# Write You Some Proofs for Great Good

https://github.com/rpeszek/present-proofs-lc19

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#### Plan for this talk

- Narrow scoped, pragmatic intro to proofs with dependent types
- Focus on what can be done vs how
- Anything wrong with List?
- Anything wrong with Maybe?
- Anything wrong with Bool?
- Q: Proofs and software engineering do these make sense together?
- Concerns

&#; Performance; Termination / Totality; Maintenance; ...

#### Proofs by who writes them

	Programmers *	Automated Logic Solvers
Amount of work		Free Lunch!
What can be done	A Lot	Limitted
Examples	Dependently Typed Languages	Refinement Types LiquidHaskell
	(focus of this talk)	

#### Motivation (unfair)

Recent experience setting up Node.js on my dev laptop:

```
RangeError: Invalid typed array length: -4095 at new Uint8Array (<anonymous>) at new FastBuffer(buffer.js:72:1)...
```

Googling helped (I downgraded Node to 10.6.0 and the app started)

(Unfair criticism, compiling old project on newer node, C FFI? ...)
Can we eradicate errors like these in functional programs?

#### Motivation (call-side safety)

```
(!!) :: [a] -> Int -> a
safeGet :: [a] -> Int -> Maybe a
-- Liquid:
{-@ (!!) :: x: [a] -> {i:Nat | i < len x} -> a @-}
(!!) :: [a] -> Int -> a
-- Dep Typed:
(!!) :: Vect n a -> Fin n -> a
(!!!) :: Vect n a -> SNat m -> MaybeB (m < n) a
(!!!!): (n:Nat) -> (xs:List a) -> {auto ok: InBounds n xs} -> a
```

- Questionable improvement
- Refinements

- Precise types (talk focus)
- Mixed bag... and much more

#### **Type Precision**

(example Haskell code)

(life-coding Idris)

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Motivation/DepTyped.idr

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Motivation/DepTyped.hs

#### Why proofs?

- Formal verification
- Curry Howard (Why proofs == Why programs)\*
- Enable `Type Precision` (focus of this talk)

```
data List a =

Empty
| Cons a (List a)

Cons a (List a)

| Cons a (List a)

| Cons a (List a)

| Cons a (List a)
```

#### (code)

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/AnIntro.hs
https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/MaybeB.hs

#### **Problem in Paradise - Questions**

Should type checker know basic algebra?

```
a | True <==> True (Bool algebra)
a + b == b + a (Nat, Int, Float ... algebra) ...
```

#### Answers:

- Dependently Types Langs: No (Programmers supply proofs)
- Refinement Types / LiquidHaskell: **Yes** (*SMT solver does the work*)

### **Type Equality**

```
data a :~: b where
Refl :: a :~: a
```

```
test1 = Refl :: 5 :~: 5 -- GOOD

test10 = Refl :: 4 :~: 5 -- ERR

test2 = Refl :: 2 + 3 :~: 3 + 2 -- GOOD

test20 :: SNat n1 -> SNat n2 -> n1 + n2 :~: n2 + n1

test20 __ = Refl -- ERR
```

(base) Data.Type.Equality

#### **Example Combinators**

- library over op semantics
- "pattern-matching on a variable of type (a :~: b) produces a proof that a ~ b" haddoc

```
sym :: (a :~: b) -> (b :~: a)

trans :: (a :~: b) -> (b :~: c) -> (a :~: c)

apply :: (f :~: g) -> (a :~: b) -> (f a :~: g b)

inner :: (f a :~: g b) -> (a :~: b)

castWith :: (a :~: b) -> a -> b

gcastWith :: (a :~: b) -> ((a ~ b) => r) -> r

gcastWith Refl x = x
```

(base) Data.Type.Equality

#### **Proofs - Bool Algebra**

(code)

https://github.com/rpeszek/present-proofs-lc19/blob/master/src/Present/ProofsBoolAlg.hs

#### **Better Bool ... Decidability**

```
import Data.Void

data Dec prop = Yes prop |
    No (prop -> Void)
```

#### **Proofs - Nat (Performance)**

unsafeCoerce replacements

#### Some Learning/References

- intro books
  - Type Driven Development in Idris great book
    - https://github.com/rpeszek/ldrisTddNotes/wiki
  - TAPL great book (not really dep types but still)
  - Programming foundation books (penn/Pierce et al, Wadler)
- Haskell projects (with reading references)
  - singletons
  - equational-reasoning-in-haskell
  - liquidhaskell
- blogs
  - blog.jle.im (Justin Le)
  - typesandkinds (Richard Eisenberg)
- youtube
  - <u>Introduction to Agda</u> series by Daniel Peebles published by Edward Kmett