# Width-Based Backward Search:

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# Introduction

- We studied the performance of width-based planners over Duality and Regression,
- We proposed backward and bidirectional width-based search algorithms,
- Challenges of regression in classical planning were discussed.

## Main Findings

- Width-based search solves dual problems efficiently when |G|=1, but challenging when |G|>1.
- Backward BFWS(f5) and k-BFWS(f5) perform worse than their forward versions but can be orthogonal.
- Width-based bidirectional search algorithms show trade-off in terms of coverage and meeting-in-the-middle.
- FB: forward *k*-BFWS(f5) running first and then backward *k*-BFWS(f5), *k*=1, can be integrated as a quick preprocessing step.
- Modeling matters: partial states, missing invariants and underspecified action schemas cause unnecessary challenges on regression.



Backward width-based search solves more problems over the STRIPS regression model than using forward width-based search over dual problems. Regression / progression models / algorithms are orthogonal when integrated over different bidirectional algorithms and state-of-the-art planners.





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## **Duality**

- $P^d = \langle F, O^d, I^d, G^d \rangle$
- $a^d \in O^d$ ,  $a^d = \langle del, add, pre \rangle$
- $ullet I^d \subseteq F \setminus G$
- ullet  $G^d \subseteq F \setminus I$

## **RESULTS 1**

P: original problem;  $P^d$  dual problem; |G|=1 instances with single-goal; |G|>1 instances conjunctive goals.

	IW  G  = 1		BFWS(f5)  G  > 1	
	P	$\mathbf{P}^{\mathbf{d}}$	P	$\mathbf{P}^{\mathbf{d}}$
Instances	37921	88856	1095	1095
Solved	35918	87830	765	67
Percentage	95%	99%	<b>70%</b>	6%

# **Regression State Model**

- $S^R = \langle S, S_0, S_G, A, f, c \rangle$
- $A(s) = \{a \mid del(a) \cap s = \emptyset, add(a) \cap s \neq \emptyset\}$
- $\bullet$   $s_0 = G$
- $\bullet S_G = \{s \mid s \subseteq I\}$
- $f(a, s) = s \setminus add(a) \cup pre(a)$

## **RESULTS 2**

Solved instances by backward (B) vs. forward (F) k-BFWS(f5) and BFWS(f5).

Domain	F-k	B-k	F	В
Solved (1095)	734	372	765	391
Average time	13.39	46.26	13.10	69.53
Average quality	154.93	176.78	167.13	189.55

#### **Bidirectional Search**

1) *front-to-end* estimates the heuristic value of a state s according to how close it is to the **closest goal state**.

2) *front-to-front* estimates the heuristic value of a state s according to how close it is to the **opposite search frontier**.

## **RESULTS 3**

**k-BDWS**: the combination of **forward and backward** k-BFWS(f5) and checks intersection with respect to the **novelty 1 frontier** of the opposite direction.

R: checks with random states in the *Close* list; H checks with the last expanded state; C: checks with the full *Close* list. M: solved by meet-in-the-middle.

	Dual	Dual-FB	k-BDWS -e	k-BDWS -e R	k-BDWS -e H	k-BDWS -e C
Solved	841	864	713	629	714	596
F-Solved	_	841	410	418	536	298
<b>B-solved</b>	-	23	41	95	146	31
M-solved	_	-	262	116	32	267