There are two basic strategies for setting the time constants used by leaky units. One strategy is to manually fix them to values that remain constant, for example by sampling their values from some distribution once at initialization time. Another strategy is to make the time constants free parameters and learn them. Having such leaky units at different time scales appears to help with long-term dependencies (Mozer, 1992; Pascanu et al., 2013).

## 10.9.3 Removing Connections

Another approach to handle long-term dependencies is the idea of organizing the state of the RNN at multiple time-scales (El Hihi and Bengio, 1996), with information flowing more easily through long distances at the slower time scales.

This idea differs from the skip connections through time discussed earlier because it involves actively *removing* length-one connections and replacing them with longer connections. Units modified in such a way are forced to operate on a long time scale. Skip connections through time *add* edges. Units receiving such new connections may learn to operate on a long time scale but may also choose to focus on their other short-term connections.

There are different ways in which a group of recurrent units can be forced to operate at different time scales. One option is to make the recurrent units leaky, but to have different groups of units associated with different fixed time scales. This was the proposal in Mozer (1992) and has been successfully used in Pascanu et al. (2013). Another option is to have explicit and discrete updates taking place at different times, with a different frequency for different groups of units. This is the approach of El Hihi and Bengio (1996) and Koutnik et al. (2014). It worked well on a number of benchmark datasets.

## 10.10 The Long Short-Term Memory and Other Gated RNNs

As of this writing, the most effective sequence models used in practical applications are called **gated RNNs**. These include the **long short-term memory** and networks based on the **gated recurrent unit**.

Like leaky units, gated RNNs are based on the idea of creating paths through time that have derivatives that neither vanish nor explode. Leaky units did this with connection weights that were either manually chosen constants or were parameters. Gated RNNs generalize this to connection weights that may change at each time step.

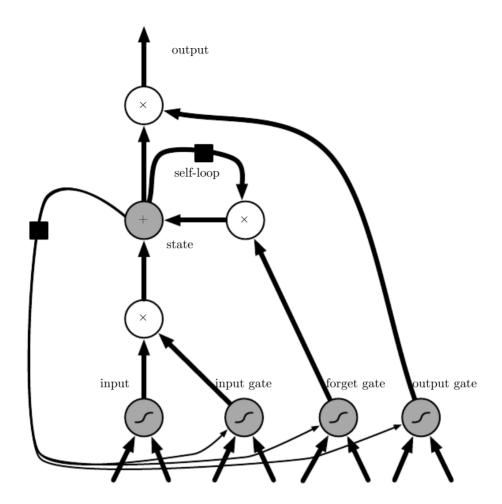


Figure 10.16: Block diagram of the LSTM recurrent network "cell." Cells are connected recurrently to each other, replacing the usual hidden units of ordinary recurrent networks. An input feature is computed with a regular artificial neuron unit. Its value can be accumulated into the state if the sigmoidal input gate allows it. The state unit has a linear self-loop whose weight is controlled by the forget gate. The output of the cell can be shut off by the output gate. All the gating units have a sigmoid nonlinearity, while the input unit can have any squashing nonlinearity. The state unit can also be used as an extra input to the gating units. The black square indicates a delay of a single time step.

Leaky units allow the network to accumulate information (such as evidence for a particular feature or category) over a long duration. However, once that information has been used, it might be useful for the neural network to forget the old state. For example, if a sequence is made of sub-sequences and we want a leaky unit to accumulate evidence inside each sub-subsequence, we need a mechanism to forget the old state by setting it to zero. Instead of manually deciding when to clear the state, we want the neural network to learn to decide when to do it. This

is what gated RNNs do.

## 10.10.1 LSTM

The clever idea of introducing self-loops to produce paths where the gradient can flow for long durations is a core contribution of the initial long short-term memory (LSTM) model (Hochreiter and Schmidhuber, 1997). A crucial addition has been to make the weight on this self-loop conditioned on the context, rather than fixed (Gers et al., 2000). By making the weight of this self-loop gated (controlled by another hidden unit), the time scale of integration can be changed dynamically. In this case, we mean that even for an LSTM with fixed parameters, the time scale of integration can change based on the input sequence, because the time constants are output by the model itself. The LSTM has been found extremely successful in many applications, such as unconstrained handwriting recognition (Graves et al., 2009), speech recognition (Graves et al., 2013; Graves and Jaitly, 2014), handwriting generation (Graves, 2013), machine translation (Sutskever et al., 2014), image captioning (Kiros et al., 2014b; Vinyals et al., 2014b; Xu et al., 2015) and parsing (Vinyals et al., 2014a).

The LSTM block diagram is illustrated in figure 10.16. The corresponding forward propagation equations are given below, in the case of a shallow recurrent network architecture. Deeper architectures have also been successfully used (Graves et al., 2013; Pascanu et al., 2014a). Instead of a unit that simply applies an element-wise nonlinearity to the affine transformation of inputs and recurrent units, LSTM recurrent networks have "LSTM cells" that have an internal recurrence (a self-loop), in addition to the outer recurrence of the RNN. Each cell has the same inputs and outputs as an ordinary recurrent network, but has more parameters and a system of gating units that controls the flow of information. The most important component is the state unit  $s_i^{(t)}$  that has a linear self-loop similar to the leaky units described in the previous section. However, here, the self-loop weight (or the associated time constant) is controlled by a forget gate unit  $f_i^{(t)}$  (for time step t and cell i), that sets this weight to a value between 0 and 1 via a sigmoid unit:

$$f_i^{(t)} = \sigma \left( b_i^f + \sum_j U_{i,j}^f x_j^{(t)} + \sum_j W_{i,j}^f h_j^{(t-1)} \right), \tag{10.40}$$

where  $\boldsymbol{x}^{(t)}$  is the current input vector and  $\boldsymbol{h}^{(t)}$  is the current hidden layer vector, containing the outputs of all the LSTM cells, and  $\boldsymbol{b}^f$ ,  $\boldsymbol{U}^f$ ,  $\boldsymbol{W}^f$  are respectively biases, input weights and recurrent weights for the forget gates. The LSTM cell

internal state is thus updated as follows, but with a conditional self-loop weight  $f_i^{(t)}$ :

$$s_i^{(t)} = f_i^{(t)} s_i^{(t-1)} + g_i^{(t)} \sigma \left( b_i + \sum_j U_{i,j} x_j^{(t)} + \sum_j W_{i,j} h_j^{(t-1)} \right), \tag{10.41}$$

where b, U and W respectively denote the biases, input weights and recurrent weights into the LSTM cell. The **external input gate** unit  $g_i^{(t)}$  is computed similarly to the forget gate (with a sigmoid unit to obtain a gating value between 0 and 1), but with its own parameters:

$$g_i^{(t)} = \sigma \left( b_i^g + \sum_j U_{i,j}^g x_j^{(t)} + \sum_j W_{i,j}^g h_j^{(t-1)} \right). \tag{10.42}$$

The output  $h_i^{(t)}$  of the LSTM cell can also be shut off, via the **output gate**  $q_i^{(t)}$ , which also uses a sigmoid unit for gating:

$$h_i^{(t)} = \tanh\left(s_i^{(t)}\right) q_i^{(t)} \tag{10.43}$$

$$q_i^{(t)} = \sigma \left( b_i^o + \sum_j U_{i,j}^o x_j^{(t)} + \sum_j W_{i,j}^o h_j^{(t-1)} \right)$$
 (10.44)

which has parameters  $b^o$ ,  $U^o$ ,  $W^o$  for its biases, input weights and recurrent weights, respectively. Among the variants, one can choose to use the cell state  $s_i^{(t)}$  as an extra input (with its weight) into the three gates of the *i*-th unit, as shown in figure 10.16. This would require three additional parameters.

LSTM networks have been shown to learn long-term dependencies more easily than the simple recurrent architectures, first on artificial data sets designed for testing the ability to learn long-term dependencies (Bengio *et al.*, 1994; Hochreiter and Schmidhuber, 1997; Hochreiter *et al.*, 2001), then on challenging sequence processing tasks where state-of-the-art performance was obtained (Graves, 2012; Graves *et al.*, 2013; Sutskever *et al.*, 2014). Variants and alternatives to the LSTM have been studied and used and are discussed next.

## 10.10.2 Other Gated RNNs

Which pieces of the LSTM architecture are actually necessary? What other successful architectures could be designed that allow the network to dynamically control the time scale and forgetting behavior of different units?

Some answers to these questions are given with the recent work on gated RNNs, whose units are also known as gated recurrent units or GRUs (Cho et al., 2014b; Chung et al., 2014, 2015a; Jozefowicz et al., 2015; Chrupala et al., 2015). The main difference with the LSTM is that a single gating unit simultaneously controls the forgetting factor and the decision to update the state unit. The update equations are the following:

$$h_i^{(t)} = u_i^{(t-1)} h_i^{(t-1)} + (1 - u_i^{(t-1)}) \sigma \left( b_i + \sum_j U_{i,j} x_j^{(t-1)} + \sum_j W_{i,j} r_j^{(t-1)} h_j^{(t-1)} \right),$$
(10.45)

where u stands for "update" gate and r for "reset" gate. Their value is defined as usual:

$$u_i^{(t)} = \sigma \left( b_i^u + \sum_j U_{i,j}^u x_j^{(t)} + \sum_j W_{i,j}^u h_j^{(t)} \right)$$
 (10.46)

and

$$r_i^{(t)} = \sigma \left( b_i^r + \sum_j U_{i,j}^r x_j^{(t)} + \sum_j W_{i,j}^r h_j^{(t)} \right). \tag{10.47}$$

The reset and updates gates can individually "ignore" parts of the state vector. The update gates act like conditional leaky integrators that can linearly gate any dimension, thus choosing to copy it (at one extreme of the sigmoid) or completely ignore it (at the other extreme) by replacing it by the new "target state" value (towards which the leaky integrator wants to converge). The reset gates control which parts of the state get used to compute the next target state, introducing an additional nonlinear effect in the relationship between past state and future state.

Many more variants around this theme can be designed. For example the reset gate (or forget gate) output could be shared across multiple hidden units. Alternately, the product of a global gate (covering a whole group of units, such as an entire layer) and a local gate (per unit) could be used to combine global control and local control. However, several investigations over architectural variations of the LSTM and GRU found no variant that would clearly beat both of these across a wide range of tasks (Greff et al., 2015; Jozefowicz et al., 2015). Greff et al. (2015) found that a crucial ingredient is the forget gate, while Jozefowicz et al. (2015) found that adding a bias of 1 to the LSTM forget gate, a practice advocated by Gers et al. (2000), makes the LSTM as strong as the best of the explored architectural variants.