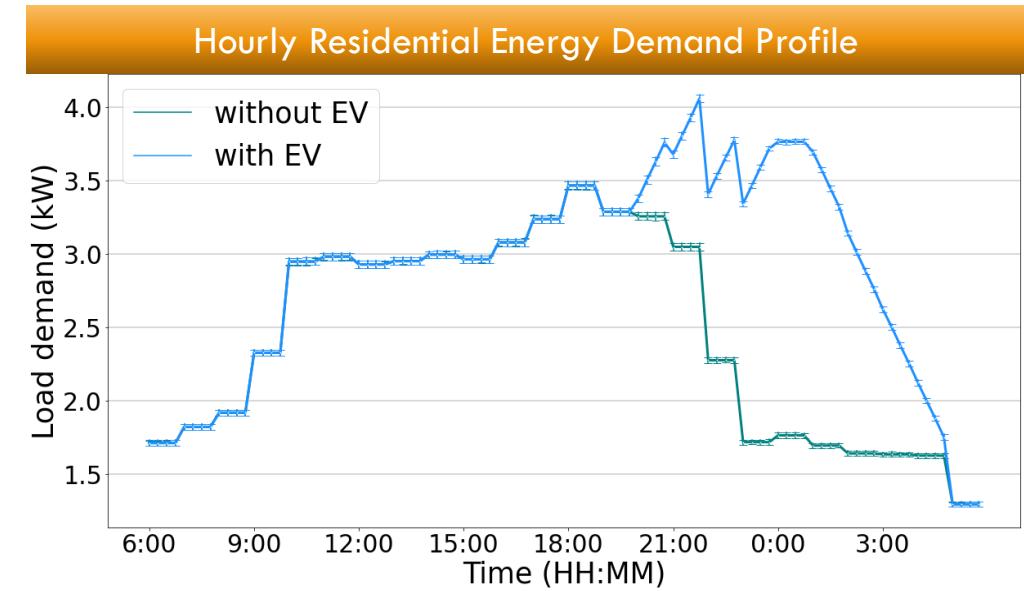


Image source: Reuters



Residential EV charging accounts for a significant amount of increase in average household energy consumption

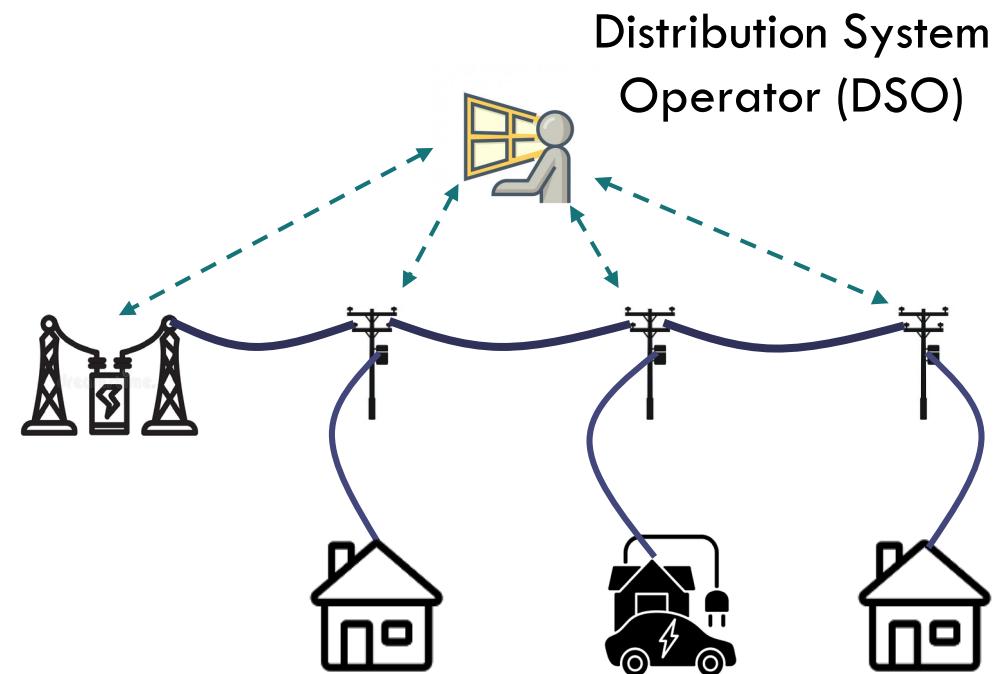
# PROBLEM STATEMENT

Find out the best schedule for residential EV charging which

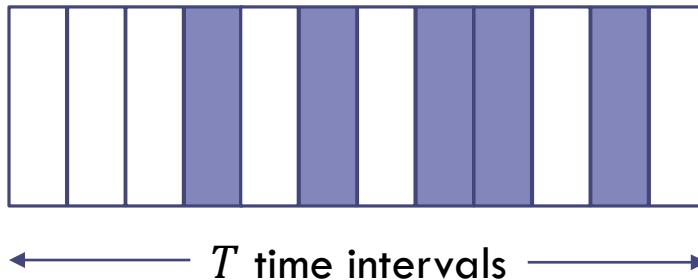
- accommodates consumer preferences.
- maintains network reliability.

Reliable network

- Node voltages within acceptable limits (0.95 – 1.05 p.u.).
- Line power flows less than line capacities.



# PROBLEM FORMULATION: A SINGLE RESIDENTIAL CONSUMER



$z_i^t = 0$  : No EV charging  
 $z_i^t = 1$  : EV charging

$p_{i,EV}^t = z_i^t P_{i,EV}$   
Power consumed only  
for selected intervals

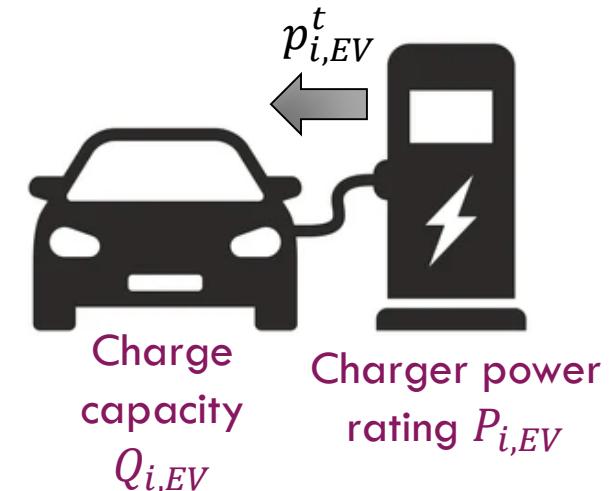
Find optimal time intervals to charge EV at minimum cost.

- $c_i^t$ : tariff rate
- $p_i^t$ : power consumption

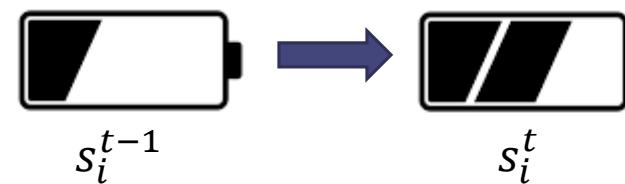
$$p_i^t = p_{i,EV}^t + p_{i,0}^t$$

- Goal:

$$\min \sum_{t=1}^T c_i^t p_i^t$$



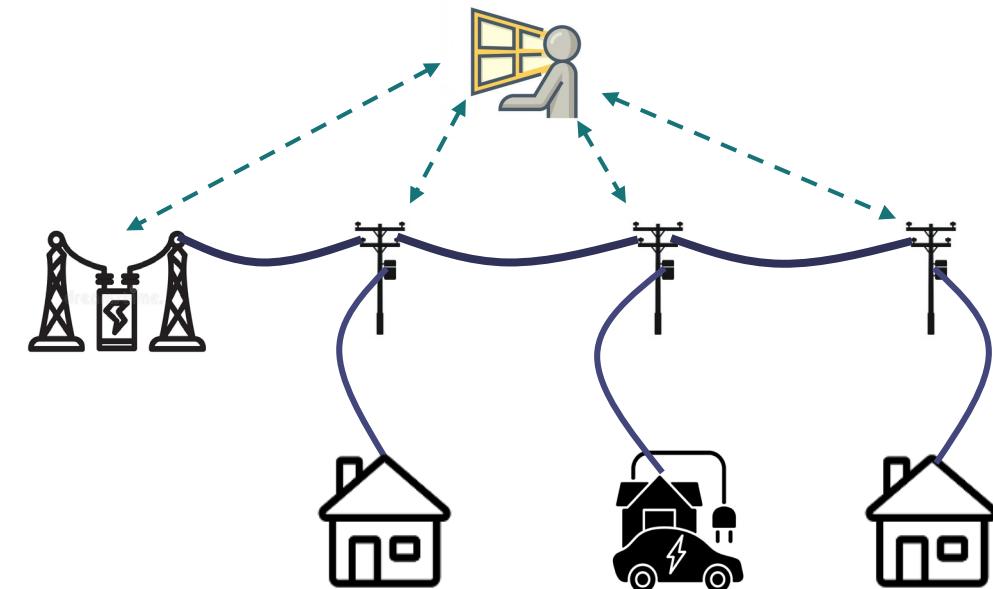
Evolution of state of charge



$$s_i^t = s_i^{t-1} + \frac{p_{i,EV}^t}{Q_{i,EV}}$$

# PROBLEM FORMULATION: DISTRIBUTION SYSTEM OPERATOR

- DSO reliability objectives:
  - Edge power flows within line ratings.
  - Node voltages within engineering standards.
- ANSI standard for distribution network voltages[1].
  - Lower limit:  $\alpha = 0.95 \text{ pu}$
  - Upper limit:  $\beta = 1.05 \text{ pu}$ .
  - $\alpha \mathbf{1} \leq \mathbf{v} \leq \beta \mathbf{1}$
- DSO personal objectives:
  - Minimize losses.
  - Minimize voltage deviation.



[1] American National Standards Institute ANSI. ANSI C84.1-2020: Electric Power Systems Voltage Ratings (60 Hz), 2020

# REVS: RELIABILITY AWARE EV CHARGE SCHEDULING

$$\begin{aligned}
 & \min \sum_{t=1}^T c_i^t p_i^t \\
 \text{over } & p_i^t, s_i^t, z_i^t \quad \forall t \\
 \text{s.t. } & p_i^t = p_{i,0}^t + p_{i,EV}^t \quad \forall t \\
 & p_{i,EV}^t = z_i^t P_{i,EV} \quad \forall t \\
 & s_i^t = s_i^{t-1} + \frac{p_{i,EV}^t}{Q_{i,EV}} \quad \forall t \\
 & z_i^t \in \{0, 1\} \quad \forall t \\
 & z_i^t = 0 \quad \forall t \leq t_{\text{start}}, \forall t \geq t_{\text{end}} \\
 & s_i^{t_{\text{start}}} = s_{i,\text{init}}, s_i^{t_{\text{end}}} \geq s_{i,\text{final}}
 \end{aligned}$$

Consumer optimization  
(MILP)

$$\begin{aligned}
 & \min \sum_{t=1}^T C(\mathbf{p}^t) \\
 \text{over } & \mathbf{p}^t \\
 \text{s.t. } & \alpha \mathbf{1} \leq -2R\mathbf{p}^t + \mathbf{1} \leq \beta \mathbf{1} \quad \forall t \\
 & -\bar{\mathbf{f}} \leq \mathbf{A}^{-1}\mathbf{p} \leq \bar{\mathbf{f}} \quad \forall t
 \end{aligned}$$

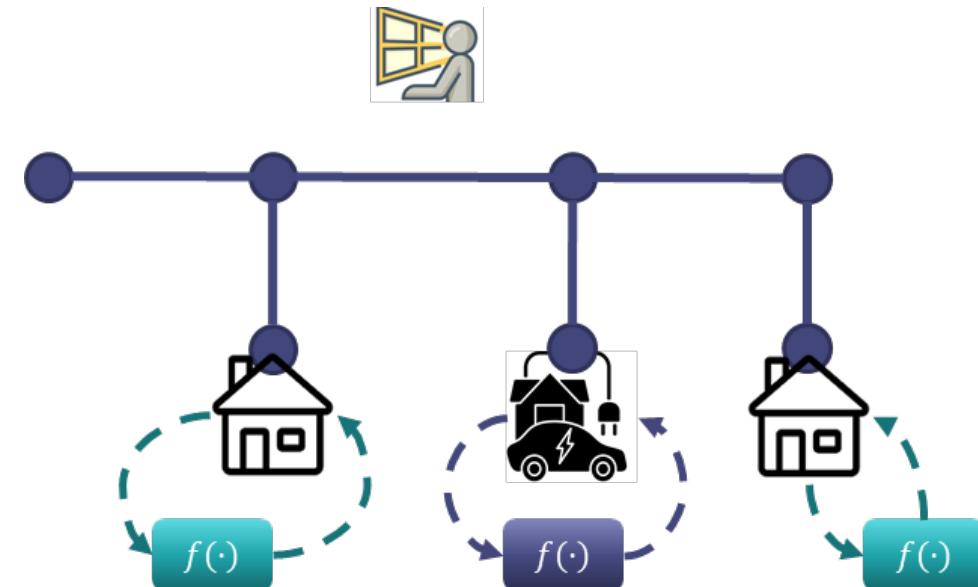
DSO optimization  
(LP or QP)

$$\begin{aligned}
 & \min \left[ \sum_{t=1}^T C(\mathbf{p}^t) + \sum_{i \in \mathcal{H}} \sum_{t=1}^T c_i^t p_i^t \right] \\
 \text{over } & p_i^t, s_i^t, z_i^t \quad \forall t, \forall i \in \mathcal{H} \\
 \text{s.t. } & p_i^t = p_{i,0}^t + p_{i,EV}^t \quad \forall t, \forall i \in \mathcal{H} \\
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 & s_i^{t_{\text{start}}} = s_{i,\text{init}} \quad \forall i \in \mathcal{H} \\
 & s_i^{t_{\text{end}}} = s_{i,\text{final}} \quad \forall i \in \mathcal{H} \\
 & p_i^t = 0 \quad \forall t, \forall i \notin \mathcal{H} \\
 & \alpha \leq 1 - 2 \sum_j R_{ij} p_j^t \leq \beta \quad \forall t, \forall i \\
 & -\bar{f}_k \leq \sum_j [\mathbf{A}^{-1}]_{kj} p_j^t \leq \bar{f}_k \quad \forall t, \forall k \in \mathcal{E}
 \end{aligned}$$

Overall optimization  
(MILP or MIQP)

# INDIVIDUAL APPROACH

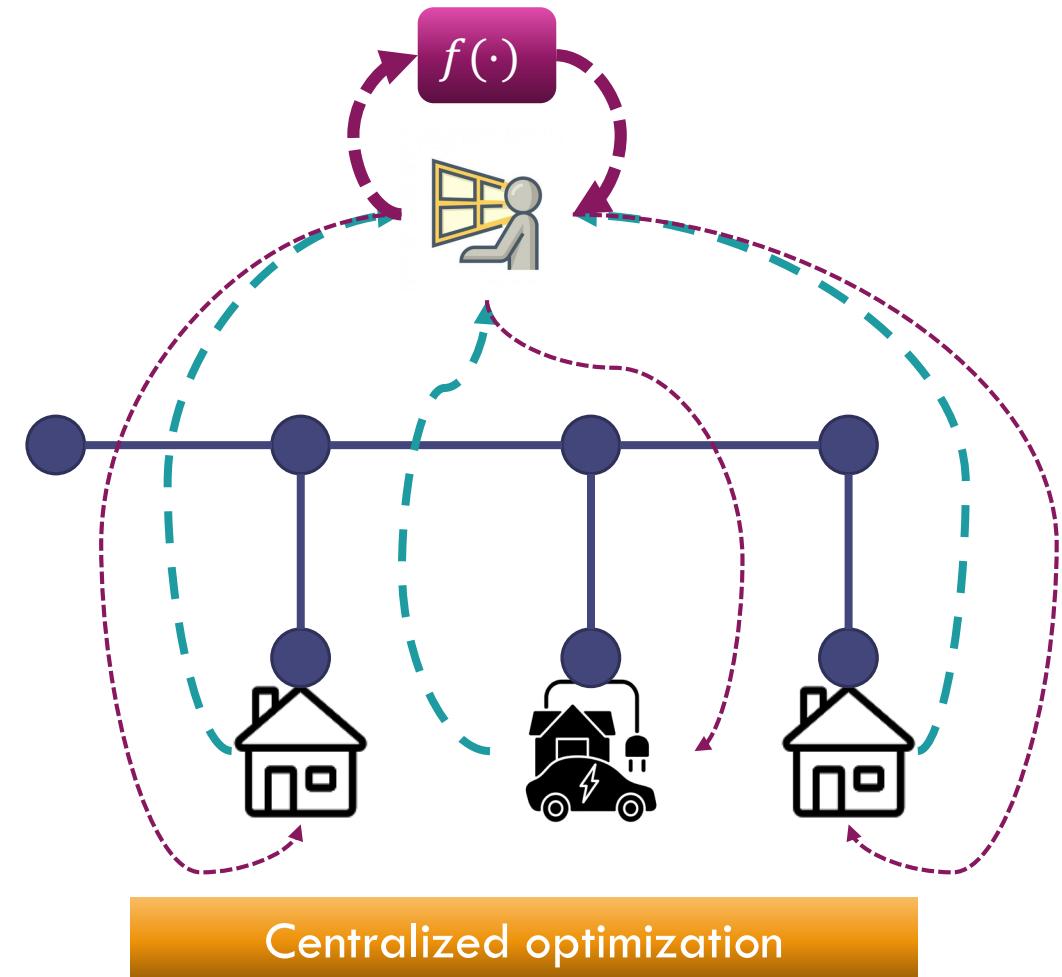
- Each consumer solves own problem.
- No private information shared.
- No communication requirement.
- Optimal solution for individual consumer.
- Suboptimal or infeasible solution for DSO.



Individual optimization

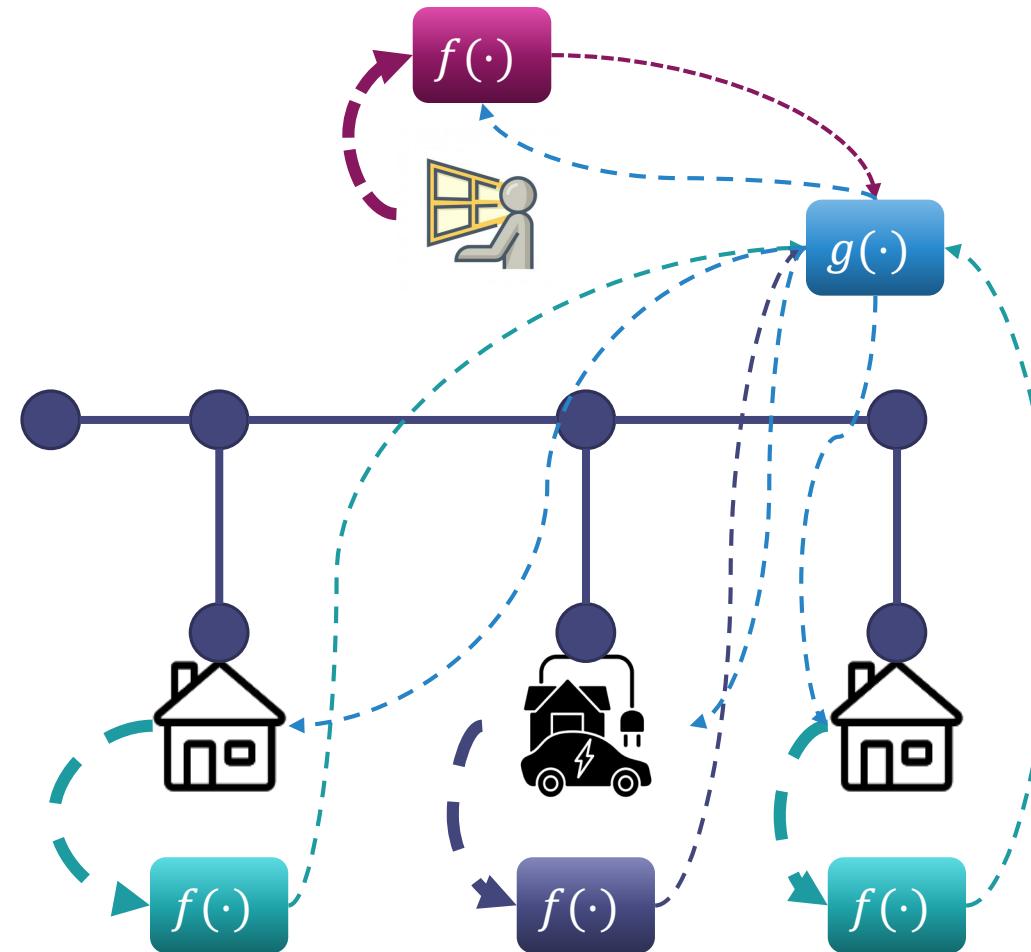
# CENTRALIZED APPROACH

- All consumers share personal information with DSO.
- High bandwidth for communication required.
- Optimal solution guaranteed for consumers and DSO.



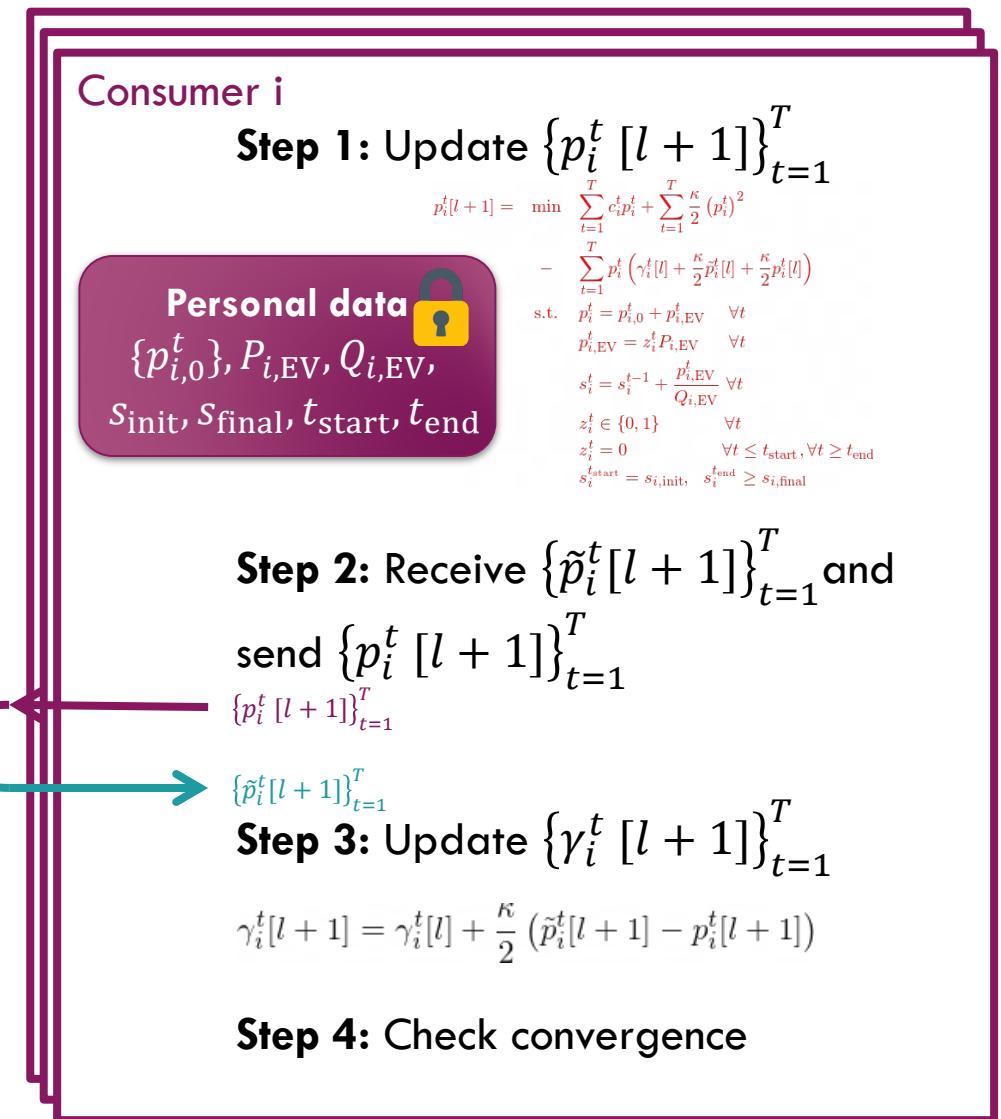
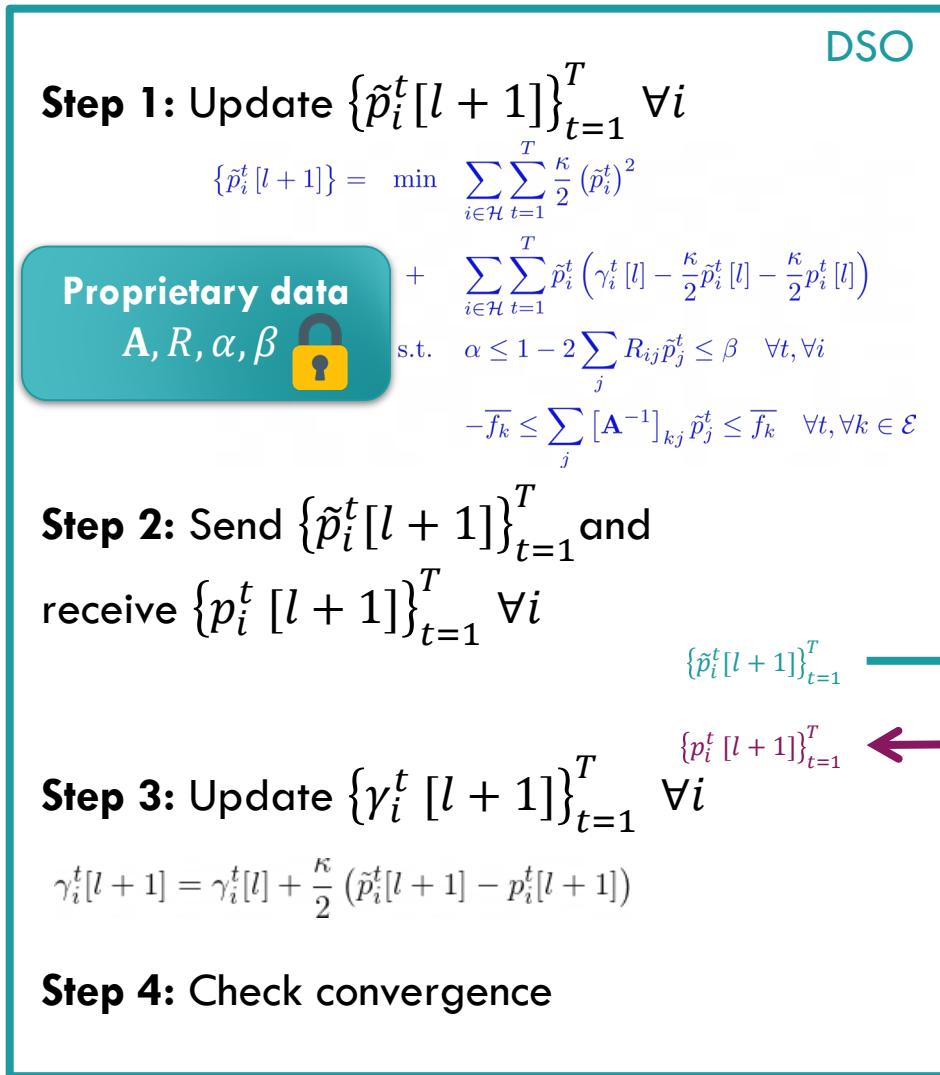
# OUR APPROACH

- All consumers solve their own problem.
- DSO solves reliability problem.
- Optimal solutions are exchanged to reach consensus.
- Limited communication requirement.
- Limited exchange of information.
- Sub-optimal solution for consumers and DSO.

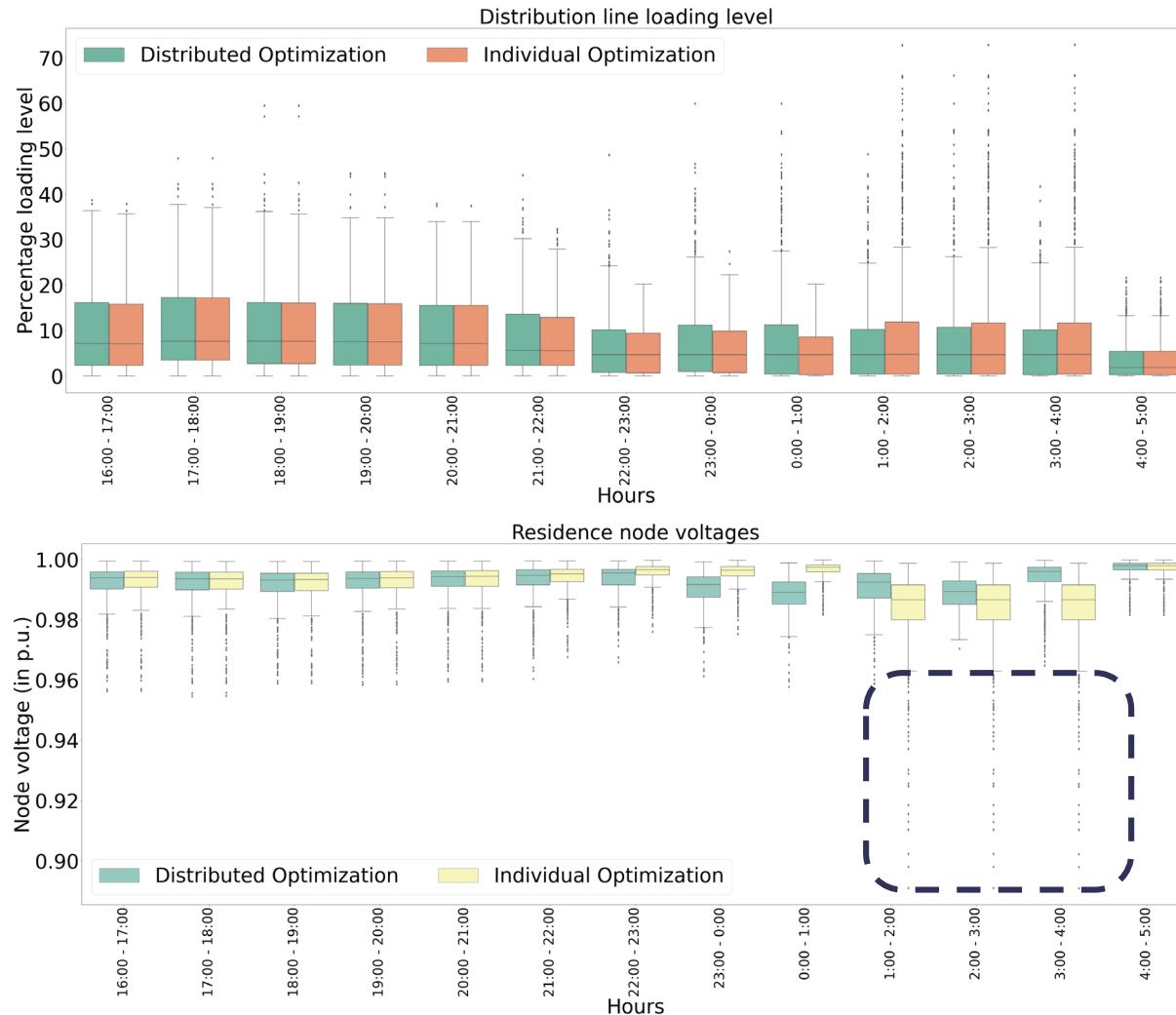


Distributed optimization

# PROPOSED DISTRIBUTED APPROACH



# RESULTS



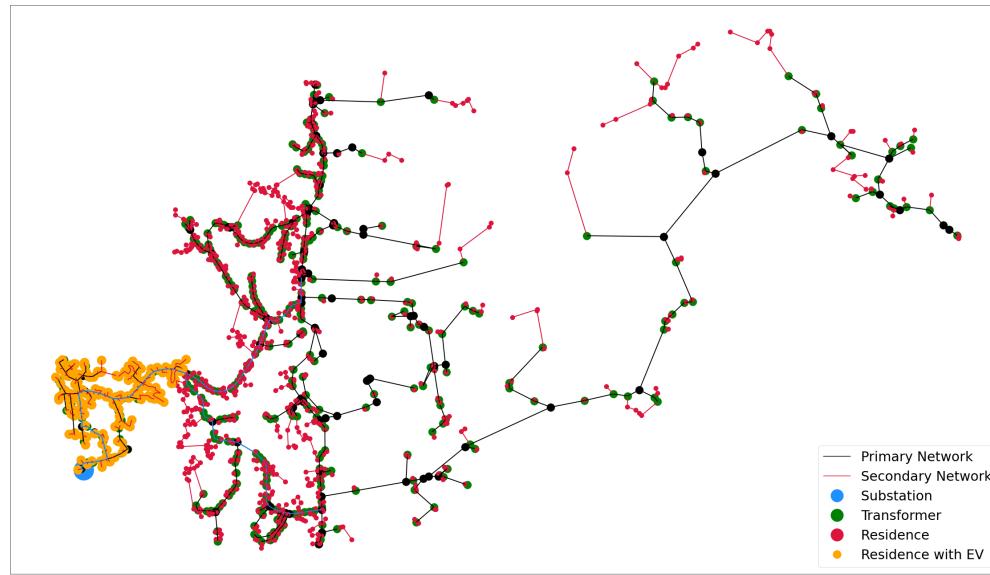
Electricity hourly tariff rates

Time Interval (HH:MM)	00:00 – 05:00	05:00 – 15:00	15:00 – 18:00	18:00 – 00:00
Tariff (\$/kWh)	0.07866	0.09511	0.21436	0.09511

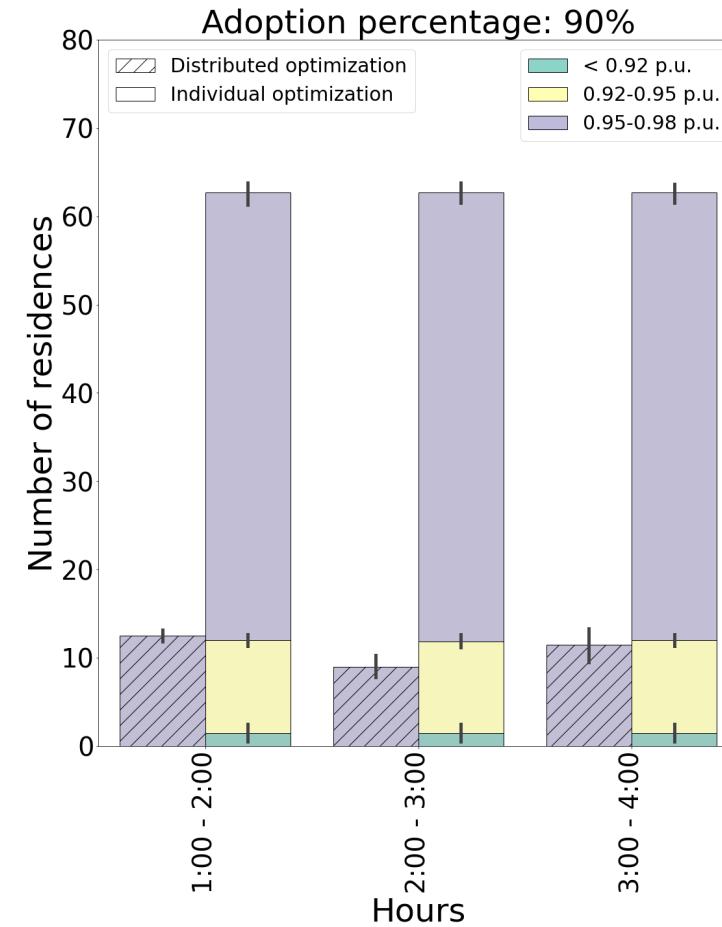
## Key observations

- Line limits are not violated even at high EV adoption levels.
- Voltage limits are violated when EV charging is done in an uncoordinated way.

# RESULTS



- We study impact of 90% EV adoption in a residential community.
- Individual optimization is compared to the proposed distributed approach.



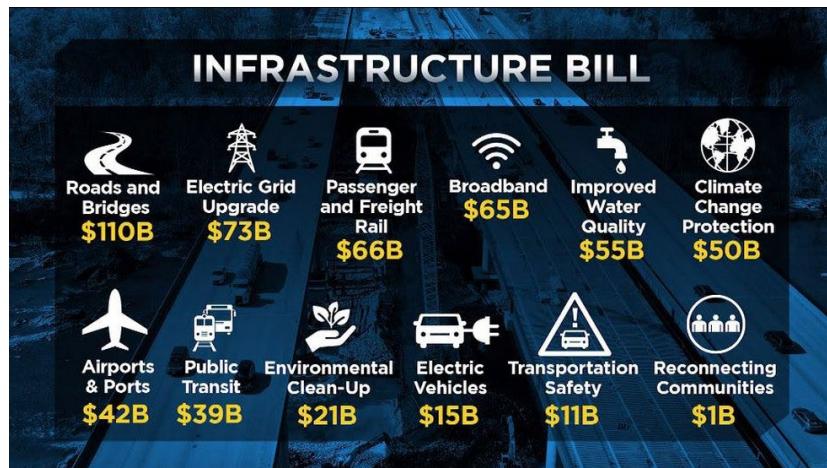
Higher level of reliability attained if consumers coordinate with the DSO

1. Thorve et.al, "High Resolution Synthetic Residential Energy Use Profiles for the United States", Nature Scientific Data, 2022 (accepted for publication).
2. Meyur et.al, "Realistic Ensembles of Power Distribution Networks", Proceedings of the National Academy of Sciences (PNAS), 2022 (provisionally accepted for publication).

# CONCLUSIONS AND FUTURE WORK

Biden signs \$1.2 trillion infrastructure bill with funding for EVs, transmission, hydrogen

Published Nov. 8, 2021 • Updated Nov. 16, 2021



Source: The Associated Press, Nov 7, 2021

**Biden's \$1.2 trillion infrastructure bill could take years to transform U.S.**

By Jeff Stein and Michael Laris

August 10, 2021 at 12:43 p.m. EDT

## Powering Smart Transportation

Smart Charging Infrastructure Pilot Program



The Smart Charging Infrastructure Pilot (or "SCIP") Program supports electric vehicle (EV) adoption in Virginia and will inform the design of managed charging programs and other EV customer offerings in the future.

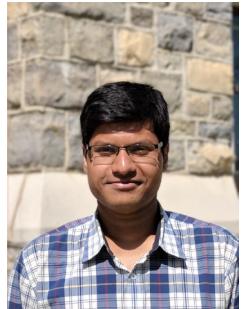
The SCIP Program provides rebates for qualifying EV charging stations, charging infrastructure and installation, commonly referred to as "make-ready," and network fees. See rebate amounts in the table below.

*March 23, 2021 Update: The DCFC and Multi-family rebate segments are fully subscribed.*

*June 20, 2022 Update: The SCIP Program will end December 31, 2022. All applications must be submitted by November 30, 2022. All charging stations must be installed, active and communicating data by December 31, 2022 to receive rebate payments.*

Source: Dominion Energy Smart Charger Rebate Plan

# OUR TEAM



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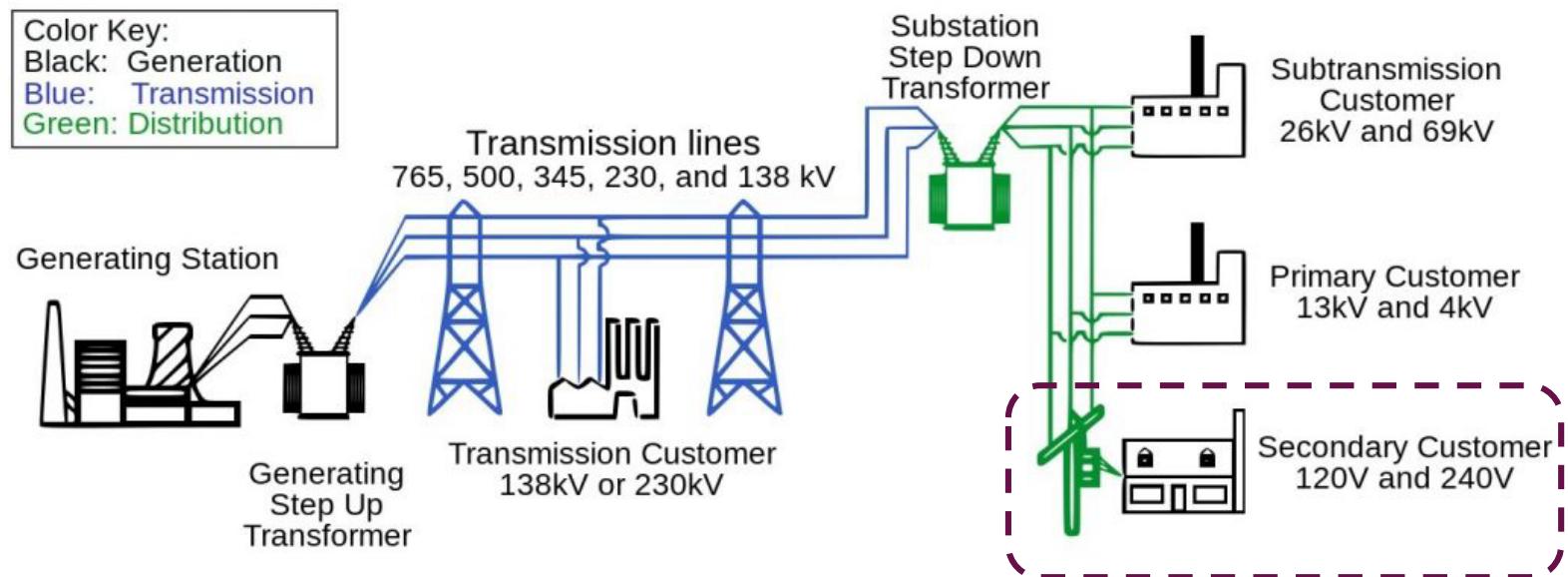
# QUESTIONS

# APPENDIX

# THE POWER GRID

Power grid consists of

- Generation
- Transmission system
- Distribution system



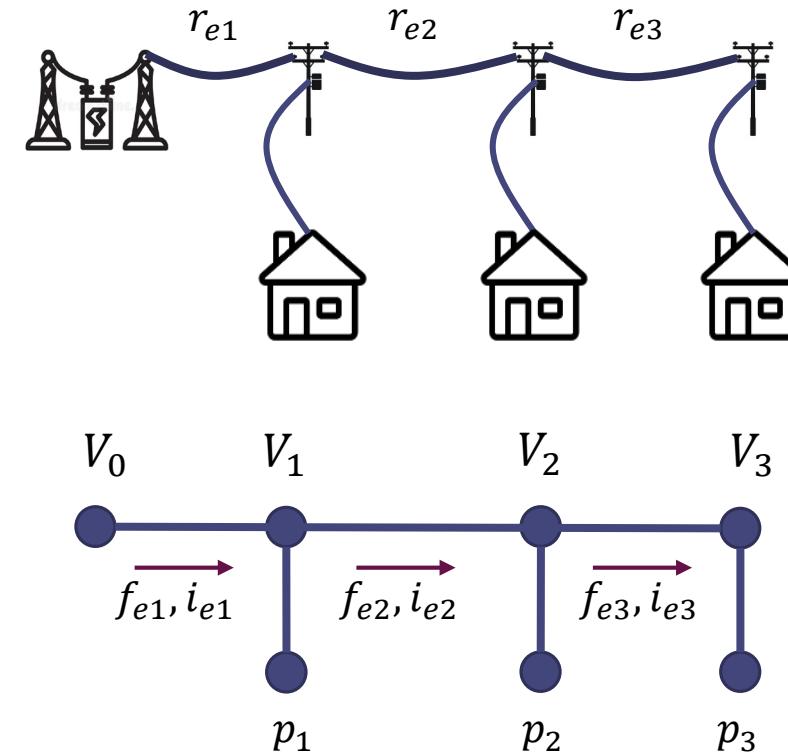
# DISTRIBUTION SYSTEM

- The distribution network has a tree structure.
  - Power flows in one direction.
- Voltage drop along each edge  $e := (i, j)$
$$V_i - V_j = i_e r_e$$
- Maximum voltage drop for nodes far away from root.
- Linearized Distribution Flow (LDF) Model [1].
$$v_i - v_j = 2r_e f_e$$

- Linearizes the relation between voltage and power flow.

$$V_i - V_j = r_e i_e \quad \xrightarrow{\text{LDF}} \quad v_i - v_j = 2r_e f_e$$

$$v_i = V_i^2$$



# POWER FLOW PROBLEM

Given power consumption at nodes in the network  
find the node voltages and edge power flows.

- How to find edge flows from power consumption?
  - $\mathbf{p} = \mathbf{A}_{\text{red}}^T \mathbf{f}$
- How to infer voltages from power consumption?
  - $\mathbf{R} = \mathbf{A}_{\text{red}}^{-1} \mathbf{D}_R (\mathbf{A}_{\text{red}}^{-1})^T$
  - $\mathbf{v} = v_0 \mathbf{1} - 2 \mathbf{R} \mathbf{p}$

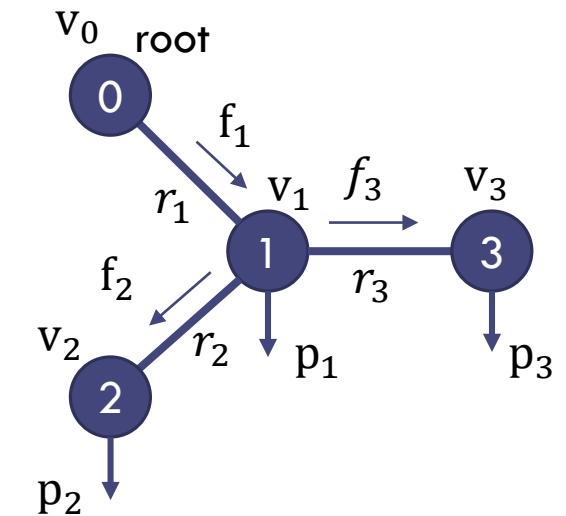
$$\mathbf{A} = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 0 & -1 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{bmatrix}$$

$$\mathbf{A}_{\text{red}} = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\mathbf{D}_R = \begin{bmatrix} r_1 & 0 & 0 \\ 0 & r_2 & 0 \\ 0 & 0 & r_3 \end{bmatrix}$$

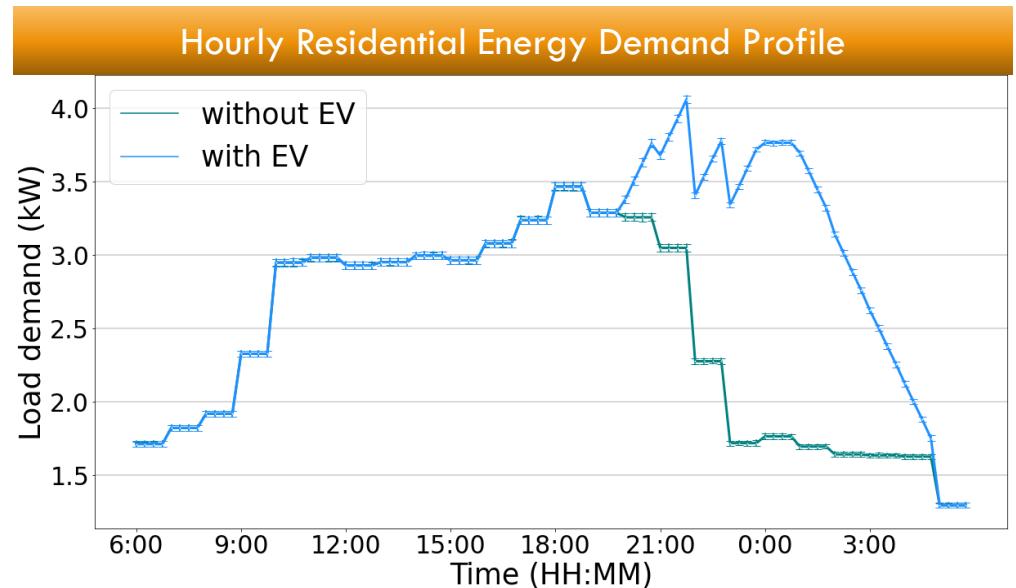
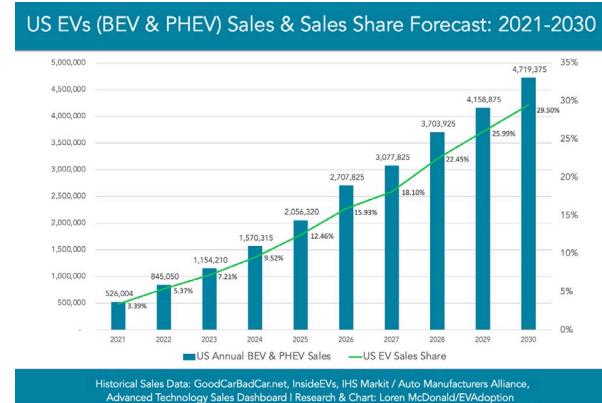
*Sanity check*

$$\mathbf{p} = \begin{bmatrix} p_1 \\ p_2 \\ p_3 \end{bmatrix} = \begin{bmatrix} 1 & -1 & -1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} f_1 \\ f_2 \\ f_3 \end{bmatrix} = \mathbf{A}_{\text{red}}^T \mathbf{f}$$



# MOTIVATION

- ❑ Electrification of vehicles.
  - ❑ EV sales projected to go up 10 times by 2030.
  - ❑ EV charging outlets at residences.
- ❑ Residential charging of EVs alters the average residential energy demand profile.



# PRIOR WORKS

- ❑ Optimization techniques are a popular choice for the scheduling problem [1,2].
- ❑ Reinforcement learning and other neural networks-based frameworks [3,4].
- ❑ Centralized approaches require exchange of private information.
- ❑ Alternating Direction Method of Multipliers (ADMM) based distributed approach for inverter control proposed in [5].

[1] Yijia Cao, Shengwei Tang, Canbing Li, Peng Zhang, Yi Tan, Zhikun Zhang, and Junxiong Li. An optimized EV charging model considering TOU price and SOC curve. *IEEE Transactions on Smart Grid*, 3(1):388–393, 2012.

[2] Yue Zhao, Yan Chen, and Brian Keel. Optimal scheduling of home energy management system with plug-in electric vehicles using model predictive control, Sep 2018.

[3] Yongsheng Cao, Hao Wang, Demin Li, and Guanglin Zhang. Smart online charging algorithm for electric vehicles via customized actor–critic learning. *IEEE Internet of Things Journal*, 9(1):684–694, 2022..

[4] Salman Sadiq Shuvo and Yasin Yilmaz. Cibecs: Consumer input based electric vehicle charge scheduling for a residential home. In *2021 North American Power Symposium (NAPS)*, pages 1–6, 2021.

[5] Emiliano Dall’Anese, Sairaj V. Dhople, Brian B. Johnson, and Georgios B. Giannakis. Decentralized optimal dispatch of photovoltaic inverters in residential distribution systems. *IEEE Transactions on Energy Conversion*, 29(4):957–967, 2014.

# PROBLEM FORMULATION: DISTRIBUTION SYSTEM OPERATOR

## □ DSO reliability objectives:

- Edge power flows within line ratings.
- Node voltages within engineering standards.

## □ ANSI standard for distribution network

voltages[1].

- Lower limit:  $\alpha = 0.95$  pu
- Upper limit:  $\beta = 1.05$  pu.
- $\alpha\mathbf{1} \leq \mathbf{v} \leq \beta\mathbf{1}$

## □ DSO personal objectives:

- Minimize losses.
- Minimize voltage deviation.

$$\begin{array}{ll}\min & \sum_{t=1}^T C(\mathbf{p}^t) \\ \text{over} & \mathbf{p}^t \\ \text{s.t.} & \alpha\mathbf{1} \leq -2R\mathbf{p}^t + \mathbf{1} \leq \beta\mathbf{1} \quad \forall t \\ & -\bar{\mathbf{f}} \leq \mathbf{A}^{-1}\mathbf{p} \leq \bar{\mathbf{f}} \quad \forall t\end{array}$$



If ensuring reliability  
is the sole objective

$$\begin{array}{ll}\text{find} & \mathbf{p}^t \\ \text{s.t.} & \alpha\mathbf{1} \leq -2R\mathbf{p}^t + \mathbf{1} \leq \beta\mathbf{1} \quad \forall t \\ & -\bar{\mathbf{f}} \leq \mathbf{A}^{-1}\mathbf{p} \leq \bar{\mathbf{f}} \quad \forall t\end{array}$$

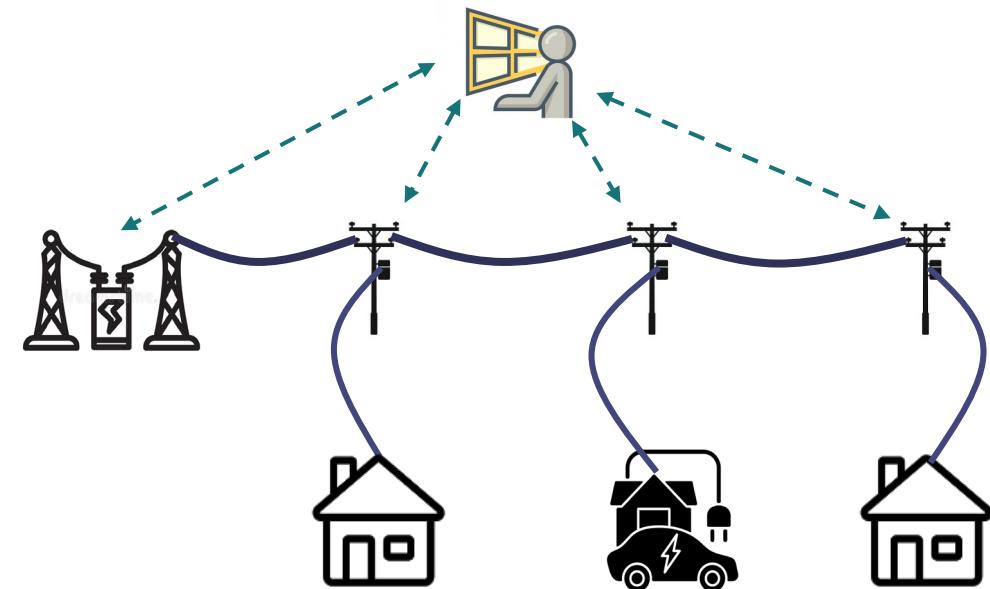
# MOTIVATION

## ❑ Impact on network

- Increased edge power flow.
- Drop in node voltages.

## ❑ Distribution system operator (DSO) needs a framework to

- accommodate residential EV charging according to consumer personal preferences
- maintain network reliability



When can you charge your EVs?

# PROPOSED DISTRIBUTED APPROACH

- Introduce new variable  $\tilde{p}_i^t$  for each residence.
- ADMM[1] based iterative solution.

$$\begin{aligned}
 \min \quad & \sum_{t=1}^T C(\mathbf{p}^t) + \sum_{i \in \mathcal{H}} \sum_{t=1}^T c_i^t p_i^t \\
 \text{over} \quad & p_i^t, s_i^t, z_i^t, \tilde{p}_i^t \quad \forall t, \forall i \in \mathcal{H} \\
 \text{s.t.} \quad & p_i^t = p_{i,0}^t + p_{i,EV}^t \quad \forall t, \forall i \in \mathcal{H} \\
 & p_{i,EV}^t = z_i^t P_{i,EV} \quad \forall t, \forall i \in \mathcal{H} \\
 & s_i^t = s_i^{t-1} + \frac{p_{i,EV}^t}{Q_{i,EV}} \quad \forall t, \forall i \in \mathcal{H} \\
 & z_i^t \in \{0, 1\} \quad \forall t, \forall i \in \mathcal{H} \\
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 & s_i^{t_{\text{end}}} = s_{i,\text{final}} \quad \forall i \in \mathcal{H} \\
 & \alpha \leq 1 - 2 \sum_j R_{ij} \tilde{p}_j^t \leq \beta \quad \forall t, \forall i \\
 & -\bar{f}_k \leq \sum_j [\mathbf{A}^{-1}]_{kj} \tilde{p}_j^t \leq \bar{f}_k \quad \forall t, \forall k \in \mathcal{E} \\
 & p_i^t = \tilde{p}_i^t \quad \forall t, \forall i \in \mathcal{H}
 \end{aligned}$$

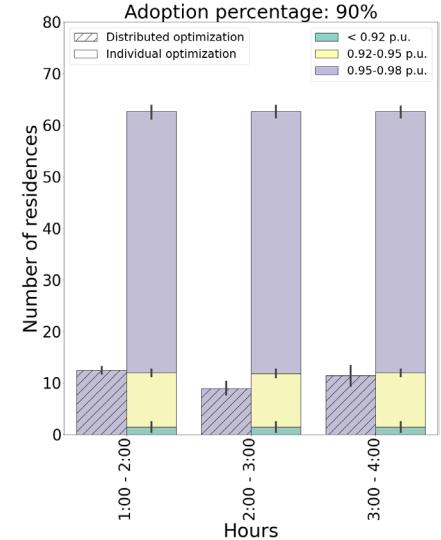
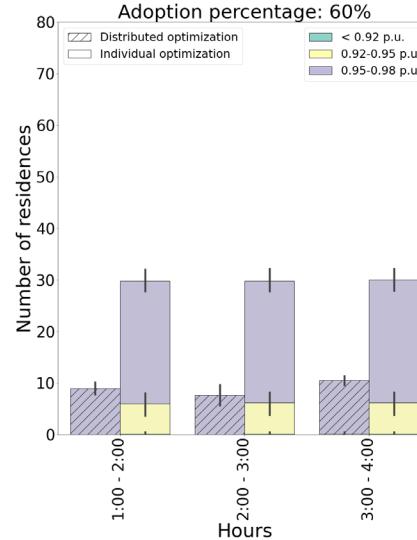
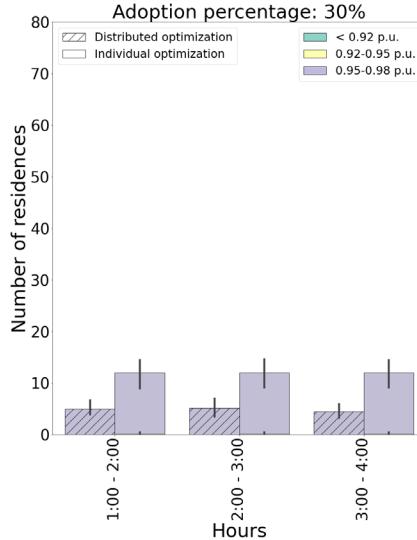
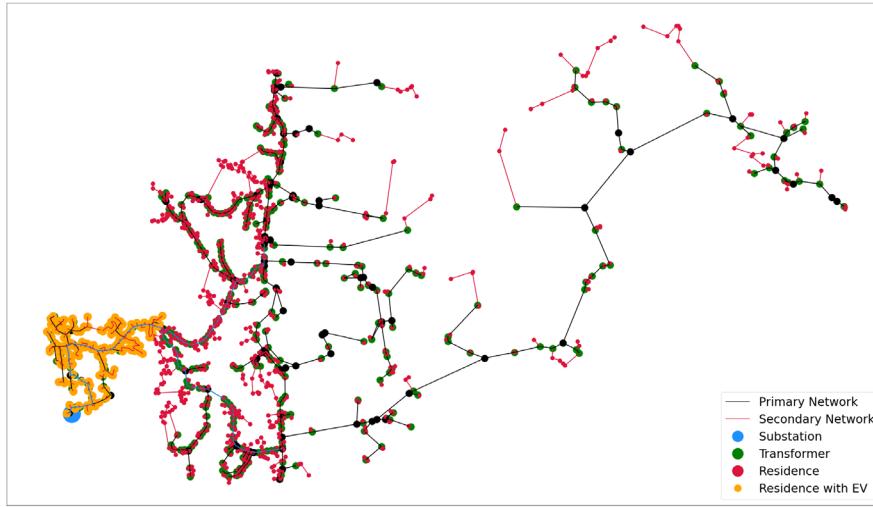
**DSO problem (QP)**

$$\begin{aligned}
 \{\tilde{p}_i^t[l+1]\} = \min \quad & \sum_{i \in \mathcal{H}} \sum_{t=1}^T \frac{\kappa}{2} (\tilde{p}_i^t)^2 \\
 \text{+} \quad & \sum_{i \in \mathcal{H}} \sum_{t=1}^T \tilde{p}_i^t \left( \gamma_i^t[l] - \frac{\kappa}{2} \tilde{p}_i^t[l] - \frac{\kappa}{2} p_i^t[l] \right) \\
 \text{s.t.} \quad & \alpha \leq 1 - 2 \sum_j R_{ij} \tilde{p}_j^t \leq \beta \quad \forall t, \forall i \\
 & -\bar{f}_k \leq \sum_j [\mathbf{A}^{-1}]_{kj} \tilde{p}_j^t \leq \bar{f}_k \quad \forall t, \forall k \in \mathcal{E}
 \end{aligned}$$

**Consumer  $i$  problem (MIQP)**

$$\begin{aligned}
 p_i^t[l+1] = \min \quad & \sum_{t=1}^T c_i^t p_i^t + \sum_{t=1}^T \frac{\kappa}{2} (p_i^t)^2 \\
 \text{-} \quad & \sum_{t=1}^T p_i^t \left( \gamma_i^t[l] + \frac{\kappa}{2} \tilde{p}_i^t[l] + \frac{\kappa}{2} p_i^t[l] \right) \\
 \text{s.t.} \quad & p_i^t = p_{i,0}^t + p_{i,EV}^t \quad \forall t \\
 & p_{i,EV}^t = z_i^t P_{i,EV} \quad \forall t \\
 & s_i^t = s_i^{t-1} + \frac{p_{i,EV}^t}{Q_{i,EV}} \quad \forall t \\
 & z_i^t \in \{0, 1\} \quad \forall t \\
 & z_i^t = 0 \quad \forall t \leq t_{\text{start}}, \forall t \geq t_{\text{end}} \\
 & s_i^{t_{\text{start}}} = s_{i,\text{init}}, \quad s_i^{t_{\text{end}}} \geq s_{i,\text{final}}
 \end{aligned}$$

# RESULTS



- Different EV adoption percentages in a residential community.
- Individual optimization is compared to the proposed distributed approach.

Higher level of reliability attained through the distributed approach