

EECE 230X – Introduction to Computation and Programming

Programming Assignment 9

- This programming assignment consists of 4 problems
- Prerequisites: Topic 11
- Related material: Data structures: lists of lists, 2-dimensional lists, dictionaries, and stacks

Problem 1. Check if matrix has equal elements

Write a function `equalElements(M)`, which given an $m \times n$ matrix M of numbers, checks whether or not M has equal elements. That is, the function checks whether or not there are $(i_1, j_1) \neq (i_2, j_2)$, where $0 \leq i_1 < m$, $0 \leq j_1 < n$, $0 \leq i_2 < m$, and $0 \leq j_2 < n$, such that $M[i_1][j_1] = M[i_2][j_2]$. If so, the function should return the tuple of tuples $((i_1, j_1), (i_2, j_2))$, for any such (i_1, j_1) and (i_2, j_2) . Otherwise, the function should return a tuple of tuples $((-1, -1), (-1, -1))$. If the matrix has more than two equal elements, the indices of any pair of equal elements are a valid answer.

- a) $O(m^2n^2)$ **time solution.** Do it first using 4 nested loops on i_1, j_1, i_2 , and j_2 .
- b) $O(mn)$ **expected time solution using a dictionary.** Do it now in $O(mn)$ expected time using a dictionary.

Don't try to read the following hint unless you are stuck (to read it you need to magnify the PDF file and properly read it in reverse order); try first to solve it on your own without help.

(*Hint:* (((1) adjust row index like this))))

Test program:

```
import numpy as np
M1 = [[1,2],[3,4]]
M2 = [[1,2],[3,1]]
M3 = [[1,3,0,5],[2,5,2,-1],[5,6,-2,6]]
M4 = [[1,3,0,5],[20,50,2,-1],[51,61,-2,16]]
for M in (M1,M2,M3,M4):
    print(np.matrix(M))
    print(equalElements(M),"\n")
```

Output:

```
[[1 2]
 [3 4]]
((-1, -1), (-1, -1))

[[ 1  2]
 [ 3  1]]
((0, 0), (1, 1))

[[ 1  3  0  5]
 [ 2  5  2 -1]
 [ 5  6 -2  6]]
```

((0, 3), (1, 1))

```
[[ 1  3  0  5]
 [20 50  2 -1]
 [51 61 -2 16]]
((-1, -1), (-1, -1))
```

Problem 2. Check if two strings are anagrams using dictionaries

Two strings `s1` and `s2` are called *anagrams* if `s2` can be formed by rearranging the characters of `s1`.

Examples:

- "3EE02CEC" and "EECE230C" are anagrams
- "EECE230C" and "EECE230C" are anagrams
- "3EEE02CE" and "EECE230C" are not anagrams since "C" appears once in the first string and twice is in the second (and "E" appears 4 times in the first string and 3 times is in the second).
- "aaabaab" and "baabaaa" are anagrams
- "aaabaab" and "abba" are not anagrams

Write a function `anagrams(s1,s2)`, which given two strings `s1` and `s2`, returns `True` if they are anagrams, and `False` otherwise.

Aim for $O(n_1 + n_2)$ expected time, where $n_1 = \text{len}(s1)$ and $n_2 = \text{len}(s2)$. Use dictionaries.

(*Hint:* The operator `D1==D2` checks if dictionaries `D1` and `D2` have equal key:value pairs.)

Test program/Output:

<code>print(anagrams("", ""))</code>	<code>True</code>
<code>print(anagrams("i", "i"))</code>	<code>True</code>
<code>print(anagrams("is", "si"))</code>	<code>True</code>
<code>print(anagrams("fun", "nfu"))</code>	<code>True</code>
<code>print(anagrams("aaabaab", "abba"))</code>	<code>False</code>
<code>print(anagrams("aaabaab", "baabaaa"))</code>	<code>True</code>
<code>print(anagrams("EECE230", "EECE230"))</code>	<code>True</code>
<code>print(anagrams("EECE230", "3EE02CE"))</code>	<code>True</code>
<code>print(anagrams("EECE230", "3EEE02E"))</code>	<code>False</code>

Problem 3. Longest zero sum sublist using a dictionary

Write a function `longestZeroSumSublist(L)`, which given a list `L` of integers, finds a (contiguous) sublist of `L` whose sum is zero and whose length is maximal.

If the list does not have a non-empty sublist whose elements sum to zero, your function should return empty list.

Examples: In each of the following examples, a zero-sum sublist of maximal length is underlined.

1 10 <u>-1 -1 2</u> 3 -5 26
1 10 <u>-1 -1 4 3</u> -5 26
1 10 <u>1 -1</u> 4 3 -5 26
1 10 1 <u>0</u> 4 3 -5 26
1 10 1 1 4 3 -5 26
<u>-1 -1 2</u> 3 -5 26
2 2 <u>-1 0 -1 2</u>
1 <u>0 -2 1 0 1 -1 0 -1 2</u> -2 -2

Note also that there are possibly more than one zero-sum sublist of maximal length, e.g., in the first example, we have two zero-sum sublists of maximal length: 1 10 -1 -1 2 3 -5 26 and 1 10 -1 -1 2 3 -5 26. You are not asked to find all zero-sum sublists of maximal length; any one of them is a valid answer.

Below is the naive solution of this problem, which takes $O(n^2)$ steps, where n is the length of `L`.

```
def longestZeroSumSubListSlow(L): #  $O(n^2)$ 
    print(L)
    n = len(L)
    if n== 0: return []
    iMax = 0
    jMax = -1
    for i in range(n):
        cumulativeSum = 0
        for j in range(i,n):
            cumulativeSum+= L[j]
            if cumulativeSum==0 and j - i > jMax-iMax:
                iMax = i
                jMax = j
    return L[iMax:jMax+1]
```

You are asked to do it in $O(n)$ expected time using a dictionary.

Don't try to read the following hint unless you are stuck (to read it you need to magnify the PDF file); try first to solve it on your own without help.

(*Hint* : • Keep track of the cumulative sum. Let $s_i = L[1] + \dots + L[i]$. Then $L[j] + \dots + L[i] = s_j - s_i$, hence $L[j] + \dots + L[i] = 0$ if and only if $s_i = s_j$. Therefore, the length of the longest increasing subarray ending at j is $j - i$, where i is the first index such that $s_i = s_j$. How do we find i ? Use dictionary D whose keys are cumulative sums. The value associated with key s is the index of the first occurrence of the cumulative sum s .)

Test program:

```
print(longestZeroSumSubList([1, 10, -1, -1, 2, 3, -5, 26]))
print(longestZeroSumSubList([1, 10, -1, -1, 4, 3, -5, 26]))
print(longestZeroSumSubList([1, 10, 1, -1, 4, 3, -5, 26]))
print(longestZeroSumSubList([1, 10, 1, 0, 4, 3, -5, 26]))
print(longestZeroSumSubList([1, 10, 1, 1, 4, 3, -5, 26]))
print(longestZeroSumSubList([-1, -1, 2, 3, -5, 26]))
print(longestZeroSumSubList([2, 2, -1, 0, -1, 2]))
print(longestZeroSumSubList([1, 0, -2, 1, 0, 1, -1, 0, -1, 2, -2, -2]))
```

Output:

```
[-1, -1, 2]
[-1, -1, 4, 3, -5]
[1, -1]
[0]
[]
[-1, -1, 2]
[2, -1, 0, -1]
[0, -2, 1, 0, 1, -1,
 0, -1, 2]
```

Problem 4. Application of stacks: parentheses and braces checker

Write a function `parenthesesAndBracesChecker(s)`, which given a string `s` checks if the parentheses `"(" "`)`"` and braces `"[" "]"` match.

For example the parenthesis and braces match in "a(aa)aa", "aa(b(cd))e[ab]", and "([aa(b)c[[aaaaa]]r(d))]", but they don't match in "a([b])", "((aab)d", "(((", or "ef)"]).

Test your function on the above examples. Aim for $O(n)$ time, where $n = \text{len}(s)$.

(*Hint 1:* Use a stack.)

Don't try to read the following hint unless you are stuck (to read it you need to magnify the PDF file and properly read it in reverse order); try first to solve it on your own without help.

(Hint 2: gärlt eht äi oetwarko eht lätv meel määw — jähags "j" so "j" a een way fl .äi heep jähags "j" so "j" a een way fl .j" das ,["j"]-,"j" meef taeffid dähags eht meag! gärlt eht mees