

# Correcting mutation rates for observer bias

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February 29, 2024

## Computing the mutation rates that would be observed given real mutation rates

Suppose that, for a sequence of length  $L$ , you know

- the real (unobserved) mutation rate for each position  $j$ :  $\mu_j$  ( $0 \leq \mu_j < 1$ ;  $1 \leq j \leq L$ )
- the real (unobserved) fraction of reads that start at position  $a$  and end at position  $b$ :  $\eta_{ab}$  ( $0 \leq \eta_{ab} \leq 1$ ;  $1 \leq a \leq b \leq L$ )

To reframe the problem in terms of probabilities, three events can happen:

$S$  The read spans position  $j$ , i.e.  $a \leq j \leq b$ .

$M$  Base  $j$  is mutated in the read.

$G$  The read contains no pair of mutations that are closer than the minimum gap  $g$ .

You want to calculate the mutation rate that you would observe at each position  $j$  due to the observer bias:  $m_j$ .