

小白专场:

一元多项式的 加法与乘法运算



题意理解

设计函数分别求两个一元多项式的乘积与和

已知两个多项式:

$$(1) 3x^4 - 5x^2 + 6x - 2$$

(2)
$$5x^{20} - 7x^4 + 3x$$

多项式和:

$$5x^{20} - 4x^4 - 5x^2 + 9x - 2$$

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已知两个多项式:

$$(1) 3x^4 - 5x^2 + 6x - 2$$

(2)
$$5x^{20} - 7x^4 + 3x$$

多项式的乘积:

$$(a+b)(c+d) = ac+ad+bc+bd$$

多项式乘积:

 $15x^{24}-25x^{22}+30x^{21}-10x^{20}-21x^8+35x^6-33x^5+14x^4-15x^3+18x^2-6x$



题意理解

设计函数分别求两个一元多项式的乘积与和

输入样例:

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3520 -7431

 $3x^4-5x^2+6x-2$

 $5x^{20}-7x^4+3x$

输出样例:

15 24 -25 22 30 21 -10 20 -21 8 35 6 -33 5 14 4 -15 3 18 2 -6 1 5 20 -4 4 -5 2 9 1 -2 0

 $15x^{24}-25x^{22}+30x^{21}-10x^{20}-21x^8+35x^6-33x^5+14x^4-15x^3+18x^2-6x$

 $5x^{20}-4x^4-5x^2+9x-2$



求解思路

- 1.多项式表示
- 2. 程序框架
- 3. 读多项式
- 4. 加法实现
- 5. 乘法实现
- 6. 多项式输出



多项式的表示

仅表示非零项

数组:

- 🖒 编程简单、调试容易
- ? 需要事先确定数组大小

一种比较好的实现方法是: 动态数组

下面介绍链表表示

链表:

- ♂动态性强
- √编程略为复杂、调试比较困难



多项式的表示

数据结构设计

```
typedef struct PolyNode *Polynomial;
struct PolyNode {
       int coef;
       int expon;
       Polynomial link;
};
              20
```



程序框架搭建

```
int main()
{

读入多项式1

读入多项式2

乘法运算并输出

加法运算并输出
```

需要设计的函数:

- > 读一个多项式
- > 两多项式相乘
- > 两多项式相加
- > 多项式输出

```
int main()
   Polynomial P1, P2, PP, PS;
   P1 = ReadPoly();
   P2 = ReadPoly();
   PP = Mult(P1, P2);
   PrintPoly(PP);
   PS = Add(P1, P2);
   PrintPoly(PS);
   return 0;
```



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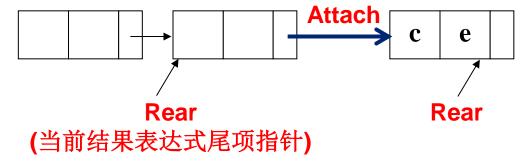




Rear初值是多少?

两种处理方法:

1. Rear初值为NULL 在Attach函数中根据Rear是 否为NULL做不同处理

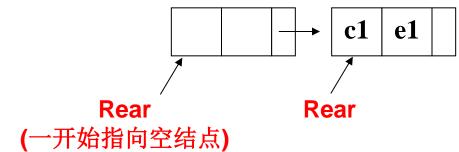




Rear初值是多少?

两种处理方法:

- 1. Rear初值为NULL
- 2. Rear指向一个空结点





```
void Attach( int c, int e, Polynomial *pRear )
{
    Pel(Polynomial)malloc(sizeof(struct PolyNode));
    P->coef = c; /* 对新结点赋值 */
    P->expon = e;
    P->link = NULL;
    (*pRear)->link = P;
    *pRear = P; /* 修改pRear值 */
}
```





```
Polynomial ReadPoly()
  Polynomial P, Rear, t;
  int c, e, N;
  scanf("%d", &N);
  P = (Polynomial)malloc(sizeof(struct PolyNode)); /* 链表头空结点 */
  P->link = NULL;
  Rear = P;
  while ( N-- ) {
       scanf("%d %d", &c, &e);
                                    /* 将当前项插入多项式尾部 */
       Attach(c, e, &Rear);
   t = P; P = P->link; free(t); /* 删除临时生成的头结点 */
   return P;
```



如何将两个多项式相加

```
Polynomial Add( Polynomial P1, Polynomial P2)
         t1 = P1; t2 = P2;
         P = (Polynomial)malloc(sizeof(struct PolyNode)); P->link = NULL;
         Rear = P;
         while (t1 && t2) {
                  if (t1->expon == t2->expon) {
                  else if (t1->expon > t2->expon) {
                  else {
         while (t1) {
         while (t2) {
         return P;
```



方法:

1. 将乘法运算转换为加法运算

```
将P1当前项(ci,ei)乘P2多项式,再加到结果多项式里t1 = P1; t2 = P2;
P = (Polynomial)malloc(sizeof(struct PolyNode)); P->link = NULL;
Rear = P;
while (t2) {
    Attach(t1->coef*t2->coef, t1->expon+t2->expon, &Rear);
    t2 = t2->link;
}
```

2.逐项插入

将P1当前项(c1_i,e1_i)乘P2当前项(c2_i,e2_i),并插入到结果多项式中。关键是要找到插入位置 初始结果多项式可由P1第一项乘P2获得(如上)



```
Polynomial Mult( Polynomial P1, Polynomial P2)
        t1 = P1; t2 = P2;
         while (t2) { /* 先用P1的第1项乘以P2,得到P*/
        t1 = t1->link;
         while (t1) {
                  t2 = P2; Rear = P;
                  while (t2) {
                           e = t1->expon + t2->expon;
                           c = t1->coef * t2->coef;
                           t2 = t2->link;
                  t1 = t1->link;
```



```
Polynomial Mult(Polynomial P1, Polynomial P2)
         Polynomial P, Rear, t1, t2, t;
         int c, e;
         if (!P1 || !P2) return NULL;
         t1 = P1; t2 = P2;
         P = (Polynomial)malloc(sizeof(struct PolyNode)); P->link = NULL;
         Rear = P;
         while (t2) {
                                   /* 先用P1的第1项乘以P2, 得到P */
                   Attach(t1->coef*t2->coef, t1->expon+t2->expon, &Rear);
                   t2 = t2->link:
         t1 = t1 - \sinh;
         while (t1) {
                   t2 = P2; Rear = P;
                   while (t2) {
                            t2 = t2->link:
                   t1 = t1->link;
```

```
Polynomial Mult(Polynomial P1, Polynomial P2)
         while (t1) {
                   t2 = P2; Rear = P;
                                                                 插入: (-4,2)
                   while (t2) {
                            e = t1->expon + t2->expon;
                            c = t1->coef * t2->coef;
                            while (Rear->link && Rear->link->expon > e)
                                      Rear = Rear->link;
                             if (Rear->link && Rear->link->expon == e) {
                            else {
                            t2 = t2->link;
                   t1 = t1 - \sinh;
```



```
Polynomial Mult(Polynomial P1, Polynomial P2)
                     while (Rear->link && Rear->link->expon > e)
                            Rear = Rear->link:
                     if (Rear->link && Rear->link->expon == e) {
                            if (Rear->link->coef + c)
                                      Rear->link->coef += c;
                            else {
                                      t = Rear->link;
                                      Rear->link = t->link;
                                      free(t);
                      else {
                            t = (Polynomial)malloc(sizeof(struct PolyNode));
                            t->coef = c; t->expon = e;
                            t->link = Rear->link;
                            Rear->link = t; Rear = Rear->link;
                                                    Rear
```

```
Polynomial Mult(Polynomial P1, Polynomial P2)
         t1 = P1; t2 = P2;
         while (t2) { /* 先用P1的第1项乘以P2,得到P */
         t1 = t1 - \sinh;
         while (t1) {
                  t2 = P2; Rear = P;
                  while (t2) {
                            e = t1->expon + t2->expon;
                            c = t1->coef * t2->coef;
                            t2 = t2->link;
                  t1 = t1->link;
         t2 = P; P = P->link; free(t2);
         return P;
```



如何将多项式输出

```
void PrintPoly( Polynomial P )
{ /* 输出多项式 */
        int flag = 0;
                                       /* 辅助调整输出格式用 */
        if (!P) {printf("0 0\n"); return;}
        while ( P ) {
                 if (!flag)
                          flag = 1;
                 else
                          printf(" ");
                 printf("%d %d", P->coef, P->expon);
                 P = P - \sinh;
        printf("\n");
```

