Defining Your Own Functions in Common Lisp

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Lisp:

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 - In a <u>dynamically</u> typed language (e.g., Lisp, Python, or Javascript), a <u>variable / formal parameter does not have</u> <u>a fixed type</u> and <u>may well store values of different types at different times</u>.

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As Lisp is dynamically typed, the above Lisp definition does <u>not</u> declare the types of the formal parameters n and x, and also does <u>not</u> declare the return type of f: The two argument values we pass into a call of f <u>can be</u> <u>numbers of any type</u>; the type of the result returned by f will depend on the types of the argument values.

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For example, if one argument value is an integer and the other a floating-point number, the returned result will be a floating-point number. But if both argument values are integers, then the result will be an integer.

If either argument value isn't a number, a type-mismatch error will be reported when the call (+ n x) is executed.

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- 5. There is <u>no</u> RETURN keyword before the expression whose value is to be returned.

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• The call (f 3 4.2) is analogous to the Java call f(3, 4.2F) and returns 7.2.

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- The call (f 3.0 4.0) returns 7.0. (Note that the Java call f(3.0F, 4.0F) would be **illegal** as the 1st argument of the Java function f is declared to have type **int**!)

A Simple Common Lisp Function Definition

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- The call (f 3 4) returns the *integer* 7, as the values of the parameters n and x are integers.

For any integer $k \ge 0$, a new Common Lisp function that takes k arguments can be defined as follows:

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(defun <func name> (<param><sub>1</sub> ... <param><sub>k</sub>)
  <body-expr>)
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A call of the function can be written as follows:

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(<func name> \langle arg \rangle_1 ... \langle arg \rangle_k)
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Another Example of a Common Lisp Function Definition
The following Java function was considered earlier:
// factorial(n) returns 1 * 2 * ... * (n-1) * n if <math>1 \le n \le 20
static long factorial (int n)
  return (n == 1)
           : factorial(n-1) * n;
We now write a Common Lisp analog of this function.
To do this, we use the following facts:
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We also note that:

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Note: Do <u>not</u> put these last two closing parentheses on separate lines! That would waste screen space and also serve no good purpose because Lisp programmers read and write code in editors that match parentheses for them!

The QUOTE Special Operator

QUOTE is a special operator you will use most often!

(QUOTE e) evaluates to e; e is not evaluated!

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453

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If F is the name of some Lisp function, then:
Evaluation of (F '(+ 3 4)) passes the list (+ 3 4)
   as argument to a call of the function F.
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455

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    Evaluation of (F 'X) passes the symbol X

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456

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- Evaluation of (F 'X) passes the symbol X as argument to a call of F.
- Evaluation of (F X) passes the value of the variable denoted by X as argument to a call of F.

•

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• `can do things 'can't. It's useful for writing macros, but you won't need to use `in this course.

Built-in Common Lisp Functions for Taking Lists Apart: CAR/FIRST and CDR/REST

Notation: For S-expressions e and e', we write $e \Rightarrow e'$ to mean that e evaluates to e'. **Examples:**

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Examples: (+ 4 5) \Rightarrow (SQRT (+ 4 5.0)) \Rightarrow (SQRT (3 SQRT)) \Rightarrow
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If e ⇒ a nonempty list L, then:
 (CAR e) ⇒ the <u>first</u> element of that list L.
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• If e \Rightarrow a nonempty list L, then:
     (CAR e) \Rightarrow the first element of that list L.
  Examples: (CAR '(DOG CAT (AT (3 +)))) \Rightarrow DOG
               (CAR '(DOG)) \Rightarrow DOG
               (CAR '((AT (3 +)) DOG CAT)) \Rightarrow (AT (3 +))
• If e \Rightarrow a nonempty list L, then:
     (CDR \ e) \Rightarrow the list obtained from L
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• (CAR NIL) \Rightarrow NIL and (CDR NIL) \Rightarrow NIL.
 This is illogical, but sometimes convenient!
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 This is illogical, but sometimes convenient!
 In Scheme, the car and cdr of an empty list are <u>undefined</u>.
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 E.g.: We get an error if (CAR (+ 3 4)), (CDR (+ 3 4)), (CAR (CAR '(A B))), or (CDR (CAR '(A B))) is evaluated!
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    Example: (CAR '(DOG CAT (AT (3 +)))) ⇒ DOG
```

- If e ⇒ a nonempty list L, then:
 (CDR e) ⇒ the list obtained from L
 by <u>omitting</u> its first element.
 Example: (CDR '(DOG CAT (AT (3 +)))) ⇒ (CAT (AT (3 +)))
- (CAR NIL) ⇒ NIL and (CDR NIL) ⇒ NIL.
 This is illogical, but sometimes convenient!
 In Scheme, the car and cdr of an empty list are <u>undefined</u>.
- If e ⇒ an atom other than NIL, then evaluation of (CAR e) or (CDR e) will produce an error!
 E.g.: We get an error if (CAR (+ 3 4)), (CDR (+ 3 4)),
- (CAR (CAR '(A B))), or (CDR (CAR '(A B))) is evaluated!
- Q. What happens if (CAR '(+ 3 4)) is evaluated? What happens if (CDR '(+ 3 4)) is evaluated?

Α.

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- A. $(CAR '(+ 3 4)) \Rightarrow + (CDR '(+ 3 4)) \Rightarrow (3 4)$

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 by <u>omitting</u> its first element.
- (CAR NIL) \Rightarrow NIL and (CDR NIL) \Rightarrow NIL.

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Alternative Names for CAR and CDR

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- REST is another name for CDR in Common Lisp.

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- FIRST is another name for CAR in Common Lisp.
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Thus:
$$(FIRST e) = (CAR e)$$
 $(REST e) = (CDR e)$

The names FIRST and REST have the advantage of being descriptive, but "CAR" and "CDR" provide the basis for the C...R function names we will consider later.

The following remarks regarding the origin of the names CAR and CDR are from pp. 42 - 3 of Touretzky:

These

names are relics from the early days of computing, when Lisp first ran on a machine called the IBM 704. The 704 was so primitive it didn't even have transistors—it used vacuum tubes. Each of its "registers" was divided into several components, two of which were the address portion and the decrement portion. Back then, the name CAR stood for Contents of Address portion of Register, and CDR stood for Contents of Decrement portion of Register. Even though these terms don't apply to modern computer hardware, Common Lisp still uses the acronyms CAR and CDR when referring to cons cells, partly for historical reasons, and partly because these names can be composed to form longer names such as CADR and CDDAR, as you will see shortly.