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#### 1 Programme de rendu

### renderer/shaders/terrain.vs

```
#version 330 core
 2
    in vec2
                pos;
    in vec2
                uv;
    in float
                height;
    in vec2
                normal;
    in int
                textureID;
                     visibility;
    out float
10
    \verb"out vec3"
                    pass_normal;
11
    out vec2
                     pass_uv;
12
    flat out int pass_textureID;
13
    out vec3
                     viewVec;
14
15
    //view and projection matrix
    uniform mat4 mvp_matrix;
18
    //transformation matrix
19
    uniform mat4 transf_matrix;
20
    # define TERRAIN_SIZE (16.0)
# define TERRAIN_RENDER_DISTANCE (64)
21
22
23
24
25
26
27
    # define RENDER_DISTANCE (TERRAIN_RENDER_DISTANCE * TERRAIN_SIZE)
    void main(void) {
         vec4 world_pos = transf_matrix * vec4(pos.x, height, pos.y, 1.0);
28
29
30
31
         viewVec = normalize(-world_pos.xyz);
         gl_Position = mvp_matrix * world_pos;
         //fog calculation, visibility = pow(distance, 8)
32
33
34
         visibility = 0.0f;
         visibility = length(gl_Position.xz) / float(RENDER_DISTANCE);
         visibility = visibility * visibility;
visibility = visibility * visibility;
visibility = visibility * visibility;
35
36
37
38
39
         visibility = clamp(visibility, 0, 1);
         pass_normal = normalize(vec3(normal.x, 1.0, normal.y));
40
         pass_uv = uv;
41
         pass_textureID = textureID;
42
    }
```

### renderer/shaders/terrain.fs

```
#version 330 core
 3
                  visibility;
    in float
    in vec3
                  pass_normal;
    in vec2 pass_uv;
flat in int pass_textureID;
                   viewVec;
    in vec3
    out vec4 vertexColor;
10
    uniform vec3 sky_color;
    uniform vec3 sunray;
13
14
    uniform sampler2D textureSampler;
15
    # define TX_UNIT (1 / 5.0)
# define MIN_INTENSITY (0.2)
16
17
    # define SPECULAR_DAMPING (4.0)
```

```
19
20
    void main(void) {
21
22
         //texture
         float uvx = (pass_uv.x * TX_UNIT + pass_textureID * TX_UNIT);
         float uvy = pass_uv.y;
         vec3 txcolor = texture(textureSampler, vec2(uvx, uvy)).rgb;
         vec3 color = txcolor;
26
        //phong ligthing model
float intensity = max(dot(pass_normal, sunray), MIN_INTENSITY);
27
28
         color *= intensity;
29
30
         //specular lighting
31
         vec3 reflectVec = reflect(-sunray, pass_normal);
         float specAngle = max(dot(reflectVec, viewVec), 0.0);
         float specular = pow(specAngle, SPECULAR_DAMPING);
color += specular * vec3(1.0, 1.0, 1.0);
36
         //apply fog
37
         vertexColor = vec4(mix(color, sky_color, visibility), 1.0);
    }
38
```

### renderer/includes/renderer.h

```
#ifndef RENDERER_H
    # define RENDERER_H
    # include "array_list.h"
# include "hmap.h"
    # include "cmaths.h"
    # include "vec.h"
    # include "mat.h"
 8
    # include "glh.h"
# include "tinycthread.h"
10
    # include "noise.h"
    # include <string.h>
    # include <unistd.h>
    # include <string.h>
    # include <time.h>
    # include <fcntl.h>
16
18
    /** the camera data structures */
19
    typedef struct s_camera {
20
          t_vec3f pos; //camera world position
21
          t_vec3f rot; //camera rotation toward (x, y, z) axis
         t\_vec3f vview; //view vector (direction where we are currently lookin at) float \; fov; //field of view
22
         float
                   near_distance; //near plane distance
far_distance; //far plane distance
movespeed; // move speed
24
25
         float
         float
26
27
28
29
30
         float
         t_mat4f mview; //view matrix
         t_mat4f mproj; //projection matrix
         t_mat4f mviewproj; //projection matrix times view matrix t_vec2i terrain_index; //current world terrain index of the camera
31
                         t_camera;
    //terrain detail (number of vertex per line)
# define TERRAIN_DETAIL (16)
    //terrain width (and height)
# define TERRAIN_SIZE (16)
    # define TERRAIN_UNIT (TERRAIN_SIZE / (float)TERRAIN_DETAIL)
    // number of terrain to render
                                            in term of distance
    # define TERRAIN_RENDER_DISTANCE (64)
    // distance where terrain are kept loaded in memory
# define TERRAIN_LOADED_DISTANCE (TERRAIN_RENDER_DISTANCE)
    // distance where terrain are kept loaded in memory # define TERRAIN_KEEP_LOADED_DISTANCE (TERRAIN_LOADED_DISTANCE)
43
    # define MAX_NUMBER_OF_TERRAIN_LOADED (TERRAIN_KEEP_LOADED_DISTANCE *
         TERRAIN_KEEP_LOADED_DISTANCE * 2 * 2)
45
    // number of floats per vertex
    # define TERRAIN_VERTEX_SIZE ((1 + 2) * sizeof(float) + 1 * sizeof(int))
    # define TX_WATER (0)
    # define TX_GRASS (1)
    # define TX_DIRT (2)
51
    # define TX_STONE (3)
    # define TX_SNOW (4)
# define TX_MAX (5)
53
    typedef struct s_image {
55
         int w, h;
                         t image:
59
    typedef struct s_texture {
         t_image * image;
```

```
GLuint txID;
62
                      t_texture;
63
     /** a terrain */
64
    typedef struct s_terrain {
66
         t_vec2i index;
67
         t mat4f mat:
68
         GLuint
                 vao:
69
         GLuint
                 vbo:
70
71
         float
                 * vertices;
         int
                  initialized;
72
    }
                      t_terrain;
73
74
    # define WORLD_OCTAVES (10)
75
76
    /** the world */
77
    typedef struct s_world {
78
         t_hmap
                          * terrains;
79
                          * octaves[WORLD_OCTAVES];
         t_noise
80
           _array_list
                          * generators;
81
         float
                          max_height;
82
         t_image
                           * heightmap;
83
                          time;
         int
84
    }
                      t world;
85
    typedef struct s_generator {
86
                  (*heightGen)(t_world *, struct s_generator *, float, float);
(*colorGen)(t_world *, struct s_generator *, float, float);
87
         float
88
         int
29
         int
                  (*canGenerateAt)(t_world *, struct s_generator *, float, float);
90
         float
                  heightGenStep;
91
         int
                  octaves:
92
        float
                 amplitude;
93
         float
                 persistance;
94
         float
                  frequency;
95
         float
                 lacunarity;
96
    }
                      t_generator;
97
98
    /** the renderer part of the program */
99
    typedef struct s_renderer {
100
                           * program; //the rendering GPU program
         t_glh_program
101
         GLuint
                          terrain_indices; //terrain indices buffer
                          terrain_vertices; //terrain vertices buffer (static grid)
* render_list; //the list of terrain to render
102
         GLuint
103
         t_array_list
104
                          * delete_list; //the list of terrain to delete
         t_array_list
105
         t texture
                           texture;
106
         int
                           vertexCount; //number of vertices drawn on last frame
107
         t_vec3f
                           sunray; //sun light vector
108
    }
                      t_renderer;
109
    typedef struct s_env {
110
         t_glh_context
111
                         * context:
112
         t_world
                          world;
113
         t_renderer
                          renderer:
                          camera; //user camera
114
         t_camera
         thrd_t
115
                          thrd:
116
         int
                          is_running;
117
                      t env:
118
119
    extern t_env g_env;
120
121
    //get env
122
    t_env * getEnv(void);
123
124
    //renderer related functions
125
     void rendererInit(t_renderer * renderer);
126
    void rendererDelete(t_renderer * renderer);
127
    void rendererUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
        camera);
128
    void rendererRender(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
        camera);
129
130
    //world related functions
131
    void
                  worldInit(t_world * world, char * bmpfile, float maxheight, long seed);
132
                  worldDelete(t_world * world);
133
    void
                  worldUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera
         * camera);
134
    void
                 worldGetGridIndex(t_world * world, float worldX, float worldZ, int * gridX, int *
        gridY);
    t_terrain * worldGetTerrain(t_world * world, int gridX, int gridY);
135
                      worldGetGeneratorAt(t_world * world, float wx, float wz);
136
    t_generator *
137
138
    /** generators */
139
             generatorsInit(t_world * world);
    void
140
             generatorsDelete(t_world * world);
141
142
    //terrains
143
    t_terrain * terrainNew(t_world * world, int gridX, int gridY);
```

```
144
    void
                  terrainDelete(t_terrain * terrain);
145
    int
                  terrainHash(t_terrain * terrain);
146
                  terrainCmp(t_terrain * left, t_terrain * right);
    int
147
    void
                  terrainLoadHeightMap(t_terrain * terrains, int * n, char const * bmpfile);
148
                 terrainGenerate(t_world * world, t_terrain * terrain);
    void
149
150
    //camera related functions
    void cameraInit(t_camera * camera);
void cameraDelete(t_camera * camera);
151
152
    void cameraUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
153
         camera);
154
155
    //heightmaps (bmp file)
    t_{\tt lmage}
156
                   * imageNew(char const * path);
                      imageDelete(t_image * t_image);
157
    void
                      heightmapGetHeight(t_image * image, float x, float y);
158
    int
159
160
    //inputs
161
    void inputInit(t_glh_context * context);
162
    void inputUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
163
164
    #endif
```

#### renderer/srcs/camera.c

```
#include "renderer.h"
    void cameraInit(t_camera * camera) {
4
        camera->pos.x = TERRAIN_SIZE * 2, camera->pos.y = TERRAIN_SIZE * 2, camera->pos.z =
        TERRAIN_SIZE * 2; camera->rot.pitch = 0, camera->rot.yaw = 0, camera->rot.roll = 0;
5
6
        camera -> fov = DEG_TO_RAD(70.0f);
        camera->near_distance = 0.01f;
camera->far_distance = TERRAIN_RENDER_DISTANCE * TERRAIN_RENDER_DISTANCE * TERRAIN_SIZE;
8
9
        camera->movespeed = 2.0f;
10
11
    void cameraDelete(t_camera * camera) {
13
14
15
    static void cameraUpdateMatrices(t_camera * camera) {
16
17
         //matrices
18
        t_vec3f * viewvec = &(camera->vview);
19
        t_mat4f * view = &(camera->mview);
        t_mat4f * proj = &(camera->mproj);
20
21
22
23
24
25
26
27
28
29
        t_mat4f * viewproj = &(camera->mviewproj);
        //view vector
        float pitch = DEG_TO_RAD(camera->rot.pitch);
        float yaw = DEG_TO_RAD(camera->rot.yaw);
        float roll = DEG_TO_RAD(camera->rot.roll);
float cospitch = cos(pitch);
        viewvec->x = cospitch * sin(yaw);
        viewvec->y = -sin(pitch);
30
31
        viewvec >y = Sin(pitch),
viewvec >z = -cospitch * cos(yaw);
vec3f_normalize(viewvec, viewvec);
32
33
34
        //view matrix
        mat4f_identity(view);
35
        mat4f_rotateX(view, view, pitch);
        mat4f_rotateY(view, view, yaw);
37
        mat4f_rotateZ(view, view, roll);
38
        mat4f_translate(view, view, -camera->pos.x, -camera->pos.y);
39
40
        //projection matrix
41
        float aspect = 1.6f;
42
        mat4f_perspective(proj, aspect, camera->fov, camera->near_distance, camera->far_distance);
43
44
         //combine view and projection
45
        mat4f_mult(viewproj, proj, view);
46
   }
47
48
    void cameraUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
        camera) {
49
        //update camera matrices
50
        cameraUpdateMatrices(camera);
51
         //update camera world index
52
        worldGetGridIndex(world, camera->pos.x, camera->pos.z, &(camera->terrain_index.x), &(camera->
             terrain index.y));
53
   }
```

### renderer/srcs/generator.c

```
#include "renderer.h"
 2
 3
    static float clamp(float val, float min, float max) {
  return (val > max ? max : val < min ? min : val);</pre>
 4
 5
 6
7
    static int mountainGenColor(t_world * world, t_generator * generator, float wx, float wy, float
         wz) {
 8
         float r = wy / world->max_height;
 9
         if (r <= 0.08f) {
         return (TX_WATER);
} else if (r <= 0.60f) {
  return (TX_GRASS);</pre>
10
11
12
13
         } else if (r \le 0.75f) {
              return (TX_DIRT);
14
15
         } else if(r \le 0.90f) {
              return (TX_STONE);
16
17
         return (TX_SNOW);
18
    }
19
20
21
    static float normalizeHeight(t_world * world, float heightFactor) {
         heightFactor += 1;
         heightFactor *= 0.5f;
heightFactor = clamp(heightFactor, 0.0f, 1.0f);
22
23
24
25
26
         return (world->max_height * heightFactor);
27
28
    /** the height generator function for moutains */
    static float genNoiseHeight(t_world * world, t_generator * generator, float wx, float wz) {
29
30
         float heightFactor = 0.0f;
         float frequency = generator->frequency;
float amplitude = generator->amplitude;
31
32
         for (int i = 0 ; i < generator->octaves ; i++) {
33
34
              heightFactor += pnoise2(world->octaves[i], wx * frequency, wz * frequency) * amplitude;
              frequency *= generator -> lacunarity;
35
              amplitude *= generator -> persistance;
36
37
         return (normalizeHeight(world, heightFactor));
38
    }
39
40
    static float heightmapGenHeight(t_world * world, t_generator * generator, float wx, float wz) {
         int px = (int)(wx / TERRAIN_UNIT);
int py = (int)(wz / TERRAIN_UNIT);
41
42
         px = clamp(px, 0, world->heightmap->w - 1);
py = clamp(py, 0, world->heightmap->h - 1);
43
46
         int rgb = heightmapGetHeight(world->heightmap, px, py);
         float height = rgb / (255.0f * 3.0f);
return (height * world->max_height);
47
48
49
    }
50
51
    static int heightmapCanGenerate(t_world * world, t_generator * generator, float wx, float wz) {
         int px = (int)(wx / TERRAIN_UNIT);
int py = (int)(wz / TERRAIN_UNIT);
52
54
         return (px >= 0 && py >= 0 && px < world->heightmap->w && py < world->heightmap->h);
55
56
57
    static int canGenerate(t_world * world, t_generator * generator, float wx, float wz) {
58
         return (1);
59
60
61
    static void registerGenerator(t_world * world;
                                      float (*heightGen)(t_world *, struct s_generator *, float, float),
63
                                      int (*colorGen)(t_world *, struct s_generator *, float, float)
                                      int (*canGen)(t_world *, struct s_generator *, float, float), float heightGenStep, int octaves,
64
65
                                      float amplitude, float persistance,
float frequency, float lacunarity) {
66
67
68
         t_generator generator;
69
         generator.heightGen = heightGen;
         generator.colorGen = colorGen;
71
72
73
74
75
76
77
78
79
         generator.canGenerateAt = canGen;
         generator.heightGenStep = heightGenStep;
         generator.octaves = octaves;
         generator.amplitude = amplitude;
         generator.frequency = frequency;
         generator.persistance = persistance;
         generator.lacunarity = lacunarity;
         array_list_add(world->generators, &generator);
    }
80
81
    void generatorsInit(t_world * world) {
         if (world->heightmap == NULL) {
```

```
printf("No heightmaps set, generating terrain procedurally\n"); float step = TERRAIN_UNIT / 16.0f;
83
84
85
             registerGenerator(world, genNoiseHeight, mountainGenColor, canGenerate, step, 4, 1.0f,
                 0.5f, 0.03f, 2.0f);
86
        } else {
87
             printf("Heightmap in use\n");
             registerGenerator (world, heightmapGenHeight, mountainGenColor, heightmapCanGenerate,
88
                 TERRAIN_UNIT, 0, 0, 0, 0, 0);
89
        }
   }
90
91
    void generatorsDelete(t_world * world) {
93
        array_list_delete(world->generators);
94
        free(world->generators);
95
```

### renderer/srcs/heightmap.c

```
#include "renderer.h"

int heightmapGetHeight(t_image * image, float x, float y) {
   int idx = ((int)x * image -> h + (int)y) * 3;
   unsigned char * rgb = (unsigned char*)(image + 1);
   unsigned char b = rgb[idx + 0];
   unsigned char g = rgb[idx + 1];
   unsigned char r = rgb[idx + 2];
   return (r + g + b);
}
```

#### renderer/srcs/image.c

```
#include "renderer.h"
 3
    # define BMP_HEADER_SIZE (54)
 4
5
6
7
    t_image * imageNew(char const * path) {
          int fd = open(path, O_RDONLY);
 8
         if (fd == -1) {
              return (NULL);
10
11
12
13
14
         char header[BMP_HEADER_SIZE];
         read(fd, &header, sizeof(header));
15
          //magic
16
         if (header[0] != 'B' || header[1] != 'M') {
17
              close(fd);
18
              return (NULL);
19
20
21
22
23
24
25
26
         int offset = *((int*)(header + 0x0A));
int w = *((int*)(header + 0x12));
int h = *((int*)(header + 0x16));
         t_image * image = (t_image*)malloc(sizeof(t_image) + 3 * w * h);
         if (image == NULL) {
              close(fd);
27
28
              return (NULL);
29
30
31
32
         image -> w = w;
         image ->h = h;
          //read useless bytes
33
34
35
         lseek(fd, offset - BMP_HEADER_SIZE, SEEK_CUR);
         //read raw bytes
36
37
38
39
40
         read(fd, image + 1, w * h * 3);
         close(fd);
         return (image);
    }
41
42
    void imageDelete(t_image * map) {
43
         free(map);
```

## renderer/srcs/input.c

```
#include "renderer.h"
3
    static void inputKey(GLFWwindow * winptr, int key, int scancode, int action, int mods) {
        //close
5
        if (key == GLFW_KEY_ESCAPE) {
            glfwSetWindowShouldClose(winptr, 1);
6
8
   }
9
10
    static void inputUpdateCamera(t_camera * camera) {
12
        float movespeed = camera->movespeed;
13
        static float rotspeed = 0.3f;
14
15
        t_glh_window * win = glhGetWindow();
16
17
        //camera speed
18
        if (glfwGetKey(win->pointer,
                                       GLFW_KEY_KP_ADD) == GLFW_PRESS) {
19
             camera->movespeed *= 1.2f;
20
        } else if (glfwGetKey(win->pointer, GLFW_KEY_KP_SUBTRACT) == GLFW_PRESS) {
21
22
23
            camera -> movespeed *= 0.833f;
24
25
        //rotation
        camera->rot.pitch += ((win->mouseY - win->prev_mouseY) * rotspeed);
26
27
28
29
        camera->rot.yaw += ((win->mouseX - win->prev_mouseX) * rotspeed);
        if (glfwGetKey(win->pointer, GLFW_KEY_W) == GLFW_PRESS) {
            camera -> pos.x += camera -> vview.x * movespeed;
31
32
            camera -> pos.y += camera -> vview.y * movespeed;
            camera->pos.z += camera->vview.z * movespeed;
33
34
        } else if (glfwGetKey(win->pointer, GLFW_KEY_S) == GLFW_PRESS) {
            camera -> pos.x += -camera -> vview.x * movespeed;
35
36
37
            camera->pos.y += -camera->vview.y * movespeed;
            camera -> pos.z += -camera -> vview.z * movespeed;
38
39
        if (glfwGetKey(win->pointer, GLFW_KEY_D) == GLFW_PRESS) {
40
            camera -> pos.x += -camera -> vview.z * movespeed;
41
            camera ->pos.z += camera ->vview.x * movespeed;
42
43
        else if (glfwGetKey(win->pointer, GLFW_KEY_A) == GLFW_PRESS) {
            camera->pos.x += camera->vview.z * movespeed;
camera->pos.z += -camera->vview.x * movespeed;
44
45
46
47
   }
   void inputUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
        camera) {
        inputUpdateCamera(camera);
50
        inputUpdateDebug(context, world, renderer, camera);
51
52
53
    void inputInit(t_glh_context * context) {
        glfwSetInputMode(context->window->pointer, GLFW_CURSOR, GLFW_CURSOR_DISABLED);
56
        glfwSetKeyCallback(context->window->pointer, inputKey);
```

### renderer/srcs/main.c

```
#include "renderer.h"
        void printUsage(char * binary, FILE * dst) {
   fprintf(dst, "usage: ./%s [FLAGS]\n", binary);
   fprintf(dst, "flags available are:\n");
   fprintf(dst, "\t-r {SEED} for random/infinite terrain generation\n");
   fprintf(dst, "\t-f [FILE] for a bmp terrain heightmap loading\n");
   fprintf(dst, "\t-h [MAX_HEIGHT] to define maximum height of meshes\n");
   fprintf(dst, "examples:\n");
   fprintf(dst, "\t./%s -r 42 -h 256\n", binary);
   fprintf(dst, "\t./%s -t \"texture.bmp\" -h 12\n", binary);
}
  3
  4
  5
  6
  7
8
10
11
12
        }
13
14
         t_env g_env;
15
16
         t_env * getEnv(void) {
17
                    return (&(g_env));
18
         static int threadLoop(void * args) {
                                                                                            = getEnv();
21
                    t env
                                                             * env
22
                                                                                          = env->context;
                                                             * context
                    t_glh_context
```

```
23
24
          t_renderer
                             * renderer = &(env->renderer);
                                            = &(env->world):
          t_world
                             * world
25
26
                                            = &(env->camera);
          t_camera
                             * camera
 27
          printf("Thread loop started!\n");
 28
          while (env->is_running) {
 30
               //update the camera and the world
 31
               worldUpdate(context, world, renderer, camera);
 32
 33
               //10 ups
 34
               usleep(50 * 1000);
 35
 37
          printf("Thread loop stopped!\n");
 39
 40
          return (0);
 41
     }
 42
 43
     int main(int argc, char **argv) {
 44
 45
          //get binary name
 46
          char * binary = argc == 0 ? "renderer" : argv[0];
 47
 48
          //parse arguments
 49
          int optind;
          char mode = 'r';
long seed = time(NULL);
 50
 51
 52
          float maxheight = 1.0f;
 53
          char * bmpfile = NULL;
 54
          for (optind = 1; optind < argc; optind++) {</pre>
 55
 56
               if (argv[optind][0] != '-' || argv[optind][2] != 0) {
 57
                     printUsage(binary, stderr); return (EXIT_FAILURE);
 58
 59
 60
               mode = argv[optind][1];
 61
 62
               switch (argv[optind][1]) {
                   case 'r': if (optind + 1 < argc) { seed = atoi(argv[++optind]); } break;
case 'f': if (optind + 1 >= argc) { printUsage(binary, stderr); return (EXIT_FAILURE)
; } else { bmpfile = strdup(argv[++optind]); } break;
case 'h': if (optind + 1 >= argc) { printUsage(binary, stderr); return (EXIT_FAILURE)
; } else { maxheight = atof(argv[++optind]); } break;
 63
 64
 65
 66
                    default: printUsage(binary, stderr); return (EXIT_FAILURE);
 67
               }
 68
          }
 69
 70
          if (argc <= 1) {
 71
72
               printUsage(binary, stdout);
printf("\n");
 73
 74
          maxheight, bmpfile);
 75
 76
          printf("Initializing openGL...\n");
 77
 78
          glhInit();
 79
 80
          printf("Creating gl context...\n");
 81
          t_env * env = getEnv();
 82
 83
          env->context = glhCreateContext();
 84
 85
          t_glh_context * context = env->context;
 86
 87
          if (context == NULL) {
               fprintf(stderr, "Failed to create gl context.\n");
return (EXIT_FAILURE);
 88
 89
 90
          }
 91
          if (context->window == NULL) {
    fprintf(stderr, "Failed to create gl window.\n");
 92
 93
 94
               return (EXIT_FAILURE);
 95
 96
 97
          printf("Making gl context current...\n");
 98
          glhMakeContextCurrent(context);
99
100
                                       = &(env->world);
          t_world * world
          t_renderer * renderer
101
                                       = &(env->renderer);
102
          t_camera * camera
                                       = &(env->camera);
103
                                       = &(env->thrd);
          thrd_t * thrd
104
105
          printf("Initializing camera...\n");
106
          cameraInit(camera):
```

```
107
108
         printf("Initializing renderer...\n");
109
         rendererInit(renderer);
110
111
         printf("Initializing inputs...\n");
         inputInit(context);
113
         printf("Initializing world...\n");
114
         worldInit(world, bmpfile, maxheight, seed);
115
116
117
         printf("Creating calculator thread...\n");
118
         thrd_create(thrd, threadLoop, &env);
119
120
         printf("Rendering started...\n");
121
122
         long int total = 0;
123
         long int count = 0;
124
125
         env->is_running = 1;
126
127
         long t1, t2;
128
         while (!glhWindowShouldClose(context->window) && env->is_running) {
129
130
              MICROSEC(t1);
131
132
              //update the window
133
              glhWindowUpdate(context->window);
134
135
136
              inputUpdate(context, world, renderer, camera);
137
138
              //camera
139
              cameraUpdate(context, world, renderer, camera);
140
141
              //update the renderer
142
              rendererUpdate(context, world, renderer, camera);
143
144
145
              rendererRender(context, world, renderer, camera);
146
147
              MICROSEC(t2);
148
              total += (t2 - t1);
149
              count++:
150
151
              //swap buffers
152
              glhSwapBuffer(context->window);
153
154
155
         env->is_running = 0;
156
         //wait for calculator thread to finish
printf("Waiting for thread to finish...\n");
thrd_join(env->thrd, NULL);
157
158
159
160
161
         printf("Loop ended\n");
162
163
         printf("Deleting camera...\n");
164
         cameraDelete(camera);
165
166
         printf("Deleting world...\n");
167
         worldDelete(world);
168
169
         printf("Deleting renderer...\n");
170
         rendererDelete (renderer);
171
172
         printf("Destroying gl context..\n");
173
         glhDestroyContext(context);
174
175
         printf("Stopping openGL...\n");
176
         glhStop();
177
178
         printf("All done\n");
179
180
         printf("Moyenne: %ld\n", total / 1000 / count);
181
182
         return (0);
183
```

## renderer/srcs/renderer.c

```
1 #include "renderer.h"
2
3 GLuint u_mvp_matrix;
4 GLuint u_transf_matrix;
```

```
GLuint u_sky_color;
 6
     GLuint u_time;
     GLuint u_sunpos;
 8
     static void rendererBindAttributes(t_glh_program * program) {
          glhProgramBindAttribute(program, 0, "pos");
glhProgramBindAttribute(program, 1, "uv");
glhProgramBindAttribute(program, 2, "height");
glhProgramBindAttribute(program, 3, "normal");
glhProgramBindAttribute(program, 4, "textureID");
11
12
13
14
    }
15
16
     static void rendererLinkUniforms(t_glh_program * program) {
   u_mvp_matrix = glhProgramGetUniform(program, "mvp_matrix");
   u_transf_matrix = glhProgramGetUniform(program, "transf_matrix");
17
20
          u_sky_color = glhProgramGetUniform(program, "sky_color");
21
22
          u_time = glhProgramGetUniform(program, "time");
          u_sunpos = glhProgramGetUniform(program, "sunray");
23
24
25
26
    }
     static void rendererGenerateBufferIndices(t_renderer * renderer) {
27
          long size = sizeof(unsigned short) * (TERRAIN_DETAIL - 1) * (TERRAIN_DETAIL - 1) * 6;
28
29
          unsigned short * indices = (unsigned short *) malloc(size);
30
          int x, z;
31
32
          int i00, i01, i11, i10;
int i = 0;
33
          for (x = 0; x < TERRAIN_DETAIL - 1; x++) {
34
                for (z = 0 ; z < TERRAIN_DETAIL - 1; z++) {
35
36
                     i00 = x * TERRAIN_DETAIL + z;
                     i01 = i00 + 1;
i10 = (x + 1) * TERRAIN_DETAIL + z;
37
38
                     i11 = i10 + 1;
indices[i++] = i00;
39
40
                     indices[i++] = i11;
41
42
                     indices[i++] = i10;
43
                     indices[i++] = i00;
44
                     indices[i++] = i01;
45
                     indices[i++] = i11;
46
                }
47
          }
48
          renderer -> terrain_indices = glhVBOGen();
glhVBOBind(GL_ELEMENT_ARRAY_BUFFER, renderer -> terrain_indices);
glhVBOData(GL_ELEMENT_ARRAY_BUFFER, size, indices, GL_STATIC_DRAW);
49
50
51
52
          glhVBOUnbind(GL_ELEMENT_ARRAY_BUFFER);
53
54
          free(indices);
55
    }
56
57
     static void rendererGenerateBufferVertices(t_renderer * renderer) {
58
59
          long size = sizeof(float) * 4 * TERRAIN_DETAIL * TERRAIN_DETAIL;
60
          float * vertices = (float *) malloc(size);
61
          float unit = 1 / (float)(TERRAIN_DETAIL - 1);
62
63
          int x, z;
int i = 0;
64
          for (x = 0; x < TERRAIN_DETAIL; x++) {
65
                for (z = 0; z < TERRAIN_DETAIL; z++) {
   vertices[i++] = x * unit;</pre>
66
67
68
                     vertices[i++] = z * unit;
                     vertices[i++] = x % 2 == 0 ? 0.0f : 1.0f;
vertices[i++] = z % 2 == 0 ? 0.0f : 1.0f;
69
70
71
72
73
74
                }
          renderer->terrain_vertices = glhVBOGen();
75
76
77
78
          glhVBOBind(GL_ARRAY_BUFFER, renderer->terrain_vertices);
glhVBOData(GL_ARRAY_BUFFER, size, vertices, GL_STATIC_DRAW);
          glhVBOUnbind(GL_ARRAY_BUFFER);
79
          free (vertices);
80
81
     static void rendererGenerateBuffers(t_renderer * renderer) {
83
          rendererGenerateBufferIndices(renderer):
84
          rendererGenerateBufferVertices(renderer);
85
86
87
     void rendererInit(t_renderer * renderer) {
88
          //init math lib
90
          cmaths_init();
```

```
92
            //create the program
 93
            renderer -> program = glhProgramNew();
 94
 95
            //load shaders
            GLuint fs = glhShaderLoad("./shaders/terrain.fs", GL_FRAGMENT_SHADER);
GLuint vs = glhShaderLoad("./shaders/terrain.vs", GL_VERTEX_SHADER);
glhProgramAddShader(renderer->program, fs, GLH_SHADER_FRAGMENT);
glhProgramAddShader(renderer->program, vs, GLH_SHADER_VERTEX);
 96
 97
 98
 99
100
101
            //link
            glhProgramLink(renderer->program, rendererBindAttributes, rendererLinkUniforms);
102
103
104
            //generate terrain indices
            rendererGenerateBuffers(renderer);
105
106
107
            //initialize lists
            renderer -> render_list = array_list_new(256, sizeof(t_terrain *));
renderer -> delete_list = array_list_new(256, sizeof(t_terrain *));
108
109
110
            //image
111
112
            renderer->texture.txID = glhGenTexture();
            renderer -> texture.image = imageNew("./res/textures.bmp");
unsigned char * pixels = (unsigned char*)(renderer -> texture.image + 1);

113
114
115
            glBindTexture(GL_TEXTURE_2D, renderer->texture.txID);
printf("txID: %u w : %d h : %d\n", renderer->texture.txID, renderer->texture.image->w,
116
            renderer->texture.image->h);
glTexImage2D(GL_TEXTURE_2D, 0, GL_RGB, renderer->texture.image->w, renderer->texture.image->h
, 0, GL_BGR, GL_UNSIGNED_BYTE, pixels);
117
118
119
            glGenerateMipmap(GL_TEXTURE_2D);
            glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, GL_LINEAR_MIPMAP_LINEAR); glTexParameterf(GL_TEXTURE_2D, GL_TEXTURE_LOD_BIAS, -1.6f);
120
121
122
123
            //enable depth test
            glEnable(GL_DEPTH_TEST);
glEnable(GL_CULL_FACE);
124
125
126
            glCullFace(GL_BACK);
127
128
            //set default sun ray
129
            vec3f_set(&(renderer->sunray), 1.0f, 1.0f, 1.0f);
130
            vec3f_normalize(&(renderer->sunray), &(renderer->sunray));
131
132
            //swap interval for 60 fps max
133
            glfwSwapInterval(1);
134
      }
135
136
      static void rendererInitTerrain(t_renderer * renderer, t_terrain * terrain) {
137
138
            terrain -> initialized = 1:
139
140
            //allocate terrain model on GPU
            terrain->vao = glhVAOGen();
terrain->vbo = glhVBOGen();
141
142
143
144
            //bind vao
145
            glhVAOBind(terrain->vao);
146
147
            //bind indices
148
            glhVBOBind(GL_ELEMENT_ARRAY_BUFFER, renderer->terrain_indices);
149
            //bind static grid
150
            glhVBOBind(GL_ARRAY_BUFFER, renderer->terrain_vertices);
glhVAOSetAttribute(0, 2, GL_FLOAT, 0, 4 * sizeof(float), NULL); //default vertices pos
glhVAOSetAttribute(1, 2, GL_FLOAT, 0, 4 * sizeof(float), (void*)(2 * sizeof(float))); //
151
152
153
                 default vertices uv
154
            glhVBOUnbind(GL_ARRAY_BUFFER);
155
            glhVAOEnableAttribute(0);
            glhVAOEnableAttribute(1);
156
157
158
            //bind buffer
            glhVBOBind(GL_ARRAY_BUFFER, terrain->vbo);
159
160
            //set attruibutes
            glhVAOSetAttribute(2, 1, GL_FLOAT, 0, TERRAIN_VERTEX_SIZE, NULL); //height glhVAOSetAttribute(3, 2, GL_FLOAT, 0, TERRAIN_VERTEX_SIZE, (void*)(1 * sizeof(float))); //
161
162
                  normal
            glhVAOSetAttributeI(4, 3, GL_INT, TERRAIN_VERTEX_SIZE, (void*)((2 + 1) * sizeof(float))); //
                  texture ID
            glhVBOUnbind(GL_ARRAY_BUFFER);
164
165
            //enable attributes
166
            glhVAOEnableAttribute(2);
            glhVAOEnableAttribute(3);
167
168
            glhVAOEnableAttribute(4);
169
170
            //unbind vao
171
            glhVAOUnbind();
172
      }
173
```

```
174
       void rendererUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
               camera) {
175
176
                //clear lists
177
               array_list_clear(renderer->render_list);
178
               array_list_clear(renderer->delete_list);
179
180
                //update lists
               HMAP_ITER_START(world->terrains, t_terrain *, terrain) {
181
182
183
                       t vec3f diff:
184
                      diff.x = terrain->index.x - camera->terrain_index.x;
185
                      diff.y = 0;
186
                      diff.z = terrain->index.y - camera->terrain_index.y;
                              //if to far, delete this terrain
188
189
                      if (diff.x <= -TERRAIN_KEEP_LOADED_DISTANCE || diff.z <= -TERRAIN_KEEP_LOADED_DISTANCE ||
                              diff.x >= TERRAIN_KEEP_LOADED_DISTANCE || diff.z >= TERRAIN_KEEP_LOADED_DISTANCE) {
190
191
                              array_list_add(renderer->delete_list, &terrain);
192
                      } else {
193
194
                              float distance = vec3f_length(&diff);
195
                              if (distance < TERRAIN_RENDER_DISTANCE) {</pre>
                                     float normalizer = 1 / distance;
196
197
                                     diff.x *= normalizer;
198
                                     diff.z *= normalizer;
199
200
                                     float dot = vec3f_dot_product(&(camera->vview), &diff);
if (distance <= 2 || acos_f(dot) < camera->fov) {
201
202
                                            array_list_add(renderer->render_list, &terrain);
203
204
                             }
205
                      }
206
               HMAP_ITER_END(world->terrains, t_terrain *, terrain);
207
208
209
                //remove terrains
210
               ARRAY_LIST_ITER_START(renderer->delete_list, t_terrain **, terrain_ptr, i) {
211
                       t_terrain * terrain = *terrain_ptr;
212
                       hmap_remove_key(world->terrains, &(terrain->index));
213
                      terrainDelete(terrain);
214
215
               ARRAY_LIST_ITER_END(renderer->delete_list, t_terrain **, terrain_ptr, i);
216
217
               array_list_clear(renderer->delete_list);
218 }
219
220
        static int rendererRenderTerrain(t_renderer * renderer, t_terrain * terrain) {
221
               static int vertexCount = (TERRAIN_DETAIL - 1) * (TERRAIN_DETAIL - 1) * 6;
222
223
                //if it vertices arent up to date
224
               if (terrain->vertices != NULL) {
225
                       //update them
226
                       glhVBOBind(GL_ARRAY_BUFFER, terrain->vbo);
                      glhVBOData(GL_ARRAY_BUFFER, TERRAIN_DETAIL * TERRAIN_DETAIL * TERRAIN_VERTEX_SIZE,
227
                             terrain->vertices, GL_STATIC_DRAW);
228
                       //release data
229
                      free(terrain->vertices);
230
                      terrain -> vertices = NULL;
231
                      glhVBOUnbind(GL_ARRAY_BUFFER);
232
233
234
               //load the matrix as a uniform variable
235
               glhProgramLoadUniformMatrix4f(u_transf_matrix, (float*)(&(terrain->mat)));
236
237
               //sun light
238
               glhProgramLoadUniformVec3f(u_sunpos, renderer->sunray.x, renderer->sunray.y, renderer->sunray
                      .z);
239
240
               //bind the model
241
               glhVAOBind(terrain->vao);
242
243
244
               glhDrawElements(GL_TRIANGLES, vertexCount, GL_UNSIGNED_SHORT, NULL);
245
246
               return (vertexCount);
247
248
        \verb|static| void renderer Prepare Program (t_glh_context * context, t_world * world, t_renderer * leaves to the program of the
249
               renderer, t_camera * camera) {
250
               //set the texture
251
               glActiveTexture(GL_TEXTURE0);
252
               glBindTexture(GL_TEXTURE_2D, renderer->texture.txID);
253
254
               //bind the program
255
               glhProgramUse(renderer -> program);
256
```

```
257
         //load uniforms
258
         glhProgramLoadUniformMatrix4f(u_mvp_matrix, (float*)&(camera->mviewproj));
259
         glhProgramLoadUniformVec3f(u_sky_color, 0.46f, 0.70f, 0.99f);
260
         glhProgramLoadUniformInt(u_time, world->time);
261
262
    void rendererRender(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
         camera) {
264
         //viewport
265
         glhViewPort(0, 0, context->window->width, context->window->height);
266
267
         //clear color buffer
268
         glhClearColor(0.46f, 0.70f, 0.99f, 1.0f);
         glhClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
269
270
271
         //prepare the renderer (bind program, textures and uniforms)
272
        rendererPrepareProgram(context, world, renderer, camera);
273
274
         //total vertex drawn
275
         renderer -> vertexCount = 0;
276
277
         //for every terrain which has to be rendered
278
         ARRAY_LIST_ITER_START(renderer->render_list, t_terrain **, terrain_ptr, i) {
279
280
             //get the terrain
281
             t_terrain * terrain = *terrain_ptr;
282
283
             //if it is not initialized, initialize it
if (!terrain->initialized) {
284
285
                 rendererInitTerrain(renderer, terrain);
286
287
288
             if (terrain->initialized) {
289
                 renderer -> vertexCount += rendererRenderTerrain(renderer, terrain);
290
             }
291
292
         ARRAY_LIST_ITER_END(renderer->render_list, t_terrain *, terrain, i);
293
294
         glhVAOUnbind();
295
         glhProgramUse(NULL);
296
297
298
299
    void rendererDelete(t_renderer * renderer) {
300
         cmaths_deinit();
301
         glhProgramDelete(renderer->program);
302
         glhVBODelete(renderer -> terrain_indices);
303
         glhVBODelete(renderer->terrain_vertices);
304
         array_list_delete(renderer->render_list);
305
         free(renderer->render_list);
306
         imageDelete(renderer -> texture.image);
307
         glhDeleteTexture(renderer -> texture.txID);
308
    }
```

## renderer/srcs/terrain.c

```
#include "renderer.h"
 1
 3
    static void terrainCalculateNormal(t_world * world, t_generator * generator, float * nx, float *
 4
                                               float wx, float wy, float wz) {
         float dx = generator->heightGenStep;
         float dz = generator->heightGenStep;
 6
         *nx = (generator->heightGen(world, generator, wx + dx, wz) - wy) / dx;
*nz = (generator->heightGen(world, generator, wx, wz + dz) - wy) / dz;
 8
 9
    }
10
11
    static void terrainGenerateVertices(t_world * world, float vertices[], int gridX, int gridY) {
         float nx, nz;
12
13
         int i = 0;
14
         for (int x = 0 ; x < TERRAIN_DETAIL ; x++) {</pre>
             for (int y = 0; y < TERRAIN_DETAIL; y++) {</pre>
15
16
                  float wx = (gridX * (TERRAIN_DETAIL - 1) + x) * TERRAIN_UNIT;
float wz = (gridY * (TERRAIN_DETAIL - 1) + y) * TERRAIN_UNIT;
17
18
19
                   t_generator * generator = worldGetGenerator(world, wx, wz);
20
21
22
                   float wy = generator->heightGen(world, generator, wx, wz);
                  int textureID = generator ->colorGen(world, generator, wx, wy, wz);
23
                  terrainCalculateNormal(world, generator, &nx, &nz, wx, wy, wz);
24
                  *(vertices + i++) = wy;
                  *(vertices + i++) = nx;
26
                  *(vertices + i++) = nz;
```

```
28
29
                 *((int*)(vertices + i++)) = textureID;
            }
        }
31
   }
   void terrainGenerate(t_world * world, t_terrain * terrain) {
        int gridX = terrain->index.x;
        int gridY = terrain->index.y;
terrain->vertices = (float *) malloc(TERRAIN_DETAIL * TERRAIN_DETAIL * TERRAIN_VERTEX_SIZE);
35
36
37
38
        terrainGenerateVertices(world, terrain->vertices, gridX, gridY);
39
40
    /** delete the given terrain */
    void terrainDelete(t_terrain *
                                     terrain) {
        if (terrain->initialized) {
43
            terrain->initialized = 0;
44
            glhVAODelete(terrain->vao);
45
            glhVBODelete(terrain->vbo);
46
47
48
        if (terrain->vertices != NULL) {
49
            free(terrain->vertices);
            terrain -> vertices = NULL;
51
52
        free(terrain);
53
   }
54
    /** allocate a new terrain on heap + gpu */
    t_terrain * terrainNew(t_world * world, int gridX, int gridY) {
56
57
        //allocate the terrain
        t_terrain * terrain = (t_terrain*)malloc(sizeof(t_terrain));
60
        if (terrain == NULL) {
61
            return (NULL);
62
63
64
        terrain->index.x = gridX;
65
        terrain->index.y = gridY;
        terrain -> vertices = NULL;
67
        terrain->initialized = 0;
68
69
        //generate the transformation matrix for this terrain
70
        mat4f_identity(&(terrain->mat));
71
        mat4f_translate(&(terrain->mat), &(terrain->mat), terrain->index.x * TERRAIN_SIZE, 0, terrain
            ->index.y * TERRAIN_SIZE);
72
73
74
75
76
        mat4f_scale(&(terrain->mat), &(terrain->mat), TERRAIN_SIZE);
        terrainGenerate(world, terrain);
        return (terrain);
   }
```

## renderer/srcs/world.c

```
#include "renderer.h"
3
    static void worldLoadHeightmap(t_world * world, char * file) {
4
5
6
7
        if (file == NULL) {
             world->heightmap = NULL;
        } else {
             world->heightmap = imageNew(file);
8
   }
    static unsigned int world_vec2i_hash(t_vec2i * vec) {
   unsigned int hash = vec->x * (TERRAIN_KEEP_LOADED_DISTANCE * 2 + 1) + vec->y;
11
12
13
        return (hash);
14
    void worldInit(t_world * world, char * bmpfile, float max_height, long seed) {
17
        glhCheckError("pre worldInit()");
18
19
        world->time = 0;
20
21
22
23
24
        world->max_height = max_height;
         worldLoadHeightmap(world, bmpfile);
        world->generators = array_list_new(16, sizeof(generator));
        generatorsInit(world);
25
         //create the terrain hash map
        world->terrains = hmap_new(TERRAIN_KEEP_LOADED_DISTANCE * 4, (t_hf)world_vec2i_hash, (t_cmpf)
            vec2i_nequals, (t_f)NULL, (t_f)NULL);
(world->terrains == NULL) {
28
             fprintf(stderr, "world.c : 1.10 : worldInit() : not enough memory\n");
29
             return ;
```

```
30
 31
 32
          //noise creation
 33
 34
          for (i = 0 ; i < WORLD_OCTAVES ; i++) {</pre>
 35
               world->octaves[i] = noiseNew();
               noiseNextInt(&seed);
 37
               noiseSeed(world->octaves[i], seed);
 38
 39
 40
          glhCheckError("post worldInit()");
 41
     }
 42
     void worldDelete(t_world * world) {
          if (world->heightmap != NULL) {
               imageDelete(world->heightmap);
 45
 46
 47
 48
          HMAP_ITER_START(world->terrains, t_terrain *, terrain) {
 49
               terrainDelete(terrain);
 50
 51
          HMAP_ITER_END(world->terrains, t_terrain *, terrain);
          hmap_delete(world->terrains);
free(world->terrains);
 53
 54
 55
 56
          int i;
for (i = 0 ; i < WORLD_OCTAVES ; i++) {</pre>
 57
 58
               noiseDelete(world->octaves[i]);
 59
 60
          generatorsDelete(world);
 62
 63
     t_generator * worldGetGeneratorAt(t_world * world, float wx, float wz) {
 64
 65
          return (array_list_get(world->generators, 0));
     }
 66
 67
 68
     void worldGetGridIndex(t_world * world, float worldX, float worldZ, int * gridX, int * gridY) {
    *gridX = (int)worldX / TERRAIN_SIZE;
    *gridY = (int)worldZ / TERRAIN_SIZE;
 69
 70
71
72
          if (worldX < 0) {</pre>
 73
74
               *gridX -= 1;
          7
75
76
77
          if (worldZ < 0) {</pre>
              *gridY -= 1;
 78
 79
     }
 80
 81
     t_terrain * worldGetTerrain(t_world * world, int gridX, int gridY) {
          t_vec2i index;
 82
 83
          index.x = gridX;
          index.y = gridY;
 84
 85
          return (hmap_get(world->terrains, &index));
 86
     static void worldLoadNewTerrains(t_world * world, t_camera * camera) {
 89
          int indexx = MAX(0, camera->terrain_index.x - TERRAIN_LOADED_DISTANCE);
 90
          int indexy = MAX(0, camera->terrain_index.y - TERRAIN_LOADED_DISTANCE);
int maxx = camera->terrain_index.x + TERRAIN_LOADED_DISTANCE;
int maxy = camera->terrain_index.y + TERRAIN_LOADED_DISTANCE;
 91
 92
 93
          int gridX, gridY;
for (gridX = indexx ; gridX < maxx; gridX++) {</pre>
 94
 95
 96
               for (gridY = indexy ; gridY < maxy; gridY++) {</pre>
 97
 98
                    if (gridX < 0 || gridY < 0) {
99
                         continue;
100
101
102
                    //if this terrain isnt generated yet
103
                    if (worldGetTerrain(world, gridX, gridY) == NULL) {
104
                         //can it be generated?
                         float wx = gridX * TERRAIN_SIZE;
float wz = gridY * TERRAIN_SIZE;
t_generator * generator = worldGetGeneratorAt(world, wx, wz);
106
107
108
109
                            (!generator->canGenerateAt(world, generator, wx, wz)) {
                         i f
                              continue;
110
111
112
113
                         //if so, generate it
114
                         t_terrain * terrain = terrainNew(world, gridX, gridY);
115
116
                         if (terrain != NULL) {
```

```
117
                          hmap_insert(world->terrains, terrain, &(terrain->index));
118
                     }
                 }
119
             }
120
        }
121
122
123
    void worldUpdate(t_glh_context * context, t_world * world, t_renderer * renderer, t_camera *
124
         camera) {
125
         //load new terrains
126
         worldLoadNewTerrains(world, camera);
127
         world->time++;
128
```

#### 2 Bibliothèque mathématiques

### maths/includes/cmaths.h

```
#ifndef CMATHS_H
2
    # define CMATHS_H
   # include <math.h>
    # include <stdlib.h>
    # include <stdio.h>
    # include <string.h>
   # ifndef DEG_TO_RAD
10
   # define DEG_TO_RAD(X) (X * 0.01745329251f)
11
   # endif
12
13
   # ifndef RAD_TO_DEG
   # define RAD_TO_DEG(X) (X * 57.2957795131f)
16
17
   # ifndef MAX
18
   # define MAX(X, Y) (X > Y ? X : Y)
19
   # endif
20
21
   # ifndef MIN
22
23
   # define MIN(X, Y) (X < Y ? X : Y)</pre>
   # endif
24
    # ifndef ABS
   # define ABS(X) (X < 0 ? -X : X)</pre>
27
28
    # endif
    int cmaths_init(void);
   int cmaths_deinit(void);
            acos_f(float x);
    float
            asin_f(float x);
   float
            atan_f(float x);
   float
36
37
38
39
            sin_f(float x);
   float
            cos_f(float x);
    float
   float
           tan_f(float x);
            sqrt_f(float x);
   float
   #endif
```

### maths/includes/mat4f.h

```
#ifndef MAT4F_H
   # define MAT4F_H
   # include "cmaths.h"
   # include "vec.h"
67
    typedef struct s_mat4f {
8
        float m00;
        float m01;
10
        float m02;
11
        float m03;
12
13
        float m10;
        float m11;
        float m12;
15
        float m13;
```

```
17
18
        float m20:
19
        float m21;
20
        float m22;
21
        float m23;
22
        float m30;
24
        float m31;
25
        float m32:
26
        float m33;
27
                      t_mat4f;
28
29
    /** create a new matrix */
   t_mat4f * mat4f_new(void);
   /** delete the given matrix */
33
    void mat4f_delete(t_mat4f * mat);
34
35
    /** copy */
36
    t_mat4f * mat4f_copy(t_mat4f * dst, t_mat4f * src);
37
    /** set identity */
    t_mat4f * mat4f_identity(t_mat4f * dst);
40
41
    /** set to zero */
42
    t_mat4f * mat4f_zero(t_mat4f * dst);
43
44
    /** transpose */
    t_mat4f * mat4f_transpose(t_mat4f * dst, t_mat4f * src);
45
46
47
    t_mat4f * mat4f_scale(t_mat4f * dst, t_mat4f * mat, float f);
   /** translate */
   t_mat4f * mat4f_translate(t_mat4f * dst, t_mat4f * src, float tx, float ty, float tz);
t_mat4f * mat4f_translate3(t_mat4f * dst, t_mat4f * src, t_vec3f * translate);
51
52
53
54
    /** rotate */
    t_mat4f * mat4f_rotate(t_mat4f * dst, t_mat4f * src, float angle, t_vec3f * axis);
    t_mat4f * mat4f_rotateX(t_mat4f * dst, t_mat4f * src, float angle);
    t_mat4f * mat4f_rotateY(t_mat4f * dst, t_mat4f * src, float angle);
   t_mat4f * mat4f_rotateZ(t_mat4f * dst, t_mat4f * src, float angle);
t_mat4f * mat4f_rotateXYZ(t_mat4f * dst, t_mat4f * src, t_vec3f * rot);
60
61
    /** transformation matrix */
   t_mat4f * mat4f_transformation(t_mat4f * dst, t_vec3f * translate, t_vec3f * rot, t_vec3f * scale
        );
63
    /** determinant */
   float mat4f_determinant(t_mat4f * mat);
66
67
    /** invert */
    t_mat4f * mat4f_invert(t_mat4f * dst, t_mat4f * src);
68
69
70
71
   /** mult */
    t_mat4f * mat4f_mult(t_mat4f * dst, t_mat4f * left, t_mat4f * right);
72
    /** transform vec4f */
74
    t_vec4f * mat4f_transform_vec4f(t_vec4f * dst, t_mat4f * left, t_vec4f * right);
75
76
   /** projections matrix bellow: */
77
78
    /** orthographic matrix */
   t_mat4f * mat4f_orthographic(t_mat4f * dst, float left, float right, float bot, float top, float
near, float far);
79
80
81
    /** perspective matrix */
    t_mat4f * mat4f_perspective(t_mat4f * dst, float aspect, float fov, float near, float far);
83
    /** to string: return a string allocated with malloc() */
85
    char * mat4f_str(t_mat4f * mat);
86
87
    #endif
```

### maths/includes/vec2i.h

```
#ifndef VEC2I_H
# define VEC2I_H

# include "cmaths.h"

typedef struct s_vec2i {
union {
int x:
```

```
int uvx;
10
       };
11
12
        union {
13
            int y;
            int uvy;
15
16
   }
                    t_vec2i;
17
   /** create a new vec2i */
18
19
   t_vec2i * vec2i_new(void);
20
21
    /** delete the vec2i */
   void vec2i_delete(t_vec2i * vec);
   /** set the vec2i to 0 */
   t_vec2i * vec2i_zero(t_vec2i * dst);
26
27
28
   /** set the vec2i values */
   t_vec2i * vec2i_set(t_vec2i * dst, int x, int y);
   t_vec2i * vec2i_set2(t_vec2i * dst, t_vec2i * vec);
30
   /** add two vec2i */
   t_vec2i * vec2i_add(t_vec2i * dst, t_vec2i * left, t_vec2i * right);
33
34
   /** sub two vec2i */
35
   t_vec2i * vec2i_sub(t_vec2i * dst, t_vec2i * left, t_vec2i * right);
36
37
   /** mult the vec2i by the given scalar */
   t_vec2i * vec2i_mult(t_vec2i * dst, t_vec2i * vec, int scalar);
39
   t_vec2i * vec2i_mult2(t_vec2i * dst, t_vec2i * left, t_vec2i * right);
41
    /** scale product */
42
   int vec2i_dot_product(t_vec2i * left, t_vec2i * right);
43
44
   /** length */
45
   int vec2i_length_squared(t_vec2i * vec);
46
   int vec2i_length(t_vec2i * vec);
48
   /** normalize */
   t_vec2i * vec2i_normalize(t_vec2i * dst, t_vec2i * vec);
51
   /** negate */
52
   t_vec2i * vec2i_negate(t_vec2i * dst, t_vec2i * src);
53
   /** angle between two vec */
55
   int vec2i_angle(t_vec2i * left, t_vec2i * right);
    /** mix the two vectors */
   t_vec2i * vec2i_mix(t_vec2i * dst, t_vec2i * left, t_vec2i * right, int ratio);
59
60
   /** comparison */
   int vec2i_equals(t_vec2i * left, t_vec2i * right);
61
    /** to string: return a string allocated with malloc() */
   char * vec2i_str(t_vec2i * vec);
65
66
   #endif
```

## maths/includes/vec3f.h

```
#ifndef VEC3F_H
   # define VEC3F_H
   # include "cmaths.h"
6
7
   typedef struct s_vec3f {
        union {
8
            float x;
9
             float r;
10
            float pitch;
11
        };
12
13
        union {
14
            float y;
15
             float g;
16
             float yaw;
17
18
19
        union {
            float z;
            float b;
22
            float roll;
        };
```

```
24
25
                      t_vec3f;
    /** create a new vec3f */
    t_vec3f * vec3f_new(void);
    /** delete the vec3f */
   void vec3f_delete(t_vec3f * vec);
31
32
    /** set the vec3f to 0 */
33
    t_vec3f * vec3f_zero(t_vec3f * dst);
    /** set the vec3f values */
   t_vec3f * vec3f_set(t_vec3f * dst, float x, float y, float z);
t_vec3f * vec3f_set3(t_vec3f * dst, t_vec3f * vec);
   /** add two vec3f */
40
   t_vec3f * vec3f_add(t_vec3f * dst, t_vec3f * left, t_vec3f * right);
41
42
    /** sub two vec3f */
43
    t_vec3f * vec3f_sub(t_vec3f * dst, t_vec3f * left, t_vec3f * right);
44
45
    /** mult the vec3f by the given scalar */
   t_vec3f * vec3f_mult(t_vec3f * dst, t_vec3f * vec, float scalar);
t_vec3f * vec3f_mult3(t_vec3f * dst, t_vec3f * left, t_vec3f * right);
48
49
    /** cross product */
50
    t_vec3f * vec3f_cross(t_vec3f * dst, t_vec3f * left, t_vec3f * right);
51
52
    /** scale product */
   float vec3f_dot_product(t_vec3f * left, t_vec3f * right);
    /** length */
   float vec3f_length_squared(t_vec3f * vec);
float vec3f_length(t_vec3f * vec);
57
58
59
    /** normalize */
60
   t_vec3f * vec3f_normalize(t_vec3f * dst, t_vec3f * vec);
61
    /** negate */
63
    t_vec3f * vec3f_negate(t_vec3f * dst, t_vec3f * src);
65
    /** angle between two vec */
   float vec3f_angle(t_vec3f * left, t_vec3f * right);
67
68
    /** mix the two vectors */
69
    t_vec3f * vec3f_mix(t_vec3f * dst, t_vec3f * left, t_vec3f * right, float ratio);
70
71
72
73
    /** comparison */
    int vec3f_equals(t_vec3f * left, t_vec3f * right);
74
75
    /** hash */
    int vec3f_hash(t_vec3f * vec);
76
77
    /** round vec3f */
78
79
    t_vec3f * vec3f_round(t_vec3f * dst, t_vec3f * vec, int decimals);
   /** to string: return a string allocated with malloc() */
    char * vec3f_str(t_vec3f * vec);
   #endif
```

### maths/srcs/cmaths.c

```
#include "cmaths.h"
3
   float * sin_table;
5
   float atan_f(float x) {
6
7
        float xabs = ABS(x);
       return (0.78539816339f * x - x * (xabs - 1) * (0.2447f + 0.0663f * xabs));
8
10
   float acos_f(float x) {
11
        //lagrange interpolation:
       return ((-0.69813170079773212f * x * x - 0.87266462599716477f) * x + 1.5707963267948966f);
12
13
   }
14
15
   float asin_f(float x) {
16
       return (-acos_f(x) + 1.5707963267948966f);
17
18
19
   float tan_f(float x) {
20
       return (sin_f(x) / cos_f(x));
21
```

```
float sin_f(float x) {
         unsigned int index = (unsigned int)RAD_TO_DEG(ABS(x)) % 360;
         return (index > 180 ? -sin_table[index - 180] : sin_table[index]);
   float cos_f(float x) {
   return (sin_f(x + 1.5707963267948966f));
30
31
32
    float sqrt_f(float x) {
        unsigned int i = *(unsigned int*) &x;
34
         i += 127 << 23;
         i >>= 1;
36
         return (*(float*) &i);
37
38
39
    int cmaths_init(void) {
40
41
         sin_table = (float *) malloc(sizeof(float) * 4 * 360);
42
         if (sin_table == NULL) {
43
             return (0);
45
        int i, j;
for (i = 0, j = 0 ; i < 180; i++) {
    sin_table[j++] = (float)sin((double)DEG_TO_RAD((float)i));
.</pre>
46
47
48
49
50
51
         return (1);
52
    int cmaths_deinit(void) {
        free(sin_table);
55
         sin_table = NULL;
56
57
         return (1);
    }
58
```

### maths/srcs/mat4f.c

```
#include "mat4f.h"
2
   t_mat4f * mat4f_new(void) {
       return ((t_mat4f*)malloc(sizeof(t_mat4f)));
   void mat4f_delete(t_mat4f * mat) {
8
       free(mat);
9
10
   t_mat4f * mat4f_copy(t_mat4f * dst, t_mat4f * src) {
      if (dst == NULL) {
           if ((dst = mat4f_new()) == NULL) {
13
               return (NULL);
16
17
       memcpy(dst, src, sizeof(t_mat4f));
18
       return (dst);
19
   }
20
21
   t_mat4f * mat4f_identity(t_mat4f * dst) {
22
       if (dst == NULL) {
           if ((dst = mat4f_new()) == NULL) {
               return (NULL);
25
26
27
28
29
30
       dst->m00 = 1, dst->m01 = 0, dst->m02 = 0, dst->m03 = 0;
       dst->m30 = 0, dst->m31 = 0, dst->m32 = 0, dst->m33 = 1;
       return (dst);
34
35
36
   t_mat4f * mat4f_zero(t_mat4f * dst) {
       if (dst == NULL) {
37
           if ((dst = mat4f_new()) == NULL) {
38
               return (NULL);
39
       memset(dst, 0, sizeof(t_mat4f));
41
       return (dst);
43
   }
```

```
45
               t_mat4f * mat4f_transpose(t_mat4f * dst, t_mat4f * src) {
    46
    47
                                 if (dst == NULL) {
    48
                                               if ((dst = mat4f_new()) == NULL) {
    49
                                                            return (NULL);
    50
    51
                               }
    52
                               float m00 = src->m00;
    53
    54
                               float m01 = src \rightarrow m10;
                                float m02 = src->m20;
    55
    56
                                float m03 = src -> m30;
    57
                                float m10 = src->m01;
                               float m11 = src->m11;
    59
                                float m12 = src->m21;
    60
                               float m13 = src->m31;
    61
                                float m20 = src \rightarrow m02;
    62
                                float m21 = src \rightarrow m12;
    63
                                float m22 = src \rightarrow m22;
    64
                                float m23 = src \rightarrow m32;
    65
                                float m30 = src \rightarrow m03;
    66
                                float m31 = src->m13;
    67
                                float m32 = src \rightarrow m23;
    68
                               float m33 = src->m33;
    69
    70
71
72
73
                                dst->m00 = m00, dst->m01 = m01, dst->m02 = m02, dst->m03 = m03;
                                dst->m10 = m10, dst->m11 = m11, dst->m12 = m12, dst->m13 = m13; dst->m20 = m20, dst->m21 = m21, dst->m22 = m22, dst->m23 = m23; dst->m30 = m30, dst->m31 = m31, dst->m32 = m32, dst->m33 = m33;
    74
    75
                                return (dst);
    76
               }
    77
    78
                t_mat4f * mat4f_scale(t_mat4f * dst, t_mat4f * src, float scale) {
    79
                                if (dst == NULL) {
    80
                                               if ((dst = mat4f_new()) == NULL) {
    81
    82
                                                             return (NULL);
    83
    84
                                }
    85
    86
                                dst->m00 = src->m00 * scale, dst->m01 = src->m01 * scale, dst->m02 = src->m02 * scale, dst->
                                            m03 = src -> m03 * scale:
                                dst->m10 = src->m10 * scale, dst->m11 = src->m11 * scale, dst->m12 = src->m12 * scale, dst->m10 = src->m10 = src->m10 * scale, dst->m10 = src->m10 = s
    87
                                            m13 = src -> m13 * scale;
    88
                                 dst->m20 = src->m20 * scale, dst->m21 = src->m21 * scale, dst->m22 = src->m22 * scale, dst->m20 = src->m20 * scale, dst->m20 = scale, dst->m20 =
                                              m23 = src -> m23 * scale;
    89
    90
                                return (dst);
                }
    92
    93
                t_mat4f * mat4f_scale3(t_mat4f * dst, t_mat4f * src, t_vec3f * scale) {
    94
    95
                                 if (dst == NULL) {
    96
                                               if ((dst = mat4f_new()) == NULL) {
    97
                                                             return (NULL);
                                               }
    98
    99
                                }
 100
                                dst->m00 = src->m00 * scale->x, dst->m01 = src->m01 * scale->x, dst->m02 = src->m02 * scale->
101
                                            x, dst->m03 = src->m03 * scale->x;
102
                                dst->m10 = src->m10 * scale->y, dst->m11 = src->m11 * scale->y, dst->m12 = src->m12 * scale->m12 * scale->m
                                              y, dst->m13 = src->m13 * scale->y;
                                 dst->m20 = src->m20 * scale->z, dst->m21 = src->m21 * scale->z, dst->m22 = src->m22 * scale->
103
                                              z, dst->m23 = src->m23 * scale->z;
 104
 105
                                return (dst);
 106 }
 107
 108
                 t_mat4f * mat4f_translate(t_mat4f * dst, t_mat4f * src, float tx, float ty, float tz) {
                                if (dst == NULL) {
 109
                                               if ((dst = mat4f_new()) == NULL) {
 110
 111
                                                            return (NULL);
 112
                                               }
 113
                                }
 114
                                dst->m30 += src->m00 * tx + src->m10 * ty + src->m20 * tz;
 115
                                dst->m31 += src->m01 * tx + src->m11 * ty + src->m21 * tz;
dst->m32 += src->m02 * tx + src->m12 * ty + src->m22 * tz;
 116
 117
                                dst->m33 += src->m03 * tx + src->m13 * ty + src->m23 * tz;
 118
 119
                                return (dst);
 120 }
 121
 122
                 t_mat4f * mat4f_translate3(t_mat4f * dst, t_mat4f * src, t_vec3f * translate) {
 123
                                return (mat4f_translate(dst, src, translate->x, translate->y, translate->z));
 124
 125
```

```
126 t_mat4f * mat4f_rotate(t_mat4f * dst, t_mat4f * src, float angle, t_vec3f * axis) {
127
128
         if (dst == NULL) {
              if ((dst = mat4f_new()) == NULL) {
129
130
                  return (NULL);
131
132
133
134
         float c = (float)cos(angle);
         float s = (float)sin(angle);
135
136
         float oneminusc = 1.0f
137
         float xy = axis->x * axis->y;
138
         float yz = axis->y * axis->z;
         float xz = axis->x * axis->z;
139
140
         float xs = axis->x * s;
141
         float ys = axis->y * s;
142
         float zs = axis->z * s;
143
144
         float f00 = axis->x * axis->x * oneminusc + c;
145
         float f01 = xy * oneminusc + zs;
         float f02 = xz * oneminusc - ys;
146
147
          // n[3] not used
148
         float f10 = xy * oneminusc - zs;
         float f11 = axis->y * axis->y * oneminusc + c;
149
         float f12 = yz * oneminusc + xs;
150
          // n[7] not used
151
         float f20 = xz * oneminusc + ys;
float f21 = yz * oneminusc - xs;
152
153
         float f22 = axis->z * axis->z * oneminusc + c;
154
155
156
         float t00 = src \rightarrow m00 * f00 + src \rightarrow m10 * f01 + src \rightarrow m20 * f02;
157
         float t01 = src->m01 * f00 + src->m11 * f01 + src->m21 * f02;
         float t02 = src -> m02 * f00 + src -> m12 * f01 + src -> m22 * f02;
159
         float t03 = src - m03 * f00 + src - m13 * f01 + src - m23 * f02;
160
         float t10 = src - m00 * f10 + src - m10 * f11 + src - m20 * f12;
         float t11 = src->m01 * f10 + src->m11 * f11 + src->m21 * f12;
161
         float t12 = src->m02 * f10 + src->m12 * f11 + src->m23 * f12;
float t13 = src->m03 * f10 + src->m13 * f11 + src->m23 * f12;
162
163
164
          dst->m20 = src->m00 * f20 + src->m10 * f21 + src->m20 * f22;
165
          dst->m21 = src->m01 * f20 + src->m11 * f21 + src->m21 * f22;
166
         dst-m22 = src-m02 * f20 + src-m12 * f21 + src-m22 * f22;
         dst - m23 = src - m03 * f20 + src - m13 * f21 + src - m23 * f22;
167
168
         dst \rightarrow m00 = t00;
169
         dst \rightarrow m01 = t01;
170
         dst -> m02 = t02:
171
         dst->m03 = t03;
172
         dst->m10 = t10;
173
         dst->m11 = t11;
174
         dst->m12 = t12;
175
         dst -> m13 = t13;
176
         return (dst);
177
    }
178
179
     t_mat4f * mat4f_rotateX(t_mat4f * dst, t_mat4f * src, float angle) {
180
          if (dst == NULL) {
181
182
              if ((dst = mat4f_new()) == NULL) {
183
                  return (NULL);
184
185
         }
186
         float c = (float)cos(angle);
float s = (float)sin(angle);
187
188
189
         float t00 = src \rightarrow m00;
190
         float t01 = src->m01;
191
         float t02 = src->m02;
192
         float t03 = src \rightarrow m03;
         float t10 = src - m10 * c + src - m20 * s;
193
194
         float t11 = src -> m11 * c + src -> m21 * s;
195
         float t12 = src - m12 * c + src - m22 * s;
196
         float t13 = src->m13 * c + src->m23 * s;
197
         dst->m20 = src->m10 * -s + src->m20 * c;
         dst->m21 = src->m11 * -s + src->m21 * c;
198
199
         dst->m22 = src->m12 * -s + src->m22 * c;
200
         dst-m23 = src-m13 * -s + src-m23 * c;
201
         dst->m00 = t00;
202
         dst -> m01 = t01;
203
         dst \rightarrow m02 = t02;
204
         dst -> m03 = t03:
205
         dst.->m10 = t.10
206
         dst -> m11 = t11:
         dst -> m12 = t12;
207
208
         dst -> m13 = t13;
209
210
         return (dst);
211
    }
212
```

```
213 t_mat4f * mat4f_rotateY(t_mat4f * dst, t_mat4f * src, float angle) {
214
215
         if (dst == NULL) {
216
              if ((dst = mat4f_new()) == NULL) {
217
                  return (NULL);
218
219
220
221
         float c = (float)cos(angle);
222
         float s = (float)sin(angle);
223
         float t00 = src - m00 * c + src - m20 * -s;
224
         float t01 = src -> m01 * c + src -> m21 * -s;
225
         float t02 = src - > m02 * c + src - > m22 * -s;
         float t03 = src - m03 * c + src - m23 * -s;
227
         float t10 = src \rightarrow m10;
228
         float t11 = src->m11;
         float t12 = src->m12;
float t13 = src->m13;
229
230
231
         dst->m20 = src->m00 * s + src->m20 * c;
232
         dst->m21 = src->m01 * s + src->m21 * c;
233
         dst->m22 = src->m02 * s + src->m22 * c;
234
         dst->m23 = src->m03 * s + src->m23 * c;
235
         dst \rightarrow m00 = t00;
236
         dst->m01 = t01;
237
         dst -> m02 = t02;
238
         dst \rightarrow m03 = t03;
239
         dst->m10 = t10;
240
         dst -> m11 = t11;
241
         dst->m12 = t12;
242
         dst->m13 = t13;
243
         return (dst);
244 }
245
246
    t_mat4f * mat4f_rotateZ(t_mat4f * dst, t_mat4f * src, float angle) {
247
         if (dst == NULL) {
              if ((dst = mat4f_new()) == NULL) {
248
249
                  return (NULL);
250
251
252
253
         float c = (float)cos(angle);
254
         float s = (float)sin(angle);
255
         float t00 = src -> m00 * c + src -> m10 * s;
256
         float t01 = src->m01 * c + src->m11 * s;
257
         float t02 = src->m02 * c + src->m12 * s;
258
         float t03 = src->m03 * c + src->m13 * s;
259
         float t10 = src - > m00 * -s + src - > m10 * c;
260
         float t11 = src -> m01 * -s + src -> m11 * c;
261
         float t12 = src->m02 * -s + src->m12 * c;
262
         float t13 = src - m03 * -s + src - m13 * c;
263
         dst->m20 = src->m20;
264
         dst -> m21 = src -> m21;
265
         dst -> m22 = src -> m22:
266
         dst->m23 = src->m23;
         dst->m00 = t00;
267
268
         dst->m01 = t01;
269
         dst->m02 = t02;
270
         dst -> m03 = t03;
271
         dst \rightarrow m10 = t10;
272
         dst -> m11 = t11;
273
         dst -> m12 = t12:
274
         dst -> m13 = t13;
275
         return (dst);
276 }
277
278
     t_mat4f * mat4f_rotateXYZ(t_mat4f * dst, t_mat4f * src, t_vec3f * rot) {
279
         if (dst == NULL) {
280
              if ((dst = mat4f_new()) == NULL) {
281
                  return (NULL);
282
              }
283
         }
284
         mat4f_rotateX(dst, src, rot->x);
mat4f_rotateY(dst, src, rot->y);
mat4f_rotateZ(dst, src, rot->z);
285
286
287
288
         return (dst);
289
    }
290
    t_mat4f * mat4f_transformation(t_mat4f * dst, t_vec3f * translate, t_vec3f * rot, t_vec3f * scale
291
292
293
         if ((dst = mat4f_identity(dst)) == NULL) {
294
              return (NULL);
295
296
         mat4f_translate3(dst, dst, translate);
298
         mat4f_rotateXYZ(dst, dst, rot);
```

```
299
                                mat4f_scale3(dst, dst, scale);
 300
                               return (dst);
 301
                }
 302
 303
                float mat4f_determinant(t_mat4f * mat) {
 304
 305
                               if (mat == NULL) {
 306
                                             return (0);
 307
 308
                               float d = 0;
 309
310
                                d += mat->m00 * ((mat->m11 * mat->m22 * mat->m33 + mat->m12 * mat->m23 * mat->m31 + mat->m13
                                              * mat->m21 * mat->m32)
                                               - mat->m13 * mat->m22 * mat->m31 - mat->m11 * mat->m23 * mat->m32 - mat->m12 * mat->m21 *
311
                                                             mat->m33);
312
                                d = mat > m01 * ((mat - m10 * mat - m22 * mat - m33 + mat - m12 * mat - m23 * mat - m30 + mat - m13)
                                              * mat->m20 * mat->m32)
- mat->m13 * mat->m22 * mat->m30 - mat->m10 * mat->m23 * mat->m32 - mat->m12 * mat->m20 *
313
                                                              mat->m33);
314
                                d += mat -> m02 * ((mat -> m10 * mat -> m21 * mat -> m33 + mat -> m11 * mat -> m23 * mat -> m30 + mat -> m13
                                              * mat->m20 * mat->m31)
315
                                               - mat->m13 * mat->m21 * mat->m30 - mat->m10 * mat->m23 * mat->m31 - mat->m11 * mat->m20 *
                                                             mat->m33);
316
                                d = mat - m03 * ((mat - m10 * mat - m21 * mat - m32 + mat - m11 * mat - m22 * mat - m30 + mat - m12
                                              * mat->m20 * mat->m31)
317
                                              - mat->m12 * mat->m21 * mat->m30 - mat->m10 * mat->m22 * mat->m31 - mat->m11 * mat->m20 *
                                                              mat ->m32);
 318
                                return (d);
                }
 319
320
321
                 static float _mat4f_determinant3x3(float t00, float t01, float t02, float t10, float t11, float
                              t12, float t20, float t21, float t22) {
return (t00 * (t11 * t22 - t12 * t21) + t01 * (t12 * t20 - t10 * t22) + t02 * (t10 * t21 -
322
                                             t11 * t20)):
 323
                }
 324
 325
                 t_mat4f * mat4f_invert(t_mat4f * dst, t_mat4f * src) {
 326
 327
                               float determinant = mat4f_determinant(src);
 328
 329
                                if (determinant != 0) {
 330
                                              if (dst == NULL) {
 331
                                                           if ((dst = mat4f new()) == NULL) {
 332
                                                                           return (NULL);
 333
                                                            }
 334
                                              }
 335
 336
                                              float determinant_inv = 1.0f / determinant;
 337
 338
                                              float t00 = _mat4f_determinant3x3(src->m11, src->m12, src->m13, src->m21, src->m22, src->
                                              m23, src->m31, src->m32, src->m33); float t01 = -_mat4f_determinant3x3(src->m10, src->m12, src->m13, src->m20, 
339
                                                            ->m23, src->m30, src->m32, src->m33);
340
                                              \label{eq:float_to_2} \texttt{float} \ \ \texttt{t02} \ = \ \_\texttt{mat4f\_determinant3x3(src->m10, src->m11, src->m13, src->m20, src->m21, sr
                                                           m23, src \rightarrow m30, src \rightarrow m31, src \rightarrow m33);
341
                                              ->m22, src->m30, src->m31, src->m32);
 342
343
                                              ->m23, src->m31, src->m32, src->m33);
float t11 = _mat4f_determinant3x3(src->m00, src->m02, src->m03, src->m20, src->m22, src->
 344
                                              m23, src->m30, src->m32, src->m33);
float t12 = -_mat4f_determinant3x3(src->m00, src->m01, src->m03, src->m20, src->m21, src
345
                                                            ->m23, src->m30, src->m31, src->m33);
                                              float t13 =
                                                                                           _mat4f_determinant3x3(src->m00, src->m01, src->m02, src->m20, src->m21, src->
346
                                                           m22, src \rightarrow m30, src \rightarrow m31, src \rightarrow m32);
 347
 348
                                              \label{eq:float_t20} \texttt{float} \ \ \texttt{t20} \ = \ \_\texttt{mat4f\_determinant3x3(src->m01, src->m02, src->m03, src->m11, src->m12, src
                                              m13, src->m31, src->m32, src->m33);
float t21 = -_mat4f_determinant3x3(src->m00, src->m02, src->m03, src->m10, src->m12, src
 349
                                                            ->m13, src->m30, src->m32, src->m33);
 350
                                              float t22 = _mat4f_determinant3x3(src->m00, src->m01, src->m03, src->m10, src->m11, src->
                                                           m13, src->m30, src->m31, src->m33);
 351
                                              ->m12, src->m30, src->m31, src->m32);
 352
                                              \label{eq:float_t30} \texttt{float} \ \texttt{t30} \ \texttt{=} \ \texttt{-}\_\texttt{mat4f\_determinant3x3} \\ (\texttt{src-} \texttt{m01}, \ \texttt{src-} \texttt{m02}, \ \texttt{src-} \texttt{m03}, \ \texttt{src-} \texttt{m11}, \ \texttt{src-} \texttt{m12}, \ \texttt{src-} \texttt{m12}, \ \texttt{src-} \texttt{m13}, \ \texttt{src-} \texttt{m14}, \ \texttt{
 353
                                              ->m13, src->m21, src->m22, src->m23);
float t31 = _mat4f_determinant3x3(src->m00, src->m02, src->m03, src->m10, src->m12, src->
 354
                                              m13, src->m20, src->m22, src->m23);
float t32 = -_mat4f_determinant3x3(src->m00, src->m01, src->m03, src->m10, src->m11, src
 355
                                                            ->m13, src->m20, src->m21, src->m23);
356
                                              float t33 = _mat4f_determinant3x3(src->m00, src->m01, src->m02, src->m10, src->m11, src->
                                                           m12, src \rightarrow m20, src \rightarrow m21, src \rightarrow m22);
 358
                                               // transpose and divide by the determinant
                                              dst->m00 = t00 * determinant_inv;
 359
```

```
360
             dst->m11 = t11 * determinant_inv;
             dst->m22 = t22 * determinant_inv;
361
362
             dst->m33 = t33 * determinant_inv;
363
             dst->m01 = t10 * determinant_inv;
364
             dst->m10 = t01 * determinant_inv;
365
             dst->m20 = t02 * determinant_inv;
366
             dst->m02 = t20 * determinant_inv;
             dst->m12 = t21 * determinant_inv;
367
             dst->m21 = t12 * determinant_inv;
368
             dst->m03 = t30 * determinant_inv;
369
             dst->m30 = t03 * determinant_inv;
370
371
             dst->m13 = t31 * determinant_inv;
372
             dst->m31 = t13
                            * determinant_inv;
373
             dst->m32 = t23 * determinant_inv;
374
             dst->m23 = t32 * determinant_inv;
375
             return (dst);
376
377
378
        return (NULL);
379
    }
380
381
    t_mat4f * mat4f_mult(t_mat4f * dst, t_mat4f * left, t_mat4f * right) {
382
383
         if (dst == NULL) {
384
             if ((dst = mat4f_new()) == NULL) {
385
                 return (NULL);
386
             }
387
        }
388
389
         float m00 = left->m00 * right->m00 + left->m10 * right->m01 + left->m20 * right->m02 + left->
            m30 * right -> m03;
390
         float m01 = left->m01 * right->m00 + left->m11 * right->m01 + left->m21 * right->m02 + left->
            m31 * right->m03;
391
         float m02 = left->m02 * right->m00 + left->m12 * right->m01 + left->m22 * right->m02 + left->
            m32 * right->m03;
392
         float m03 = left->m03 * right->m00 + left->m13 * right->m01 + left->m23 * right->m02 + left->
            m33 * right->m03;
393
         float m10 = left->m00 * right->m10 + left->m10 * right->m11 + left->m20 * right->m12 + left->
            m30 * right->m13;
394
         float m11 =
                     left->m01 * right->m10 + left->m11 * right->m11 + left->m21 * right->m12 + left->
            m31 * right->m13;
395
         float m12 = left->m02 * right->m10 + left->m12 * right->m11 + left->m22 * right->m12 + left->
            m32 * right->m13;
396
         float m13 = left->m03 * right->m10 + left->m13 * right->m11 + left->m23 * right->m12 + left->
             m33 * right -> m13;
397
         float m20 = left->m00 * right->m20 + left->m10 * right->m21 + left->m20 * right->m22 + left->
            m30 * right -> m23;
398
         float m21 = left->m01 * right->m20 + left->m11 * right->m21 + left->m21 * right->m22 + left->
            m31 * right->m23;
399
         float m22 = left->m02 * right->m20 + left->m12 * right->m21 + left->m22 * right->m22 + left->
            m32 * right->m23;
400
         float m23 = left->m03 * right->m20 + left->m13 * right->m21 + left->m23 * right->m22 + left->
            m33 * right -> m23;
401
         float m30 = left->m00 * right->m30 + left->m10 * right->m31 + left->m20 * right->m32 + left->
            m30 * right->m33;
402
         float m31 = left->m01 * right->m30 + left->m11 * right->m31 + left->m21 * right->m32 + left->
            m31 * right->m33;
403
         float m32 = left->m02 * right->m30 + left->m12 * right->m31 + left->m22 * right->m32 + left->
            m32 * right->m33;
404
         float m33 = left->m03 * right->m30 + left->m13 * right->m31 + left->m23 * right->m32 + left->
            m33 * right -> m33;
405
406
         dst \rightarrow m00 = m00;
407
         dst->m01 = m01;
408
         dst->m02 = m02;
409
         dst->m03 = m03;
410
         dst -> m10 = m10:
411
         dst -> m11 = m11;
412
         dst -> m12 = m12:
413
         dst -> m13 = m13;
         dst->m20 = m20;
414
         dst -> m21 = m21;
415
416
         dst->m22 = m22;
417
         dst->m23 =
                    m23;
418
         dst -> m30 = m30:
419
         dst -> m31 = m31;
420
         dst -> m32 = m32;
421
         dst -> m33 = m33;
422
423
        return (dst);
424
    }
425
426
    t_vec4f * mat4f_transform_vec4f(t_vec4f * dst, t_mat4f * left, t_vec4f * right) {
427
        if (dst == NULL) {
428
             if ((dst = vec4f_new()) == NULL) {
429
                 return (NULL);
430
```

```
431
432
          float x = left->m00 * right->x + left->m10 * right->y + left->m20 * right->z + left->m30 *
433
              right ->w;
434
          float y = left \rightarrow m01 * right \rightarrow x + left \rightarrow m11 * right \rightarrow y + left \rightarrow m21 * right \rightarrow z + left \rightarrow m31 *
              right ->w;
435
          float z = left \rightarrow m02 * right \rightarrow x + left \rightarrow m12 * right \rightarrow y + left \rightarrow m22 * right \rightarrow z + left \rightarrow m32 *
              right ->w;
          float w = left->m03 * right->x + left->m13 * right->y + left->m23 * right->z + left->m33 *
436
437
438
          dst \rightarrow x = x;
439
          dst -> y = y;
          dst \rightarrow z = z;
440
          dst -> w = w;
441
442
443
          return (dst);
444 }
445
446
     t_mat4f * mat4f_orthographic(t_mat4f * dst, float left, float right, float bot, float top, float
         near, float far)
447
          if (dst == NULL)
448
              if ((dst = mat4f_new()) == NULL) {
449
                   return (NULL);
450
          }
451
452
          dst \rightarrow m00 = 2.0f / (right - left);
453
          dst->m01 = 0;
454
455
          dst->m02 = 0;
456
          dst->m03 = (right + left) / (left - right);
457
458
          dst \rightarrow m10 = 0;
459
          dst -> m11 = 2.0f / (top - bot);
          dst \rightarrow m12 = 0;
460
461
          dst \rightarrow m13 = (top + bot) / (bot - top);
462
463
          dst->m20 = 0;
464
          dst -> m21 = 0;

dst -> m22 = 2 / (near - far);
465
466
          dst-m23 = (far + near) / (near - far);
467
468
          dst -> m30 = 0.0f;
469
          dst->m31 = 0.0f;
470
          dst -> m32 = 0.0f;
471
          dst -> m33 = 1.0f;
472
473
          return (dst);
474 }
475
     476
477
478
              if ((dst = mat4f_new()) == NULL) {
479
                   return (NULL);
              }
480
481
          }
482
          float y_scale = (float) (1.0f / tan(fov / 2.0f) * aspect);
483
          float x_scale = y_scale / aspect;
485
         float frustrum_length = far - near;
486
          dst->m00 = x_scale;
487
          dst -> m01 = 0.0f;
488
489
          dst -> m02 = 0.0f;
490
          dst \rightarrow m03 = 0.0f;
491
492
          dst->m10 = 0.0f;
          dst->m11 = y_scale;
493
494
          dst -> m12 = 0.0f;
495
          dst -> m13 = 0.0f;
496
497
          dst->m20 = 0.0f;
498
          dst->m21 = 0.0f;
499
          dst->m22 = -((far + near) / frustrum_length);
500
          dst -> m23 = -1.0f;
501
          dst->m30 = 0.0f;
502
          dst -> m31 = 0.0f;
503
          dst \rightarrow m32 = -((2.0f * near * far) / frustrum_length);
504
505
          dst -> m33 = 0.0f;
506
507
          return (dst);
508 }
509
     char * mat4f_str(t_mat4f * mat) {
   if (mat == NULL) {
510
511
              return (strdup("mat4f(NULL)"));
512
```

#### maths/srcs/vec2i.c

```
#include "vec2i.h"
3
   t_vec2i * vec2i_new(void) {
        return ((t_vec2i *)malloc(sizeof(t_vec2i)));
5
    void vec2i_delete(t_vec2i * vec) {
       free(vec);
10
    t_{vec2i} * vec2i_{zero}(t_{vec2i} * dst)  {
11
12
        if (dst == NULL) {
            if ((dst = vec2i_new()) == NULL) {
13
14
                 return (NULL);
             }
        memset(dst, 0, sizeof(t_vec2i));
        return (dst);
19 }
20
21
   t_vec2i * vec2i_set(t_vec2i * dst, int x, int y) {
22
23
        if (dst == NULL) {
             if ((dst = vec2i_new()) == NULL) {
24
                 return (NULL);
25
             }
27
        dst \rightarrow x = x;
        dst \rightarrow y = y;
28
29
        return (dst);
30 }
31
32
    t_vec2i * vec2i_set2(t_vec2i * dst, t_vec2i * vec) {
       if (dst == vec) {
34
             return (dst);
36
        return (vec2i_set(dst, vec->x, vec->y));
37
   }
38
39
    t_vec2i * vec2i_add(t_vec2i * dst, t_vec2i * left, t_vec2i * right) {
40
       if (dst == NULL) {
41
             if ((dst = vec2i
                                _new()) == NULL) {
42
                 return (NULL);
             }
43
        dst->x = left->x + right->x;
dst->y = left->y + right->y;
45
46
47
        return (dst);
48 }
49
50
    t_vec2i * vec2i_sub(t_vec2i * dst, t_vec2i * left, t_vec2i * right) {
       if (dst == \overline{NULL}) {
             if ((dst = vec2i_new()) == NULL) {
52
                  return (NULL);
53
54
55
        dst->x = left->x - right->x;
dst->y = left->y - right->y;
56
57
58
        return (dst);
59 }
61
   t_vec2i * vec2i_mult(t_vec2i * dst, t_vec2i * vec, int scalar) {
        if (dst == NULL) {
62
             if ((dst = vec2i_new()) == NULL) {
63
                  return (NULL);
64
             }
65
66
67
        dst \rightarrow x = vec \rightarrow x * scalar;
68
        dst \rightarrow y = vec \rightarrow y * scalar;
69
        return (dst);
   t_vec2i * vec2i_mult2(t_vec2i * dst, t_vec2i * left, t_vec2i * right) {
   if (dst == NULL) {
```

```
if ((dst = vec2i_new()) == NULL) {
    return (NULL);
74
75
76
77
 78
         dst \rightarrow x = left \rightarrow x * right \rightarrow x;
 79
         dst \rightarrow y = left \rightarrow y * right \rightarrow y;
         return (dst);
 81
    }
 82
    int vec2i_dot_product(t_vec2i * left, t_vec2i * right) {
 83
         return (left->x * right->x + left->y * right->y);
 84
 85
 86
    int vec2i_length_squared(t_vec2i * vec) {
         return (vec2i_dot_product(vec, vec));
 90
 91
    int vec2i_length(t_vec2i * vec) {
 92
         return ((int)sqrt(vec2i_length_squared(vec)));
 93
 94
 95
     t_vec2i * vec2i_normalize(t_vec2i * dst, t_vec2i * vec) {
         if (dst == NULL) {
98
              if ((dst = vec2i_new()) == NULL) {
99
                  return (NULL);
              }
100
         }
101
102
103
         int norm = 1 / vec2i_length(vec);
104
         dst \rightarrow x = vec \rightarrow x * norm;
         dst->y = vec->y * norm;
105
106
         return (dst);
107
108
109
     t_vec2i * vec2i_negate(t_vec2i * dst, t_vec2i * src) {
110
         if (dst == NULL) {
111
              if ((dst = vec2i_new()) == NULL) {
112
                  return (NULL);
113
              }
114
         dst->x = -src->x;
dst->y = -src->y;
115
116
         return (dst);
117
118 }
119
120
     int vec2i_angle(t_vec2i * left, t_vec2i * right) {
121
         int dls = vec2i_dot_product(left, right) / (vec2i_length(left) * vec2i_length(right));
122
         if (dls < -1.0f) {
123
              dls = -1.0f;
124
         } else if (dls > 1.0f) {
125
              dls = 1.0f;
126
127
         return ((int)acos(dls));
128 }
129
130 t_vec2i * vec2i_mix(t_vec2i * dst, t_vec2i * left, t_vec2i * right, int ratio) {
132
         if (dst == NULL) {
133
              if ((dst = vec2i_new()) == NULL) {
                  return (NULL);
134
135
         }
136
137
138
          dst \rightarrow x = left \rightarrow x * ratio + right \rightarrow x * (1 - ratio);
         dst->y = left->y * ratio + right->y * (1 - ratio);
139
140
         return (dst);
141
    }
142
143
    int vec2i_equals(t_vec2i * left, t_vec2i * right) {
144
         return (left == right || (left->x == right->x && left->y == right->y));
145
146
147
     char * vec2i_str(t_vec2i * vec) {
148
        if (vec == NULL) {
              return (strdup("vec2i(NULL)"));
150
         char buffer[128];
---in+f(buffer, "vec2i(%d; %d)", vec->x, vec->y);
151
152
         return (strdup(buffer));
153
    }
154
```

```
#include "vec3f.h"
   t_vec3f * vec3f_new(void) {
         return ((t_vec3f *)malloc(sizeof(t_vec3f)));
    void vec3f_delete(t_vec3f * vec) {
8
         free(vec);
10
11
    t_vec3f * vec3f_zero(t_vec3f * dst) {
12
         if (dst == NULL) {
13
              if ((dst = vec3f_new()) == NULL) {
14
                   return (NULL);
15
16
         memset(dst, 0, sizeof(t_vec3f));
17
18
         return (dst);
    }
19
20
21
    t_vec3f * vec3f_set(t_vec3f * dst, float x, float y, float z) {
         if (dst == NULL) {
              if ((dst = vec3f_new()) == NULL) {
24
                   return (NULL);
25
              }
26
27
28
         }
         dst \rightarrow x = x;
         dst -> y = y;
29
         dst \rightarrow z = z;
         return (dst);
31
   }
32
33
    t_{vec3f} * vec3f_{set3}(t_{vec3f} * dst, t_{vec3f} * vec) {
34
        if (dst == vec) {
35
              return (dst);
36
37
         return (vec3f_set(dst, vec->x, vec->y, vec->z));
38
40
    t_vec3f * vec3f_add(t_vec3f * dst, t_vec3f * left, t_vec3f * right) {
        if (dst == NULL) {
41
              if ((dst = vec3f_new()) == NULL) {
42
43
                   return (NULL);
              }
44
45
46
         dst \rightarrow x = left \rightarrow x + right \rightarrow x;
47
         dst \rightarrow y = left \rightarrow y + right \rightarrow y;
         dst \rightarrow z = left \rightarrow z + right \rightarrow z;
         return (dst);
50 }
51
   t_vec3f * vec3f_sub(t_vec3f * dst, t_vec3f * left, t_vec3f * right) {
   if (dst == NULL) {
52
53
54
              if ((dst = vec3f_new()) == NULL) {
                   return (NULL);
              }
57
         dst->x = left->x - right->x;
dst->y = left->y - right->y;
58
         dst->z = left->z - right->z;
60
61
         return (dst);
62 }
63
    t_vec3f * vec3f_mult(t_vec3f * dst, t_vec3f * vec, float scalar) {
        if (dst == NULL) {
              if ((dst = vec3f_new()) == NULL) {
66
67
                   return (NULL);
68
69
70
         dst->x = vec->x * scalar;
71
72
         dst \rightarrow y = vec \rightarrow y * scalar;
         dst \rightarrow z = vec \rightarrow z * scalar;
73
         return (dst);
74
76
77
    t_vec3f * vec3f_mult3(t_vec3f * dst, t_vec3f * left, t_vec3f * right) {
         if (dst == NULL) {
              if ((dst = vec3f_new()) == NULL) {
    return (NULL);
78
79
              }
80
81
         dst \rightarrow x = left \rightarrow x * right \rightarrow x;
         dst \rightarrow y = left \rightarrow y * right \rightarrow y;
         dst->z = left->z * right->z;
85
         return (dst);
86 }
```

```
88
     /** cross product */
     t_{ec3f} * vec3f_{ec3f} * vec3f_{ec3f} * dst, t_{ec3f} * left, t_{ec3f} * right) {
 29
 90
          if (dst == NULL) {
              if ((dst = vec3f_new()) == NULL) {
                   return (NULL);
 94
          }
 95
          dst->x = left->y * right->z - left->z * right->y;
dst->y = left->z * right->x - left->x * right->z;
 96
 97
          dst->z = left->x * right->y - left->y * right->x;
 98
 99
          return (dst);
100 }
    float vec3f_dot_product(t_vec3f * left, t_vec3f * right) {
    return (left->x * right->x + left->y * right->y + left->z * right->z);
102
103
104
105
106
     float vec3f_length_squared(t_vec3f * vec) {
107
         return (vec3f_dot_product(vec, vec));
108
109
110
    float vec3f_length(t_vec3f * vec) {
111
          return ((float)sqrt(vec3f_length_squared(vec)));
112
113
     t_vec3f * vec3f_normalize(t_vec3f * dst, t_vec3f * vec) {
114
115
116
          if (dst == NULL) {
117
              if ((dst = vec3f_new()) == NULL) {
118
                   return (NULL);
119
120
121
          float norm = 1 / vec3f_length(vec);
122
123
          dst \rightarrow x = vec \rightarrow x * norm;
124
          dst->y = vec->y * norm;
125
          dst -> z = vec -> z * norm;
126
          return (dst);
127
128
129
     t_vec3f * vec3f_negate(t_vec3f * dst, t_vec3f * src) {
          if (dst == NULL) {
130
              if ((dst = vec3f_new()) == NULL) {
131
132
                   return (NULL);
133
               }
134
135
          dst -> x = -src -> x;

dst -> y = -src -> y;
136
          dst \rightarrow z = -src \rightarrow z;
137
138
          return (dst);
139
     }
140
     float vec3f_angle(t_vec3f * left, t_vec3f * right) {
141
142
          float dls = vec3f_dot_product(left, right) / (vec3f_length(left) * vec3f_length(right));
143
          if (dls < -1.0f) {
              dls = -1.0f;
          } else if (dls > 1.0f) {
146
               dls = 1.0f;
147
148
          return ((float)acos(dls));
149
150
151
     t_vec3f * vec3f_mix(t_vec3f * dst, t_vec3f * left, t_vec3f * right, float ratio) {
152
153
          if (dst == NULL) {
154
               if ((dst = vec3f_new()) == NULL) {
155
                   return (NULL);
156
               }
          }
157
158
          dst->x = left->x * ratio + right->x * (1 - ratio); 
 <math>dst->y = left->y * ratio + right->y * (1 - ratio);
159
160
161
          dst \rightarrow z = left \rightarrow z * ratio + right \rightarrow z * (1 - ratio);
162
          return (dst);
163
164
     int vec3f_equals(t_vec3f * left, t_vec3f * right) {
165
166
          return (left == right || (left->x == right->x && left->y == right->y && left->z == right->z))
167
168
169
     char * vec3f_str(t_vec3f * vec) {
170
         if (vec == NULL) {
171
               return (strdup("vec3f(NULL)"));
172
```

```
char buffer[160];
sprintf(buffer, "vec3f(%f; %f; %f)", vec->x, vec->y, vec->z);
return (strdup(buffer));
176 }
```

### 3 Listes et table de hashage

### data\_structures/includes/array\_list.h

```
#ifndef ARRAY_LIST_H
    # define ARRAY_LIST_H
   # include "common.h"
   # include <string.h>
   # include <stdlib.h>
    # include <stdio.h>
8
9
    typedef struct s_array_list {
10
        char
11
        unsigned long int
                              capacity;
12
        unsigned long int
                              size;
13
        unsigned int
                              elem_size;
        unsigned int
                              default_capacity;
15
                     t_array_list;
16
17
18
    * Create a new array list
    * nb : number of elements which the array can hold on first allocation
19
20
    * elem_size : size of an elements
21
22
    * e.g: t_array_list array = array_list_new(16, sizeof(int));
23
   t_array_list * array_list_new(unsigned long int nb, unsigned int elem_size);
25
26
    /** Add an element at the end of the list */
27
    int array_list_add(t_array_list * array, void * data);
    /** Clear the list (remove every data, and resize it to the default capacity) */
30
    void array_list_clear(t_array_list * array);
33
       Delete DEFINETELY the list from memory
34
    */
35
    void array_list_delete(t_array_list * array);
36
37
    /** remove the element at given index */
    void array_list_remove(t_array_list * array, unsigned int idx);
39
    * Sort the array list using std quicksort algorythm
41
42
                t_array_list array = array_list_new(16, sizeof(char) * 2);
array_list_push(&array, "d");
array_list_push(&array, "a");
array_list_push(&array, "f");
43
44
45
46
47
48
                 array_list_sort(&array, (t_cmp_function)strcmp);
   void array_list_sort(t_array_list * array, t_cmp_function cmpf);
50
51
    /**
52
53
    * Add every elements the end of the list
54
        this function is faster than calling multiples 'array_list_add()'
55
        so consider using it :)
    void array_list_add_all(t_array_list * array, void * buffer, unsigned long int nb);
59
60
    * Get raw data of your array list
        (buffer of every data)
You should really not use this function
61
62
63
64
   void * array_list_raw(t_array_list * array);
    /** get item by index */
    void * array_list_get(t_array_list * array, unsigned int idx);
68
69
70
    * Iterate on the array list using a macro
71
72
73
     * i.e :
                t_array_list array;
```

```
74
75
                  [...] //push strings to the list
76
77
                  // print every string which the array list holds
                  ARRAY_LIST_ITER_START(array, char *, str, i)
                      puts(str);
81
                  ARRAY_LIST_ITER_END(array, char *, str, i);
82
83
   # define ARRAY_LIST_ITER_START(L, T, X, I)\
84
85
         unsigned long int I = 0;\
        while (I < (L)->size) {\
    T X = ((T)(L)->data) + I;
86
    # define ARRAY_LIST_ITER_END(L, T, X, I) \
           ++I;\
90
91
    }
92
93
    #endif
```

### data\_structures/includes/common.h

```
#ifndef COMMON_H
    # define COMMON_H
    # include <sys/time.h>
    # include <stdlib.h>
    # include <string.h>
    # include <stdio.h>
 8
    typedef void (*t_function)();
typedef int (*t_cmp_function) (void const * a, void const * b);
10
11
    typedef unsigned long int (*t_hash_function) (void const * v);
12
13
    typedef t_function t_f;
    typedef t_cmp_function t_cmpf;
typedef t_hash_function t_hf;
16
17
    # define MICROSEC(V)
18
         struct timeval tv; \setminus
19
20
         gettimeofday(&tv, NULL);\
21
22
          = 1000000 * tv.tv_sec + tv.tv_usec;\
23
24
    #endif
```

## data\_structures/includes/hmap.h

```
#ifndef HMAP_H
    # define HMAP H
 3
    # include "common.h"
    # include "linked_list.h"
 6
 8
        Generic hash map implementation in C89:
 9
10
         ABOUT THE IMPLEMENTATION:
                given pointer address are saved for values. No copy their data are done. (same for keys
11
12
              - const where used where on constant data (well...), so you dont mess up the hash map :)
              - an array of linked list is used to handle collisions
13
14
15
         example for a string hashmap:
              t_hmap map = hmap_new(1024, (t_hf)strhash, (t_cmpf)strcmp);
hmap_insert(&map, strdup("hello world"), strdup("im a key"), strlen("Hello world") + 1);
char *helloworld = hmap_get(&map, "im a key"); //now contains "Hello world"
18
19
20
21
22
23
24
25
    typedef struct s_hmap_node {
         unsigned long int const hash; //hash of the key
         void const * data; //the data holds
         void const * key; //the key used
                        t_hmap_node;
```

```
typedef struct
                      s_hmap {
30
         t_list * values; //a buffer of value holders (to handle collision)
31
         unsigned long int capacity; //number of lists
32
         unsigned long int size; //number of value set
         t_hash_function hashf; //hash function
t_cmp_function keycmpf; //key comparison function, where node keys are sent as parameters
t_function datafreef; //function call when a data object should be freed
t_function keyfreef; //function called when a key should be freed
33
34
36
37
    }
                      t_hmap;
38
39
40
        Create a new hashmap:
41
         capacity : capacity of the hashmap (number of lists boxes in memory)
43
                   : hash function to use on inserted elements
44
                   : comparison function to use when searching a data
         cmpf
45
46
    t_hmap * hmap_new(unsigned long int const capacity, t_hash_function hashf, t_cmp_function keycmpf
         , t_function keyfreef, t_function datafreef);
47
48
49
         Delete the hashmap from the heap
50
51
         hmap : hash map
         datafreef : function which will be called on node data before the node being freed.
52
53
                               'NULL' if data shouldnt be free, 'free' if the data was allocated with a
                      i.e :
          malloc.
54
                               'myfree' if this is structure which contains multiple allocated fields
55
         keyfreef : same for the node key
56
      */
57
    void hmap_delete(t_hmap * hmap);
59
60
     * Insert a value into the hashmap:
61
62
        map : hmap
63
         data : value to insert
64
              : key reference for this data
65
         size : size of the data (i.e, 'sizeof(t_data_structure)', 'strlen(str) + 1')
67
        return the given data if it was inserted properly, NULL elseway
68
69
    void const * hmap_insert(t_hmap * hmap, void const * data, void const * key);
70
71
72
        Get data from the hashmap
73
74
         hmap : hash map
75
         key : the node's key to find
76
77
     */
    void * hmap_get(t_hmap * hmap, void const * key);
78
79
80
     * Remove the data pointer from the hash map
         return 1 if the element was removed, 0 elseway
81
     *
82
         hmap : the hash map
83
         data : pointer to the data
85
    int hmap_remove_data(t_hmap * hmap, void const * data);
86
87
88
     * Remove the data which match with the given key from the hash map
89
     * return 1 if the element was removed, 0 elseway
90
91
         hmap : the hash map
92
         key : pointer to the key
93
94
    int hmap_remove_key(t_hmap * hmap, void const * key);
95
96
97
     * Some simple builtin hashes functions, useful for tests.
98
99
         String hash is based on : http://www.cse.yorku.ca/~oz/hash.html
100
101
    unsigned long int strhash(char const * str);
    unsigned long int inthash(int const value);
102
103
104
105
     * Macro to iterate fastly though to hash map
106
107
108
             HMAP_ITER_START(hmap, char *, str) {
109
                  puts(str);
110
111
             HMAP_ITER_END(hmap, char *, str)
112
```

```
113
     # define HMAP_ITER_START(H, T, V)\
114
115
          unsigned long int i = 0;
116
          while (i < (H)->capacity) {\
117
              t_list * lst = (H) ->values + i;\
              if (lst != NULL && lst->head != NULL) {\
                   LIST_ITER_START(lst, t_hmap_node *, node) {\
    T V = (T)(node->data);
119
120
     # define {\tt HMAP\_ITER\_END(H, T, V)}
121
122
                   }\
                   LIST_ITER_END(lst, t_hmap_node *, node)\
123
124
              }\
125
               ++i;\
128
     #endif
```

# $data\_structures/includes/linked\_list.h$

```
#ifndef LINKED LIST H
   # define LINKED LIST H
3
4
   # include <stdlib.h>
5
   # include <string.h>
   # include <unistd.h>
   # include "common.h
   typedef struct s_list_node {
       struct s_list_node * next;
10
        struct s_list_node * prev;
11
12
                   t_list_node;
13
14
   typedef struct s_list {
                            * head;
       t_list_node
16
       unsigned long int
                            size;
17
                    t_list;
18
   /** initialize the given list */
19
20
   int list_init(t_list * list);
21
22
   /** Create a new linked list */
23
   t_list * list_new(void);
24
25
   /** Add an element at the end of the list */
   void * list_add(t_list * lst, void const * content, unsigned int content_size);
28
   /** Add an element in head of the list */
29
   void * list_addfront(t_list * lst, void const * content, unsigned int content_size);
30
31
32
    * Return the list node data which match with the given comparison function
33
       and reference data. (cmpf should acts like 'strcmp()')
34
   void * list_get(t_list * lst, t_cmp_function cmpf, void * cmpd);
36
37
    st Remove the node which datas match with the given comparison function
38
39
    * and the given data reference
40
41
   int list_remove(t_list * lst, t_cmp_function cmpf, void * cmpref);
   /** remove the given node from the list */
   void list_remove_node(t_list * lst, t_list_node *node);
45
   /** Remove first / last element of the list. Return 1 if it was removed, 0 else */
46
47
   int list_remove_first(t_list * lst);
48
   int list_remove_last(t_list * lst);
49
50
   /** Remove the first element of the list, and return it data */
   void * list_pop(t_list * lst);
53
   /** Return the first element of the list */
54
   void * list_head(t_list * lst);
55
   /** Clear the list (remove every node) */
57
   void list_clear(t_list * lst);
59
   /** remove the list for the heap */
   void list_delete(t_list * lst);
   /** iterate the function to every node content of the list */
63
   void list_iterate(t_list * lst, t_function f);
```

```
/** Return a buffer which holds pointers to every elements of the list, allocated with 'malloc()'
66
67
    void * list_buffer(t_list * lst);
   /** iterate on the list using a macro (optimized) */
71
72
   # define LIST_ITER_START(L, T, V)\
    {\
73
74
        if (L != NULL && L->head != NULL) {\
             t_list_node *__node = L->head->next;\
while (__node != L->head) {\
    T V = (T)(__node + 1);
75
    77
78
80
        }\
81
   }
82
83
    #endif
```

### data\_structures/srcs/array\_list.c

```
#include "array_list.h"
    t_array_list * array_list_new(unsigned long int nb, unsigned int elem_size) {
    t_array_list * array = (t_array_list *)malloc(sizeof(t_array_list));
    if (array == NULL) {
 6
             return (NULL);
 8
 9
         array->data = calloc(nb, elem_size);
10
         array->capacity = nb;
11
         array->elem_size = elem_size;
12
         array->size = 0;
13
         array->default_capacity = nb;
         return (array);
15
16
17
    static void array_list_resize(t_array_list * array, unsigned size) {
18
         array->data = realloc(array->data, size * array->elem_size);
19
         array->capacity = size;
20
21
22
23
         if (array->size > size) {
             array->size = size;
    }
24
25
    static void array_list_expand(t_array_list * array) {
26
27
28
29
30
         unsigned long int size = array->capacity * 2;
         array_list_resize(array, size);
    int array_list_add(t_array_list * array, void * data) {
    if (array->size == array->capacity) {
31
             array_list_expand(array);
33
34
         memcpy(array->data + array->size * array->elem_size, data, array->elem_size);
35
         array->size++;
36
         return (array->size);
37
    }
38
    void array_list_add_all(t_array_list * array, void * buffer, unsigned long int nb) {
         unsigned int array_idx = array->size * array->elem_size;
40
41
         while (nb) {
             unsigned int copy_nb = array->capacity - array->size;
if (copy_nb > nb) {
42
43
44
                  copy_nb = nb;
45
46
             if (copy_nb == 0) {
47
                  array_list_expand(array);
48
49
             unsigned int copy_size = copy_nb * array->elem_size;
50
51
52
             memcpy(array->data + array_idx, buffer, copy_size);
             nb -= copy_nb;
53
             array->size += copy_nb;
54
             buffer += copy_size;
             array_idx += copy_size;
    }
    void * array_list_get(t_array_list * array, unsigned int idx) {
60
         return (array->data + idx * array->elem_size);
61
```

```
63
    void array_list_remove(t_array_list * array, unsigned int idx) {
64
        if (array->size == 0 || idx >= array->size) {
65
             return ;
        unsigned int begin = idx * array->elem_size;
unsigned int end = (array->size - 1) * array->elem_size;
69
70
        memmove(array->data + begin, array->data + begin + array->elem_size, end - begin);
71
72
73
74
        array->size--;
   }
75
    void array_list_clear(t_array_list * array) {
76
77
        array - size = 0;
        array_list_resize(array, array->default_capacity);
78
79
80
    void array_list_delete(t_array_list * array) {
81
        free(array->data);
82
83
    void array_list_sort(t_array_list * array, t_cmp_function cmpf) {
85
        qsort(array->data, array->size, array->elem_size, cmpf);
86
87
88
    void * array_list_raw(t_array_list * array) {
89
        return (array->data);
    }
90
```

### data\_structures/srcs/hmap.c

```
#include "hmap.h"
    t_hmap * hmap_new(unsigned long int const capacity,
             t_hash_function hashf, t_cmp_function keycmpf,
t_function keyfreef, t_function datafreef) {
6
7
8
9
         // set the hmap capacity to the closest power of two
         unsigned long int c = 1;
         while (c < capacity) {</pre>
10
             c = c << 1;
11
12
13
        unsigned long int size = sizeof(t_list) * c;
14
        void * values = malloc(size);
15
        if (values == NULL) {
16
             return (NULL);
17
18
        memset(values, 0, size);
19
20
21
22
         t_hmap * hmap = (t_hmap *)malloc(sizeof(t_hmap));
        if (hmap == NULL) {
             free(values);
             return (NULL);
24
25
26
27
28
29
30
        hmap->values = values;
        hmap->capacity = capacity;
        hmap \rightarrow size = 0;
        hmap->hashf = hashf;
        hmap->keycmpf = keycmpf;
31
        hmap -> datafreef = datafreef;
32
        hmap->keyfreef = keyfreef;
33
34
        return (hmap);
35
36
   }
37
    void hmap_delete(t_hmap * hmap) {
38
         unsigned long int i = 0;
         while (i < hmap->capacity) {
40
             t_list * lst = hmap->values + i;
             //if the list has been initialized
41
42
             if (lst->head) {
43
                  LIST_ITER_START(lst, t_hmap_node *, node) {
44
                      if (hmap->datafreef) {
45
                           hmap -> datafreef (node -> data);
46
47
                      if (hmap->keyfreef) {
                           hmap -> keyfreef (node -> key);
51
                  LIST_ITER_END(lst, t_hmap_node *, node)
```

```
list_delete(lst);
 54
               }
               ++i:
 55
 56
 57
     }
     void const * hmap_insert(t_hmap * hmap, void const * data, void const * key)
 60
          unsigned long int hash = hmap->hashf(key); //get the hash for this key
 61
          unsigned long int addr = hash & (hmap->capacity - 1); //get the array list from the hash
 62
 63
 64
          t_hmap_node node = {hash, data, key}; //set the node buffer
 65
          t_list * lst = hmap->values + addr; //get the list from it address
 67
          /\bar{/}if the list hasnt already been initialized
 68
          if (lst->head == NULL) {
 69
               list_init(lst); //initialize it
 70
71
72
73
74
75
          list_add(lst, &node, sizeof(t_hmap_node)); //add the node to the list
          hmap -> size ++;
          return (data); //return the data
76
77
     void * hmap_get(t_hmap * hmap, void const * key) {
78
79
          unsigned long int hash = hmap->hashf(key); //get the hash for this key unsigned long int addr = hash & (hmap->capacity - 1); //get the lst list from the hash
 80
          t_list * lst = hmap->values + addr; //list of collision for this key hash
 81
 82
 83
          if (lst->size == 0) {
 84
              return (NULL);
 85
 86
          //so compare the exact key to find the wanted data
LIST_ITER_START(lst, t_hmap_node *, node) {
   if (hmap->keycmpf(key, node->key) == 0) {
 87
 88
 29
 90
                   return ((void *)node->data);
 91
 92
 93
          LIST_ITER_END(lst, t_hmap_node *, node)
 94
          return (NULL);
 95
     }
96
97
     int hmap_remove_data(t_hmap * hmap, void const * data) {
98
          unsigned long int i = 0;
99
          while (i < hmap->capacity) {
100
               t_list * lst = hmap->values + i;
               LIST_ITER_START(lst, t_hmap_node *, node) {
   if (node->data == data) {
101
102
                         //__node is the current LIST_ITER_START node of the linked list
103
104
                        list_remove_node(lst, __node);
105
                        hmap->size--;
106
107
                        if (hmap->datafreef) {
108
                             hmap->datafreef(node->key);
109
110
111
                        if (hmap->keyfreef) {
112
                             hmap -> keyfreef (node -> key);
113
114
115
                        return (1);
116
                   }
117
118
               LIST_ITER_END(array, t_hmap_node *, node)
119
               ++i;
120
          return (0);
121
122
     }
123
     int hmap_remove_key(t_hmap * hmap, void const * key) {
   unsigned long int hash = hmap->hashf(key); //get the hash for this key
124
125
126
          unsigned long int addr = hash & (hmap->capacity - 1); //get the array list from the hash
127
128
          t_list * lst = hmap->values + addr; //lst of collision for this key hash
129
130
          if (lst->size == 0) {
131
              return (0);
132
133
134
          //so compare the exact key to find the wanted data
135
          LIST_ITER_START(lst, t_hmap_node *, node) {
               if (hmap->keycmpf(key, node->key) == 0) {
   //_node is the current LIST_ITER_START node of the linked list
   list_remove_node(lst, __node);
136
137
138
139
                   hmap->size--;
```

```
140
141
                   if (hmap->datafreef) {
142
                       hmap -> datafreef (node -> key);
143
144
                   if (hmap->keyfreef) {
                       hmap -> keyfreef (node -> key);
147
148
149
                   return (1);
              }
150
151
152
         LIST_ITER_END(array, t_hmap_node *, node)
153
         return (0);
154
155
    unsigned long int strhash(char const * str) {
   if (str == NULL) {
156
157
              return (0);
158
159
160
161
          unsigned long int hash = 5381;
162
         int c;
while ((c = *str) != '\0') {
163
164
              hash = ((hash << 5) + hash) + c;
165
              str++;
166
         return (hash);
167
168
169
170
     unsigned long int inthash(int const value) {
171
         return (value);
172
```

### data\_structures/srcs/linked\_list.c

```
#include "linked_list.h"
    int list_init(t_list * list) {
    list->head = (t_list_node*)malloc(sizeof(t_list_node));
3
4
5
6
7
        if (list->head == NULL) {
             return (0);
8
        list->head->next = list->head;
9
        list->head->prev = list->head;
        list->size = 0;
11
        return (1);
12
   }
13
14
15
     * Create a new linked list
17
    t_list * list_new(void) {
        t_list * list = (t_list *) malloc(sizeof(t_list));
        if (list == NULL) {
19
20
21
             return (NULL);
22
23
24
25
26
        if (!list_init(list)) {
             free(list);
             return (NULL);
27
        return (list);
29
30
   }
31
32
        Add an element at the end of the list
33
    void * list_add(t_list * lst, void const *content, unsigned int content_size)
36
        t_list_node *node = (t_list_node*)malloc(sizeof(t_list_node) + content_size);
37
        if (node == NULL) {
38
             return (NULL);
39
40
        memcpy(node + 1, content, content_size);
41
42
        t_list_node *tmp = lst->head->prev;
43
        lst->head->prev = node;
45
        tmp->next = node;
46
        node->prev = tmp;
node->next = lst->head;
47
48
```

```
49
50
         lst->size++;
 51
52
         return (node + 1);
53
    }
 55
 56
     * Add an element in head of the list
 57
    void * list_addfront(t_list * lst, void const *content, unsigned int content_size) {
 58
         t_list_node * node = (t_list_node *) malloc(sizeof(t_list_node) + content_size);
if (node == NULL) {
 59
 60
 61
             return (NULL);
 62
 63
         memcpy(node + 1, content, content_size);
 64
 65
         t_list_node *tmp = lst->head->next;
 66
 67
         lst->head->next = node;
 68
         tmp->prev = node;
 69
70
71
72
73
         node->prev = lst->head;
         node->next = tmp;
         lst->size++;
74
75
76
77
78
         return (node + 1);
    }
    /**
 79
        remove the given node from the list
 80
 81
    void list_remove_node(t_list * lst, t_list_node *node) {
 82
         if (node->prev) {
             node->prev->next = node->next;
 83
 84
         if (node->next) {
 85
86
             node->next->prev = node->prev;
 87
 88
 89
         node -> next = NULL;
 90
         node->prev = NULL;
 91
         free(node):
92
         lst->size--;
93
    }
 94
 95
     * Remove first / last element of the list. Return 1 if it was removed, 0 else
97
    int list_remove_first(t_list * lst) {
99
         if (lst->size == 0) {
100
             return (0);
101
102
         list_remove_node(lst, lst->head->next);
103
         return (1);
104
    }
105
106
    int list_remove_last(t_list * lst) {
107
         if (1st -> size == 0) {
108
             return (0);
109
110
         list_remove_node(lst, lst->head->prev);
111
         return (1);
112
    }
113
114
115
        remove list head
116
    void * list_pop(t_list * lst) {
   if (lst->size == 0) {
117
118
             return (NULL);
119
120
121
122
         void * data = lst->head->next + 1;
123
         if (lst->size > 0)
124
125
             list_remove_first(lst);
126
127
         return (data);
128
    }
129
130
     /** return content at the begining of the list */
131
     void * list_head(t_list * lst) {
132
         if (lst->size > 0) {
133
             return ((void*)lst->head->next + 1);
134
135
         return (NULL);
```

```
136 }
137
138
139
     /** remove if the comparison return elements are equals (works like strcmp) */
140
    int list_remove(t_list * lst, t_cmp_function cmpf, void * cmpd) {
         t_list_node *node;
142
143
         node = lst->head->next;
         while (node != lst->head) {
144
145
              if (cmpf(node + 1, cmpd) == 0) {
146
                  list_remove_node(lst, node);
147
                  return (1);
148
149
              node = node->next;
150
151
         return (0);
152
    }
153
154
     /**
155
        Return the list node data which match with the given comparison function
156
         and reference data. (cmpf should acts like 'strcmp()')
157
     void * list_get(t_list * lst, t_cmp_function cmpf, void * cmpd) {
   if (lst->size == 0) {
158
159
160
              return (NULL);
161
162
         if (cmpf(lst->head + 1, cmpf) == 0) {
163
164
              return (lst->head);
165
166
167
         t_list_node *node = lst->head->next;
168
         while (node != lst->head) {
169
              if (cmpf(node + 1, cmpd) == 0) {
170
                  return (node + 1);
171
172
              node = node->next;
173
174
175
         return (NULL);
176
    }
177
178
179
      * Remove the node which datas match with the given comparison function
180
     * and the given data reference
     */
181
182
     void list_delete(t_list * lst) {
183
         if (lst->size == 0) {
184
              goto end;
185
186
187
         list_clear(lst);
188
189
     end:
         lst->head = NULL;
190
191
         lst->size = 0;
192
     }
193
194
195
     * clear the list : remove every nodes */
196
197
    void list_clear(t_list * lst) {
198
199
         t_list_node * node = lst->head->next;
200
         while (node != lst->head) {
201
              t_list_node *next = node->next;
202
              free(node);
203
              node = next;
204
205
206
         free(lst->head);
207
         list_init(lst);
208
    }
209
210
211
      * Return a buffer which holds pointers to every elements of the list, allocated with 'malloc()'
212
    void * list_buffer(t_list * lst) {
   void ** buffer = (void**)malloc(sizeof(void*) * (lst->size + 1));
   if (buffer == NULL) {
      return (NULL);
   }
}
213
214
215
216
217
218
219
         t_list_node *node = lst->head->next;
220
         unsigned int i = 0;
221
         while (node != lst->head) {
222
```

## 4 Feuille de calcul Python

### python/lagrange.py

```
import numpy as np
    import matplotlib.pyplot as plt
 2
    import math
    n = 1000
   a = -1
b = 1
 8
    h = (b - a) / float(n)
 9
10
        = [a + i * h for i in range(0, n)]
    dy = [math.acos(xi) - ((-0.69813170079773212 * xi * xi - 0.87266462599716477) * xi + 1.5707963267948966) for xi in x]
11
        = [math.acos(xi) for xi in x]
        = [(-0.69813170079773212 * xi * xi - 0.87266462599716477) * xi + 1.5707963267948966 for xi in
13
         x]
14
15
    plt.plot(x, dy, label="dy")
    plt.plot(x, y1, label="acos")
plt.plot(x, y2, label="acos Lagrange")
16
17
18
19
    plt.show()
```

### python/memory.py

```
import numpy as np
    import matplotlib.pyplot as plt
 3
    Ko = 1 / 1024.0;
    Mo = 1 / (1024.0 * 1024.0);
    nmin = 4
    nmax = 32 # nombre de point a calculer
    SUB = 16.0 # nombre de points par subdivision de terrain
10
    # nombre de points total sur la carte
11
    def N(n):
         return (n * n)
13
    # nombre de triangle total sur la carte
15
    def T(n):
         return (2 * (n - 1) * (n - 1))
16
17
18
    # nombre d'indice pour relie les triangles
19
    def I(n):
20
         return (3 * T(n))
    def M1(n):
23
24
         return (I(n) * 28)
25
26
27
    def M2(n):
         return (N(n) * 28 + 2 * I(n))
28
    def M3(n):
29
         return (N(n) * 16 + n / SUB * (16 * 4 + 2 * 4) + I(SUB))
30
31
              = [n for n in range(nmin, nmax)]
         = [M1(n) * Mo for n in x]
= [M2(n) * Mo for n in x]
32
33
    yM1
    yM2
          = [M3(n) * Mo for n in x]
    уМЗ
35
    rM1 = [M1(n) / T(n) for n in x]
rM2 = [M2(n) / T(n) for n in x]
rM3 = [M3(n) / T(n) for n in x]
    #plt.plot(x, yM1, label="M1(n)")
    #plt.plot(x, yM2, label="M2(n)")
#plt.plot(x, yM3, label="M3(n)")
41
42
43
    plt.plot(x, rM1, label="M1(n) / T(n)")
    plt.plot(x, rM2, label="M2(n) / T(n)")
plt.plot(x, rM3, label="M3(n) / T(n)")
    plt.legend()
    plt.show()
```