

## 1 5.3: Recursion (continued)

*Palindromes (cont.)*

Base case:  $\lambda \in P$  if  $x \in \Sigma$  then  $x \in P$ .

Recursive: if  $x \in \Sigma$  and  $w \in P$ .

then  $xwx \in P$

(note: this doesn't cover everything:  $xxwxx \in P$ )

*Length of a string*

Basis step:

$\text{length}(\lambda) = 0$

Recursive step:

if  $w \in \Sigma^*$  and  $x \in \Sigma$ , then  $\text{length}(wx) = \text{length}(w) + 1$

$\Sigma^{\text{even}}$ : even-length strings over  $\Sigma$ .

Basis step:

$\lambda \in \Sigma^{\text{even}}$

Recursive step:

if  $w \in \Sigma^{\text{even}}$  and  $x \in \Sigma, y \in \Sigma$ , then  $wxy \in \Sigma^{\text{even}}$