

Artificial Intelligence for Business Research @Antai

Deep Learning Basics

Renyu (Philip) Zhang

1

Agenda

- Supervised Learning Model Training
- Deep Neural Nets
- Computations in Deep Learning

2

2

1

Supervised Learning

- Given the data observations: $(X_i, Y_i), i = 1, 2, \dots, n$
- Define your model
 - Linear regression: $Y = a + b \cdot X + \epsilon$
- Define your loss function:
 - Regression: Squared error: $(Y - f(X))^2$
 - Classification: Cross entropy:
 $-\log(p)Y - \log(1 - p)(1 - Y)$
- Pick your optimizer
 - OLS estimator
 - Gradient descent
- Run your model on a CPU/GPU Cluster

Deep learning means the model family is Deep Neural Nets.

3

3

Training a Model

$$\hat{\theta} := \operatorname{argmin}_{\theta} \frac{1}{n} \sum_{i=1}^n \mathcal{L}(Y_i, f(X_i, \theta))$$

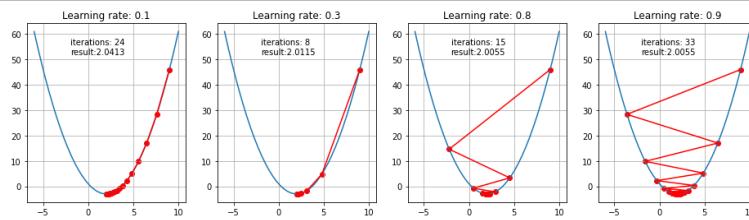
- Gradient Descent:** A first-order iterative optimization for finding a local minimum of a differentiable function.

Algorithm 1 Gradient Descent

```

1: Guess  $\mathbf{x}^{(0)}$ , set  $k \leftarrow 0$ 
2: while  $\|\nabla f(\mathbf{x}^{(k)})\| \geq \epsilon$  do
3:    $\mathbf{x}^{(k+1)} = \mathbf{x}^{(k)} - t_k \nabla f(\mathbf{x}^{(k)})$ 
4:    $k \leftarrow k + 1$ 
5: end while
6: return  $\mathbf{x}^{(k)}$ 

```



4

4

Example: OLS

- Loss function: $S(\beta) = \sum_{i=1}^n \left| y_i - \sum_{j=1}^p X_{ij}\beta_j \right|^2 = \|\mathbf{y} - \mathbf{X}\beta\|^2.$

- Closed-form Solution: $\hat{\beta} = (\mathbf{X}^\top \mathbf{X})^{-1} \mathbf{X}^\top \mathbf{y}.$

- Gradient Descent: $w^{k+1} = w^k - \alpha_k \underbrace{X^\top (Xw^k - y)}_{\nabla f(w^k)},$

- Statistics convergence vs. Optimization convergence:

- Convergence of estimator:** Is the estimator constructed by the loss function converging to the true underlying estimand? How fast? Bias and consistency?
- Convergence of optimization:** Will the optimization algorithm we use converge to the minimizer of the loss function given data? How fast?

Cost Function

$$J(\Theta_0, \Theta_1) = \frac{1}{2m} \sum_{i=1}^m [h_\Theta(x_i) - y_i]^2$$

↑
Predicted Value
↑
True Value

Gradient Descent

$$\Theta_j = \Theta_j - \alpha \frac{\partial}{\partial \Theta_j} J(\Theta_0, \Theta_1)$$

↑
Learning Rate

Now,

$$\begin{aligned} \frac{\partial}{\partial \Theta} J_\Theta &= \frac{\partial}{\partial \Theta} \frac{1}{2m} \sum_{i=1}^m [h_\Theta(x_i) - y_i]^2 \\ &= \frac{1}{m} \sum_{i=1}^m (h_\Theta(x_i) - y_i) \frac{\partial}{\partial \Theta_j} (\Theta x_i - y) \\ &= \frac{1}{m} (h_\Theta(x_i) - y) x_i \end{aligned}$$

Therefore,

$$\Theta_j := \Theta_j - \frac{\alpha}{m} \sum_{i=1}^m [(h_\Theta(x_i) - y) x_i]$$

5

5

Another Example: Logistic Regression

- Model: $\Pr(y_t = 1|x_t) = \frac{\exp(x_t' \beta)}{1 + \exp(x_t' \beta)}.$

- MLE Estimator/Cross-Entropy Loss: $\hat{\beta} = \arg \max_{\beta} [\ln \mathcal{L}(\beta)] = \arg \max_{\beta} \left[\sum_t \left(y_t \ln \left(\frac{\exp(x_t' \beta)}{1 + \exp(x_t' \beta)} \right) + (1 - y_t) \ln \left(\frac{1}{1 + \exp(x_t' \beta)} \right) \right) \right].$

- Gradient Descent: What is the gradient of logistic regression? (HW)

6

6

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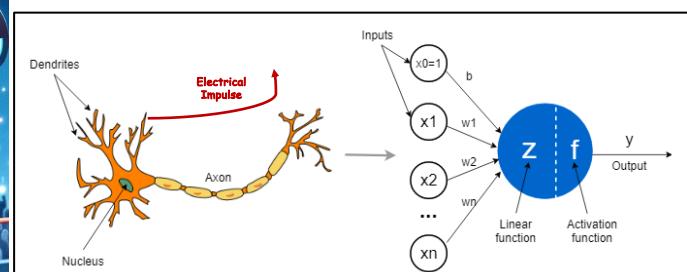
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9

Symbolic AI vs. Connectionist AI



Should machines automate **high-level human logic** or the **biological foundation of brains?**



Neuron and Artificial Neuron

10

10

Computational Power of Human

10^{16} computations in the entire history

More than 10^{16} computations per second

1945

To train GPT-4: More than 10^{25} computations.

11

11

Global Data Generated Annually

Year	Data Generated (zettabytes)
2010	~1
2011	~2
2012	~3
2013	~5
2014	~8
2015	~12
2016	~18
2017	~25
2018*	~35
2019*	~45
2020*	~60
2021*	~80
2022*	~100
2023*	~125
2024*	~150
2025*	~180

A portrait photo of a kangaroo wearing an orange hoodie and blue sunglasses standing on the grass in front of the Sydney Opera House holding a sign on the chest that says Welcome Friends!

350M 750M 3B 20B

We are here now.

Performance

Amount of data

Deep neural networks

Medium neural networks

Shallow neural networks

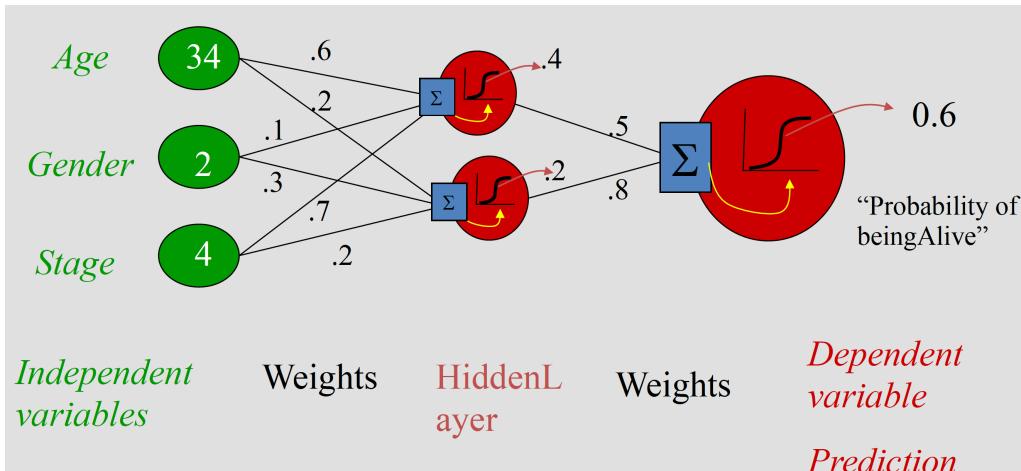
Traditional machine learning

12

12

Neural Network Models

- We build a model to predict patient mortality based on their demographics.



- University Approximation Theorem:** One hidden layer NN is enough to represent (not learn) an approximation of any function with an arbitrary degree of accuracy.

Reference: <https://www.youtube.com/watch?v=aircArUvnKk>

13

Are Simple Multilayer Perceptrons (MLP) Outdated?

nature > articles > article

Article | Open access | Published: 01 December 2021

Advancing mathematics by guiding human intuition with AI

Alex Davies¹, Petar Veličković², Lars Buesing³, Sam Blackwell⁴, Daniel Zheng⁵, Nenad Tomasev⁶, Richard Tanburn⁷, Peter Battaglia⁸, Charles Blundell⁹, András Juhász¹⁰, Marc Lackenby¹¹, Georgie Williamson¹², Demis Hassabis & Pushmeet Kohli¹³

Nature 600, 70–74 (2021) | [Cite this article](#)

266k Accesses | 128 Citations | 1624 Altmetric | [Metrics](#)

Abstract

The practice of mathematics involves discovering patterns and using these to formulate and prove conjectures, resulting in theorems. Since the 1960s, mathematicians have used computers to assist in the discovery of patterns and formulation of conjectures¹, most famously in the Birch and Swinnerton-Dyer conjecture², a Millennium Prize Problem³. Here we provide examples of new fundamental results in pure mathematics that have been discovered with the assistance of machine learning—demonstrating a method by which machine learning can aid mathematicians in discovering new conjectures and theorems. We propose a process of using machine learning to discover potential patterns and relations between mathematical objects, understanding them with attribution techniques and using these observations to guide intuition and propose conjectures. We outline this machine-learning-guided framework and demonstrate its successful application to current research questions in distinct areas of pure mathematics, in each case showing how it led to meaningful mathematical contributions on important open problems: a new connection between the algebraic and geometric structure of knots, and a candidate algorithm predicted by the combinatorial invariance conjecture for symmetric groups⁴. Our work may serve as a model for collaboration between the fields of mathematics and artificial intelligence (AI) that can achieve surprising results by leveraging the respective strengths of mathematicians and machine learning.

<https://www.bilibili.com/video/BV1YZ4y1S72j>

Deep-Learning-Based Causal Inference for Large-Scale Combinatorial Experiments: Theory and Empirical Evidence

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Note necessarily!

The key is to identify interesting and impactful applications.

Large-scale online platforms launch hundreds of randomized experiments (a.k.a. A/B tests) every day to iterate their operations and marketing strategies. The combinations of these treatments are typically not exhaustively tested, which triggers an important question of both academic and practical interest: Without observing the outcomes of all treatment combinations, how does one estimate the causal effect of any treatment combination and identify the optimal treatment combination? We develop a novel framework combining deep learning and doubly robust estimation to estimate the causal effect of any treatment combination for each user on the platform when observing only a small subset of treatment combinations. Our proposed framework (called debiased deep learning, DeDL) exploits Neyman orthogonality and combines interpretable and flexible structural layers in deep learning. We prove theoretically that this framework yields efficient, consistent, and asymptotically normal estimators under mild assumptions, thus allowing for identifying the best treatment combination when observing only a few combinations. To empirically validate our method, we collaborated with a large-scale video-sharing platform and implemented our framework for three experiments involving three treatments where each combination of treatments is tested. When observing only a subset of treatment combinations, our DeDL approach significantly outperforms other benchmarks to accurately estimate and infer the average treatment effect of any treatment combination, and to identify the optimal treatment combination.

Key words: Deep Learning, Double Machine Learning, Causal Inference, Field Experiments, Experimentation on Online Platforms

<https://www.bilibili.com/video/BV19v4y1h7Ev>

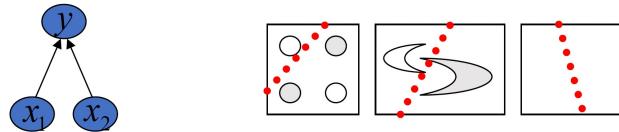
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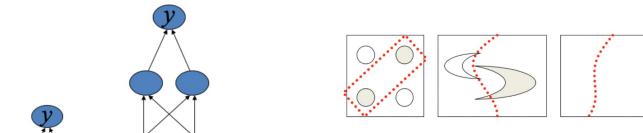
Neural Nets

- More layers, more complex functions, more powerful learning and more required data.

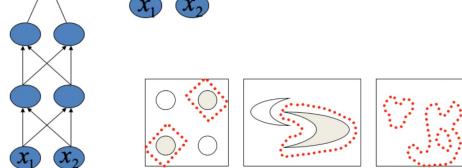
- 0 hidden layers: Linear classifier
 - Hyperplanes



- 1 hidden layer
 - Boundary of convex region



- 2 hidden layers
 - Combinations of convex regions



15

15

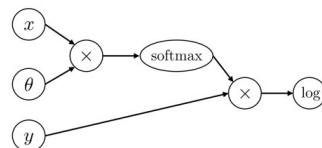
Neural Nets

- Logistic Regression:

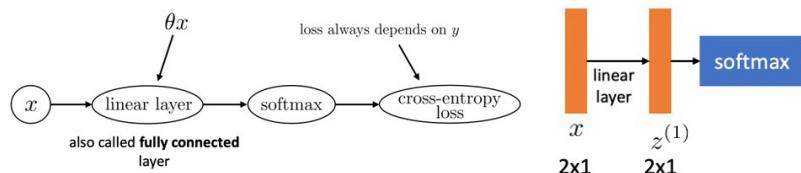
$$f_{\theta}(x) = \begin{bmatrix} x^T \theta_{y_1} \\ x^T \theta_{y_2} \\ \vdots \\ x^T \theta_{y_m} \end{bmatrix} \quad f_{\theta}(x) = \theta x$$

matrix

$$p_{\theta}(y = i|x) = \text{softmax}(f_{\theta}(x))[i] = \frac{\exp(f_{\theta,i}(x))}{\sum_{j=1}^m \exp(f_{\theta,j}(x))}$$



- A simpler representation:



16

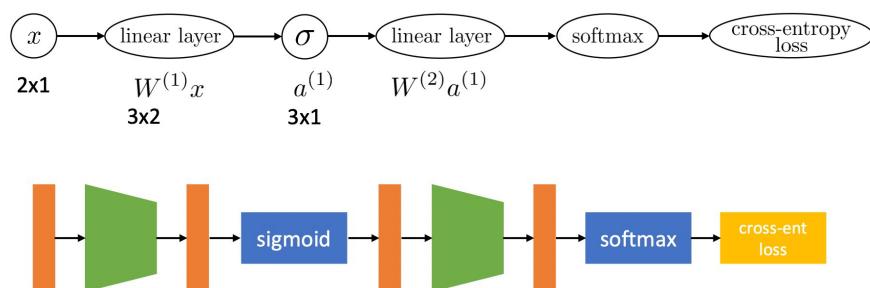
16

More Complex Neural Nets

- Add functions before SoftMax

$$\phi(x) = \begin{pmatrix} x_1 \\ x_2 \\ x_1^2 \\ x_2^2 \\ x_1 x_2 \end{pmatrix}$$

softmax($\phi(x)^T \theta$)

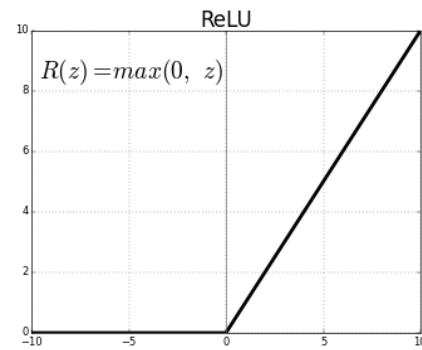
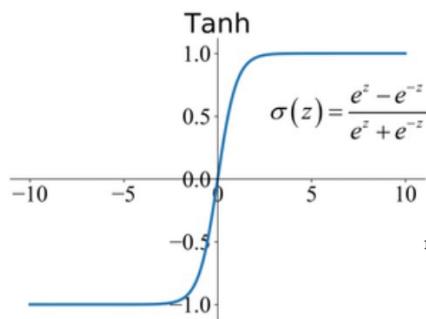
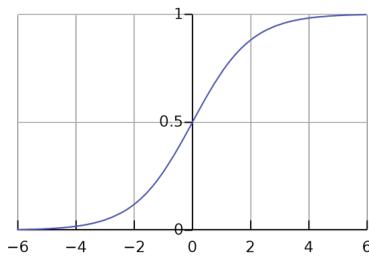


17

17

Activation Functions

- Activation functions:
 - Sigmoid
 - Tanh
 - ReLU (mostly used)



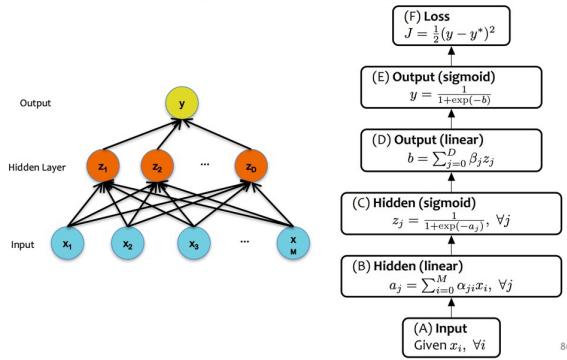
18

18

Backpropagation

Training

Backpropagation



86

Training

Backpropagation

Case 2:
Neural
Network

Adam

- Adam: The most well-used algorithm to automatically tune momentum and learning rates.
- Adam combines AdaGrad and RMSProp
- Adam is the default optimizer tuner in deep learning.

Adam

$M_0 = \mathbf{0}, R_0 = \mathbf{0}$ (Initialization)

For $t = 1, \dots, T$:

$$\begin{aligned} M_t &= \beta_1 M_{t-1} + (1 - \beta_1) \nabla L_t(W_{t-1}) \quad (1\text{st moment estimate}) \\ R_t &= \beta_2 R_{t-1} + (1 - \beta_2) \nabla L_t(W_{t-1})^2 \quad (2\text{nd moment estimate}) \\ \hat{M}_t &= M_t / (1 - (\beta_1)^t) \quad (1\text{st moment bias correction}) \\ \hat{R}_t &= R_t / (1 - (\beta_2)^t) \quad (2\text{nd moment bias correction}) \\ W_t &= W_{t-1} - \alpha \frac{\hat{M}_t}{\sqrt{\hat{R}_t + \epsilon}} \quad (\text{Update}) \end{aligned}$$

Return W_T

Hyper-parameters:

- $\alpha > 0$ – learning rate (typical choice: 0.001)
- $\beta_1 \in [0, 1]$ – 1st moment decay rate (typical choice: 0.9)
- $\beta_2 \in [0, 1]$ – 2nd moment decay rate (typical choice: 0.999)

Adam: A method for stochastic optimization

DP Kingma, J Ba
arXiv preprint arXiv:1412.6980, 2014 · arxiv.org

[PDF] arxiv.org

We introduce Adam, an algorithm for first-order gradient-based optimization of stochastic objective functions, based on adaptive estimates of lower-order moments. The method is straightforward to implement, is computationally efficient, has little memory requirements, is invariant to diagonal rescaling of the gradients, and is well suited for problems that are large in terms of data and/or parameters. The method is also appropriate for non-stationary objectives and problems with very noisy and/or sparse gradients. The hyperparameters have intuitive interpretations and typically require little tuning. Some connections to related algorithms, on which Adam was inspired, are discussed. We also analyze the theoretical convergence properties of the algorithm and provide a regret bound on the convergence rate that is comparable to the best known results under the online convex optimization framework. Empirical results demonstrate that Adam works well in practice and compares favorably to other stochastic optimization methods. Finally, we discuss AdaMax, a variant of Adam based on the infinity norm.

arxiv.org

收起 ^

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24

24

Optimization for DNN

- Initialization matters.

- Normalization/standardization matters.

Understanding the difficulty of training deep feedforward neural networks

K Glorot, Y Bengio - Proceedings of the thirteenth ..., 2010 - proceedings.mlr.press

Whereas before 2006 it appears that deep multi-layer neural networks were not successfully trained, since then several algorithms have been shown to successfully train them, with experimental results showing the superiority of deeper vs less deep architectures. All these experimental results were obtained with new initialization or training mechanisms. Our objective here is to understand better why standard gradient descent from random initialization is doing so poorly with deep neural networks, to better understand these recent ...

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Delving deep into rectifiers: Surpassing human-level performance on imagenet classification

K He, X Zhang, S Ren, J Sun - Proceedings of the IEEE ..., 2015 - openaccess.thecvf.com

Rectified activation units (rectifiers) are essential for state-of-the-art neural networks. In this work, we study rectifier neural networks for image classification from two aspects. First, we propose a Parametric Rectified Linear Unit (PReLU) that generalizes the traditional rectified unit. PReLU improves model fitting with nearly zero extra computational cost and little overfitting risk. Second, we derive a robust initialization method that particularly considers the rectifier nonlinearities. This method enables us to train extremely deep rectified models ...

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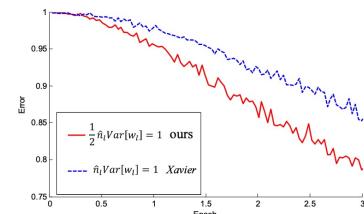


Figure 2. The convergence of a 22-layer large model (B in Table 3). The x-axis is the number of training epochs. The y-axis is the top-1 error of 3,000 random val samples, evaluated on the center crop. We use ReLU as the activation for both cases. Both our initialization (red) and “Xavier” (blue) [7] lead to convergence, but ours starts reducing error earlier.

Batch normalization: Accelerating deep network training by reducing internal covariate shift

S Ioffe, C Szegedy - International conference on machine ..., 2015 - proceedings.mlr.press

Abstract Training Deep Neural Networks is complicated by the fact that the distribution of each layer's inputs changes during training, as the parameters of the previous layers change. This slows down the training by requiring lower learning rates and careful parameter initialization, and makes it notoriously hard to train models with saturating nonlinearities. We refer to this phenomenon as internal covariate shift, and address the problem by normalizing layer inputs. Our method draws its strength from making ...

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Reference: <https://www.deeplearning.ai/ai-notes/initialization/index.html>

25

25

Gradient Descent for DNN

- How does the loss function landscape of DNN look like?
- In general, it's very complex and we don't know.

[Visualizing the loss landscape of neural nets](#)

H Li, Z Xu, G Taylor, C Studer... - Advances in neural ... 2018 - proceedings.neurips.cc

... of neural loss functions, and the effect of loss landscapes on generalization, using a range of visualization ... " method that helps us visualize loss function curvature and make meaningful ...

☆ 保存 引用 被引用次数: 1746 相关文章 所有 16 个版本

[Deep residual learning for image recognition](#)

K He, X Zhang, S Ren, J Sun - ... and pattern recognition, 2016 - openaccess.thecvf.com

... Deeper neural networks are more difficult to train. We present a residual learning framework to ease the training of networks that are substantially deeper than those used previously. ...

★ 保存 引用 被引用次数: 196717 相关文章 所有 76 个版本

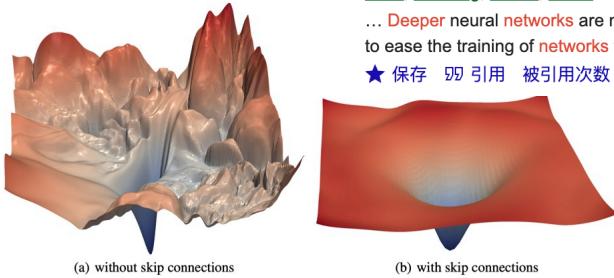


Figure 1: The loss surfaces of ResNet-56 with/without skip connections. The proposed filter normalization scheme is used to enable comparisons of sharpness/flatness between the two figures.

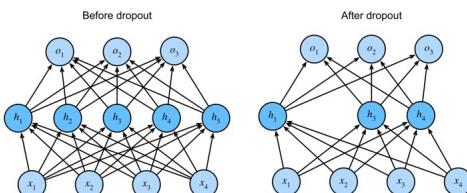
27

27

Dropout

- Deep neural nets are over-parameterized and tend to overfit.
- Training with noisy data is like regularization (Bishop 1995).
- Dropout provides a computationally efficient and effective way to add such noise into neural nets training.
- If you add a drop out layer with probability p , then each intermediate activation value h from the previous layer becomes:

$$h' = \begin{cases} 0 & \text{with probability } p \\ \frac{h}{1-p} & \text{otherwise} \end{cases}$$



[PDF] [Dropout: a simple way to prevent neural networks from overfitting](#)

N Srivastava, G Hinton, A Krizhevsky... - The journal of machine ..., 2014 - jmlr.org

... This significantly reduces overfitting and gives major improvements over other regularization methods. We show that dropout improves the performance of neural networks on ...

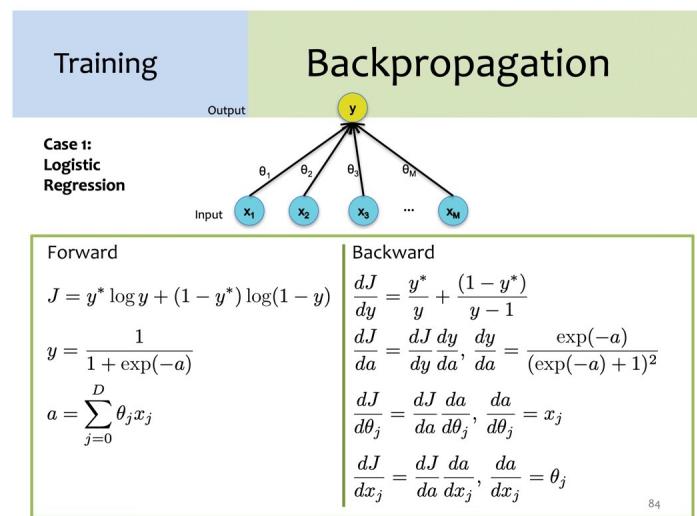
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30

30

Estimation/Training of Neural Nets

- Repeatedly apply the chain rule to obtain the gradient of the loss function with respect to the parameters and use Adam to update the parameters.
- Initialize network parameters randomly or semi-randomly; specify drop-out.
- For each epoch:
 - Shuffle data
 - For each minibatch:
 - Properly normalize the data
 - Use backpropagation to compute the gradient
 - Use Adam to update the parameters.
- Backpropagation: Chain rule.



84

31

DL Libraries

- Good news: "You will probably never implement backpropagation by yourselves unless for your homework."
- General parallel computing libraries:
 - TensorFlow (Google)
 - PyTorch (Facebook)
- Deep learning libraries:
 - Keras
 - HuggingFace
- TensorFlow/PyTorch is like NumPy but
 - Much better documentation
 - Much better supported in parallel computing (GPUs)
 - Much better solver with large data
 - Much better for deployment (probably you don't care)
- The core function of DL libraries: Take and store the derivatives in an **automated and efficient** fashion.

Operation	NumPy	PyTorch
Array/Tensor Creation	<code>'numpy.array()'</code>	<code>'torch.tensor()'</code>
Dimensions	<code>'array.ndim'</code>	<code>'tensor.dim()'</code>
Shape	<code>'array.shape'</code>	<code>'tensor.size()'</code>
Sum over all elements	<code>'numpy.sum(array)'</code>	<code>'torch.sum(tensor)'</code>
Mean	<code>'numpy.mean(array)'</code>	<code>'torch.mean(tensor)'</code>
Standard Deviation	<code>'numpy.std(array)'</code>	<code>'torch.std(tensor)'</code>
Element-wise Sum	<code>'array1 + array2'</code>	<code>'tensor1 + tensor2'</code>
Element-wise Product	<code>'array1 * array2'</code>	<code>'tensor1 * tensor2'</code>
Matrix Multiplication	<code>'numpy.dot(a, b)'</code>	<code>'torch.matmul(a, b)'</code>
Reshape	<code>'array.reshape()'</code>	<code>'tensor.view()'</code>
Transpose	<code>'array.T'</code>	<code>'tensor.t()'</code>
Max value	<code>'numpy.max(array)'</code>	<code>'torch.max(tensor)'</code>
Min value	<code>'numpy.min(array)'</code>	<code>'torch.min(tensor)'</code>
Concatenate	<code>'numpy.concatenate([a, b], axis)'</code>	<code>'torch.cat([a, b], dim)'</code>

32

Putting Everything Together

- Model: You can represent a complex function as a networks of computations.
- Loss function: Cross-entropy for classification and mean squared error for regression.
- Estimation/optimization: Use backpropagation to find the gradients fast; SGD + Adam to update the parameters with gradients.
- Implementation: Use PyTorch to code parallel vector computation; use Keras/Hugging Face to directly specify the model.

33

33

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34

34

Computing Equipment

- Self-made workstations/servers:
 - CPU + Nvidia 4090 (~US\$1,500, but very hard to get)
 - CUHK Business School DOT will deploy a server with 8 4090s soon.
- Cloud:
 - GCP https: <https://cloud.google.com/compute/vm-instance-pricing#accelerator-optimized> (US\$ 4.05 per 1 A100 per hour)
 - Amazon: <https://aws.amazon.com/ec2/instance-types/p4/> (US\$32.77 per 8 A100 per hour)
- Computing costs: Proportional to the size of the network (the number of parameters) and the size of the training data.

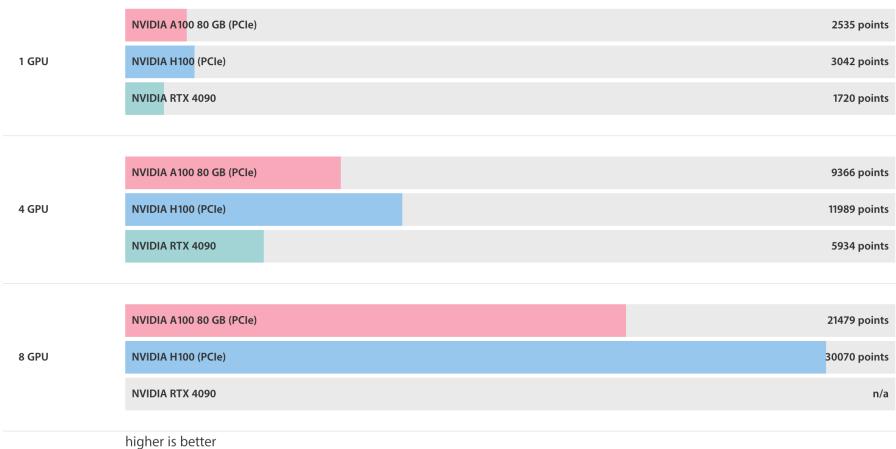
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35

GPU Comparison

- [https://bizon-tech.com/gpu-benchmarks/NVIDIA-A100-80-GB-\(PCIe\)-vs-NVIDIA-H100-\(PCIe\)-vs-NVIDIA-RTX-4090/624vs632vs637](https://bizon-tech.com/gpu-benchmarks/NVIDIA-A100-80-GB-(PCIe)-vs-NVIDIA-H100-(PCIe)-vs-NVIDIA-RTX-4090/624vs632vs637)

Resnet50 (FP16)



36

36

Model Size and Training Time

- Resnet-50, 12 million parameters, ImageNet Data, TF32, 30mins on an 8 A100s server (DGX).
 - $\sim 0.5 \times 8 \times 1.5 = 6 \sim 10$ hrs on 4090.
- BERT, 110 million parameters, 170GB BooksCorpus and Wikipedia Data, TF32, 5 hrs on DGX.
- BERT fine-tuning, Stanford Question Answering Data, 3~5 mins on DGX.
- GPT-3, 175B parameters (3.64e23 FLOPs, 300B training tokens), TF32, 128 DGX servers (A100: 80 TFLOP/s). How long does it take to pre-train GPT-3?
 - $3.64 \times 10^{23} / (80 \times 10^{12}) / 128 / 8 / 24 / 3600 \approx 51$ Days - 100 Days, which means 3 months.

37