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- Notes: In sec. 2.3 of Sethi, the tokens IDENTIFIER and UNSIGNED-INT-LITERAL are called name and number, and a token instance is called a <u>spelling</u>.

 Many authors call a token instance a <u>Lexeme</u>.

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(defun f (if let quote) (+ if let quote)),
though it'd be a bad idea to write such code.

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A <u>lexical syntax specification</u> of a programming language specifies its tokens and the sequence of token instances into which any given piece of source code should be decomposed.

Use of Grammars to Define Syntactically Valid Code

If a piece of source code should be decomposed by a compiler into a sequence of token instances $t_1 ldots t_n$ in which each t_i is an instance of token T_i , we say $T_1 ldots T_n$ is the sequence of tokens of that source code.

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 More generally, when a nonterminal of G corresponds to a language construct X (e.g., statement), we say a piece of source code is a <u>syntactically valid</u> X if its sequence of tokens belongs to the set denoted by the nonterminal.

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See https://euclid.cs.qc.cuny.edu/316/Syntactic-Validity.pdf
for more on syntactic validity.

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               | Term - Term
    Expr ::= [+ | -] Term (+ | -) Term
        is equivalent to
    Expr ::= (+ | - | <empty>) Term (+ | -) Term
       which is equivalent to these 6 BNF productions:
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                           means "zero or more γs".
Examples
    Expr ::= Term (+ | -) Term
       is equivalent to the following 2 BNF productions:
    Expr ::= Term + Term
               Term - Term
    Expr ::= [+ | -] Term (+ | -) Term
       is equivalent to
    Expr ::= (+ | - | < empty>) Term (+ | - ) Term
       which is equivalent to these 6 BNF productions:
    Expr ::= + Term + Term | - Term + Term | Term + Term
                | + Term - Term | - Term - Term | Term - Term
```

EBNF notation supplements BNF notation with (...),

```
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        which is equivalent to these 6 BNF productions:
    Expr ::= + Term + Term | - Term + Term | Term + Term
                 | + Term - Term | - Term - Term | Term - Term
    Expr ::= Term \{(+ \mid -) \mid Term\}
        is equivalent to an infinite collection of BNF
        productions, including productions such as
    Expr ::= Term + Term + Term - Term + Term - Term
```

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Here k may be 1. Thus { Digit } can be replaced with a new nonterminal (DigitSeq, say) that is defined by:

DigitSeq ::= <empty> | DigitSeq Digit

- 2. Next, replace {Op Term} with a nonterminal Rest
 defined by: Rest ::= <empty> | Rest Op Term
 (**) becomes:

```
Example: We now use the above method to translate
    Expr ::= [+ | -] Term \{(+ | -)\} Term
                                       (*)
into a finite set of BNF productions.
1. First, replace (+ | -) with a nonterminal Op
  defined by: Op ::= + -
  2. Next, replace {Op Term} with a nonterminal Rest
  defined by: Rest ::= <empty> Rest Op Term
  (**) becomes: Expr ::= [+ | -] Term Rest (***)
defined by OptSign ::= <empty> | + | -
```

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into a finite set of BNF productions.
1. First, replace (+ | -) with a nonterminal Op
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  2. Next, replace {Op Term} with a nonterminal Rest
  defined by: Rest ::= <empty> Rest Op Term
  (**) becomes: Expr ::= [+ | -] Term Rest (***)
3. Finally, replace [+ | -] with a nonterminal OptSign
  defined by OptSign ::= <empty> | + | -
  (***) becomes: Expr ::= OptSign Term Rest
The result is the following set of 8 BNF productions:
     Expr ::= OptSign Term Rest
  OptSign ::= \langle empty \rangle | + | -
     Rest ::= <empty> | Rest Op Term
       Op ::= + -
```

While the above method always works, it will often <u>not</u> find a simplest finite set of grammar productions that is equivalent to the given EBNF rule!

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```
For example, here is a simpler set of grammar productions that is equivalent to the EBNF rule

Expr ::= [+ | -] Term {(+ | -) Term}

considered above:
```

A Rule to Follow When Writing EBNF Specifications

In EBNF, when any of the characters | () [] { } is a terminal, that terminal should be <u>put in</u> <u>single quotes</u> to make it clear that the character is <u>not</u> being used with its EBNF meaning!

Sethi says the following about this on p. 47 of his book (p. 48 of the course reader):

Symbols such as { and }, which have a special status in a language description, are called *metasymbols*.

EBNF has many more metasymbols than BNF. Furthermore, these same symbols can also appear in the syntax of a language—the index i in A[i] is not optional—so care is needed to distinguish tokens from metasymbols. Confusion between tokens and metasymbols will be avoided by enclosing tokens within single quotes if needed, as in '(').

An EBNF version of the grammar in Fig. 2.6 is

```
\langle expression \rangle ::= \langle term \rangle \{ (+|-) \langle term \rangle \}
\langle term \rangle ::= \langle factor \rangle \{ (*|/) \langle factor \rangle \}
\langle factor \rangle ::= '(' \langle expression \rangle ')' | name | number
```

Parse Trees Based on EBNF Specifications

Given an EBNF specification, we define its parse trees in the same way as parse trees based on a grammar; parse trees can be used to define the set of sequences of terminals that is denoted by each nonterminal, as in the case of a grammar.

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- For example, the productions

Unless otherwise indicated, an EBNF spec's *starting nonterminal* is the *nonterminal on the left of the 1st production*, and *parse tree* means *parse tree whose root is the starting nonterminal*.

As in the case of BNF, the set (of sequences of terminals) denoted by the starting nonterminal of an EBNF specification is called the *Language generated by* that EBNF specification.

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As in the case of BNF, the set (of sequences of terminals) denoted by the starting nonterminal of an EBNF specification is called the *Language generated by* that EBNF specification.

• EBNF can be used just like BNF to define what it means for source code to be "syntactically valid":

For many programming languages L, the language designer can construct $\frac{1}{2}$ an EBNF specification G (whose terminals are L's tokens) such that:

 $T_1 ldots T_n$ belongs to the language generated by G if (and, roughly speaking, only if) $T_1 ldots T_n$ is the sequence of tokens of a possibly valid L source file.

We can then say a particular L source file is <u>syntactically valid</u> if its sequence of tokens belongs to the language generated by the grammar EBNF specification.

• More generally, when a nonterminal of *G* corresponds to a language construct *X* (e.g., *statement*), we say a piece of source code is a *syntactically valid X* if its sequence of tokens belongs to the set denoted by the nonterminal.

Not always, though it is quite common to use BNF or EBNF specifications of programming language syntax in which the terminals are tokens of the language.

The EBNF specification of TinyJ is an example!

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In addition to specifying syntactically valid sequences of tokens for language constructs, these BNF or EBNF specifications also specify what sequences of characters are instances of tokens with multiple instances:

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In addition to specifying syntactically valid sequences of tokens for language constructs, these BNF or EBNF specifications also specify what sequences of characters are instances of tokens with multiple instances: The commonest examples of such tokens are IDENTIFIER and tokens whose instances are literal constants of some type.

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In fact we've already seen an example of the use of BNF to specify such a token:

```
\langle real-number \rangle ::= \langle integer-part \rangle. \langle fraction \rangle

\langle integer-part \rangle ::= \langle digit \rangle \mid \langle integer-part \rangle \langle digit \rangle

\langle fraction \rangle ::= \langle digit \rangle \mid \langle digit \rangle \langle fraction \rangle

\langle digit \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9
```

Figure 2.3 BNF rules for real numbers.

A grammar given by by Sethi to specify unsigned floating point literals in a simple language.