

# Double Machine Learning

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## Machine Learning for Causal Inference

- Using machine learning for causal inference is generally **very challenging**.
  - Cross-validation** cannot be directly applied to hyper-parameter tuning for causal inference models (Athey and Imbens, 2016).
  - Good performance in predicting** propensity scores or outcomes cannot be directly translated into **good causal performance** (Belloni et al., 2014).
  - Regularization** in ML will introduce **additional biases** in causal inference (Belloni et al., 2016).
- What are the most critical issues in causal inference at large?
  - Confoundedness, non-overlapping, balance, etc.
  - AI/ML cannot magically solve these fundamental problems of causal inference.**
- Double machine learning (DML)** provides a framework to empower causal inference with ML.
  - Compared with other fields in business research, this is a very **fast-evolving** field of study.

### Recursive partitioning for heterogeneous causal effects

[S. Athey](#), [G. Imbens](#) - Proceedings of the National Academy of Sciences, 2016 - pnas.org  
 ... We refer to the estimators developed in this section as "causal tree" (CT) estimators. ... for constructing **trees** for **causal** effects that allow us to do valid inference for the **causal** effects in ...  
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### Inference on treatment effects after selection among high-dimensional controls

[A. Belloni](#), [V. Chernozhukov](#)... - Review of Economic Studies, 2014 - academic.oup.com  
 We propose robust methods for inference about the effect of a treatment variable on a scalar outcome in the presence of very many regressors in a model with possibly non-Gaussian ...  
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### Post-selection inference for generalized linear models with many controls

[A. Belloni](#), [V. Chernozhukov](#), Y. Wei - Journal of Business & Economic Statistics, 2016 - Taylor & Francis  
 This article considers generalized linear models in the presence of many controls. We lay out a general methodology to estimate an effect of interest based on the construction of an ...  
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## Today's Focus

### Root-N-consistent semiparametric regression

PM **Robinson** - *Econometrica: Journal of the Econometric Society*, 1988 - JSTOR

One type of semiparametric regression on an  $\text{scalar}^p \times \text{scalar}^q \text{-valued}$  random variable  $(X, Z)$  is  $\beta'X + \theta(Z)$ , where  $\beta$  and  $\theta(Z)$  are an unknown slope coefficient ...

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### Deep learning for individual heterogeneity: An automatic inference framework

MH **Farrell**, T **Liang**, S **Misra** - arXiv preprint arXiv:2010.14694, 2020 - arxiv.org

... and inference using machine learning to enrich economic models. Our framework takes a ... functions, to capture the rich heterogeneity based on potentially high dimensional or complex ...

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Robison (1988)

Chernozhukov  
et al. (2018)

Farrell et al.  
(2021)

Partial Linear  
Models

Double Machine  
Learning

DML in Action

### Double/debiased machine learning for treatment and structural parameters

V **Chernozhukov**, D **Chetverikov**, M **Demirer**, E **Duflo**... - 2018 - academic.oup.com

We revisit the classic semi-parametric problem of inference on a low-dimensional parameter  $\theta_0$  in the presence of high-dimensional nuisance parameters  $\eta_0$ . We depart from the ...

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### Applied DML: A Historical Perspective

Slides on DML: <https://bstewart.scholar.princeton.edu/sites/g/files/toruqf4016/files/bstewart/files/chern.handout.pdf>  
Applied Causal Inference Powered by ML and AI: [https://chapters.causalm1-book.org/CausalML\\_book\\_2022.pdf](https://chapters.causalm1-book.org/CausalML_book_2022.pdf)

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## Agenda

- Partial Linear Models
- General Double Machine Learning Framework
- Double Machine Learning in Action: Practical Recipe and Pitfalls

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## High-Level Takeaways of the DML Literature



Causal Inference: A Statistical Learning Approach [https://web.stanford.edu/~swager/causal\\_inf\\_book.pdf](https://web.stanford.edu/~swager/causal_inf_book.pdf)  
 Applied Causal Inference Powered by ML and AI: [https://chapters.causalm1-book.org/CausalML\\_book\\_2022.pdf](https://chapters.causalm1-book.org/CausalML_book_2022.pdf)  
 DML Package: <https://docs.doubleml.org/stable/index.html#>  
 Slides on DML: <https://bstewart.scholar.princeton.edu/sites/q/files/toruqf4016/files/bstewart/files/chern.handout.pdf>

- Provides a **general framework**, by leveraging **Neyman Orthogonality**, for estimating **treatment effects** using **ML methods**.
  - Causal inference usually requires estimating the **expected outcomes (and propensity scores) conditioned on covariates or confounders**
  - Standard econometrics methods make **strong functional form assumptions** (e.g., linear models), which require **strong substantive justifications**; if **mis-specified**, causal estimates will be **significantly biased**.
  - DML framework **automatically learns the form of conditional expectation functions** from data.
- DML framework requires:
  - Some regularity conditions (recall the assumptions for AIPW)
  - ML estimators to converge, in RMSE/L2-norm at a rate of  $o(n^{-1/4})$ , slower than  $o(n^{-1/2})$ , the rate of most parametric models according to the delta method.
- DML framework outputs:
  - **Root-n consistent estimators** for treatment effects: Convergence to the ground-truth in probability at a rate  $O(n^{-1/2})$ , a property natural and common in a **parametric world**.
  - In frequentist perspective, root-n consistency typically means **asymptotically normal**, which means you can construct **valid confidence intervals** and **do inference on your estimators**.

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## Let's First Look at a Simple Model



Causal Inference: A Statistical Learning Approach [https://web.stanford.edu/~swager/causal\\_inf\\_book.pdf](https://web.stanford.edu/~swager/causal_inf_book.pdf)  
 Applied Causal Inference Powered by ML and AI: [https://chapters.causalm1-book.org/CausalML\\_book\\_2022.pdf](https://chapters.causalm1-book.org/CausalML_book_2022.pdf)  
 DML Package: <https://docs.doubleml.org/stable/index.html#>  
 Slides on DML: <https://bstewart.scholar.princeton.edu/sites/q/files/toruqf4016/files/bstewart/files/chern.handout.pdf>

- We use the **partial linear model (PLM)** to illustrate the DML framework:
  - Why **ML** is important and useful;
  - How the **statistical theory** works.

### Partially Linear Model Set-up

- $Y$ : Outcome
- $D$ : Treatment
- $X$ : Measured confounders
- $U$  and  $V$  are our error terms
- We assume zero conditional mean:

$$Y = D\theta_0 + g_0(X) + U$$

$$D = m_0(X) + V$$

$$E[U \mid X, D] = 0 \quad E[V \mid X] = 0$$

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