Write You Some Proofs for Great Good

https://github.com/rpeszek/present-proofs-lc19

https://github.com/rpeszek/present-proofs-lc19/blob/master/doc/slides.pdf

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Why proofs?

- Curry Howard (Why proofs == Why programs)*
- Formal verification
- Enable `Type Precision` (focus of this talk)

```
data List a =

Empty
| Cons a (List a)

Cons a (List a)

| Cons a (List a)

| Cons a (List a)

| Cons a (List a)
```

Plan for this talk

- Narrow scoped, pragmatic intro to proofs with dependent types
- Focus on what can be done vs how
- Anything wrong with List?
- Anything wrong with Maybe?
- Anything wrong with Bool?
- Q: Proofs and software engineering together?
- Performance; Termination / Totality; Maintenance; ...

Proofs by who writes them

	Programmers *	Automated Logic Solvers
Work		Free Lunch!
What can be done	A Lot	Limitted
Examples	Dependently Typed Languages	Refinement Types LiquidHaskell
	(focus of this talk)	

Motivation (call-side safety)

```
(!!) :: [a] -> Int -> a
```

```
safeGet :: [a] -> Int -> Maybe a
-- Liquid:
{-@ (!!) :: x: [a] -> {i:Nat | i < len x} -> a @-}
(!!) :: [a] -> Int -> a
-- Dep Typed:
(!!) :: Vect n a -> Fin n -> a
(!!!):: Vect n a -> SNat m -> MaybeB (m < n) a
(!!!!): (n:Nat) -> (xs:List a) -> {auto ok: InBounds n xs} -> a
```

- Questionable improvement
- Refinements

Precise types (talk focus)

... and much more

https://github.com/rpeszek/present-proofs-lc19/tree/master/src/Motivation

Motivation (implementation safety)

(code)

Intro

(code) Curry-Howard vs Imperative

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/AnIntro.hs

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/MaybeB.hs

Problem in Paradise - Questions

Should type checker know basic algebra?

```
a | True <==> True (Bool algebra)
a + b == b + a (Nat, Int, Float ... algebra) ...
```

Answers:

- Dependently Types Langs: No (Programmers supply proofs)
- Refinement Types / LiquidHaskell: **Yes** (*SMT solver does the work*)

Type Equality

```
data a :~: b where
Refl :: a :~: a
```

```
test1 = Refl :: 5 :~: 5 -- GOOD

test10 = Refl :: 4 :~: 5 -- ERR

test2 = Refl :: 2 + 3 :~: 3 + 2 -- GOOD

test20 :: SNat n1 -> SNat n2 -> n1 + n2 :~: n2 + n1

test20 _ = Refl -- ERR
```

(base) Data.Type.Equality

Example Combinators

- library over op semantics
- "pattern-matching on a variable of type (a :~: b) produces a proof that a ~ b" haddoc

```
sym :: (a :~: b) -> (b :~: a)

trans :: (a :~: b) -> (b :~: c) -> (a :~: c)

apply :: (f :~: g) -> (a :~: b) -> (f a :~: g b)

inner :: (f a :~: g b) -> (a :~: b)

castWith :: (a :~: b) -> a -> b

gcastWith :: (a :~: b) -> ((a ~ b) => r) -> r

gcastWith Refl x = x
```

(base) Data.Type.Equality

Proofs - Bool Algebra

(code)

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/ProofsBoolAlg.hs

Better Bool ... Decidability

```
import Data.Void

data Dec prop = Yes prop |
    No (prop -> Void)
```

Proofs - Nat (Performance)

unsafeCoerce replacements

Some Learning/References

- intro books
 - Type Driven Development in Idris great book
 - https://github.com/rpeszek/ldrisTddNotes/wiki
 - TAPL great book (not really dep types but still)
 - Programming foundation books (penn/Pierce et al, Wadler)
- Haskell projects (with reading references)
 - singletons
 - equational-reasoning-in-haskell
 - liquidhaskell
- blogs
 - <u>blog.jle.im</u> (Justin Le)
 - typesandkinds (Richard Eisenberg)
- youtube
 - <u>Introduction to Agda</u> series by Daniel Peebles published by Edward Kmett