

# Time Horizons and Emissions Trading

**Roweno J.R.K. Heijmans**

Swedish University of Agricultural Sciences (SLU)

March 30, 2022  
SLU Seminar Series

# Introduction

# This paper

- Dynamic model of emissions trading
- Emissions cap depends on conditions prevailing in the market for allowances
- Policy ends with a hard ban on emissions

# The Climate Policy Trinity

## 1. Cap and trade

- Who can pollute? How is abatement achieved?
  - California ETS, EU ETS, RGGI, Korea ETS, Swiss ETS, ...

## 2. Market-based emissions cap

- How much pollution is allowed?
  - Price floor/ceiling/collar, quantity collar, MSR, liquidity constraints, ...

## 3. Future ban on emissions

- When should pollution stop?
  - Zero emissions pledge, permit retirement

# Pillar 1: Cap and trade

## Emissions trading

- Prominent climate policy instrument
- 16% of greenhouse gas emissions worldwide
- Jurisdictions representing 54% of global GDP
- More under way

### *The state of play of cap-and-trade in 2021*

-  in force
-  under development
-  under consideration

**EU ETS**

Launched in 2021 following the end of UK's participation in the EU ETS. The new system mostly mirrors the EU ETS Phase 4 design.

**Finland**

**Germany**

Launched a national ETS for heating and transport fuels in 2021, complementing the EU ETS. The system starts with a fixed price that increases annually.

**Ukraine**

**Kazakhstan**

**Turkey**

**Montenegro**

**Switzerland**

**China**

Fully launched its national power sector ETS in 2021 bringing the world's largest carbon market online after three years of preparation.

**Saskhain (Russia)**

**Japan**

**Saitama Tokyo**

**Republic of Korea**

Third trading phase will commence in July 2021 extending the scope, increasing auctioning and introducing financial instruments to its market.

**Taiwan (China)**

**Philippines**

**Vietnam**

**Indonesia**

**Thailand**

**Chinese Pilot**

- Beijing
- Chongqing
- Fujian
- Guangdong
- Hubei
- Shanghai
- Shenzhen
- Tianjin

**Phase 4 commences in 2021** establishing a new cap, introducing new provisions on free allocation, auctioning, MRR and the union Registry, as well as operationalising the innovation fund.

- EU Member States: Ireland
- Lithuania
- Norway

**New Zealand**

A new legislative framework for the 2021–2025 period establishes a cap on emissions from 2021 for the first time under the NZ ETS.

## Pillar 2: Market-based emissions cap

### Supply mechanisms

- Sum total of abatement required depends on emissions cap
- In practice, cap often depends on the market for allowances
- Empirically relevant classes: price and quantity mechanisms
  - Price mechanisms: supply increasing in allowance price
  - Quantity mechanisms: supply decreasing in surplus of unused allowances
- Common, but do they matter? Yes (Borenstein et al., 2019)

# **EU ETS**

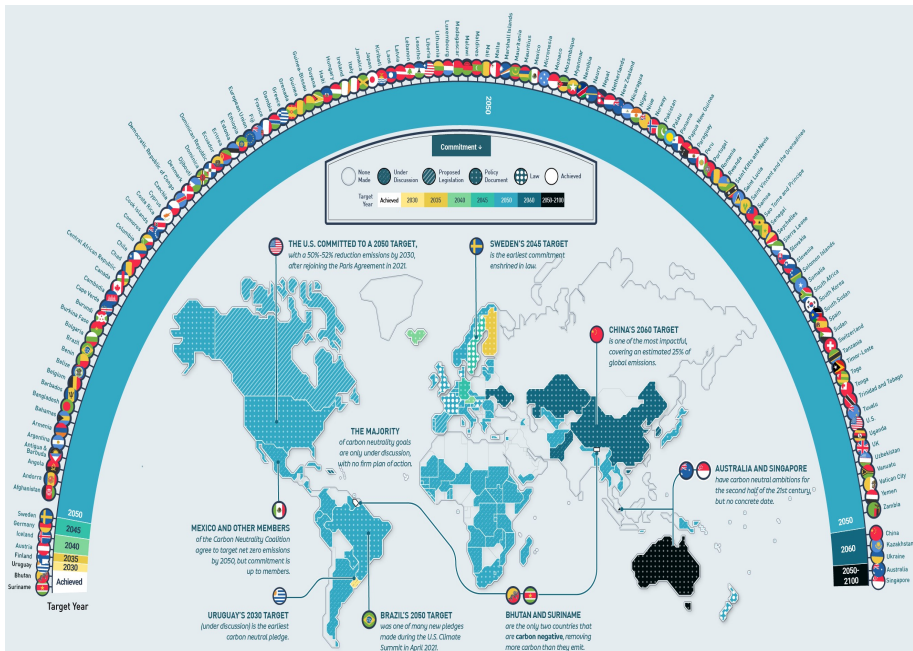
**European Union Emission  
Trading System**



## Pillar 3: Hard ban

### Future ban on emissions

- Rapidly gaining popularity
- >100 countries pledged net-zero by  $\pm$  2050 (Van Soest et al., 2021)
  - Sweden aims at zero emissions by 2045
  - First country in the world to enshrine zero-emissions target in law
- Crucial to meet climate ambitions (Höhne et al., 2021)



# Research question

What is the effect of bringing forward the ban on emissions in cap and trade schemes with a market-based emissions cap?

## Four answers

1. The reduction in emissions is bounded from below and positive under a price mechanism
2. The reduction in emissions is bounded from above and possibly negative under a price mechanism  
→ Negative reduction = increased emissions!
3. Sufficient conditions under which advancing the ban leads to strictly higher emissions under a quantity mechanism
4. Sufficient conditions under which the lower and upper bounds for price and quantity mechanisms, respectively, coincide  
→ Emissions reduction larger under price mechanism

# Model

# Cap and trade

- $N$  firms
- The policymaker supplies  $s_{it}$  allowances to firm  $i$  in period  $t$ 
  - $s_t = \sum_i s_{it}$ , the emissions cap in period  $t$
  - Determination of  $s_t$  discussed shortly
- Firm  $i$  must surrender allowances to cover emissions  $q_{it} \geq 0$ 
  - $q_t = \sum_i q_{it}$
- Allowances traded on a secondary market
  - Trade generates allowance price  $p_t$
  - Firms are price-takers – no huge firms,  $N$  large
- If  $q_t < s_t$ , the surplus is banked
  - $b_t = s_t - q_t$  and  $B_t = \sum_t b_t$
  - Banking, no borrowing:  $B_t \geq 0$  for all  $t$
  - Banked allowances usable to cover future emissions

# Time horizon of emissions trading

- The cap and trade scheme ends with a hard ban on emissions
  - Timing of the ban determines time horizon of emissions trading
  - Final period on emissions  $T$
  - Allow  $T \rightarrow \infty$ , the empirically relevant case
- Ban requires  $q_t = 0$  for all  $i$  and  $t \geq T$ 
  - Hard constraint:  $q_t = 0$  for all  $t \geq T$  even if  $B_t > 0$

# Firms' problem

- Firm  $i$  chooses emissions  $q_{it}$  to minimize the discounted sum of convex abatement costs subject to the cap and the ban at  $T$ 
  - Solution to firms' problem:  $q_t(p_t, T)$
  - Emissions decreasing in allowance price:  $\partial q_t(p_t, T)/\partial p_t < 0$
- Cost-minimization gives  $B_T = 0$ 
  - Allowances used up by period  $T$
  - Emissions banned starting from  $T$ , so  $B_T > 0$  is capital destruction
- Trade in allowances gives  $p_t \approx MAC_t$ 
  - Sell (buy) allowance when price exceeds (falls short of) marginal abatement cost
  - Assumes market economy, comp. China's pilot ETS (Cao et al., 2021)
- Marginal abatement costs satisfy  $MAC_t \approx \beta MAC_{t+1}$ 
  - Differential Hotelling rule:  $\partial p_{t+1}/\partial p_t > 0$



# Supply mechanisms

- Firms choose emissions to minimize abatement costs *subject to the emissions cap*
  - Determined through supply mechanism
- **Price mechanism:** supply increasing in allowance price
  - $\partial s_t(p_t)/\partial p_t > 0$
  - Intuition: high price means abatement expensive, efficient to loosen cap
  - Examples: price floor/ceiling, reserve price, etc.
- **Quantity mechanism:** supply decreasing in bank
  - $\partial s_t(B_t)/\partial B_t < 0$
  - Intuition: high surplus means abatement cheap, efficient to tighten cap
  - Examples: quantity-collar (MSR), liquidity provision, etc.
- Intention to balance out supply and demand
- Price-taker assumption: firms take cap as given

# Similar but different

- Price mechanism
  - Uses information on prices to determine quantities
  - Turns cap and trade into a hybrid policy
- Quantity mechanism
  - Uses information on quantities to determine quantities
  - Doubles down on quantity aspect of cap and trade

# Equilibrium

# Equilibrium

- Equilibrium is reached when total emissions equal total supply
  - Subject to borrowing constraint and ban
  - Gross oversupply ( $>$  BAU emissions) ruled out by assumption
- Let  $p^P$  denote the equilibrium price vector under a price mechanism:

$$\sum_{t=1}^T q_t(p_t^P, T) = \sum_{t=1}^T s_t(p_t^P)$$

- Let  $p^Q$  denote the equilibrium price vector under a quantity mechanism:

$$\sum_{t=1}^T q_t(p_t^Q, T) = \sum_{t=1}^T s_t(B_t(p^Q))$$

# Equilibrium

- Equilibrium is reached when total emissions equal total supply
  - Subject to borrowing constraint and ban
  - Gross oversupply ( $>$  BAU emissions) ruled out by assumption
- Let  $p^P$  denote the equilibrium price vector under a price mechanism:

$$\sum_{t=1}^T q_t(p_t^P, T) = \sum_{t=1}^T s_t(p_t^P) \implies B_T(p^P) = 0$$

- Let  $p^Q$  denote the equilibrium price vector under a quantity mechanism:

$$\sum_{t=1}^T q_t(p_t^Q, T) = \sum_{t=1}^T s_t(B_t(p^Q))$$

# Equilibrium

- Equilibrium is reached when total emissions equal total supply
  - Subject to borrowing constraint and ban
  - Gross oversupply ( $>$  BAU emissions) ruled out by assumption
- Let  $p^P$  denote the equilibrium price vector under a price mechanism:

$$\sum_{t=1}^T q_t(p_t^P, T) = \sum_{t=1}^T s_t(p_t^P) \implies B_T(p^P) = 0$$

- Let  $p^Q$  denote the equilibrium price vector under a quantity mechanism:

$$\sum_{t=1}^T q_t(p_t^Q, T) = \sum_{t=1}^T s_t(B_t(p^Q)) \implies B_T(p^Q) = 0$$

# Supply between periods

- Consider a given final period on emissions  $T$ 
  - For  $t_1 \leq t_2$ , define:

$$S^P(t_1, t_2 \mid p^P) = \sum_{t=t_1}^{t_2} s_t(p_t^P)$$

and

$$S^Q(t_1, t_2 \mid p^Q) = \sum_{t=t_1}^{t_2} s_t(B_t(p^Q))$$

## An earlier ban – another equilibrium

- Now posit another final period on emissions  $\bar{T}$ , where  $\bar{T} < T$ 
  - The final period  $\bar{T}$  is an earlier ban – more ambitious climate goal
- Let  $\bar{p}^P$  denote the equilibrium allowance price vector under a price mechanism when the final period is  $\bar{T}$ 
  - $B_{\bar{T}}(\bar{p}^P) = 0$
- Let  $\bar{p}^Q$  denote the equilibrium allowance price vector under a quantity mechanism when the final period is  $\bar{T}$ 
  - $B_{\bar{T}}(\bar{p}^Q) = 0$



# Equilibrium reduction in emissions

- Define:

$$R^P(\bar{T}, T) = \sum_{t=1}^T q_t(p^P, T) - \sum_{t=1}^{\bar{T}} q_t(\bar{p}^P, \bar{T})$$

→  $R^P(\bar{T}, T)$  is the reduction in equilibrium emissions realized by bringing forward the ban from  $T$  to  $\bar{T}$  under a price mechanism

- Define:

$$R^Q(\bar{T}, T) = \sum_{t=1}^T q_t(p^Q, T) - \sum_{t=1}^{\bar{T}} q_t(\bar{p}^Q, \bar{T})$$

→  $R^Q(\bar{T}, T)$  is the reduction in equilibrium emissions realized by bringing forward the ban from  $T$  to  $\bar{T}$  under a quantity mechanism

# Research question specified

What are the properties  $R^P(\bar{T}, T)$  and  $R^Q(\bar{T}, T)$ ?

## Bounds

# Price mechanism: lower bound

## Main result 1

$$R^P(\bar{T}, T) \geq S^P(\bar{T}, T \mid p^P) \geq 0$$

- Reduction in equilibrium emissions in response to an earlier ban is positive and bounded from below under a price mechanism
- Bringing forward the ban reduces equilibrium emissions *at least* by the amount of emissions originally supplied after the earlier ban
- Price mechanism reinforces earlier ban

# Price mechanism: intuition

- The bound is clear
  - A ban at  $\bar{T}$  preempts emissions after that period
  - Between periods  $\bar{T}$  and  $T$ ,  $S^P(\bar{T}, T \mid p^P)$  allowances were supplied
  - Since borrowing is not allowed, those emissions “disappear”
- Now suppose that  $B_{\bar{T}}(p^P) > 0$ 
  - Strictly positive number of allowances banked when final period is  $T$
- Equilibrium when the final period is  $\bar{T}$  requires  $B_{\bar{T}}(\bar{p}^P) = 0$ 
  - No capital destruction!
- $B_{\bar{T}}(p^P) > 0$  and  $B_{\bar{T}}(\bar{p}^P) = 0$  imply that  $\bar{p}_t^P < p_t^P$  for all  $t < \bar{T}$ 
  - Price must go down to support using up allowances faster
- Mechanics of a price mechanism translate a lower price into less supply
  - Emissions prior to  $\bar{T}$  go down, too, reinforcing the earlier ban.

# Quantity mechanism: upper bound

## Main result 2

$$R^Q(\bar{T}, T) \leq S^Q(\bar{T}, T \mid p^Q)$$

- Reduction in equilibrium emissions in response to an earlier ban is bounded from above and possibly negative under a quantity mechanism.
- Quantity mechanism counteracts earlier ban
- Bringing forward the ban reduces equilibrium emissions *at most* by the amount of emissions originally supplied after the earlier ban

# Quantity mechanism: intuition

- The bound again is clear
  - A ban at  $\bar{T}$  preempts emissions after that period
  - Between periods  $\bar{T}$  and  $T$ ,  $S^Q(\bar{T}, T \mid p^Q)$  allowances were supplied
- Now assume that  $B_{\bar{T}}(p^Q) > 0$
- When the ban kicks in at  $\bar{T}$ , equilibrium requires  $B_{\bar{T}}(\bar{p}^Q) = 0$
- Firms start using more allowances before period  $\bar{T}$ 
  - Smoothed out over all periods  $t < \bar{T}$
- Less banking in periods  $t < \bar{T}$
- Hence, supply of emissions is higher in all periods before  $\bar{T}$ 
  - Under quantity mechanism,  $\partial s_t(B_t)/\partial B_t > 0$
- Reduction in equilibrium emissions is at most  $S^Q(\bar{T}, T \mid p^Q)$

## Incompatibility



# Negative reduction

- Result 2 hinted at the possibility of a negative reduction  $R^Q(\bar{T}, T)$ 
  - Increased emissions due to earlier ban
- Possible?
  - Under what conditions?

# Thought experiment

Posit a period  $T^* < T$  such that:

1. Given the ban at  $T$ , equilibrium emissions are strictly positive in  $T^*$
2. Given the ban at  $T$ , equilibrium supply of allowances has already (and permanently) dried up by period  $T^*$

Such a  $T^*$  need not exist; if it exists, it need not be unique. However, if at least one  $T^*$  that satisfies 1. and 2. exists, set  $\bar{T} = T^*$ . Then  $\bar{T}$  satisfies

$$q_{\bar{T}}(p^Q, T) > 0 \quad (*)$$

$$s_t(B_t(p^Q)) = 0 \quad \forall t \geq \bar{T} \quad (**)$$

Think of pensioners receiving 401(k) benefits

# Higher emissions

## Main result 3

If  $\bar{T}$  satisfies (\*) and (\*\*), then  $R^Q(\bar{T}, T) < 0$

- Advancing the ban from  $T$  to  $\bar{T}$  strictly increases emissions
- Quantity mechanisms and zero emissions pledges incompatible

# Intuition

- If  $\bar{T}$  satisfies (\*) and (\*\*), early ban kicks in when emissions covered exclusively by banked allowances
- When the final period is  $T$ , no supply after  $\bar{T}$ 
  - Advancing ban from  $T$  to  $\bar{T}$  does not kill supply after  $\bar{T}$
- Originally, positive bank at  $\bar{T}$ 
  - Equilibrium response, more emissions before  $\bar{T}$  to get  $B_{\bar{T}} = 0$
- Higher emissions/less baking translated into more supply under quantity mechanism
- No change in supply after  $\bar{T}$ , but more supply before  $\bar{T}$
- Net emissions go up! ☹️
- Think of 401(k) again
  - Firms are like retired people by period  $\bar{T}$
  - Wage income dried up and, consuming what they set apart earlier in

# Sufficient and reasonable conditions?

Conditions (\*) and (\*\*) imply increased emissions. Are they reasonable?

- EU ETS
  - Emissions estimated to end no earlier than 2060
  - Supply estimated to end by  $\approx 2040$
- Hard ban on emissions by 2050 might increase EU ETS emissions!

## Mechanism choice

# Comparison

- It seems that price mechanisms outperform quantity mechanisms
- Careful: not so obvious
- Suppose  $S^Q(T, \bar{T} \mid p^Q) > S^P(T, \bar{T} \mid p^P)$ 
  - Upper bound on quantity mechanism reductions above lower bound on price mechanism reductions
  - Possible that quantity mechanism reduces emissions more!
- Somewhat contrived possibility

# Symmetric baselines

- Let the final period be  $T$
- Under the equilibrium price vectors  $p^P$  and  $p^Q$ , suppose that:

$$s_t(p_t^P) = s_t(B_t(p^Q)) \quad \forall t \leq T \quad (***)$$

→ Supply of allowances equal in all periods

- If  $(***)$ , supply vectors  $(s_t(p_t^P))$  and  $(s_t(B_t(p^Q)))$  are *symmetric under  $T$*



# Prices vs. Quantities

## Main result 4

If  $(s_t(p_t^P))$  and  $(s_t(B_t(p^Q)))$  are symmetric under  $T$ , then  
$$R^Q(\bar{T}, T) \leq R^P(\bar{T}, T)$$

- Advancing the ban from  $T$  to  $\bar{T}$  reduces emissions less under a quantity mechanism than under a price mechanism
- Symmetry under  $T$  sufficient, not necessary
  - For example,  $\sum_{t=\bar{T}}^T s_t(p_t^P) = \sum_{t=\bar{T}}^T s_t(B_t(p^Q))$  also works
- Symmetry under  $T$  intuitive starting point: compare effects for same baselines
  - Unless comparing apples and oranges, price mechanisms win

## Conclusions

# Fixing quantity mechanisms

- The problems with quantity mechanisms could be overcome: simply accompany the earlier ban with a manual reduction of supply
- Practical complications
  - How many allowances should be taken out?
  - When should they be taken?
- Need for ad hoc solution hints at fundamental distinction
- Quantity mechanism requires additional to work well – price mechanism takes care of itself!

# Thank you

roweno.heijmans@slu.se  
www.roweno.nl