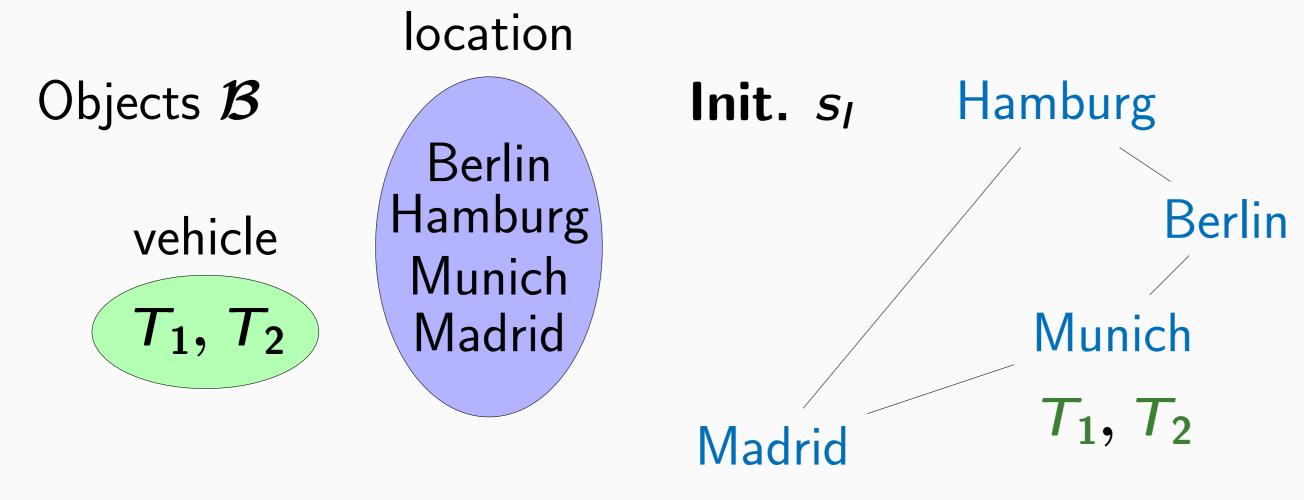
# **Endomorphisms of Lifted Planning Tasks**

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# INTRODUCTION

We propose a method for automatic detection of redundant objects in PDDL tasks.

# RUNNING EXAMPLE



Predicates:

at(v: vehicle, x: location), road(x: location, y: location)

Goal:  $at(T_1, Hamburg)$ 

Action: drive(v, x, y) =

 $at(v,x) \land road(x,y) \Longrightarrow at(v,y) \land \neg at(v,x)$ 

Redundant objects: Madrid,  $T_2$ 

#### DESIGN CHOICES

- Keep the action schema, change only its instances.
- Represent mapping between tuples of objects by a map

 $\sigma: \mathcal{B} \to \mathcal{B}$ , e.g.,  $\sigma \text{Mad} = \text{Ber and } \sigma x = x \text{ otherwise.}$ 

- $\sigma$  has to be a homomorphism from  $s_i$  to  $t_i$ , e.g., if  $s_i \models \operatorname{at}(v, x)$  then  $t_i \models \operatorname{at}(\sigma v, \sigma x)$ .
- In particular,  $\sigma$  has to be an endomorphism on  $s_I$ .

## PDDL ENDOMORPHISM

 $\sigma\colon \mathcal{B} o \mathcal{B}$  is a PDDL endomorphism if

(P1)  $\sigma$  preserves types, i.e.,  $\sigma(\tau) \subseteq \tau$  for all types  $\tau$ ,

(P2)  $\sigma$  is an endomorphism on  $s_I$ ,

(P3)  $p(\vec{b}) \in Goal \text{ iff } p(\sigma \vec{b}) \in Goal$ ,

(P4) for all reachable states s, t and each ground action  $a(\vec{b})$ 

$$\sigma$$

$$\begin{array}{c|c}
a(b) \\
\hline
\sigma \\
a(\sigma \vec{b}) \\
t
\end{array}$$

(P5) for the optimal planning, we further assume that  $cost_a(\sigma \vec{b}) \leq cost_a(\vec{b})$  for all ground actions  $a(\vec{b})$ .

#### **THEOREM**

Let  $\sigma$  be a PDDL endomorphism. If  $\pi = \langle a_1(\vec{b}_1), \dots, a_n(\vec{b}_n) \rangle$  is an (optimal) plan, then  $\pi' = \langle a_1(\sigma \vec{b}_1), \dots, a_n(\sigma \vec{b}_n) \rangle$  is an (optimal) plan as well.

### COROLLARY

If  $b \not\in \sigma(\mathcal{B})$  then b is redundant.

#### COMPUTATION

To find  $\sigma$ , we formulate the problem as an instance of CSP. (P1-P3,P5) can be easily formulated as constraints in CSP. (P4) is problematic due to delete effects. Suppose  $\sigma(T_2) = \sigma(T_1) = T_1$ ,  $\sigma(x) = x$  and  $\sigma(y) = y$ .

$$\operatorname{at}(T_1,\mathsf{x}) \qquad \operatorname{at}(T_1,\mathsf{y}) \ \operatorname{at}(T_2,\mathsf{x}) \qquad \operatorname{at}(T_2,\mathsf{x}) \ \sigma \qquad \sigma \qquad \mathsf{x} \ \operatorname{drive}(T_1,\mathsf{x},\mathsf{y}) \qquad \sigma \qquad \mathsf{x} \ \operatorname{drive}(T_1,\mathsf{x},\mathsf{y}) \qquad \operatorname{at}(T_1,\mathsf{y}) \ \operatorname{at$$

## WHAT CAN BE COLLAPSED?

 $\{at(v,x)\}\$  is a lifted mutex group with v fixed and x counted. We cannot have  $at(T_1,x) \wedge at(T_1,y)$  for  $x \neq y$  in a reachable state s. Consequently, we cannot recreate the previous counter-example with two different locations. The map  $\sigma$  defined by  $\sigma Mad = Ber$  and  $\sigma x = x$  otherwise is an PDDL endomorphism so Madrid is a redundant object.

#### **EXPERIMENTS**

domain	#ps	%obj	%op	%fact
caldera18 (20)	20	15.15	0.00	0.00
citycar14 (20)	5	7.76	0.00	0.00
parcprinter11 (20)	6	7.28	0.00	0.00
rovers06 (40)	33	3.84	11.32	6.43
satellite02 (20)	17	7.61	20.40	11.48
tpp06 (30)	1	2.22	13.44	0.42
transport11 (20)	11	4.65	9.28	7.63
visitall11 (20)	8	15.57	21.28	16.71
overall from above (530)	244	5.83	5.33	3.61
overall from op-pruned (220)	106	5.99	12.26	8.31



