

Section 3.1

b) True, if A is 3×3 upper triangle, then
 $\det(A) = a_{11}a_{22} \dots a_{nn}$

c) False,

$$A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad B = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \quad A + B = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\det(A + B) = (0)(0) - (0)(0) = 0$$

$$\det(A) = 1 \quad \det(B) = 1$$

d) True, since all # pos, det is pos

e) True, all cofactor expansions = 0, therefore,
sum = 0

$$\begin{aligned} 17) \quad \det(A) &= (6)(-1) - (-3)(-5) \\ &= -6 - 15 \\ &\boxed{= -21} \end{aligned}$$

$$\begin{aligned} 30) \quad \det(A) &= (2)(1)(-3) + (-10)(1)(0) + (3)(1)(8) \\ &\quad - (2)(1)(8) - (-10)(1)(-3) - (3)(1)(0) \\ &= -6 + 24 - 16 - 30 \\ &\boxed{= -28} \end{aligned}$$

$$\begin{aligned} 36) \quad \det(A) &= 4(-2)(-6)(-3) \\ &\boxed{= -144} \end{aligned}$$

$$\begin{aligned} 45) \quad \det(A) &= e^{2t} 3e^{3t} 16e^{-4t} + e^{3t} -4e^{-4t} 4e^{2t} + e^{-4t} 2e^{2t} 4e^{3t} \\ &\quad - e^{2t} -4e^{-4t} 9e^{3t} - e^{3t} 2e^{2t} 16e^{-4t} - e^{-4t} 3e^{3t} 4e^{2t} \\ &= 42e^{2t} \end{aligned}$$

$$54a) \det(cA) = c a_{11} a_{22} - c a_{12} a_{21}$$

$$\left(c^2 \det(A) = c^2 [a_{11} a_{22} - a_{12} a_{21}] \right)$$

$$\begin{aligned} & c^2 a_{11} a_{22} - c^2 a_{12} a_{21} \\ &= c^2 [a_{11} a_{22} - a_{12} a_{21}] \quad \checkmark \end{aligned}$$

Section 3.2

15) A is invertible if $\det(A) \neq 0$

$$\det(A) = (-1)(-1) - (1)(1)$$

$$= 1 - 1 = 0$$

| A is NOT invertible |

$$\begin{aligned} 17) \det(A) &= (-1)(-2)(5) + (2)(1)(8) + (3)(5)(-2) \\ &\quad - (-2)(1)(-1) - (5)(5)(2) - (8)(-2)(3) \end{aligned}$$

$$= 10 + 16 - 30 - 2 - 50 + 48$$

$$= -8 \neq 0$$

| A is invertible |

$$\begin{aligned} 18) \det(A) &= (2)(5)(1) + (6)(1)(2) + (-1)(3)(0) \\ &\quad - (0)(1)(2) - (1)(3)(6) - (2)(5)(-1) \end{aligned}$$

$$= 10 + 12 - 18 + 10$$

$$= 14$$

$$22) \left[\begin{array}{ccc|c} 1 & 2 & k & 0 \\ 2 & -k & 1 & 0 \\ 3 & 6 & 1 & 0 \end{array} \right]$$

$$-2R_1 + R_2 = \left[\begin{array}{ccc|c} 1 & 2 & k & 0 \\ 0 & -k-2 & 1-2k & 0 \\ 3 & 6 & 1 & 0 \end{array} \right]$$

$$-3R_1 + R_3 = \left[\begin{array}{ccc|c} 1 & 2 & k & 0 \\ 0 & -k-2 & 1-2k & 0 \\ 0 & 0 & 1-3k & 0 \end{array} \right]$$

$$1-3k = 0$$

$$\begin{aligned} -3k &= -1 \\ \underline{k &= 1/3} \end{aligned}$$

$$29) \det(B) = (-6ac - 2ad) - (-6ac - 2bc)$$

$$= -6ac - 2ad + 6ac - 2bc$$

$$\boxed{= -2ad - 2bc}$$

$$30) \det(B) = -\det(A)$$

$$= -12 \det(A)$$

$$= -12(1)$$

$$\boxed{= -12}$$

$$32) \det(B) = -bc + 4ab - (-ad + 4b)$$
$$= -bc + 4ab + ad - 4b$$

$$35) R_1 \leftrightarrow R_2$$

$$\det(B) = -\det(A)$$

$$-3R_2$$

$$\det(B) = 3 \det(A)$$

$$-4R_1 + R_3 = R_j$$

$$\det(B) = 3 \det(A)$$

$$\boxed{\det(B) = -9}$$