Fundamental of Opto-Electronics 方法论

Jiaguang Han

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Introduction

Maxwell 1.1

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \tag{1.1}$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t}$$

$$\nabla \cdot \mathbf{B} = 0$$
(1.2)
(1.3)

$$\nabla \cdot \mathbf{B} = 0 \tag{1.3}$$

$$\nabla \cdot \mathbf{D} = \rho \tag{1.4}$$

$$\oint_{loop} \mathbf{E} \cdot d\mathbf{l} = -\frac{\partial}{\partial t} \int_{area} \mathbf{B} \cdot d\mathbf{S}$$
 (1.5)

$$\oint \mathbf{H} \cdot d\mathbf{l} = \int \mathbf{J} \cdot d\mathbf{S} + \frac{\partial}{\partial t} \int_{area} \mathbf{D} \cdot d\mathbf{S} \tag{1.6}$$

$$\oint_{surf} \mathbf{B} \cdot d\mathbf{S} = 0 \tag{1.7}$$

$$\oint_{surf} D \cdot dS = Q_{enclosed}$$
 (1.8)

$$F = q(e + v \times B) \tag{1.9}$$

E:electric field strength;V/M

D:electric flux density; C/m^2

H:magnetic field strength; A/m

B:magnetic flux density; $Webers/m^2$

J:electric current density; A/m^2

 $I_0; I_{incident}, I_{reflection}, I_{transmission}, I_{absorption}, I_{lumin}, I_{scattering}, I_{interference}$

$$R = \frac{|E_R|^2}{|E_0|^2} \text{:reflectivity, or reflectance} \qquad T = \frac{|E_T|^2}{|E_0|^2} \text{:transmitivity, or transmitance}$$

$$r = \frac{|E_R|}{|E_0|} \text{:reflection coefficiency} \qquad t = \frac{|E_T|}{|E_0|} \text{:transmit coefficiency}$$

$$\lambda = c/f = 2\pi c/\omega; \frac{v}{c} = \frac{\lambda_1 f_1}{\lambda_0 f_0} = \frac{1}{n_1}, \text{ so } f_0 = f_1$$

When $l \gg l_c$,

$$T = \frac{(1 - R_1)(1 - R_2)e^{-\alpha l}}{1 - R_1 R_2 e^{-2\alpha l}} = (1 - R_1)(1 - R_2)e^{-\alpha l} \cdot \sum_{i=0}^{\infty} (R_1 R_2 e^{-2\alpha l})^i$$
(1.10)

$$I = \langle s \rangle \propto \langle E \times H \rangle = \frac{c}{4\pi} \sqrt{\frac{\varepsilon}{\mu}} \langle E^2 \rangle$$
for $E(\mathbf{r}, t) = \frac{1}{2} [A(\mathbf{r})e^{-i\omega t} + A^*(\mathbf{r})e^{i\omega t}], E = E_1 + E_2$

$$I = \langle E^2 \rangle = \langle E_1^2 \rangle + \langle E_2^2 \rangle + 2 \cdot \langle E_1 \cdot E_2 \rangle \tag{1.11}$$

if $\omega_1 = \omega_2$,

$$\langle E_1 \cdot E_2 \rangle = \frac{1}{4} \langle A_1 A_2^* + A_1^* A_2 \rangle$$

if $A_1 = a_1 e^{i\phi_1}$, $A_2 = a_2 e^{i\phi_2}$

$$\langle E_1 E_2 \rangle = \frac{1}{4} [a_1 a_2 cos(\phi_1 - \phi_2) + a_1 a_2 cos(\phi_2 - \phi_1)]$$

that is to say ,for $\delta = \phi_1 - \phi_2 = 2\pi/\lambda L_c$, $L_c = \frac{\lambda \cdot \delta}{2\pi}$

Absorption coefficiency: α , according to Lamb-Beer Law: $I=I_0e^{-\alpha l}$. Absorb ratio: $A=|\frac{I_\alpha}{I_0}|=|\frac{E_\alpha}{E_0}|$

1.2 Polarization

$$\mathbf{H} = (-\mathbf{x} \frac{b}{n} e^{j\phi_b} e^{-jkz} + \mathbf{y} \frac{a}{n} e^{j\phi_a} e^{-jkz}) e^{j\omega t}$$

for z = 0

$$\mathbf{H} = (-\mathbf{x} \frac{b}{\eta} e^{j\phi_b} + \mathbf{y} \frac{a}{\eta} e^{j\phi_a}) e^{j\omega t}$$

$$E = (xae^{j\phi_a} + ybe^{j\phi_b})e^{j\omega t}$$
(1.12)

$$real(E) = xa cos(\omega t + \phi_a) + yb cos(\omega t + \phi_b)$$
 (1.13)

for $a=b, \phi_a=\phi_b$, linear-polarization for $a=b, \phi_a-\phi_b=\pi/2$, circle-polarization

1.3. MATERIAL 5

1.3 Material

with a ϵ and μ , the material is called isotropic; with 9ϵ and 9μ , anisotropic; with 18ϵ and 18μ , bianisotropic; with ϵ , μ , χ , κ , baisotropic; homogeneous: independent on r. $\epsilon(r) = \epsilon_0$; linear material: $\epsilon E = \epsilon_0 = \epsilon(r,t)$

Classical Propagation

Interband absorption

Excitons

Luminescence

Free Electrons

Phonons