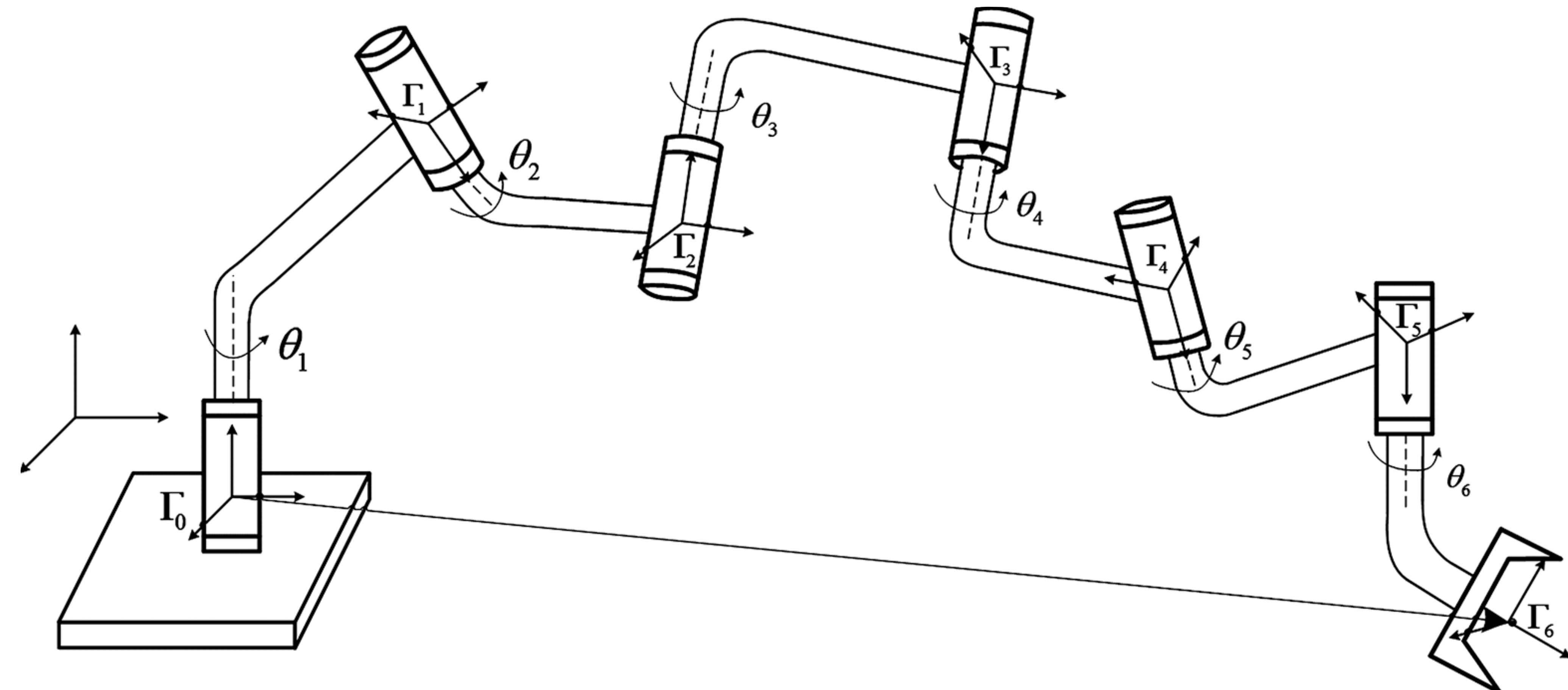


# Lecture 06

## Manipulation - I

### Forward Kinematics & Decision Making



# Course Logistics

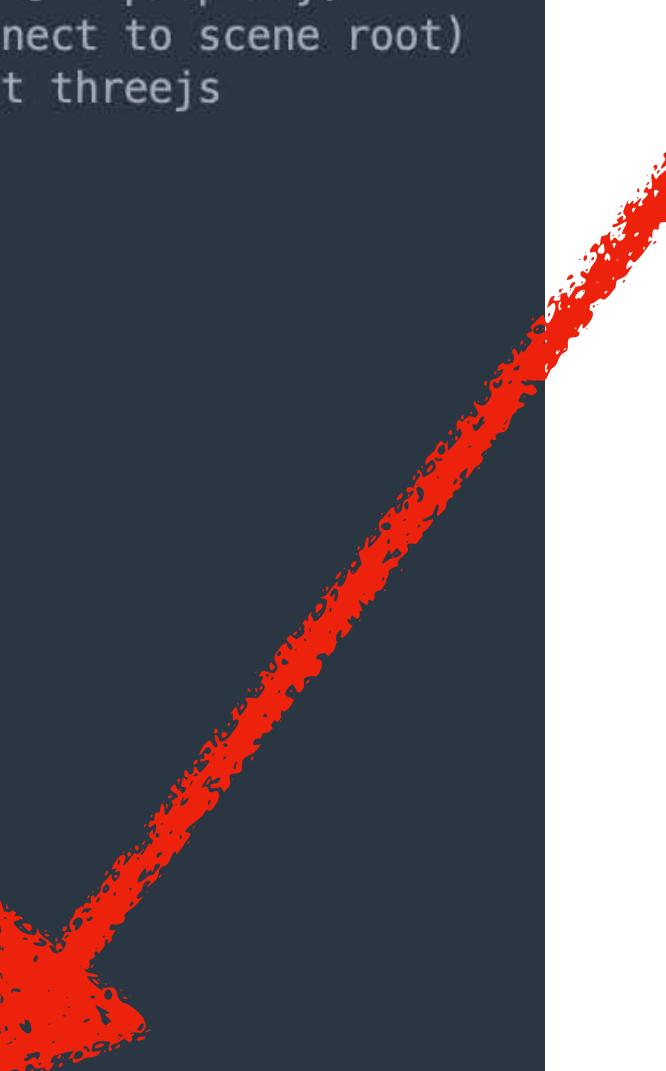
- Project 2 was posted on 02/05 and will be due **on Wed 02/12**.
- Quiz 3 will be posted tomorrow at 6 pm and will be due on Wed noon.
- Project 3 will be released on 02/12 and will be due on 02/19.
- Note:
  - After the late tokens and due date, you will have to ask Adit Kadepurkar (TA) to submit, so we can consider the late submission with 25% penalty per day.
  - Feel free to talk to Karthik during his OH if you have any questions about this.



# FAQs on P2

## What to do in `kineval/kineval_robot_init_joints.js`?

```
12 kineval.initRobotJoints = function initRobotJoints() {
13     // build kinematic hierarchy by looping over each joint in the robot
14     // (object fields can be index through array-style indices, object[field] = property)
15     // and insert threejs scene graph (each joint and link are directly connect to scene root)
16     // NOTE: kinematic hierarchy is maintained independently by this code, not threejs
17
18     var x,tempmat;
19
20     for (x in robot.joints) {
21
22         // give the joint its name as an id
23         robot.joints[x].name = x;
24
25         // initialize joint angle value and control input value
26         robot.joints[x].angle = 0;
27         robot.joints[x].control = 0;
28         robot.joints[x].servo = {};
29
30         //set appropriate servo gains for arm setpoint control
31         robot.joints[x].servo.p_gain = 0.1;
32         robot.joints[x].servo.p_desired = 0;
33         robot.joints[x].servo.d_gain = 0.01;
34
35         /* STENCIL START */
36         // STENCIL: complete kinematic hierarchy of robot for convenience.
37         // robot description only specifies parent and child links for joints.
38         // additionally specify parent and CHILDREN joints for each link
39
40
41
42
43
44
45     /* STENCIL END */
46
47 }
```



robots/robot\_mr2.js given to you has this information

```
54 // specify and create data objects for the joints of the robot
55 robot.joints = {};
56
57 robot.joints.clavicle_right_yaw = {parent:"base", child:"clavicle_right"};
58 robot.joints.clavicle_right_yaw.origin = {xyz: [0.3,0.4,0.0], rpy:[-Math.PI/2,0,0]};
59 robot.joints.clavicle_right_yaw.axis = [0.0,0.0,-1.0];
60
61 robot.joints.shoulder_right_yaw = {parent:"clavicle_right", child:"shoulder_right"};
62 robot.joints.shoulder_right_yaw.origin = {xyz: [0.0,-0.15,0.85], rpy:[Math.PI/2,0,0]};
63 robot.joints.shoulder_right_yaw.axis = [0.0,0.707,0.707];
64
65 robot.joints.upperarm_right_pitch = {parent:"shoulder_right", child:"upperarm_right"};
66 robot.joints.upperarm_right_pitch.origin = {xyz: [0.0,0.0,0.7], rpy:[0,0,0]};
67 robot.joints.upperarm_right_pitch.axis = [0.0,1.0,0.0];
68
69 robot.joints.forearm_right_yaw = {parent:"upperarm_right", child:"forearm_right"};
70 robot.joints.forearm_right_yaw.origin = {xyz: [0.0,0.0,0.7], rpy:[0,0,0]};
71 robot.joints.forearm_right_yaw.axis = [1.0,0.0,0.0];
72
73 robot.joints.clavicle_left_roll = {parent:"base", child:"clavicle_left"};
74 robot.joints.clavicle_left_roll.origin = {xyz: [-0.3,0.4,0.0], rpy:[-Math.PI/2,0,0]};
75 robot.joints.clavicle_left_roll.axis = [0.0,0.0,1.0];
76
77 // specify name of endeffector frame
78 robot.endeffector = {};
79 robot.endeffector.frame = "forearm_right_yaw";
80 robot.endeffector.position = [[0],[0],[0.5],[1]];
81
```

So we are asking you to populate the

- child (joint if any) of every link
- parent (joint) of every link

# FAQs on P2

## How do I go about kineval/kineval\_forward\_kinematics.js?

You only need functions from `kineval_matrix.js` at this point.

The suggested structure is:

1. `kineval.robotForwardKinematics()` calls `kineval.buildFKTransforms()`
2. `kineval.buildFKTransforms()` calls `traverseFKBase()`
3. `traverseFKBase()` calls `traverseFKLink()`
4. `traverseFKLink()` calls `traverseFKJoint()`
5. `traverseFKJoint()` calls `traverseFKLink()`

, traversing the kinematic tree in depth-first order from root (base) to leaves (links with no children).

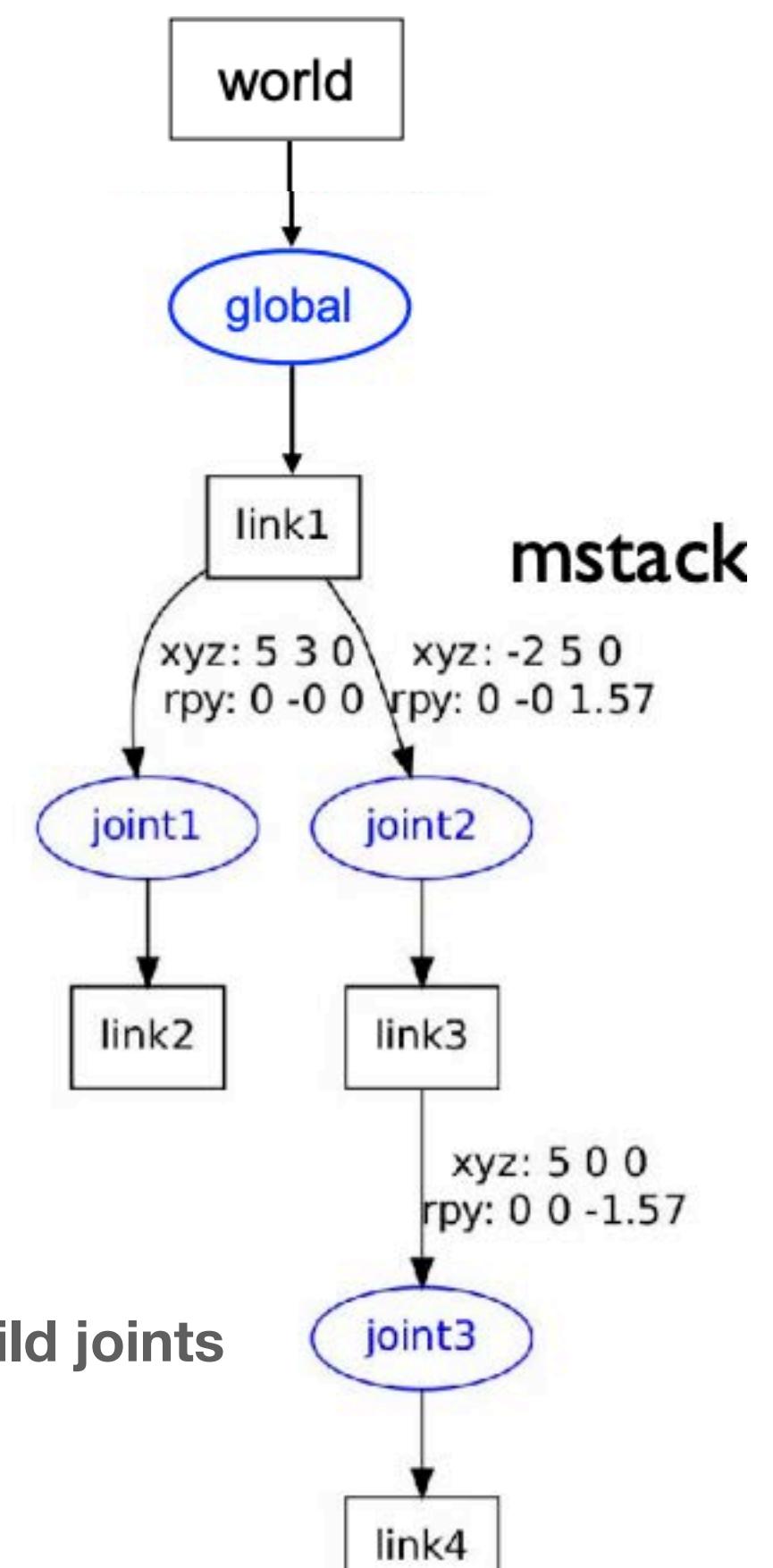
**traverseFKBase()**

**traverseFKLink()**

**traverseFKJoint()**

**traverseFKLink()**

Note: A link can have multiple child joints



# FAQs on P2

## How do I go about other robots (fetch, sawyer, baxter, etc)?

### Project Page Instructions:

- ROS uses a different default coordinate system than threejs, which needs to be taken into account in the FK computation for these three robots. ROS assumes that the Z, X, and Y axes correspond to the up, forward, and side directions, respectively. In contrast, threejs assumes that the Y, Z, and X axes correspond to the up, forward, and side directions. The variable `robot.links_geom_imported` will be set to true when geometries have been imported from ROS and set to false when geometries are defined completely within the robot description file. You will need to extend your FK implementation to compensate for the coordinate frame difference when this variable is set to true.
- You can test and debug your implementation by opening `home.html` with parameters attached to the back such as `?robot=robots/robot_mr2.js` `?robot=robots/robot_crawler.js` `?robot=robots/robot_urdf_example.js` `robots/fetch/fetch.urdf.js` `?robot=robots/sawyer/sawyer.urdf.js` `?robot=robots/baxter/baxter.urdf.js`. Your implementation should look like this:

Check for the variable `robot.links_geom_imported` inside your `traverseFKBase()`

### Project 2 Tips:

3. As ROS -> threejs changes the front/left/up direction of the axes, it directly affects only the transform of the base link and indirectly (through chained multiplication) affects all descendant joints and links. You should not change the order of multiplications and only apply the matrix on the base transform! The matrix for Y, Z, X (threejs) -> Z, X, Y (ROS) can be verified in the following way:

$$\begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \end{bmatrix} = R \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} = R \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} = R \begin{bmatrix} 0 \\ 1 \\ 0 \\ 1 \end{bmatrix}$$

Each representing Y -> Z, Z -> X, and X -> Y conversions.

If `robot.links_geom_imported` is true (For Fetch, Sawyer and Baxter), then multiply the Global Transform from robot base to the world, with additional one on the right that maps ROS to ThreeJs.

$$T_{\text{world}}_{\text{robot\_base}}$$

$$T_{\text{world}}_{\text{robot\_base}} T_{\text{ROS}}$$



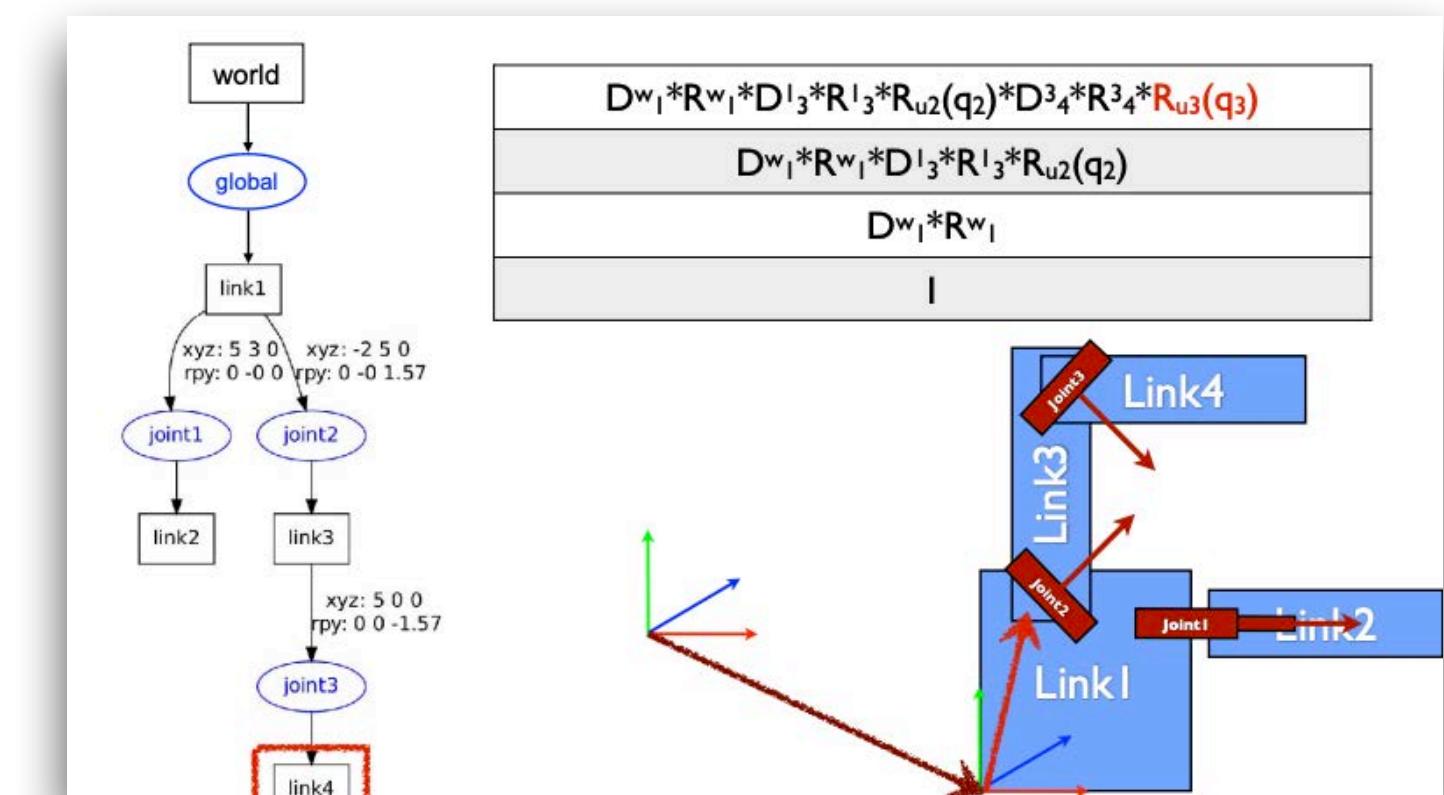
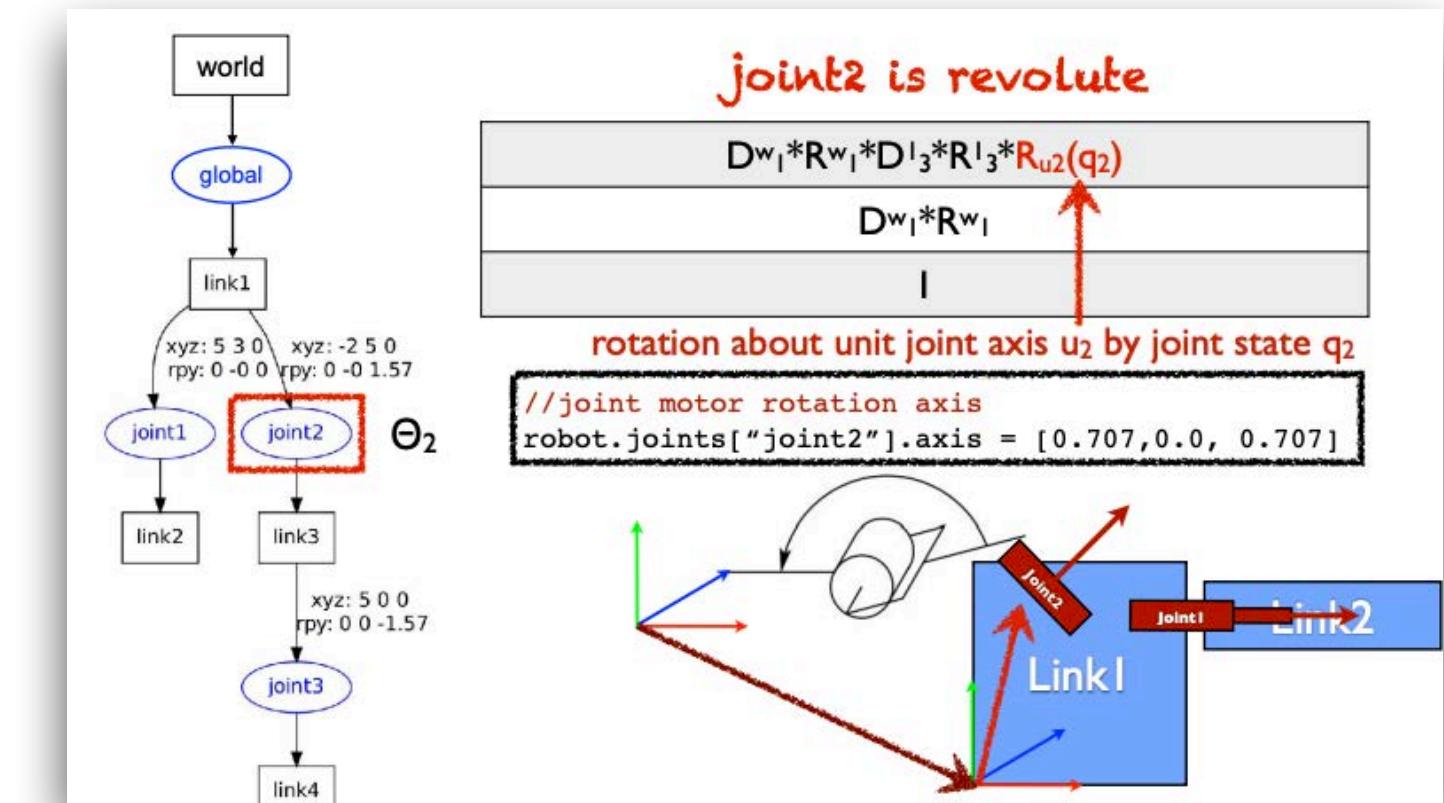
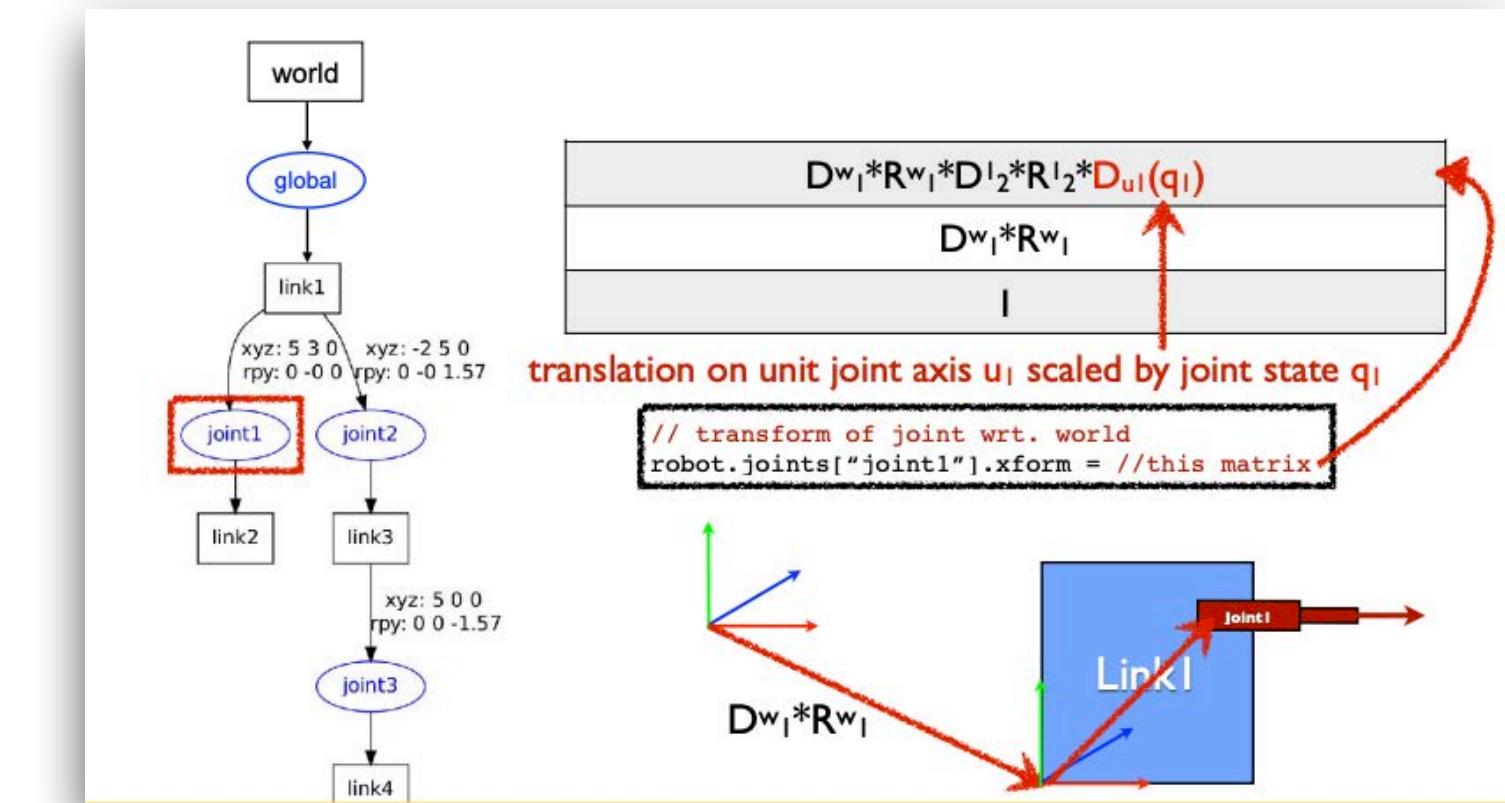
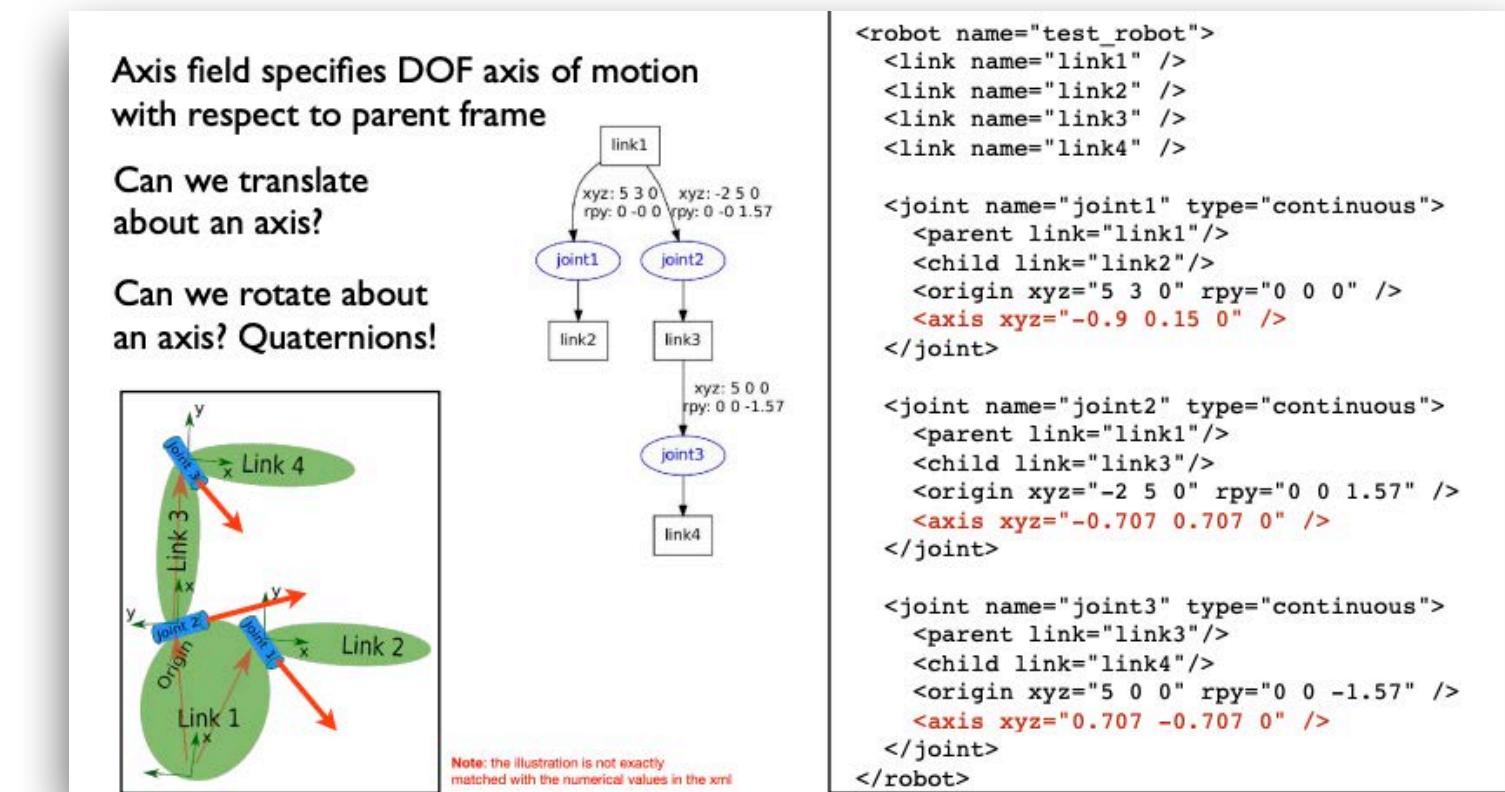
Please check Ed before coming to  
the course staff in the OH!



# Previously

```
// roll-pitch-yaw defined by ROS as corresponding to x-y-z
// http://wiki.ros.org/urdf/Tutorials/Create%20your%20Own%20URDF
robots/robot_urdf_example.js

// specify and create data objects for the joints of the robot
robot.joints = {};
robot.joints.joint1 = {parent: "link1", child: "link2"};
robot.joints.joint1.origin = {xyz: [0.5, 0.3, 0], rpy: [0, 0, 0]}; // simpler axis
robot.joints.joint1.axis = [-1.0, 0.0, 0]; // simpler axis
robot.joints.joint1.type = "continuous";
robot.joints.joint1.axis = [-0.9, 0.15, 0];
robot.joints.joint2 = {parent: "link1", child: "link3"};
robot.joints.joint2.origin = {xyz: [-0.2, 0.5, 0], rpy: [-0.707, 0.707, 0]}; // simpler axis
robot.joints.joint2.axis = [-0.707, 0.707, 0];
robot.joints.joint3 = {parent: "link3", child: "link4"};
robot.joints.joint3.origin = {xyz: [0.5, 0, 0], rpy: [0.707, -0.707, 0]}; // simpler axis
robot.joints.joint3.axis = [0.707, -0.707, 0];
// joint specifies
// • "parent" and "child" links
// • Transform parameters for joint wrt. link frame
//   • "xyz": T(x,y,z)
//   • "rpy": Rx(roll), Ry(pitch), Rz(yaw)
// • Joint "axis" of motion for DOF
// • "type" of joint motion for DOF state "angle"
//   • "continuous" for rotation without limits
//   • "revolute" for rotation within limits
//   • "prismatic" for translation within limits
/* threejs geometry definition template, will be
// create threejs geometry and insert into link
```



## Rotation by Quaternion

- Rotations are represented by unit quaternions
  - quaternion is point on 4D unit sphere geometrically
- Quaternion  $\mathbf{q} = (a, \mathbf{u}) = a + b\mathbf{i} + c\mathbf{j} + d\mathbf{k} = (\cos(\Theta/2), \mathbf{u} \sin(\Theta/2)) = [\cos(\Theta/2), u_x \sin(\Theta/2), u_y \sin(\Theta/2), u_z \sin(\Theta/2)]$
- $\mathbf{u} = [u_x, u_y, u_z]$  is rotation axis,  $\Theta$  rotation angle
- Rotating a 3D point  $\mathbf{p}$  by unit quaternion  $\mathbf{q}$  is performed by conjugation of  $\mathbf{v}$  by  $\mathbf{q}$ 
  - $\mathbf{v}' = \mathbf{qvq}^{-1}$ , where  $\mathbf{q}^{-1} = a - \mathbf{u}$ ,
  - quaternion  $\mathbf{v}$  is constructed from point  $\mathbf{p}$  as  $\mathbf{v} = 0 + \mathbf{p} = 0 + p_x\mathbf{i} + p_y\mathbf{j} + p_z\mathbf{k}$
  - rotated point  $\mathbf{p}' = [\mathbf{v}'_x \mathbf{v}'_y \mathbf{v}'_z]$  is pulled from quaternion resulting from conjugation

1) form unit quaternion from axis and motor angle  
 $\mathbf{q} = [\cos(\Theta/2), u_x \sin(\Theta/2), u_y \sin(\Theta/2), u_z \sin(\Theta/2)]$

2) convert quaternion to rotation matrix
 

- Inhomogeneous conversion to 3D rotation matrix of  $\mathbf{q} = [q_0 \ q_1 \ q_2 \ q_3]^T$

$$\begin{bmatrix} 1 - 2(q_2^2 + q_3^2) & 2(q_1q_2 - q_0q_3) & 2(q_0q_2 + q_1q_3) \\ 2(q_1q_2 + q_0q_3) & 1 - 2(q_1^2 + q_3^2) & 2(q_2q_3 - q_0q_1) \\ 2(q_1q_3 - q_0q_2) & 2(q_0q_1 + q_2q_3) & 1 - 2(q_1^2 + q_2^2) \end{bmatrix}$$

or equivalently, homogeneous conversion

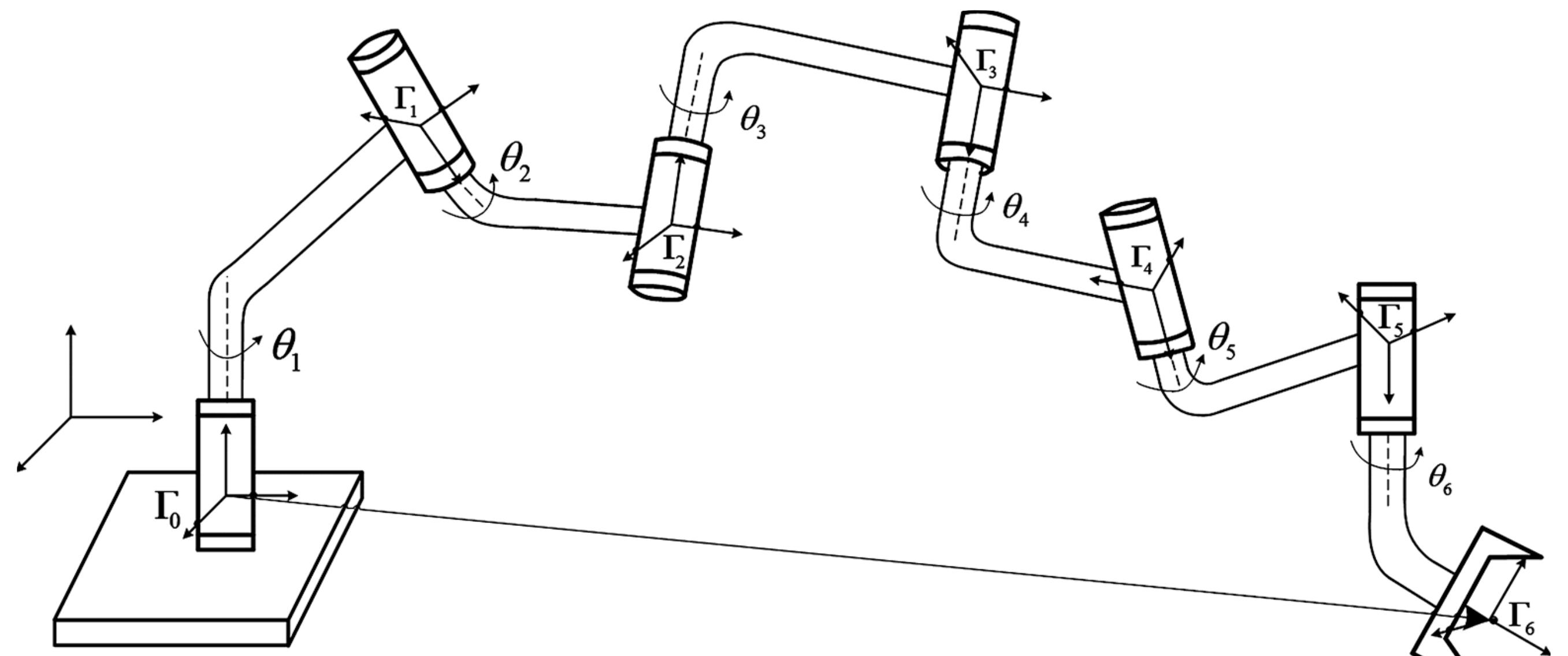
$$\begin{bmatrix} q_0^2 + q_1^2 - q_2^2 - q_3^2 & 2(q_1q_2 - q_0q_3) & 2(q_0q_2 + q_1q_3) \\ 2(q_1q_2 + q_0q_3) & q_0^2 - q_1^2 + q_2^2 - q_3^2 & 2(q_2q_3 - q_0q_1) \\ 2(q_1q_3 - q_0q_2) & 2(q_0q_1 + q_2q_3) & q_0^2 - q_1^2 - q_2^2 + q_3^2 \end{bmatrix}$$

• Rotation matrix to quaternion can also be performed

# Robot Kinematics

**Goal:** Given the structure of a robot arm, compute

- **Forward kinematics:** infer the pose of the end-effector, given the state of each joint.
- **Inverse kinematics:** infer the joint states to reach a desired end-effector pose.



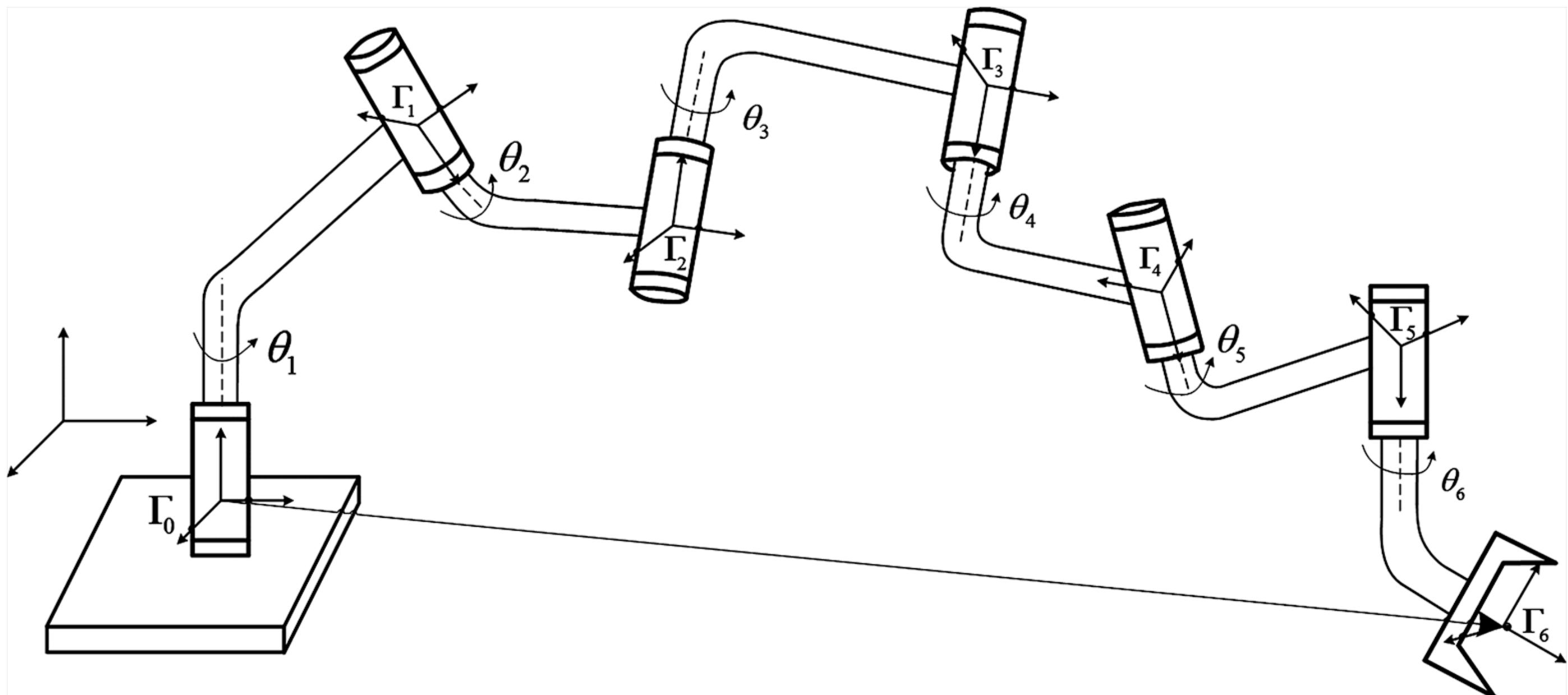
# Robot Kinematics

– **Forward kinematics**: infer the pose of the end-effector, given the state of each joint.

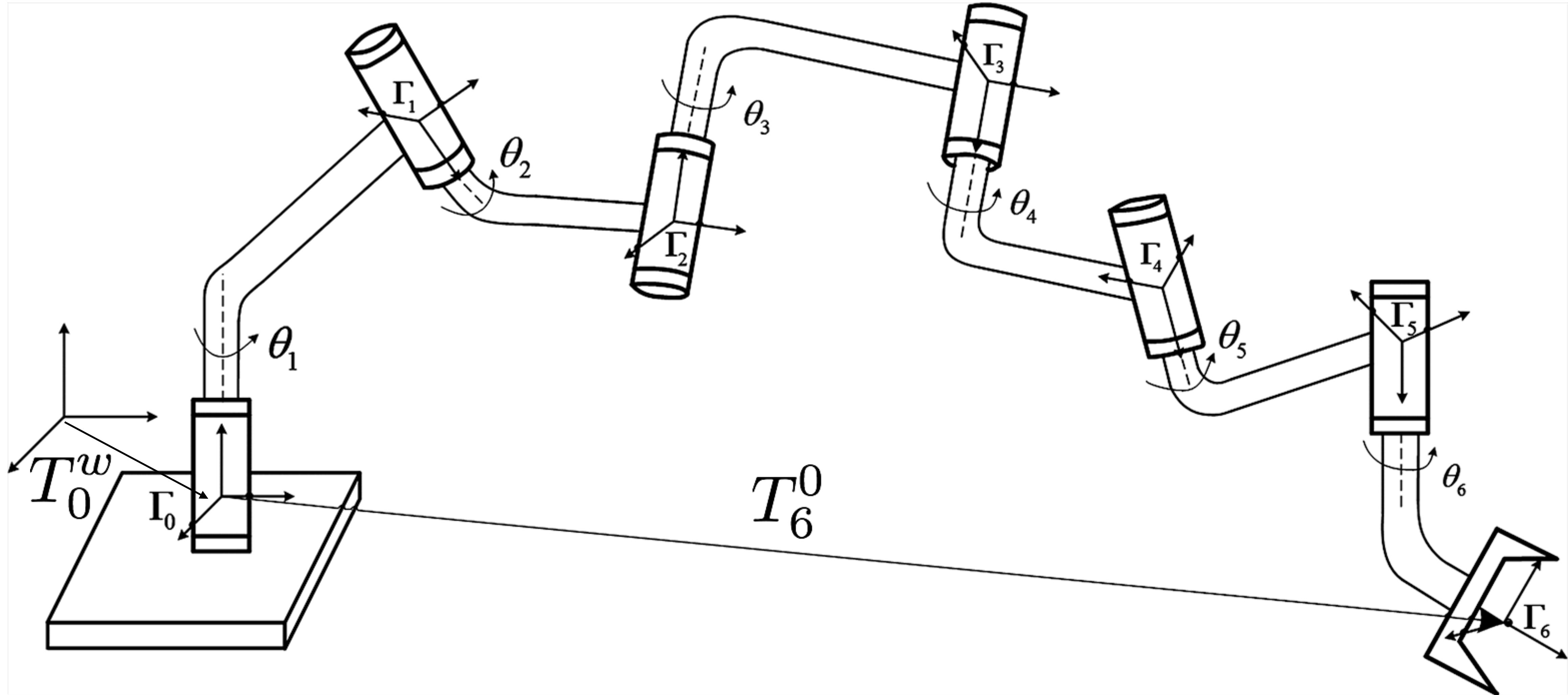
Infer: pose of each joint and link in a common world workspace

Assuming as given the:

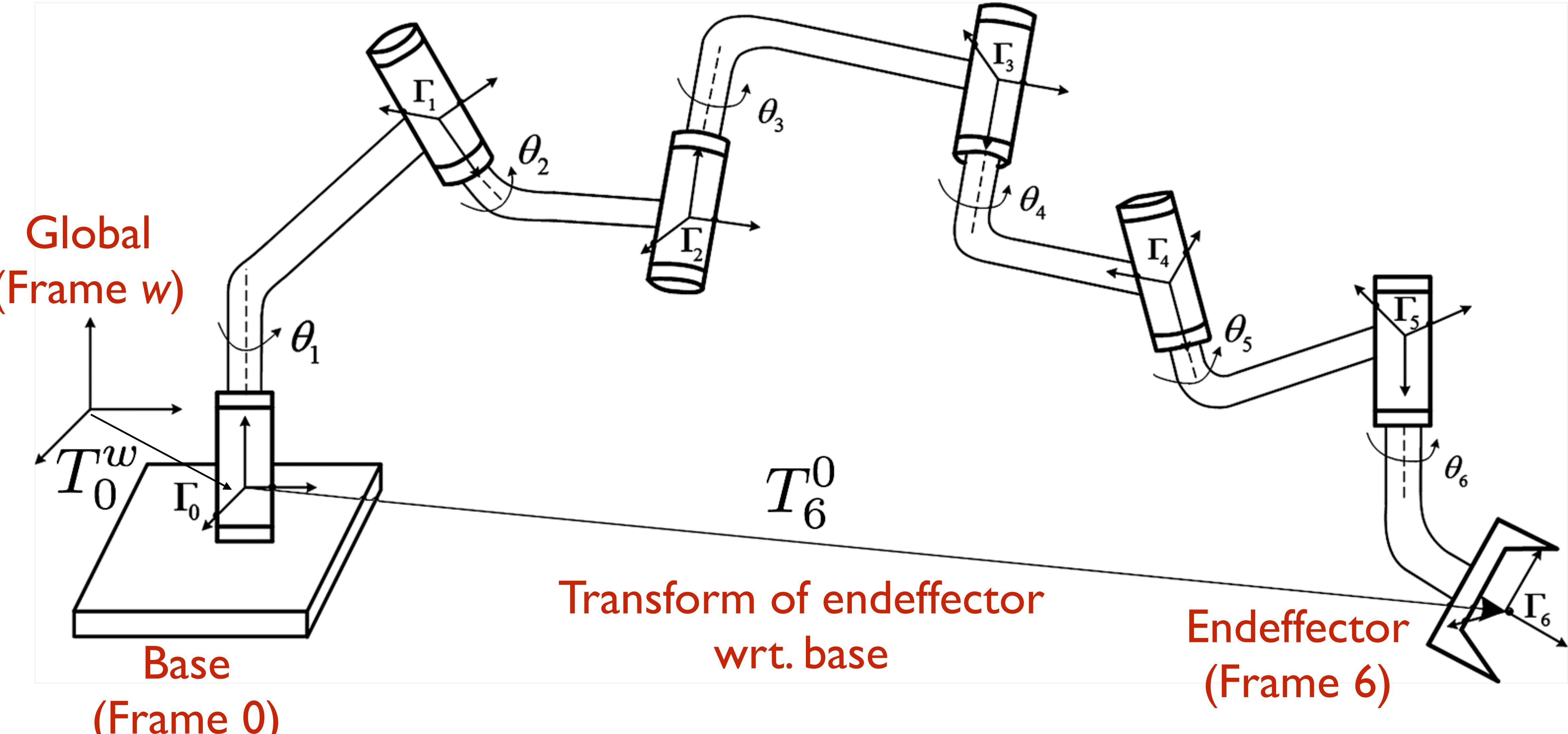
- robot's kinematic definition
- geometry of each link
- current state of all joints
  - zero configuration
  - add motor motion



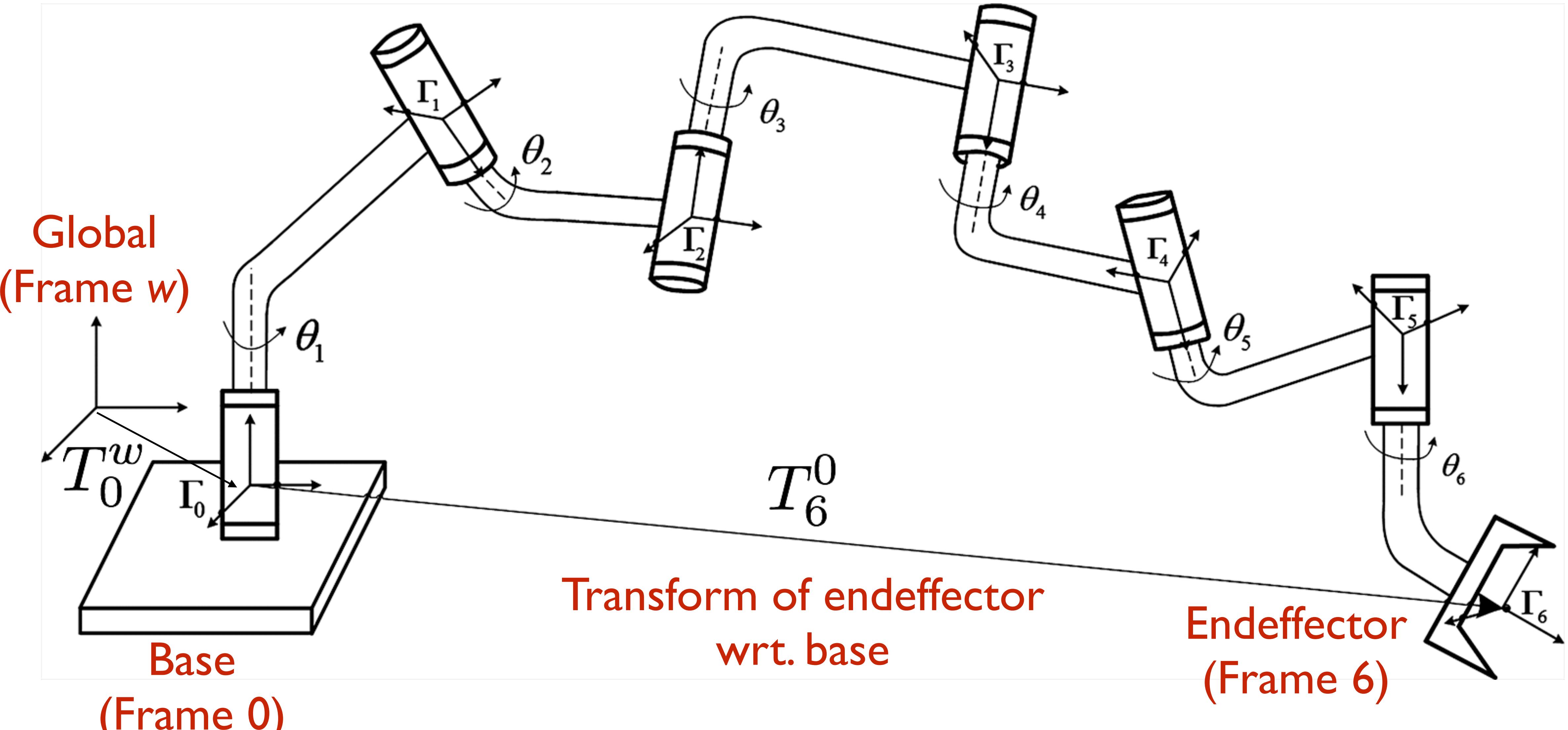
**Forward kinematics:** many-to-one mapping of robot configuration to reachable workspace endeffector poses



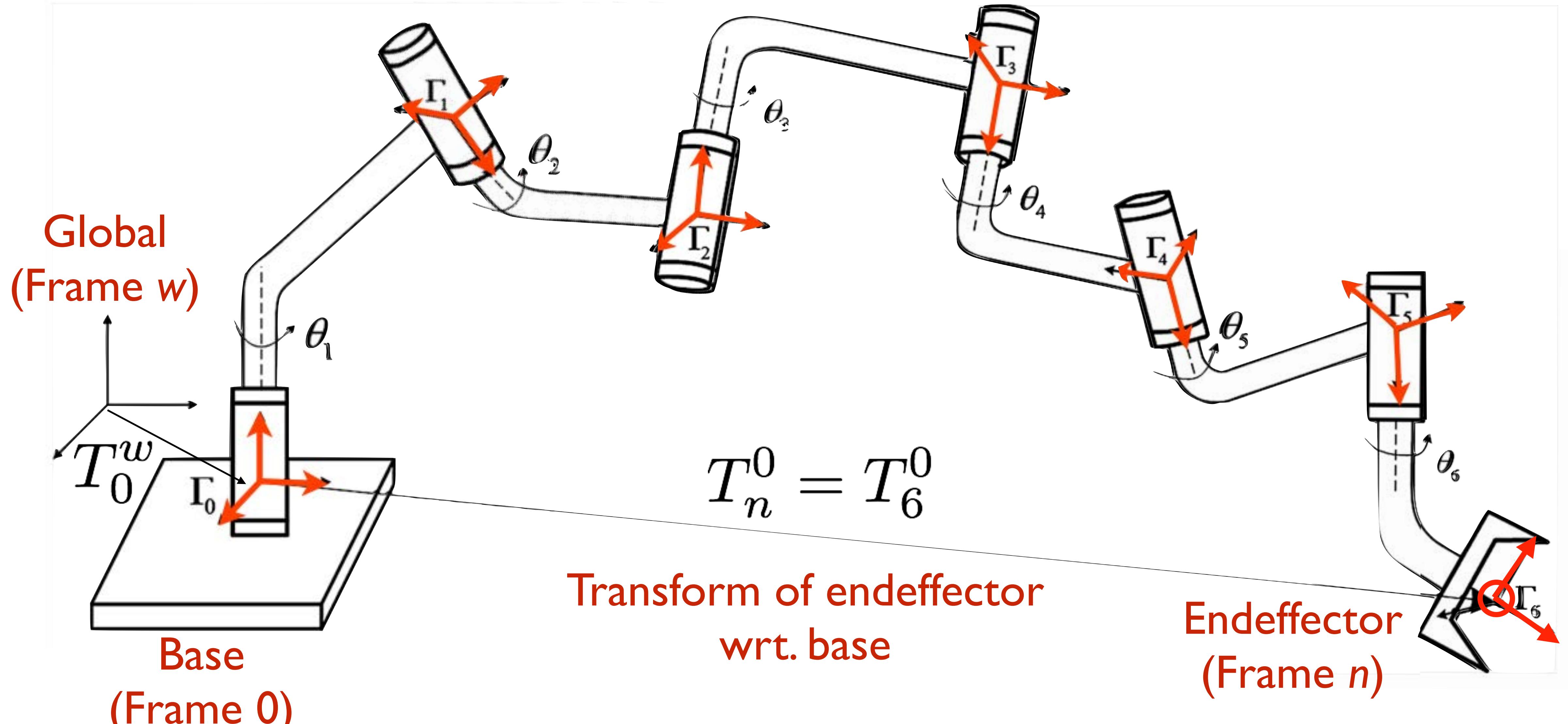
**Forward kinematics:** many-to-one mapping of robot configuration to reachable workspace endeffector poses



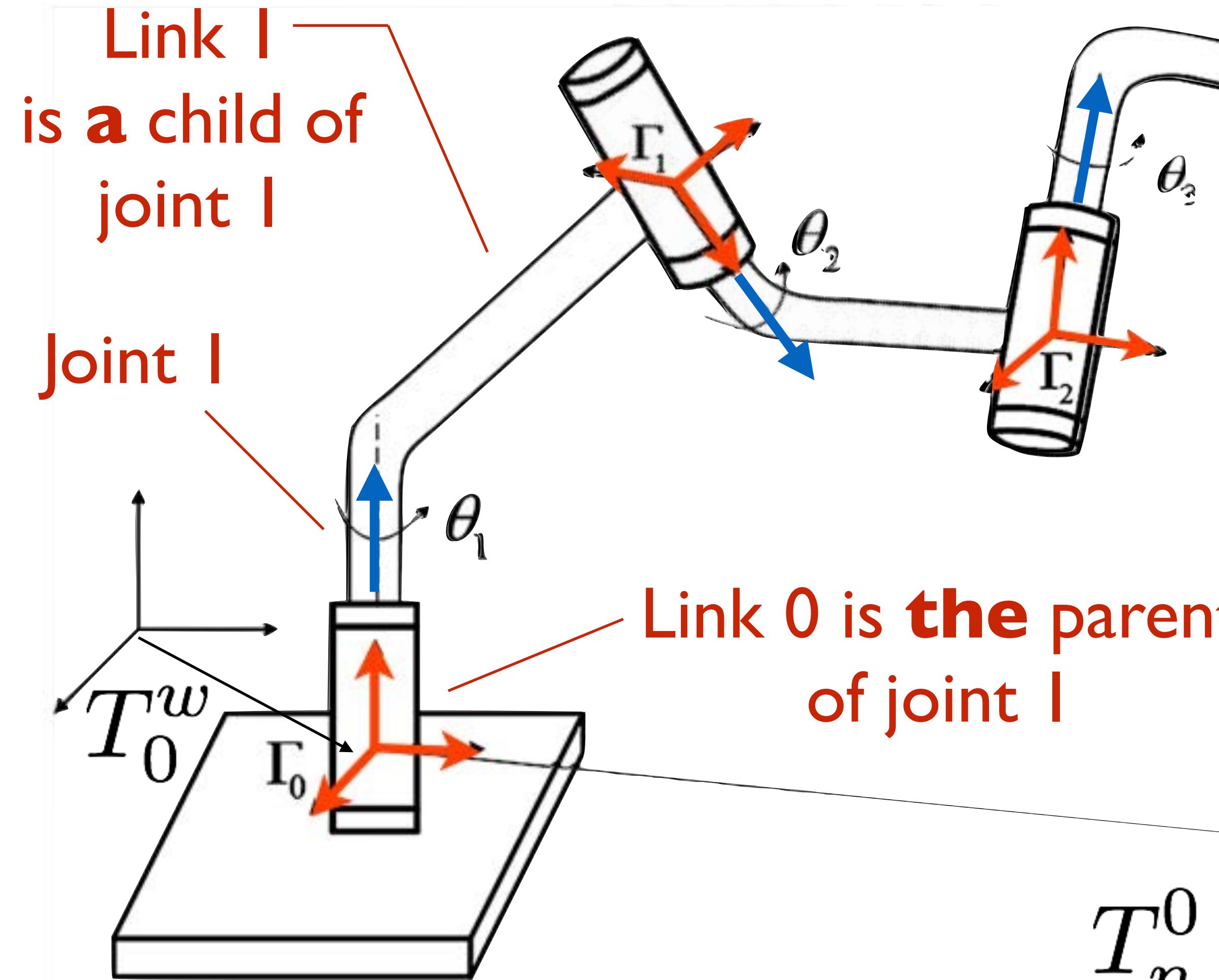
**Workspace:** 3D space defined in the global frame



**Kinematic chain:** connects  $N+1$  links together by  $N$  joints;  
with a coordinate frame on each link

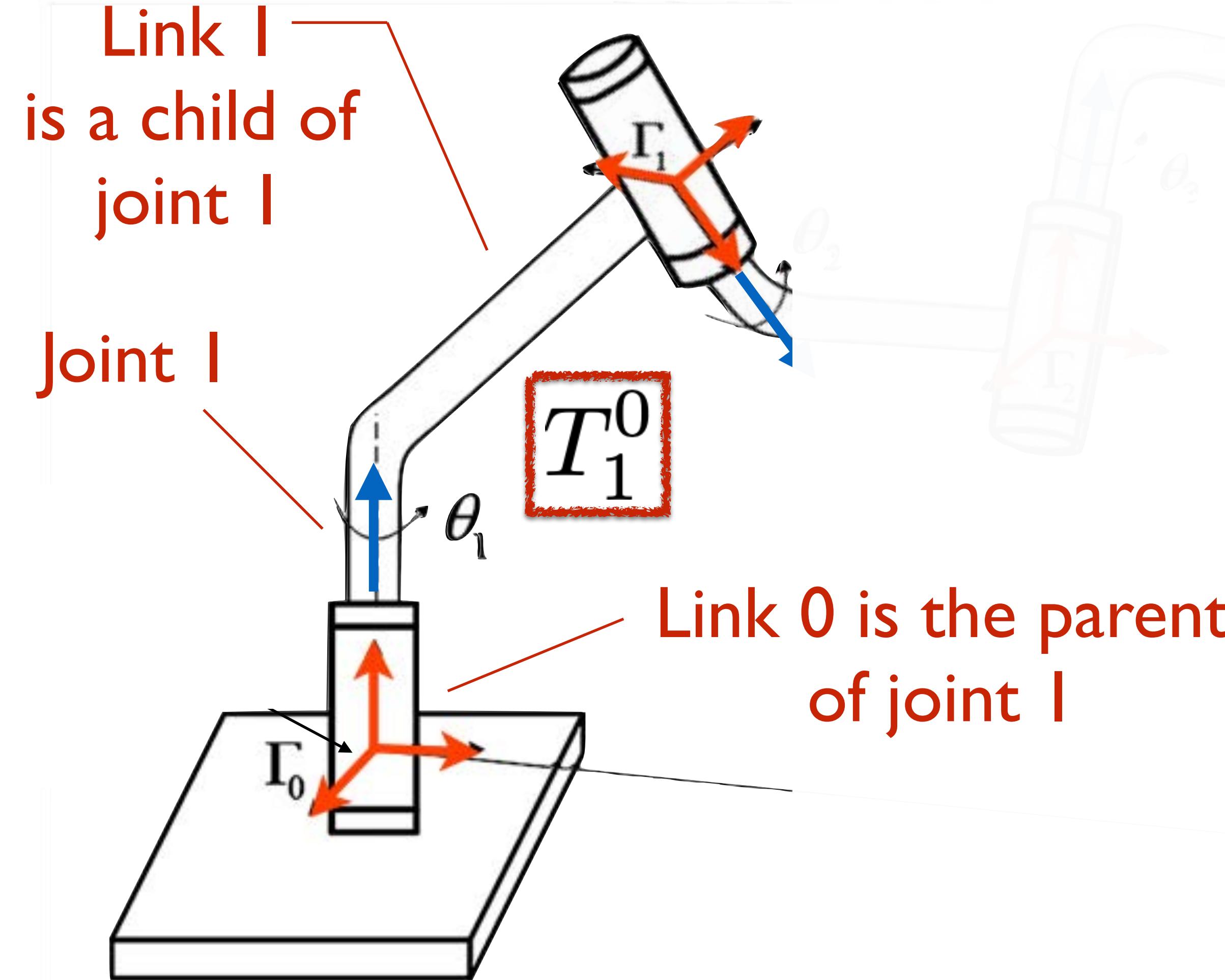


**Joint ( $q_i$ ):** relates the motion of one link (the child link) wrt. another link (the parent)  
joint motion only affects the child link



$$q_i = \begin{cases} \theta_i, & \text{if revolute} \\ d_i, & \text{if prismatic} \end{cases}$$

**Joint ( $q_i$ ):** relates the motion of one link (the child link) wrt. another link (the parent)  
joint motion only affects the child link, where its state



$$q_i = \begin{cases} \theta_i, & \text{if revolute} \\ d_i, & \text{if prismatic} \end{cases}$$

is used to express a 4-by-4 homogeneous transform  $\mathbf{A}_i(q_i)$ :

$$A_i = \begin{bmatrix} R_i^{i-1} & o^{i-1} \\ 0 & 1 \end{bmatrix}$$

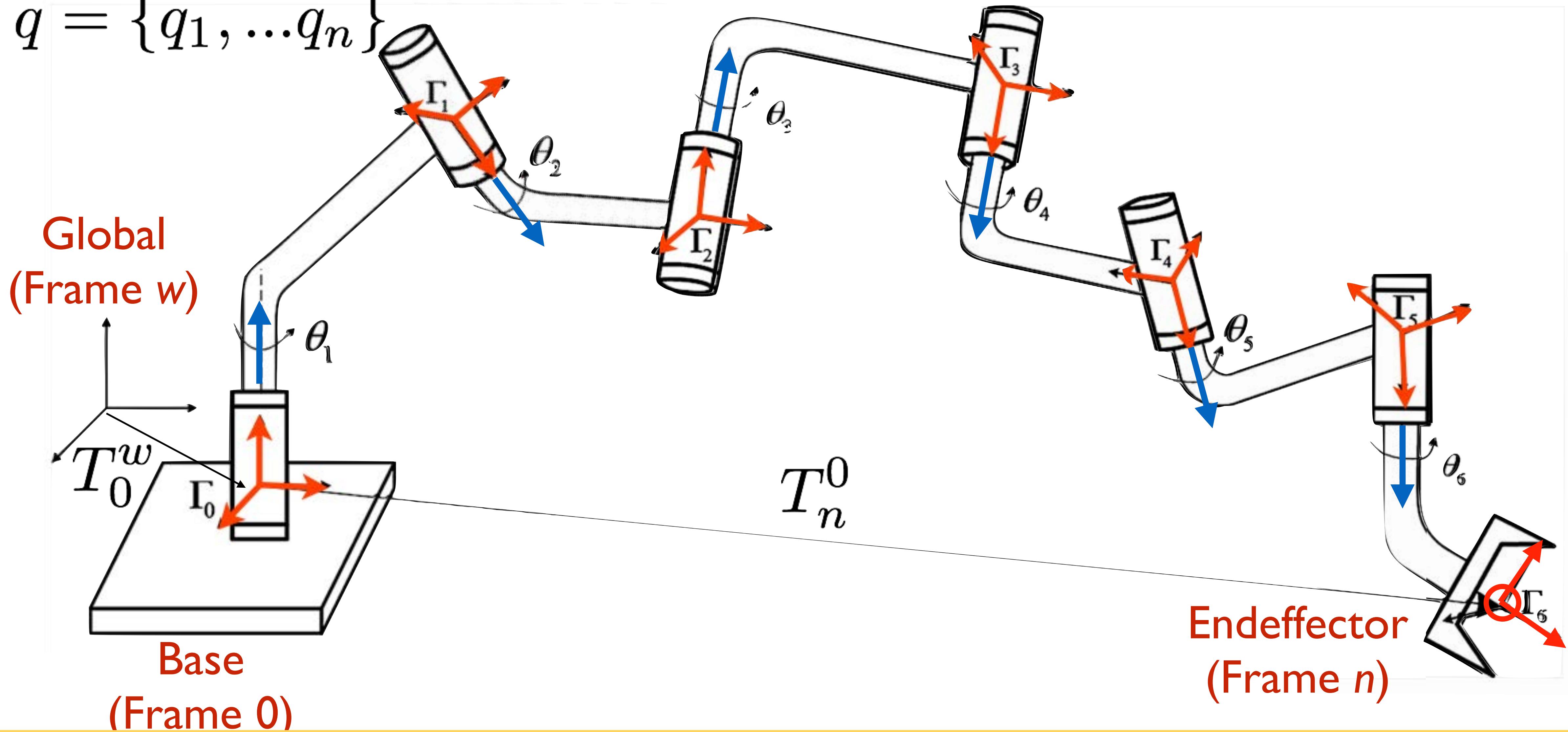
such that frames in a kinematic chain are related as by  $T_j^i$ :

$$T_j^i = \begin{cases} A_{i+1}A_{i+2}\dots A_{j-1}A_j & \text{if } i < j \\ I & \text{if } i = j \\ (T_j^i)^{-1} & \text{if } j > i \end{cases}$$

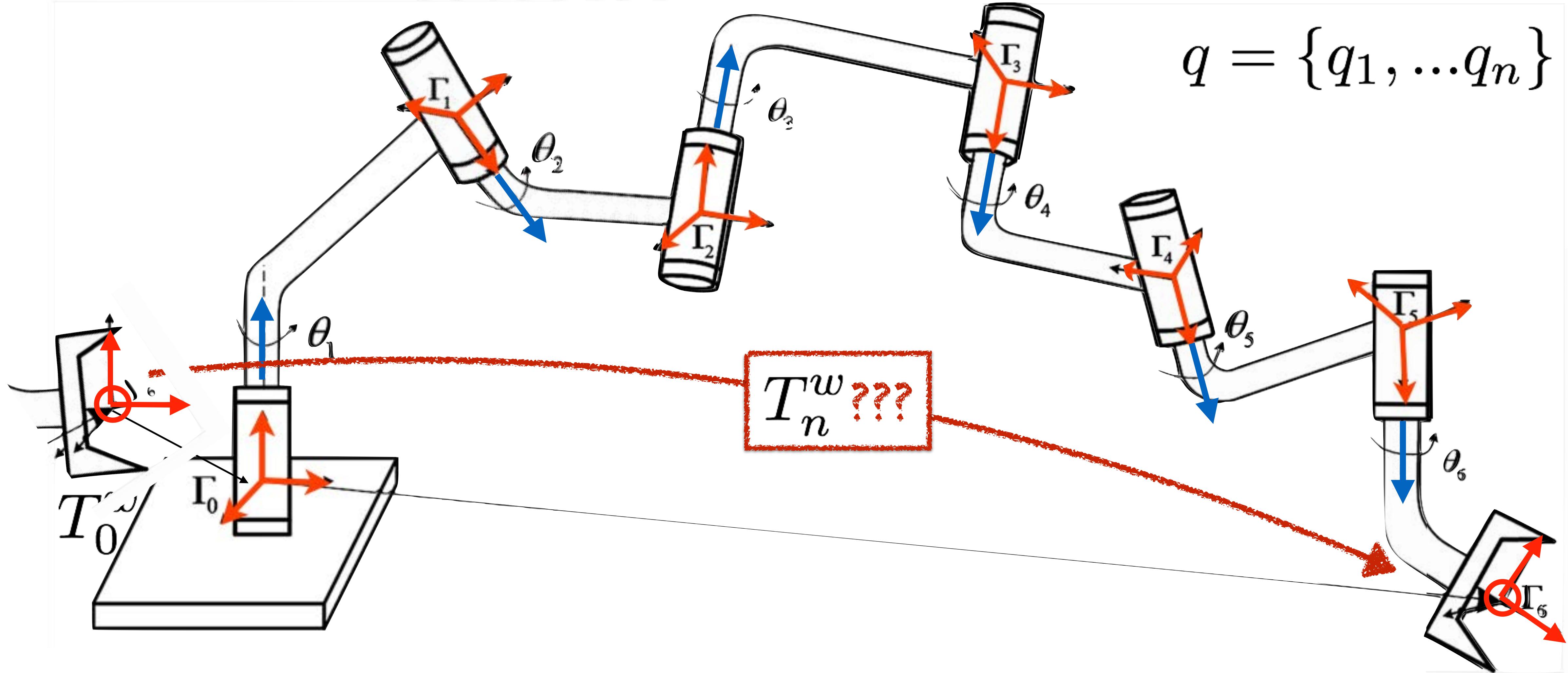
**Configuration ( $q$ ):** is the state of all joints in the kinematic chain

**Configuration space:** the space of all possible configurations

$$q = \{q_1, \dots q_n\}$$

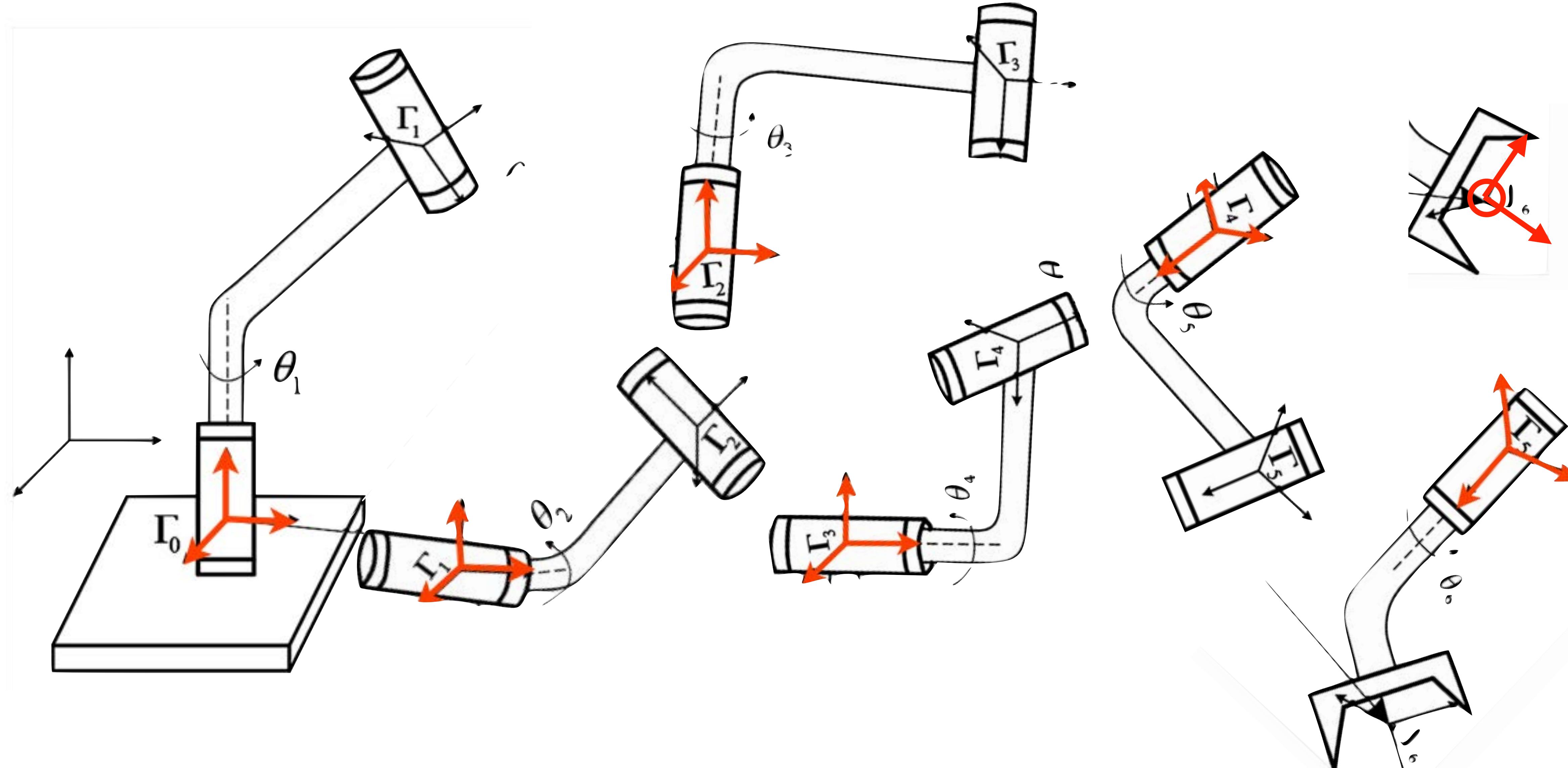


**Forward kinematics restated:** Given  $\mathbf{q}$ , find  $T^w_n$ ;  
 $T^w_n$  transforms endeffector into workspace

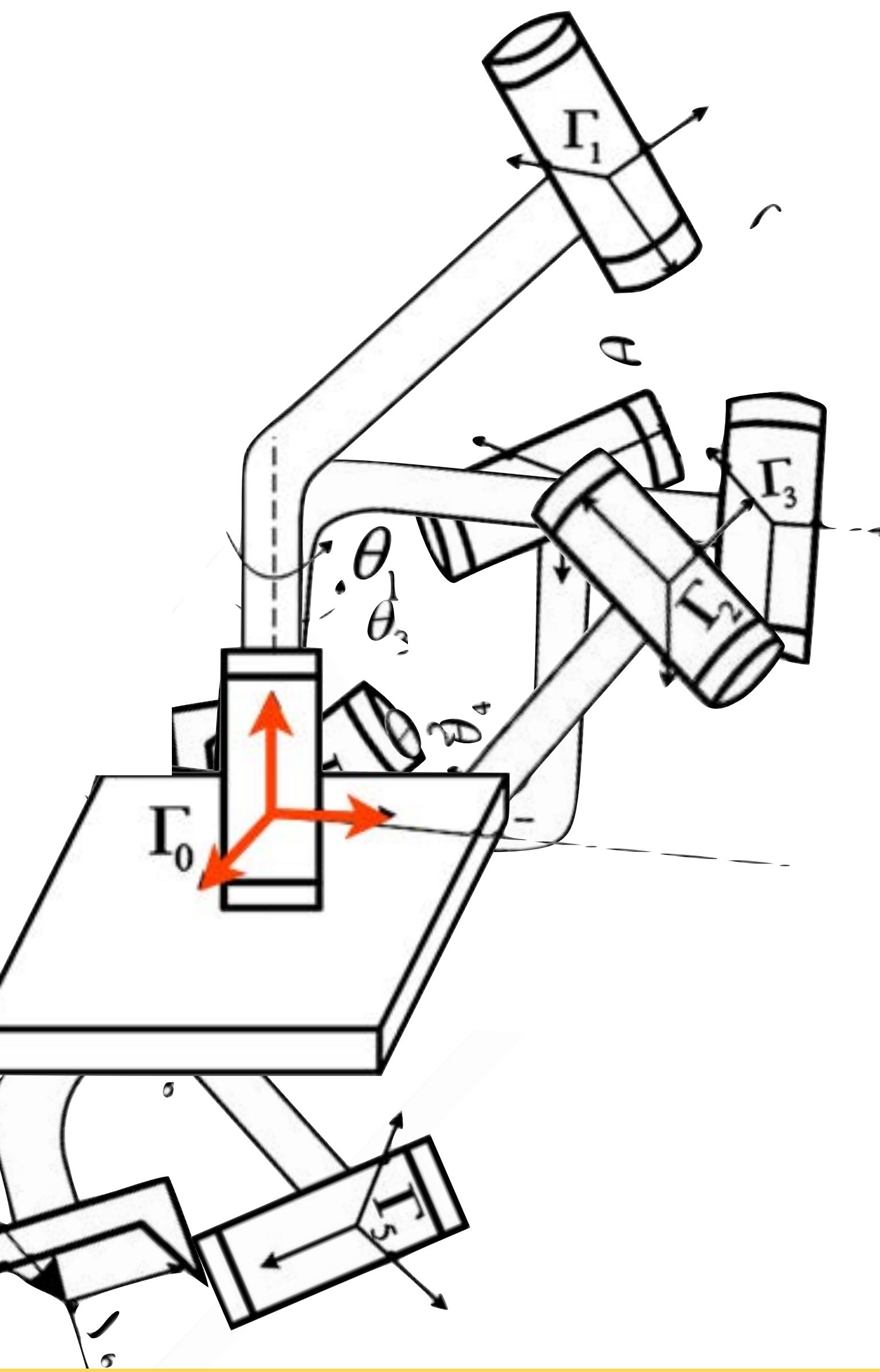


$$\mathbf{q} = \{q_1, \dots, q_n\}$$

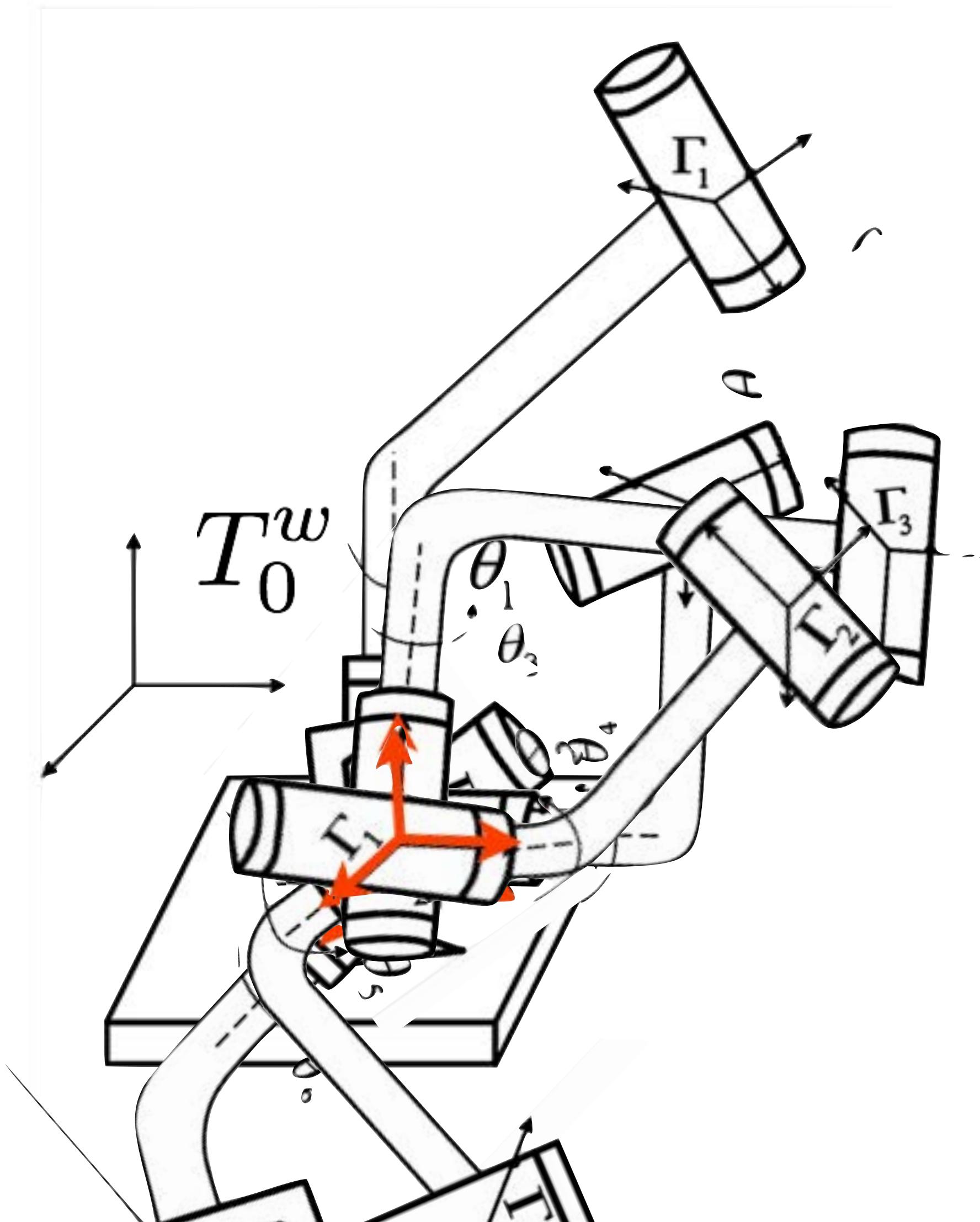
**Problem:** Every link considers itself to be the center of the universe.  
How do we properly pose link with respect to each other?

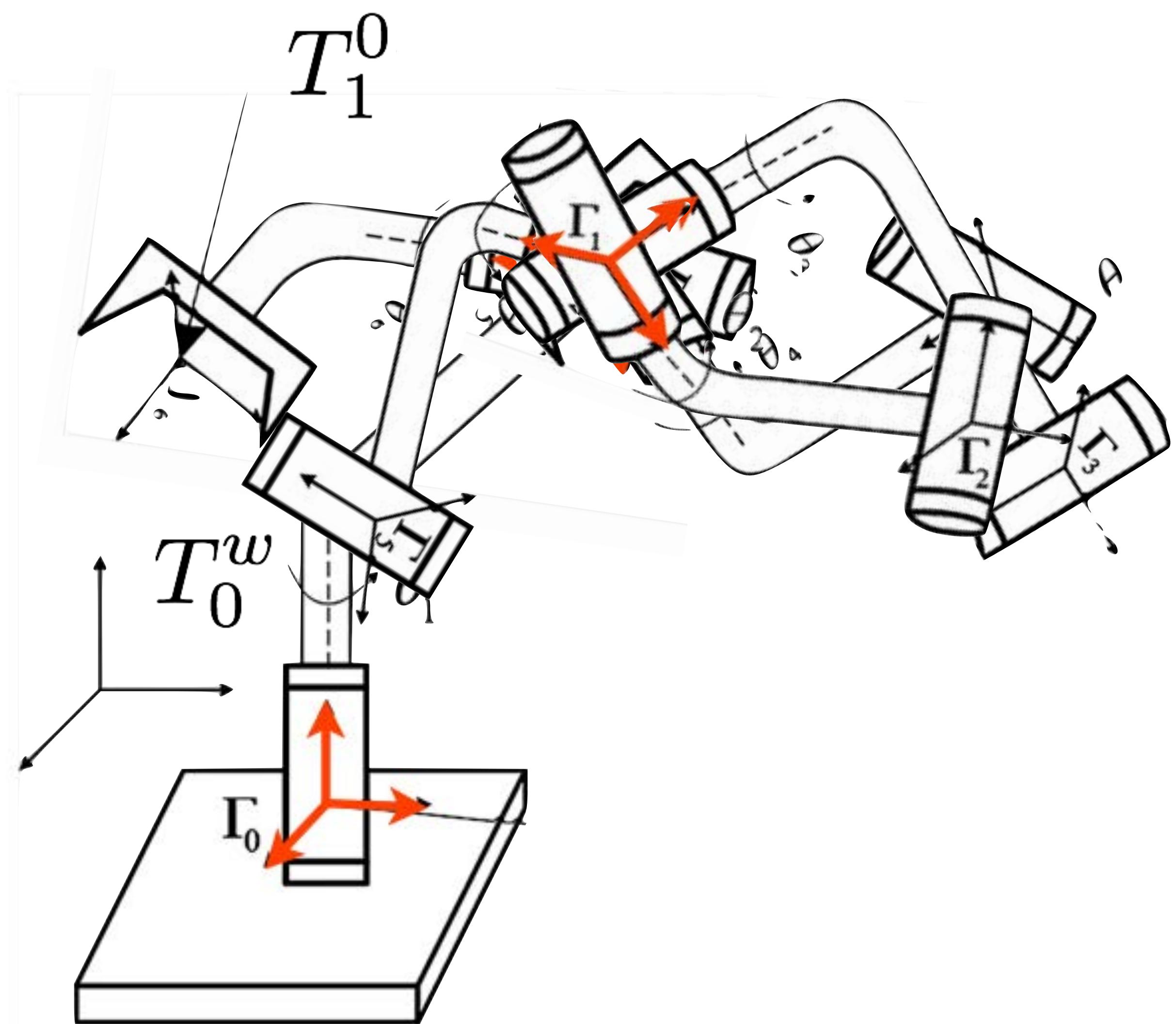


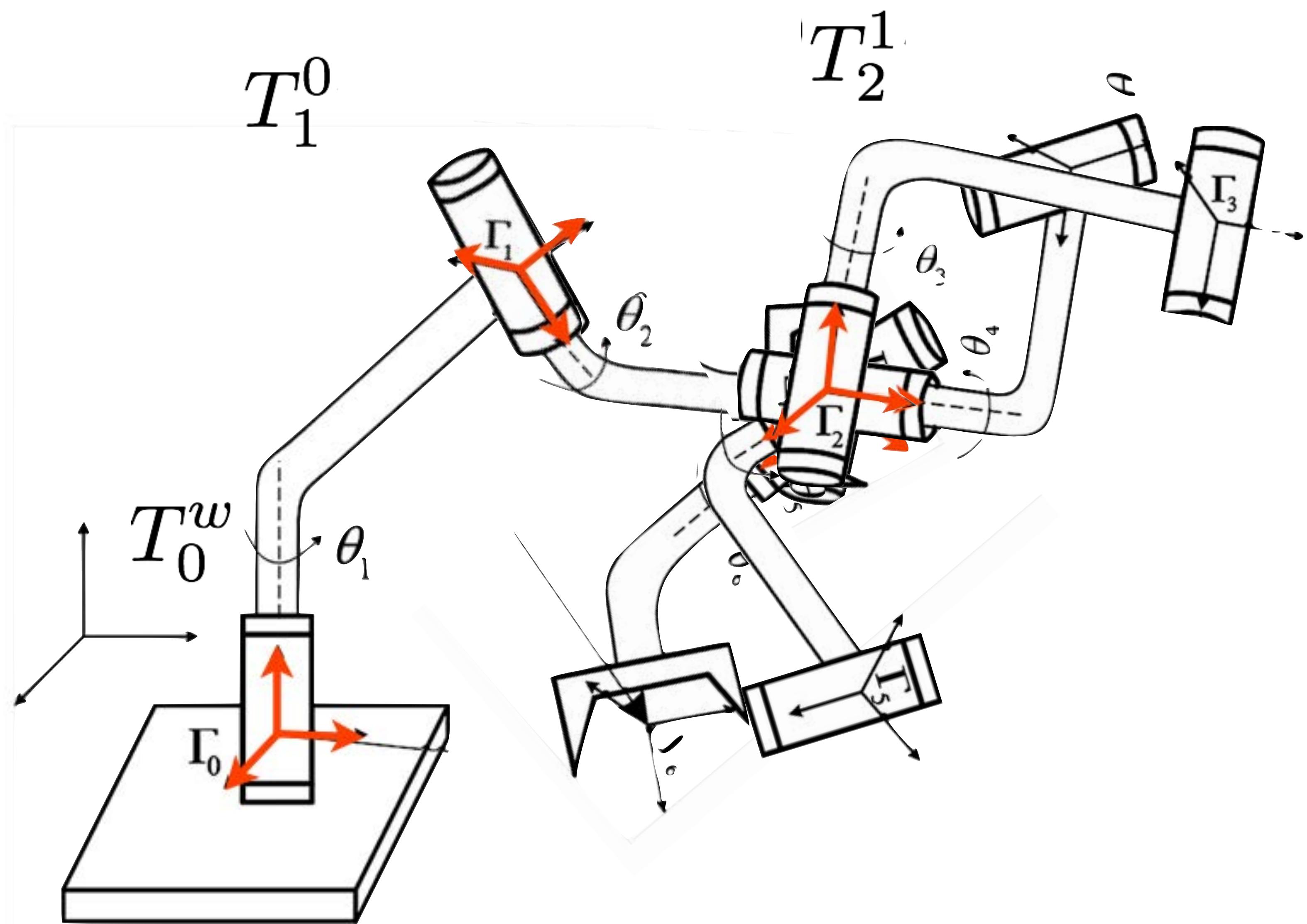
**Approach:** Consider all links to be aligned with the global origin ...

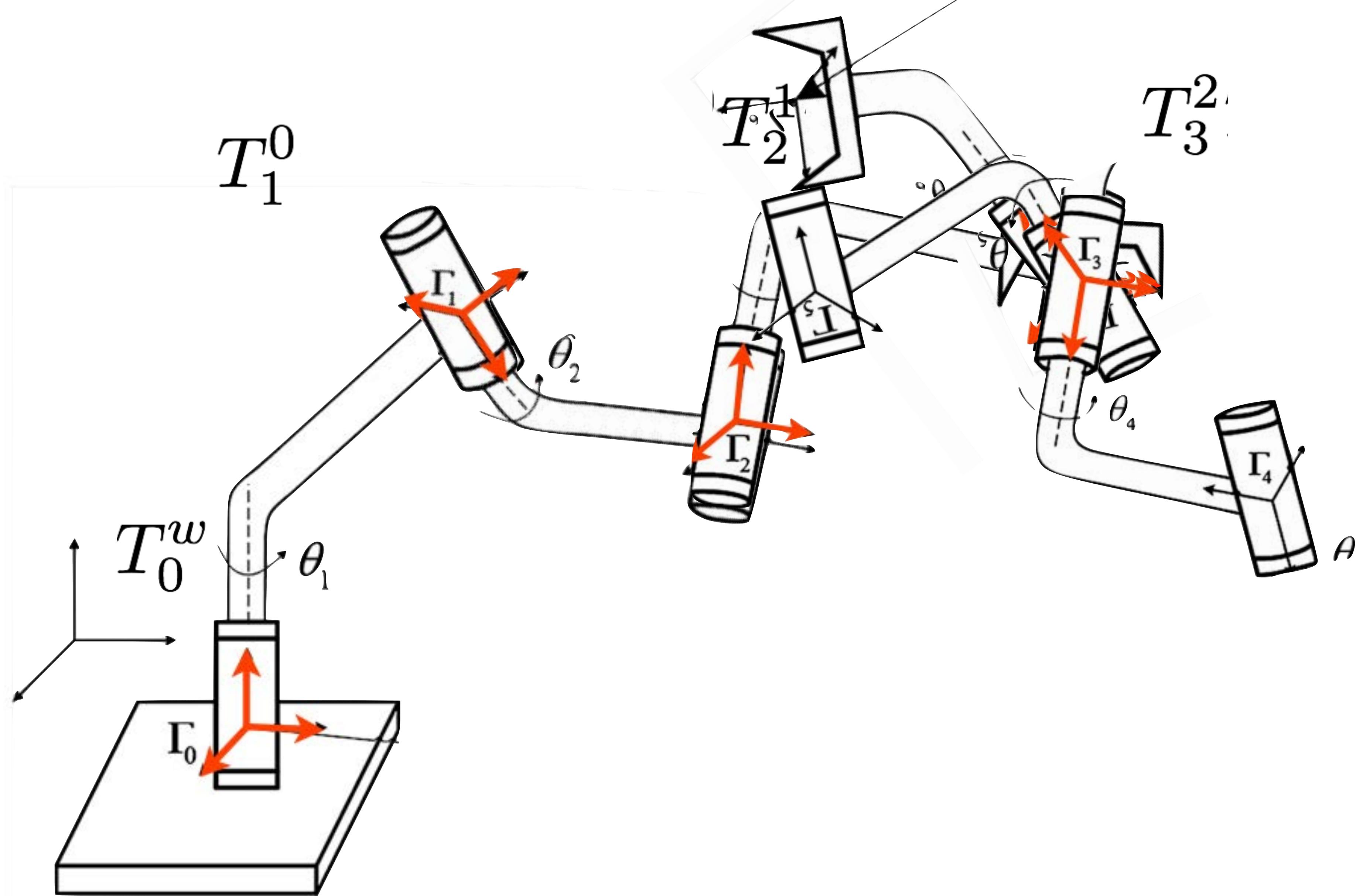


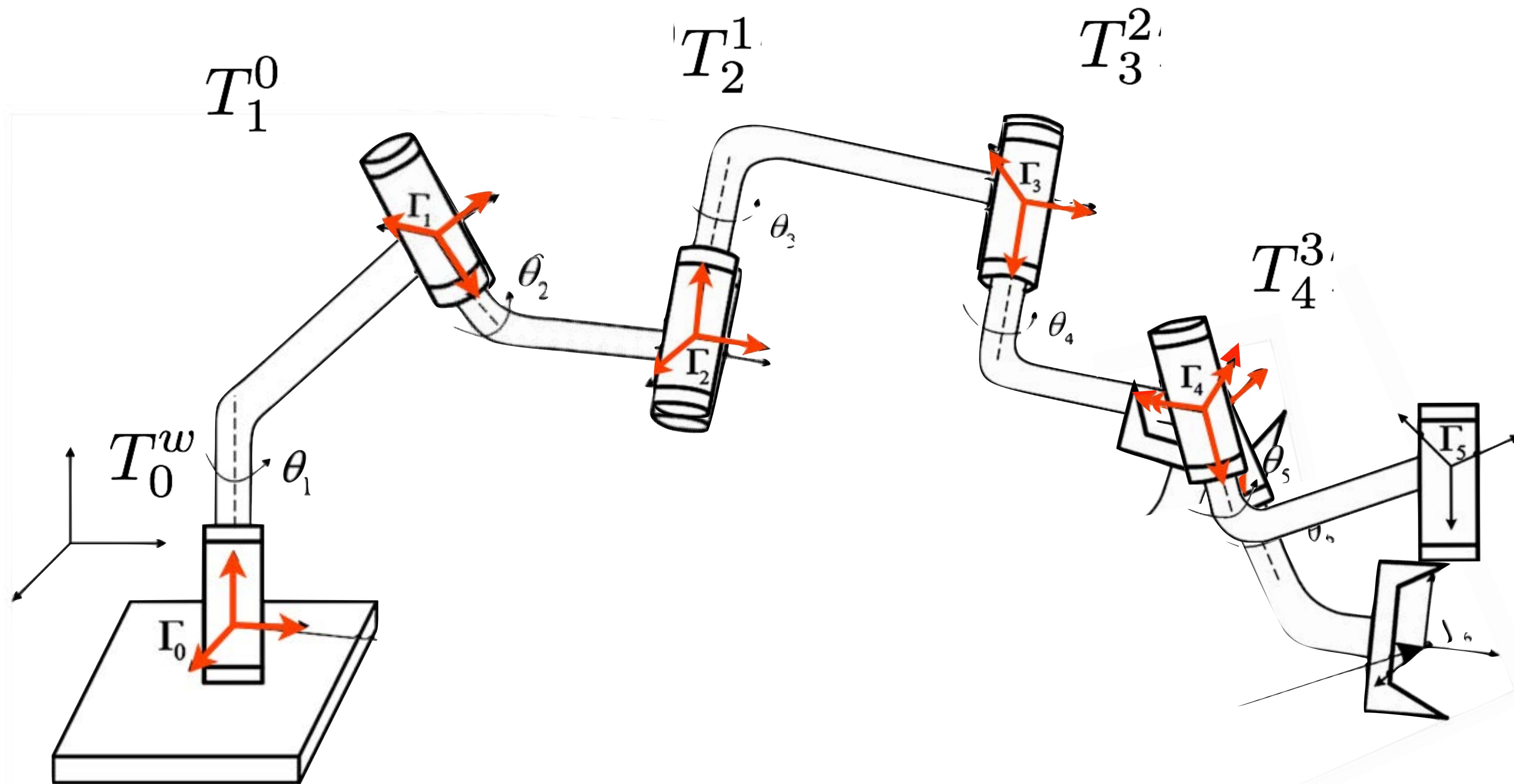
**Approach:** transform along kinematic chain bringing descendants along; each transform will consist of a rotation and a translation

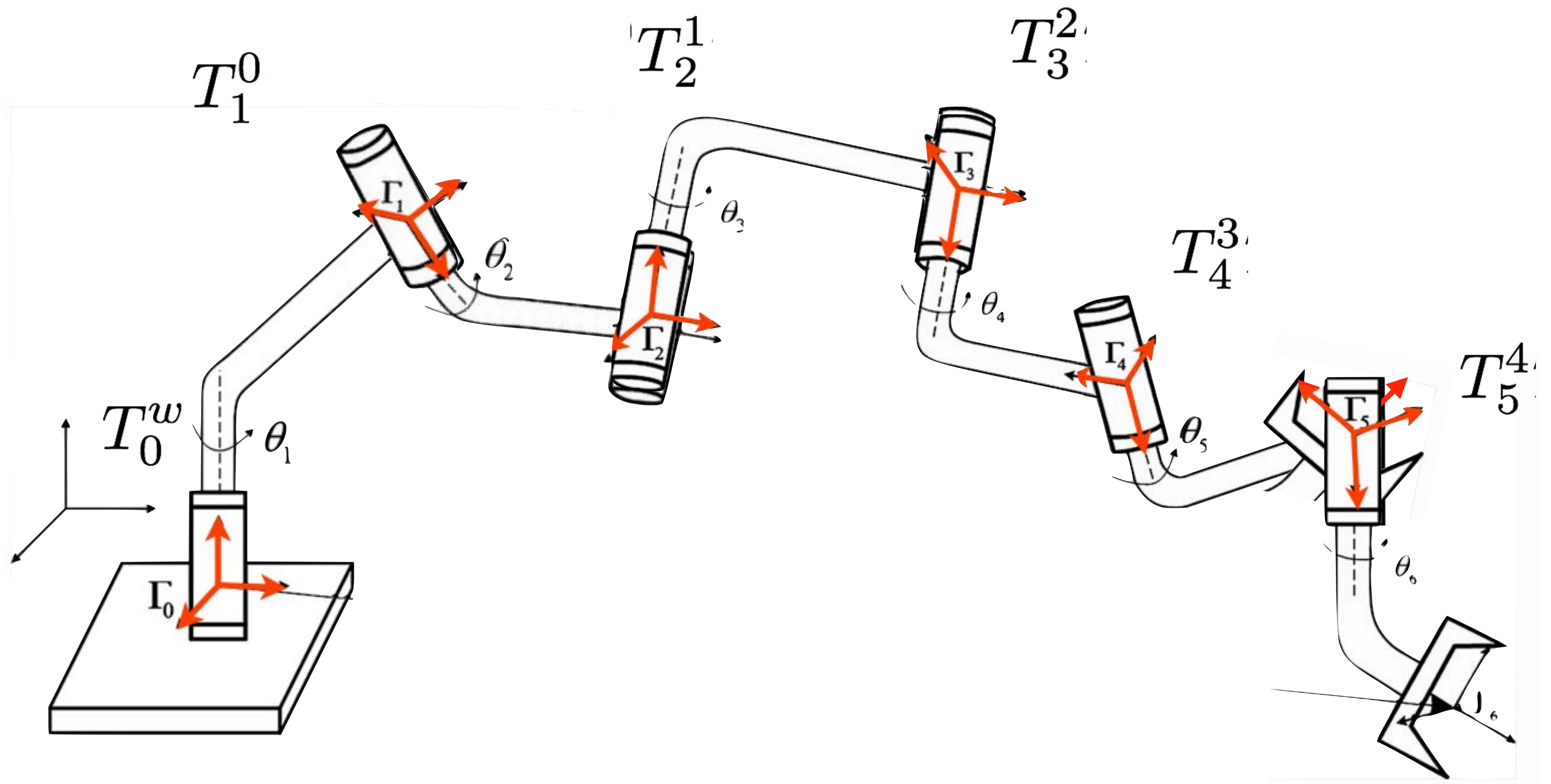


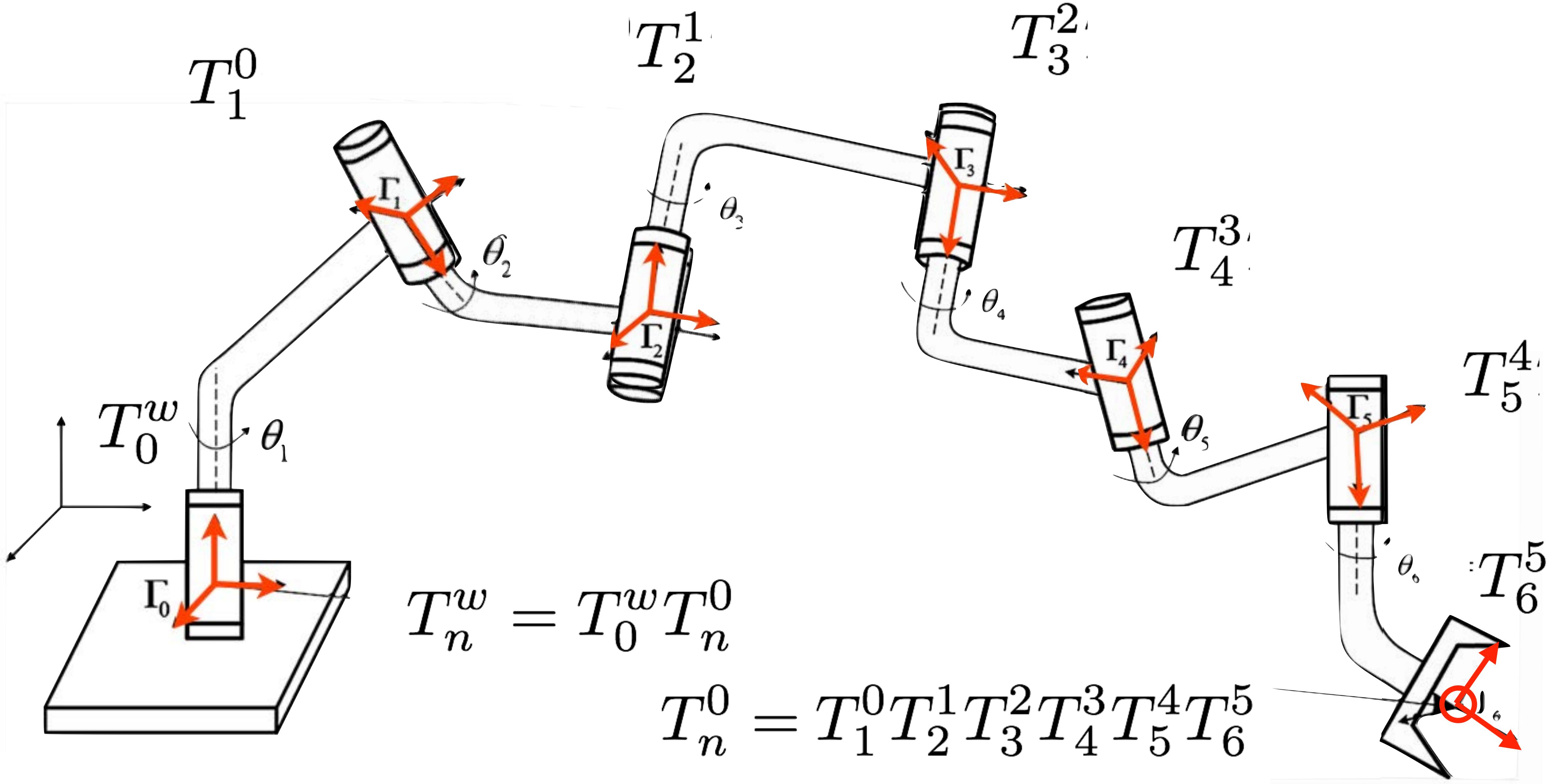




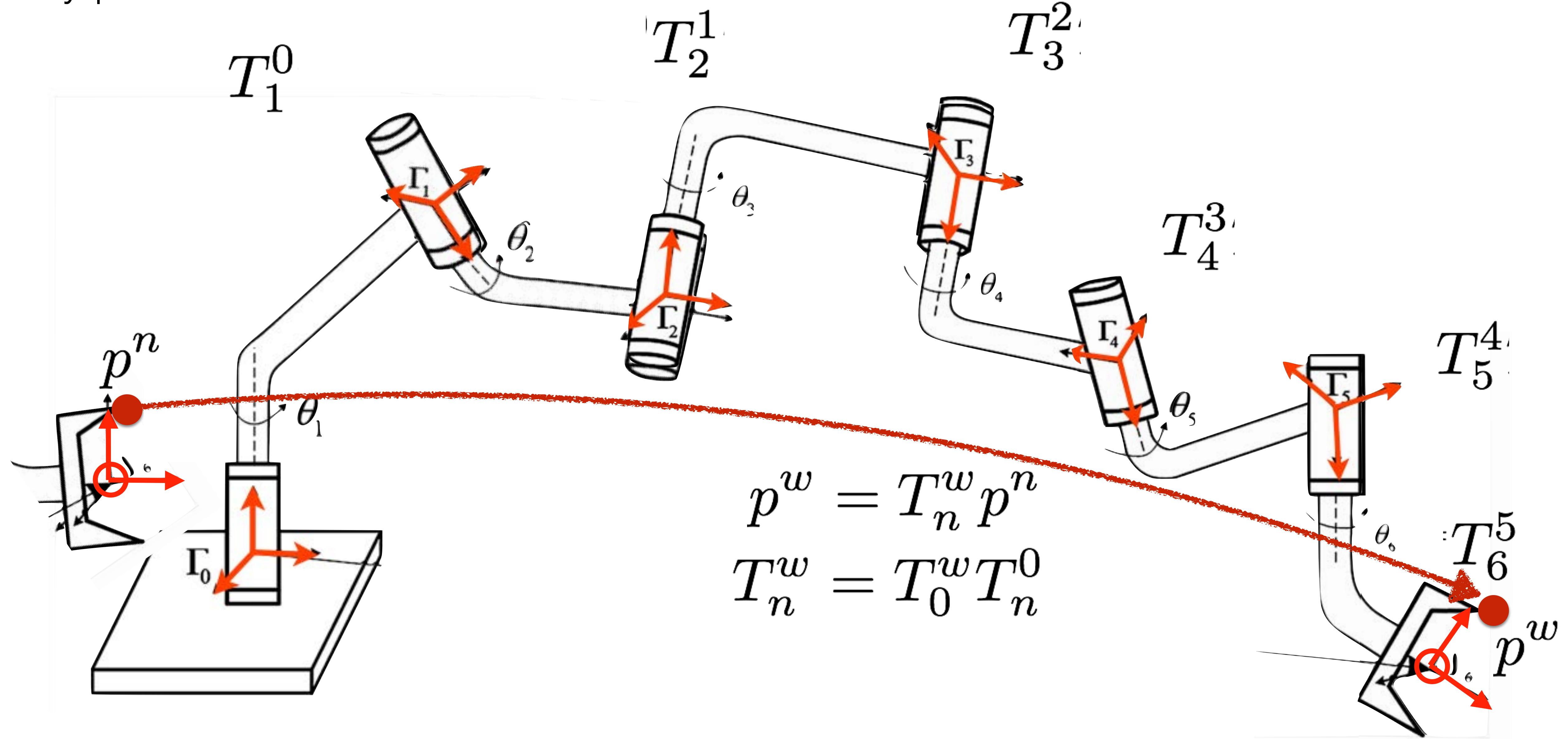




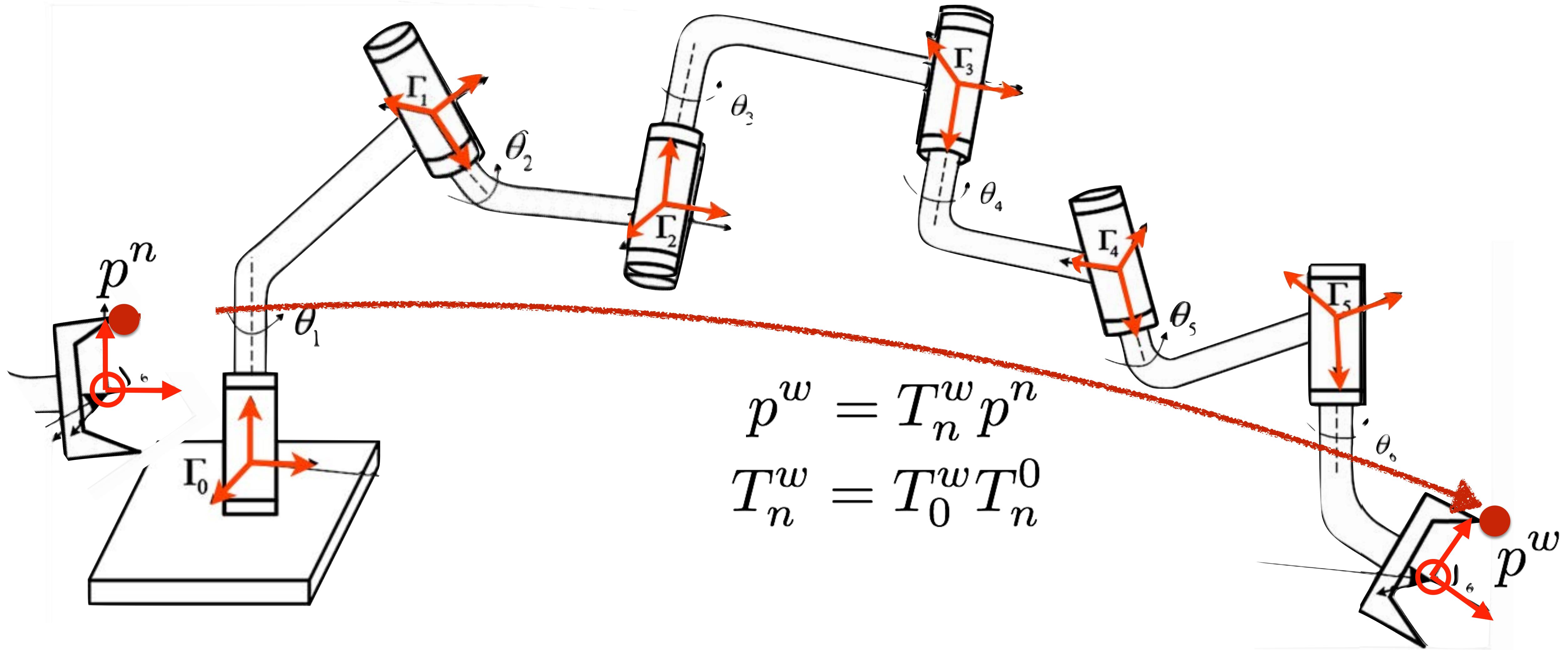




Any point on the endeffector can be transformed to its location in the world



- 1) How to represent homogeneous transforms?
- 2) How to compute transform to endeffector?



## Homogeneous Transform

defines  $SE(2)$ : Special Euclidean Group 2

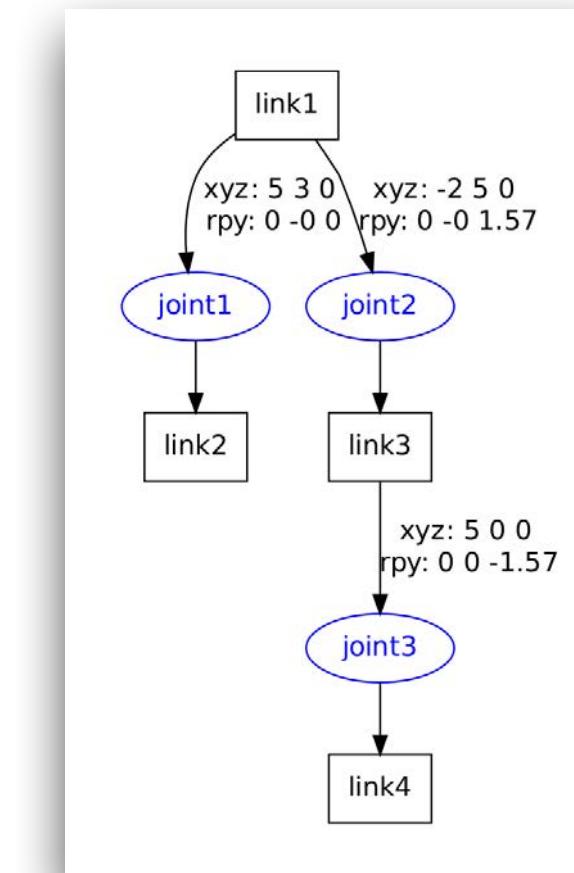
$$H = \begin{bmatrix} R_{00} & R_{01} & d_x \\ R_{10} & R_{11} & d_y \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \mathbf{R}_{2 \times 2} & \mathbf{d}_{2 \times 1} \\ \mathbf{0}_{1 \times 2} & 1 \end{bmatrix}$$

$$H \in SE(2) \quad \mathbf{R}_{2 \times 2} \in SO(2) \quad \mathbf{d}_{2 \times 1} \in \mathbb{R}^2$$

## 1) How to represent homogeneous transforms?

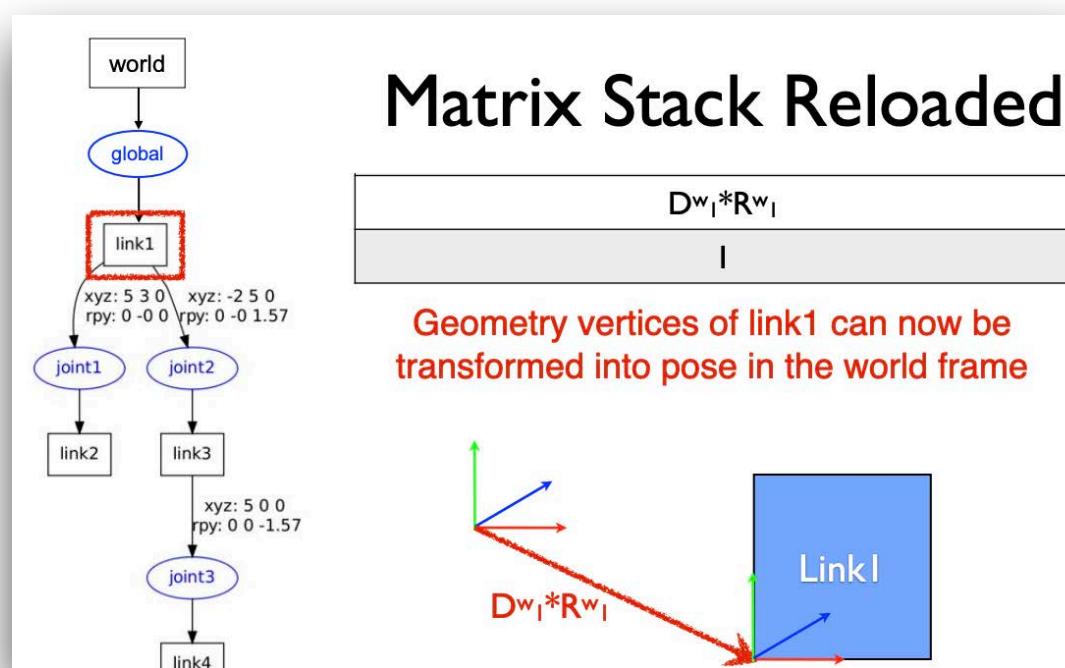
Assuming as given the:

- geometry of each link
- robot's kinematic definition



## 2) How to compute transform to endeffector?

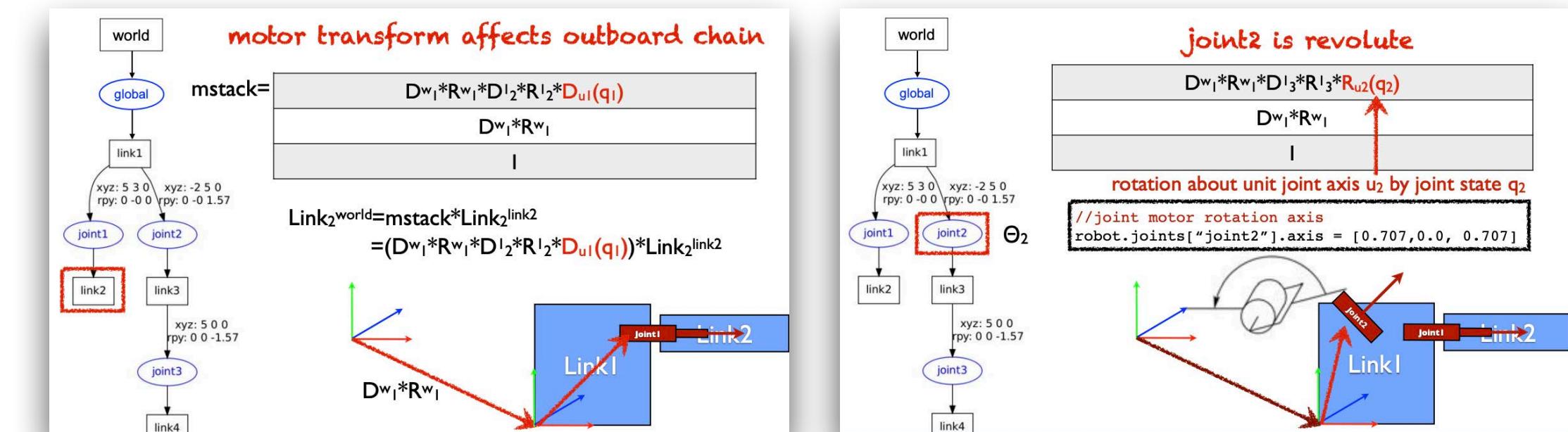
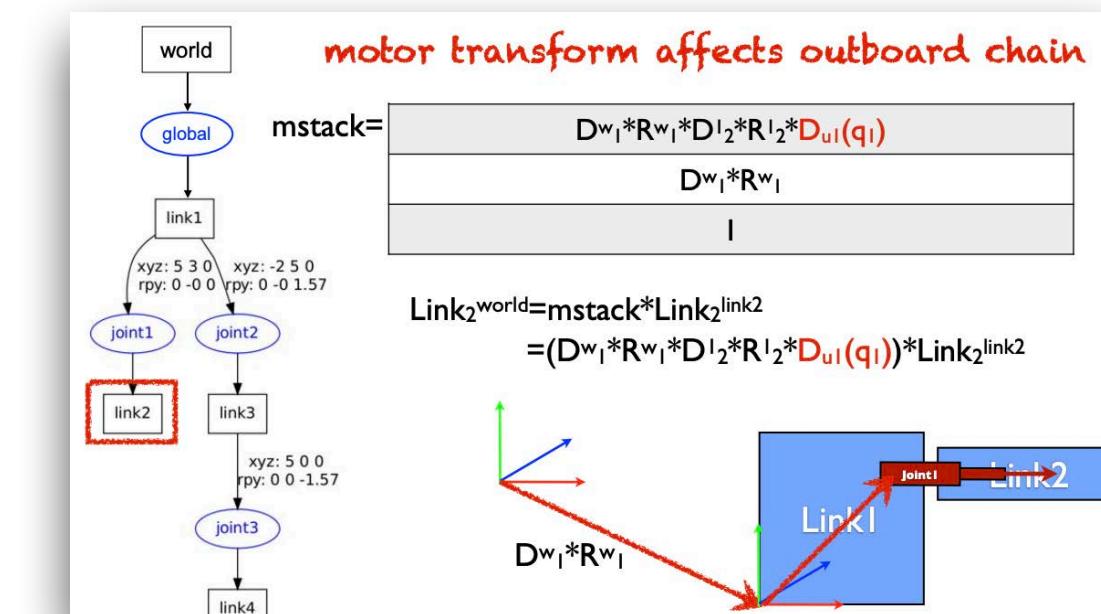
### Zero configuration



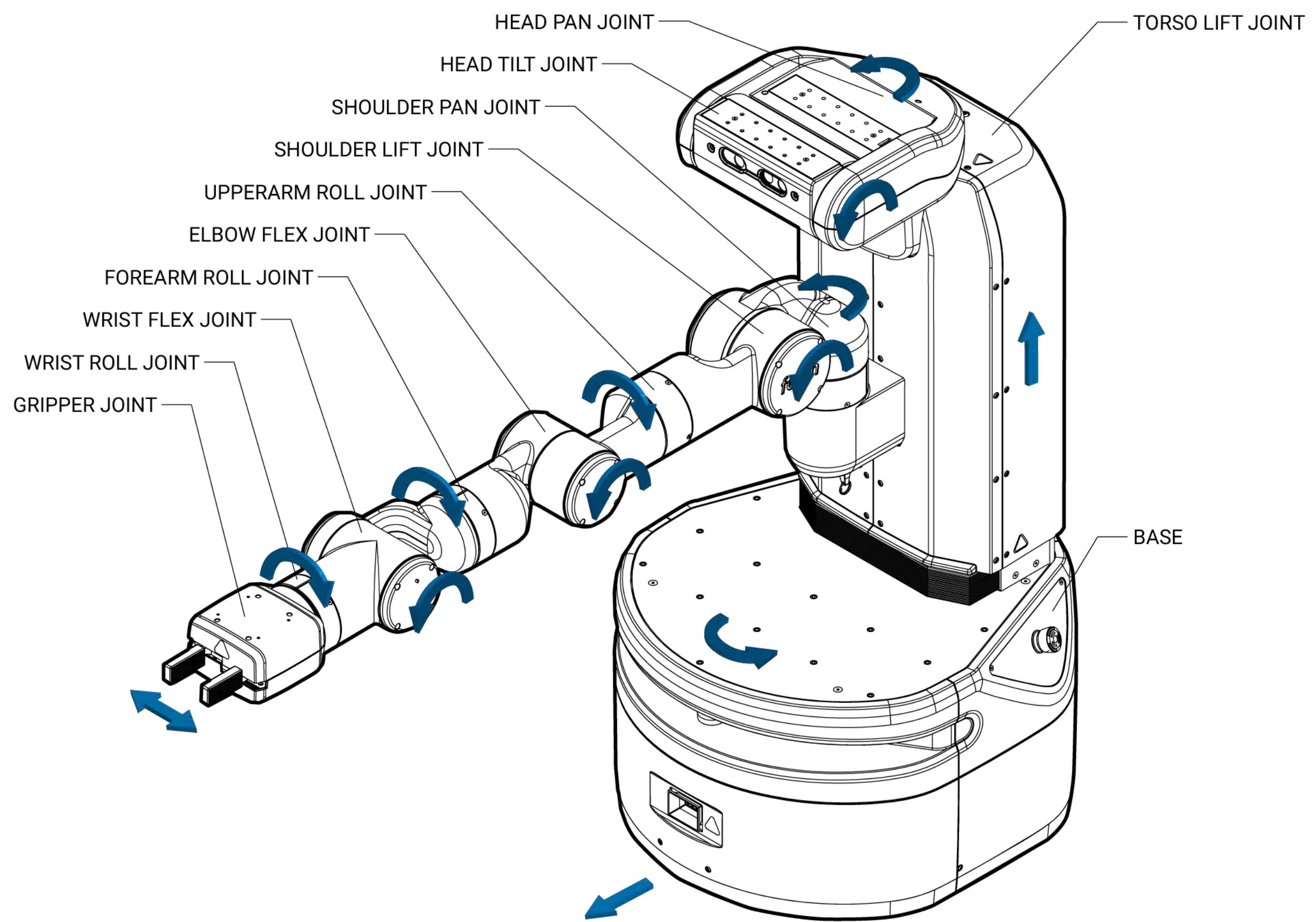
Assuming as given the:

- geometry of each link
- robot's kinematic definition
- **current state of all joints**

### Add motor motion



# Can a joint move infinitely far?



# Joint Limits

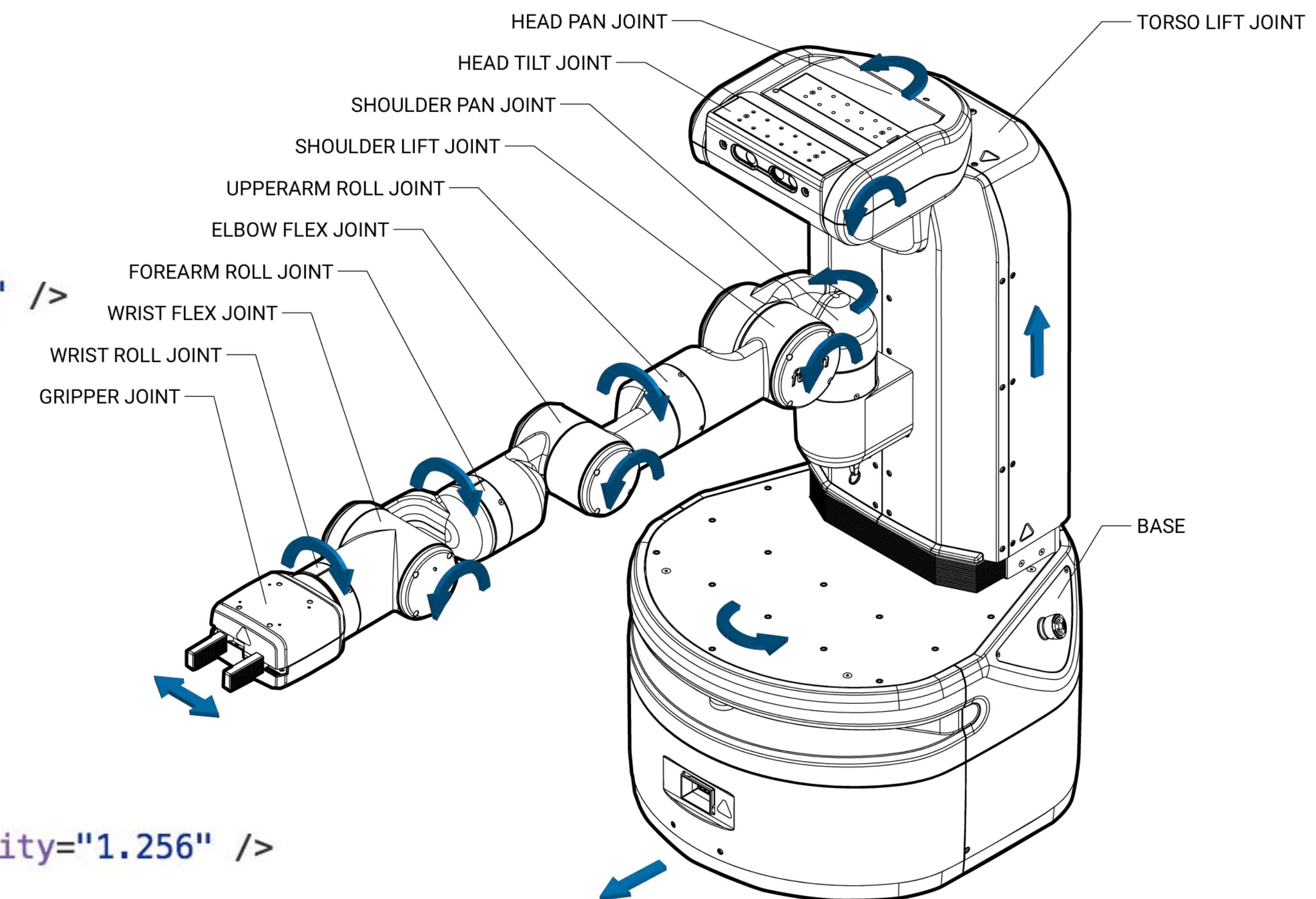
## Prismatic joint description

```
<joint name="torso_lift_joint" type="prismatic">
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />
  <parent link="base_link" />
  <child link="torso_lift_link" />
  <axis xyz="0 0 1" />
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />
</joint>
```

## Revolute joint description

```
<joint name="shoulder_pan_joint" type="revolute">
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />
  <parent link="torso_lift_link" />
  <child link="shoulder_pan_link" />
  <axis xyz="0 0 1" />
  <dynamics damping="1.0" />
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />
</joint>
```

Continuous joints have no limits



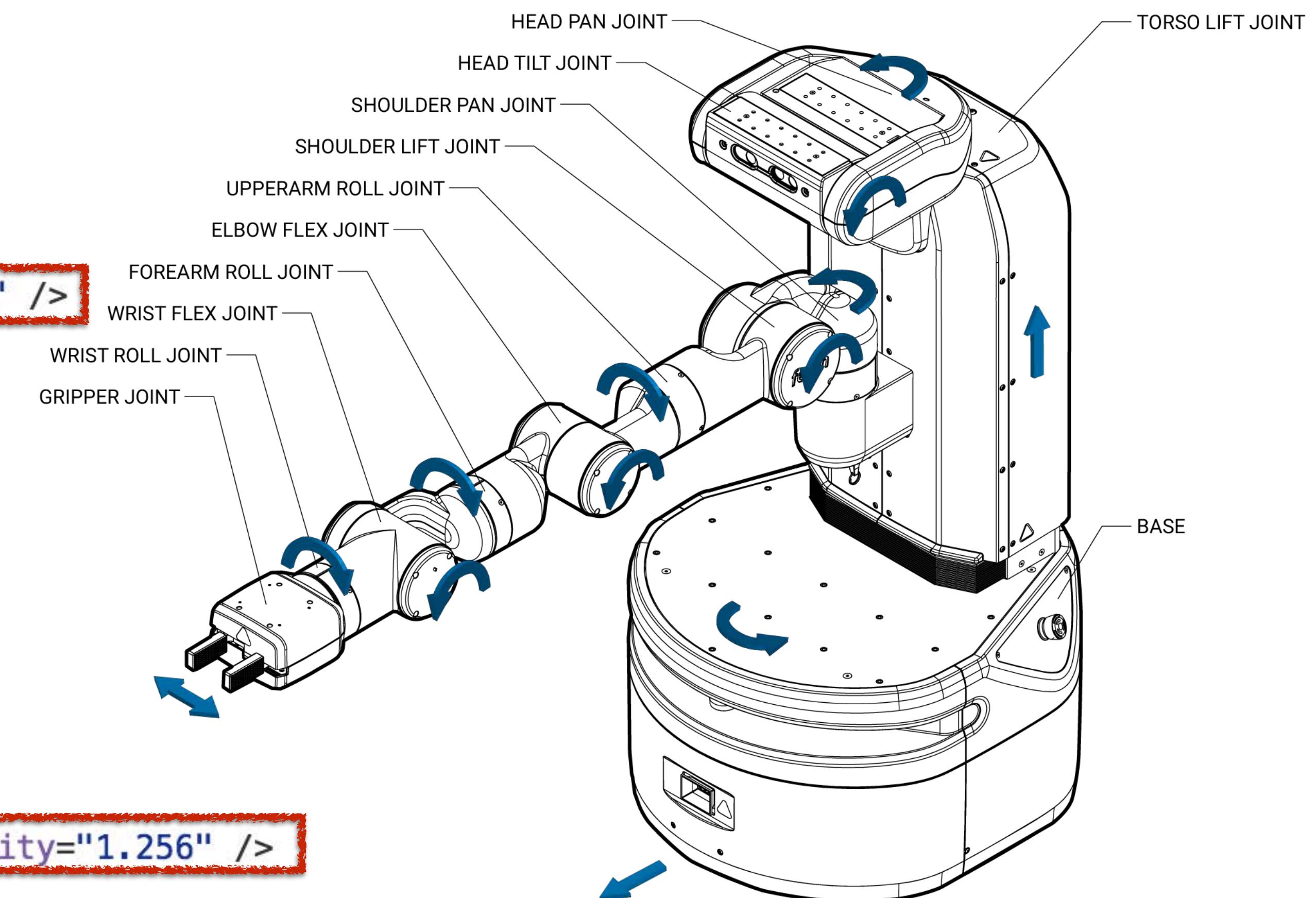
# Joint Limits

## Prismatic joint description

```
<joint name="torso_lift_joint" type="prismatic">
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />
  <parent link="base_link" />
  <child link="torso_lift_link" />
  <axis xyz="0 0 1" />
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />
<dynamics damping="100.0" /></joint>
```

## Revolute joint description

```
<joint name="shoulder_pan_joint" type="revolute">
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />
  <parent link="torso_lift_link" />
  <child link="shoulder_pan_link" />
  <axis xyz="0 0 1" />
  <dynamics damping="1.0" />
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />
</joint>
```



```

robot.joints.torso_lift_joint = {parent:"base_link", child:"torso_lift_link"};
robot.joints.torso_lift_joint.axis = [0,0,1];
robot.joints.torso_lift_joint.type = "prismatic";
robot.joints.torso_lift_joint.origin = {xyz: [-0.086875,0,0.37743], rpy:[-6.123E-17,0,0]};
robot.joints.torso_lift_joint.limit = {lower:0, upper:0.4};

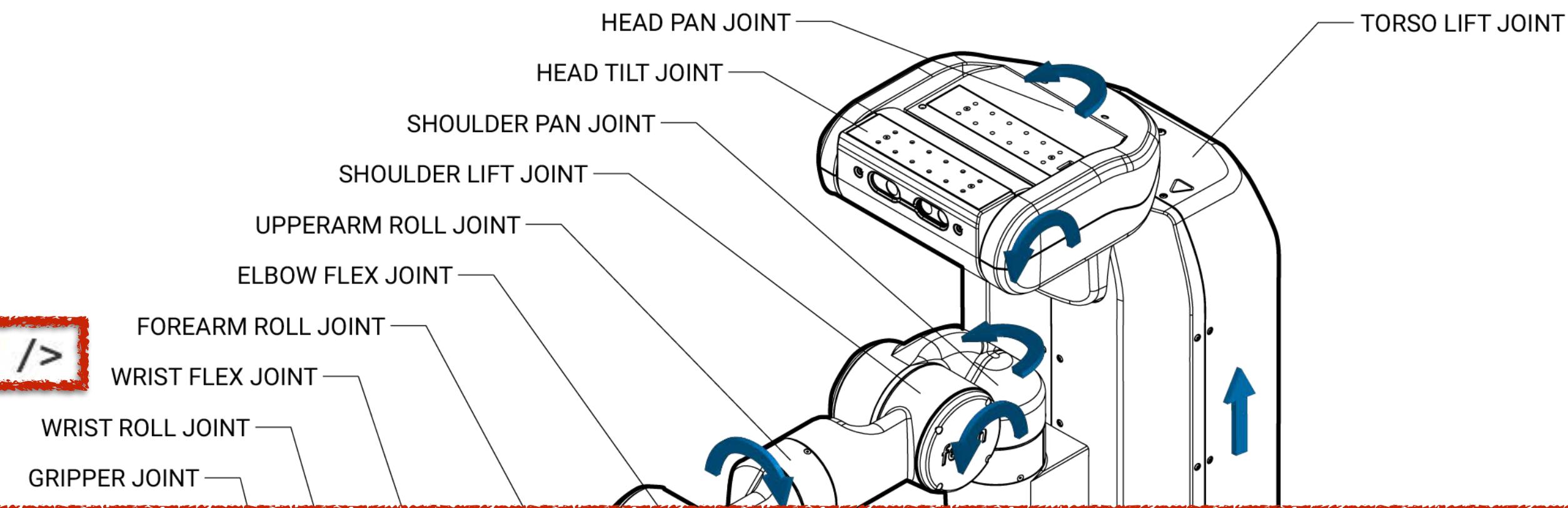
```

## Prismatic joint description

```

<joint name="torso_lift_joint" type="prismatic">
  <origin rpy="-6.123E-17 0 0" xyz="-0.086875 0 0.37743" />
  <parent link="base_link" />
  <child link="torso_lift_link" />
  <axis xyz="0 0 1" />
  <limit effort="450.0" lower="0" upper="0.4" velocity="0.1" />
  <dynamics damping="100.0" /></joint>

```



## Revolute joint description

```

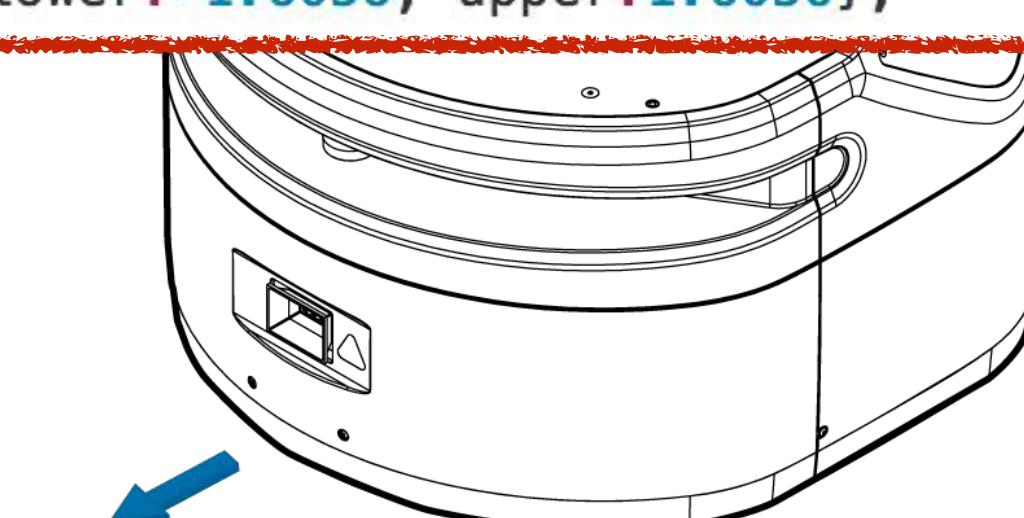
<joint name="shoulder_pan_joint" type="revolute">
  <origin rpy="0 0 0" xyz="0.119525 0 0.34858" />
  <parent link="torso_lift_link" />
  <child link="shoulder_pan_link" />
  <axis xyz="0 0 1" />
  <dynamics damping="1.0" />
  <limit effort="33.82" lower="-1.6056" upper="1.6056" velocity="1.256" />
</joint>

```

```

robot.joints.shoulder_pan_joint = {parent:"torso_lift_link", child:"shoulder_pan_link"};
robot.joints.shoulder_pan_joint.axis = [0,0,1];
robot.joints.shoulder_pan_joint.type = "revolute";
robot.joints.shoulder_pan_joint.origin = {xyz: [0.119525,0,0.34858], rpy:[0,0,0]};
robot.joints.shoulder_pan_joint.limit = {lower:-1.6056, upper:1.6056};

```



# Important notes



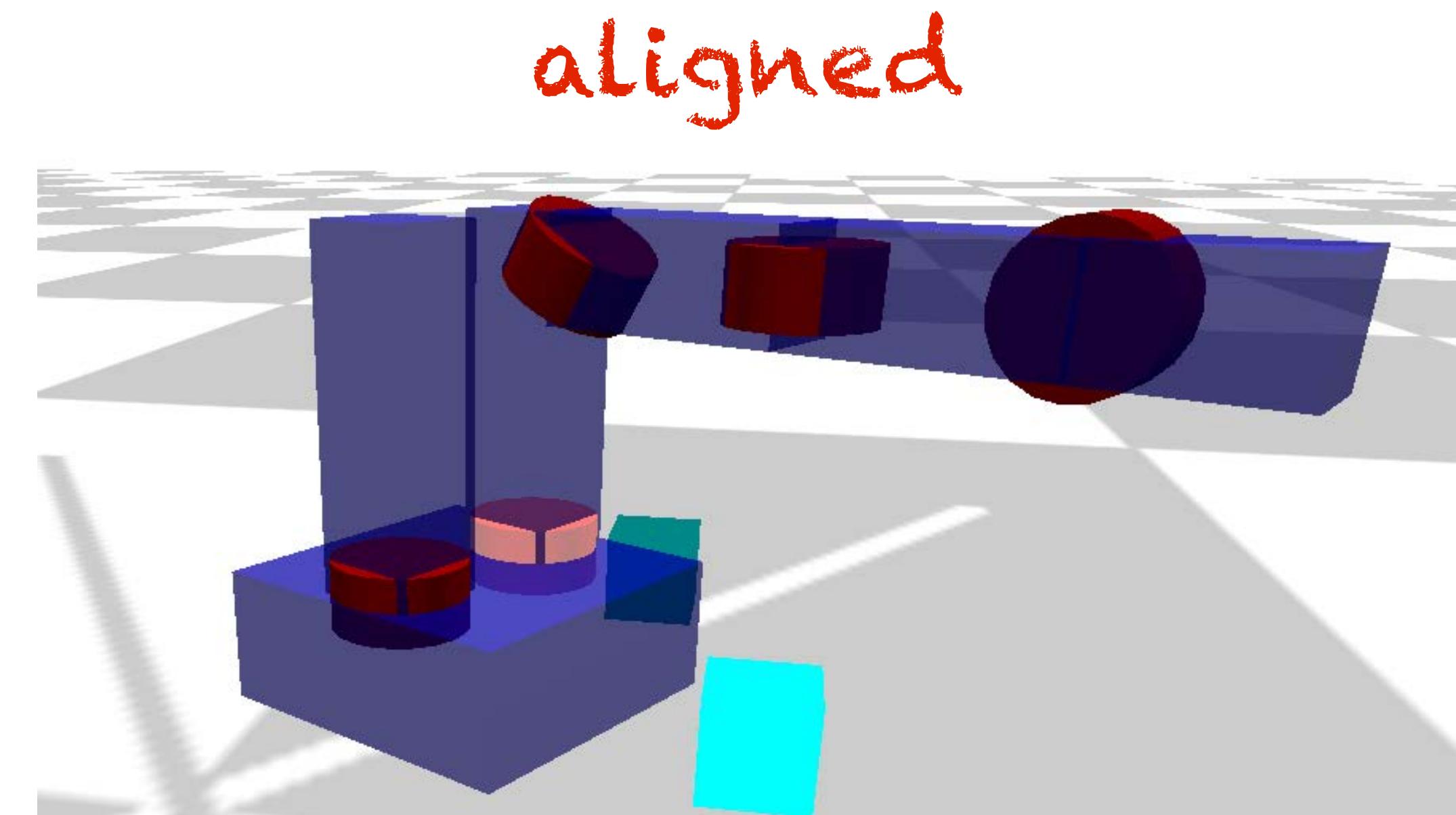
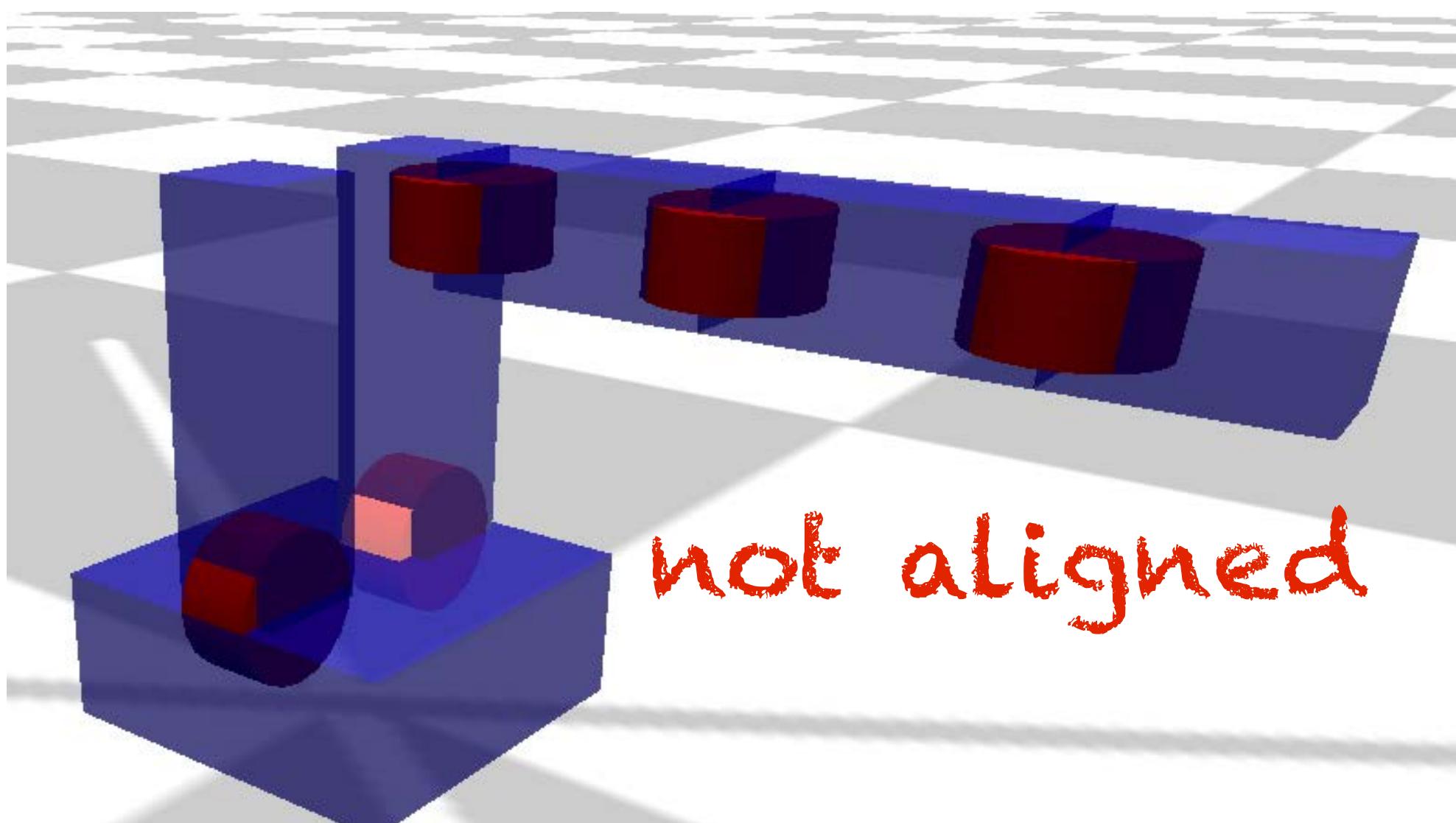
# Important notes

- Rotation order I use: **XYZ** ( $R_zR_yR_x$ )
- `vector_cross()`: code stencil tests for and uses this function
- A joint and its child link will share the same coordinate frame



# KinEval joint cylinder rendering

- threejs creates cylinders with axes aligned along y-axis
- you need to implement `vector_cross()` for KinEval to render joint cylinders properly along joint axis



# Global controls for base

- Assume we have a base that is holonomic wrt. ground plane
  - holonomic: can move in any direction
  - kineval\_userinput.js assumes:

How to perform this  
base movement?

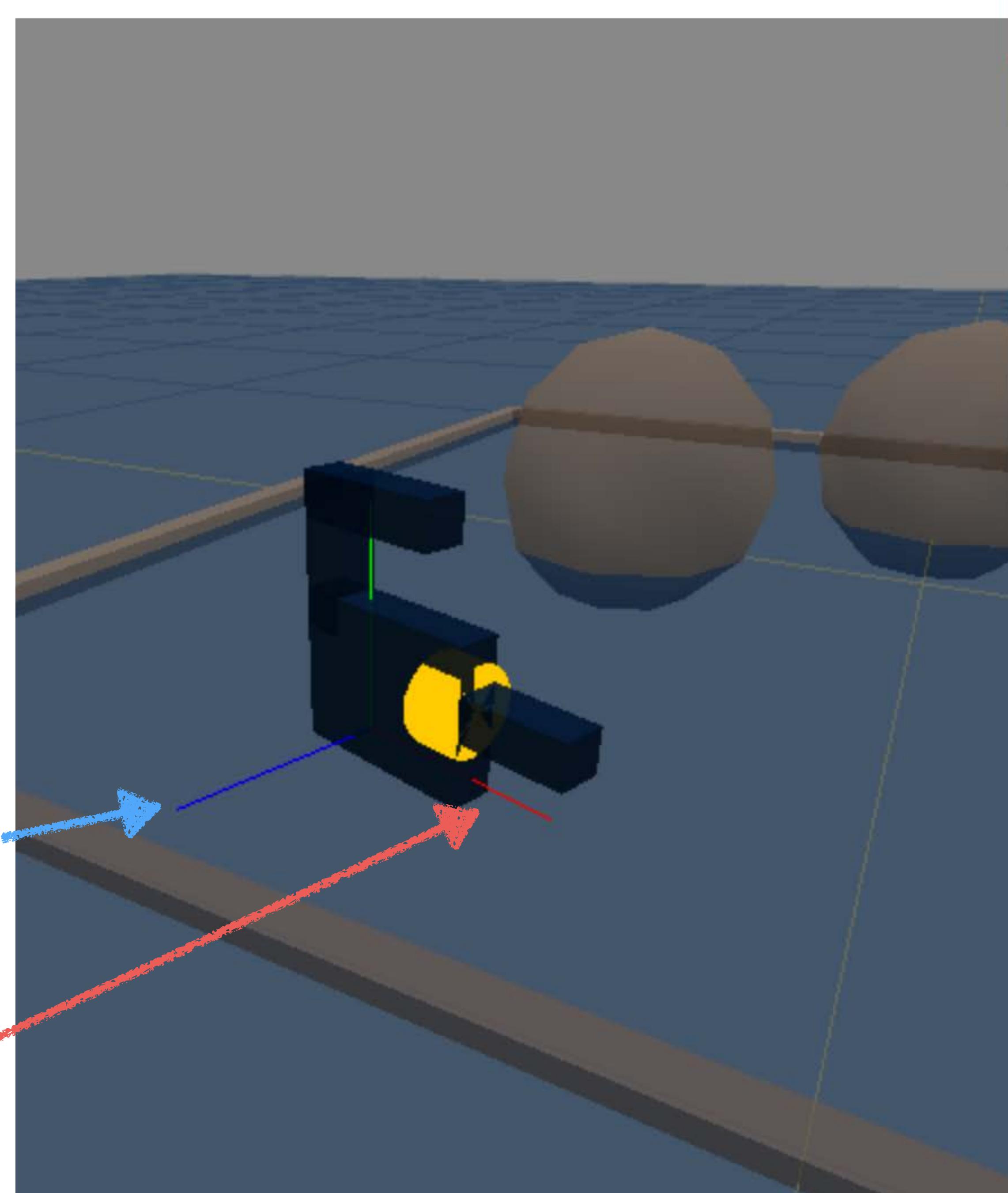


Transform vectors for heading (local z-axis) and lateral (local x-axis) of robot base into world coordinates

Store transformed vectors in variables “robot\_heading” and “robot\_lateral”

Forward heading of the robot

Lateral heading of the robot

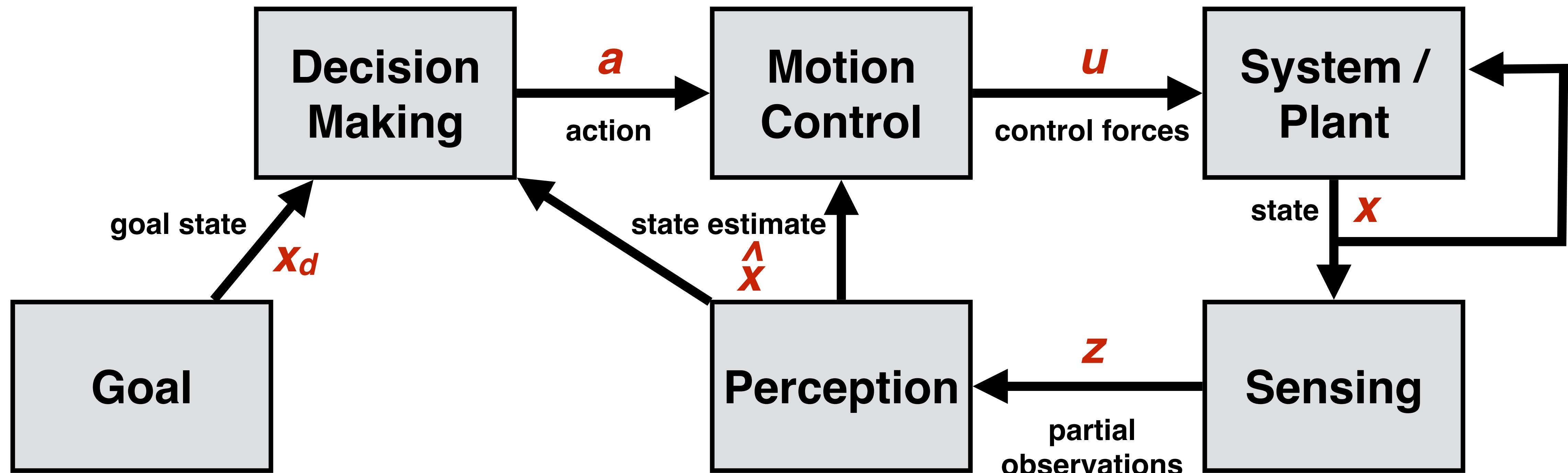


kineval	
just_starting	<input type="checkbox"/>
>User Parameters	
>Robot	
>Forward Kinematics	
>Inverse Kinematics	
>Motion Planning	
>Display	
>Geometries and Axes	
display_links	<input checked="" type="checkbox"/>
display_links...	<input type="checkbox"/>
display_base...	<input checked="" type="checkbox"/>
display_joints	<input type="checkbox"/>
display_joints...	<input type="checkbox"/>
display_joints...	<input checked="" type="checkbox"/>
display_joints...	<input type="checkbox"/>
display_wirefr...	<input type="checkbox"/>
display_collisi...	<input type="checkbox"/>
>Colors	

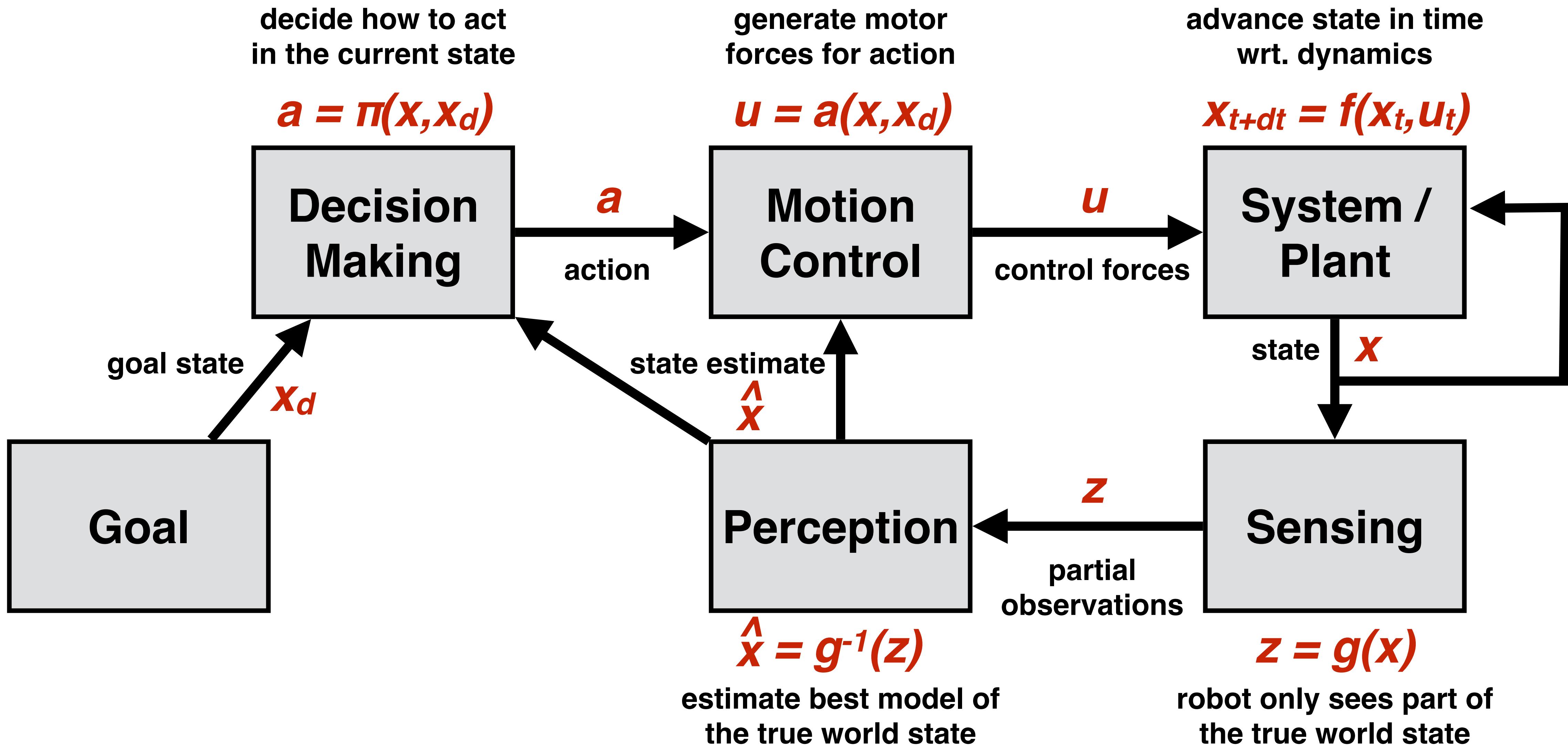
# Decision Making



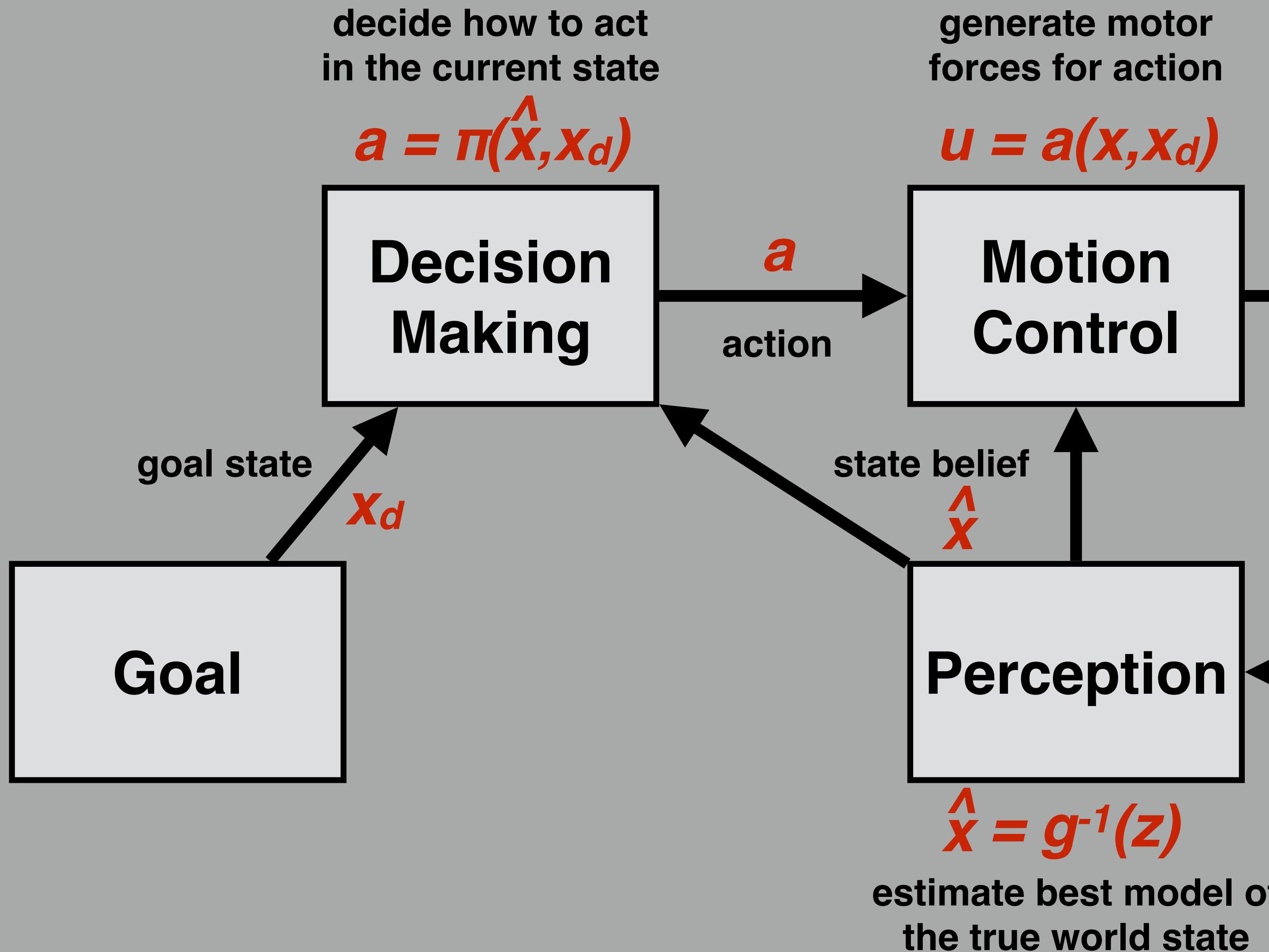
# Robot Control Loop



# Robot Control Loop



# Autonomy



# Embodiment

advance state in time  
wrt. dynamics

$$x_{t+dt} = f(x_t, u_t)$$

**System / Plant**

$$\text{state } x$$

**Sensing**

$$z = g(x)$$

robot only sees part of the true world state

# App

## Task

decide how to act  
in the current state

$$a = \pi(\hat{x}, x_d)$$

**Decision Making**

$a$

action

goal state

$x_d$

**Goal**

## State-Action

generate motor  
forces for action

$$u = a(x, x_d)$$

**Motion Control**

$u$

control forces

state belief

$\hat{x}$

**Perception**

$$\hat{x} = g^{-1}(z)$$

estimate best model of  
the true world state

## Embodiment

advance state in time  
wrt. dynamics

$$x_{t+dt} = f(x_t, u_t)$$

**System /  
Plant**

state

$x$

**Sensing**

$z$

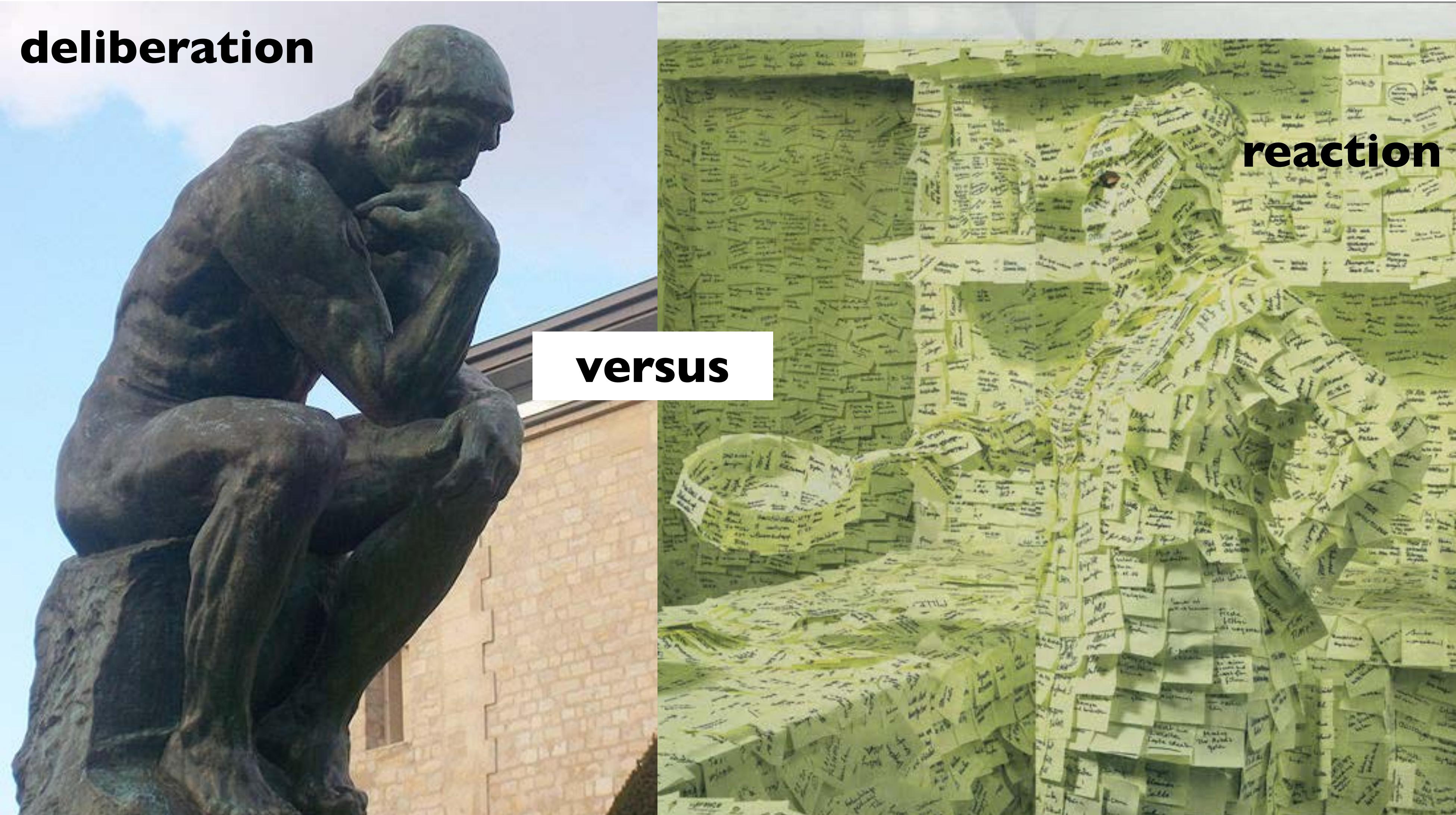
partial  
observations

$$z = g(x)$$

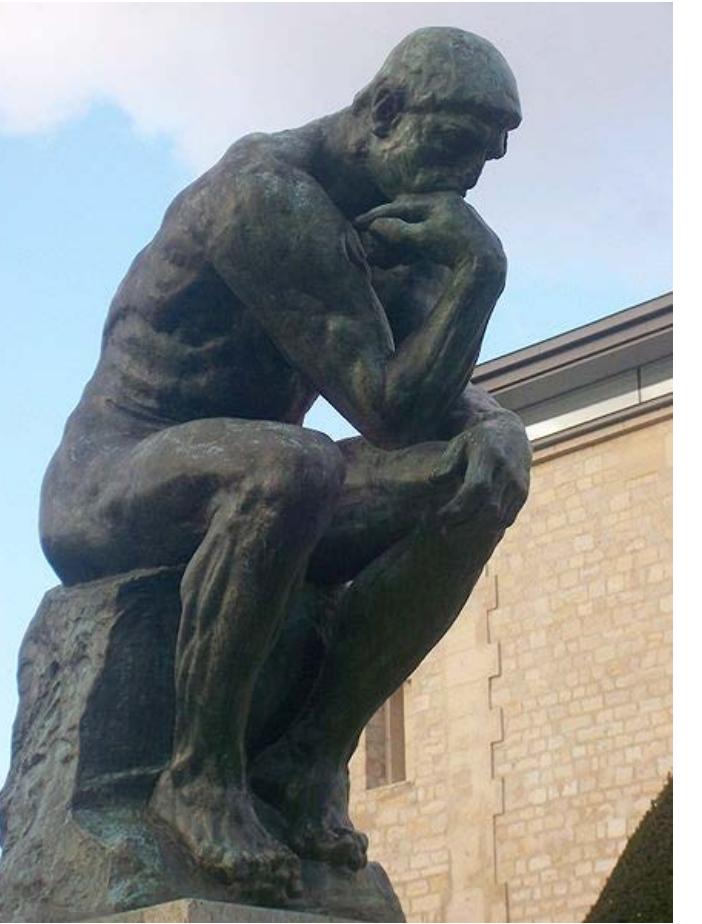
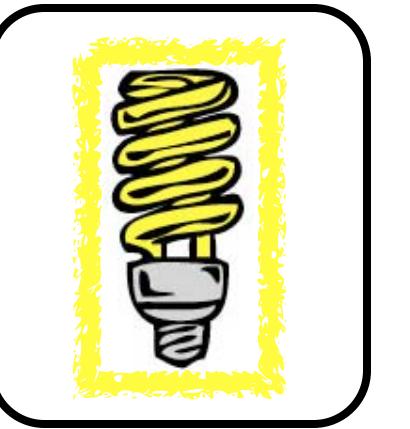
robot only sees part of  
the true world state



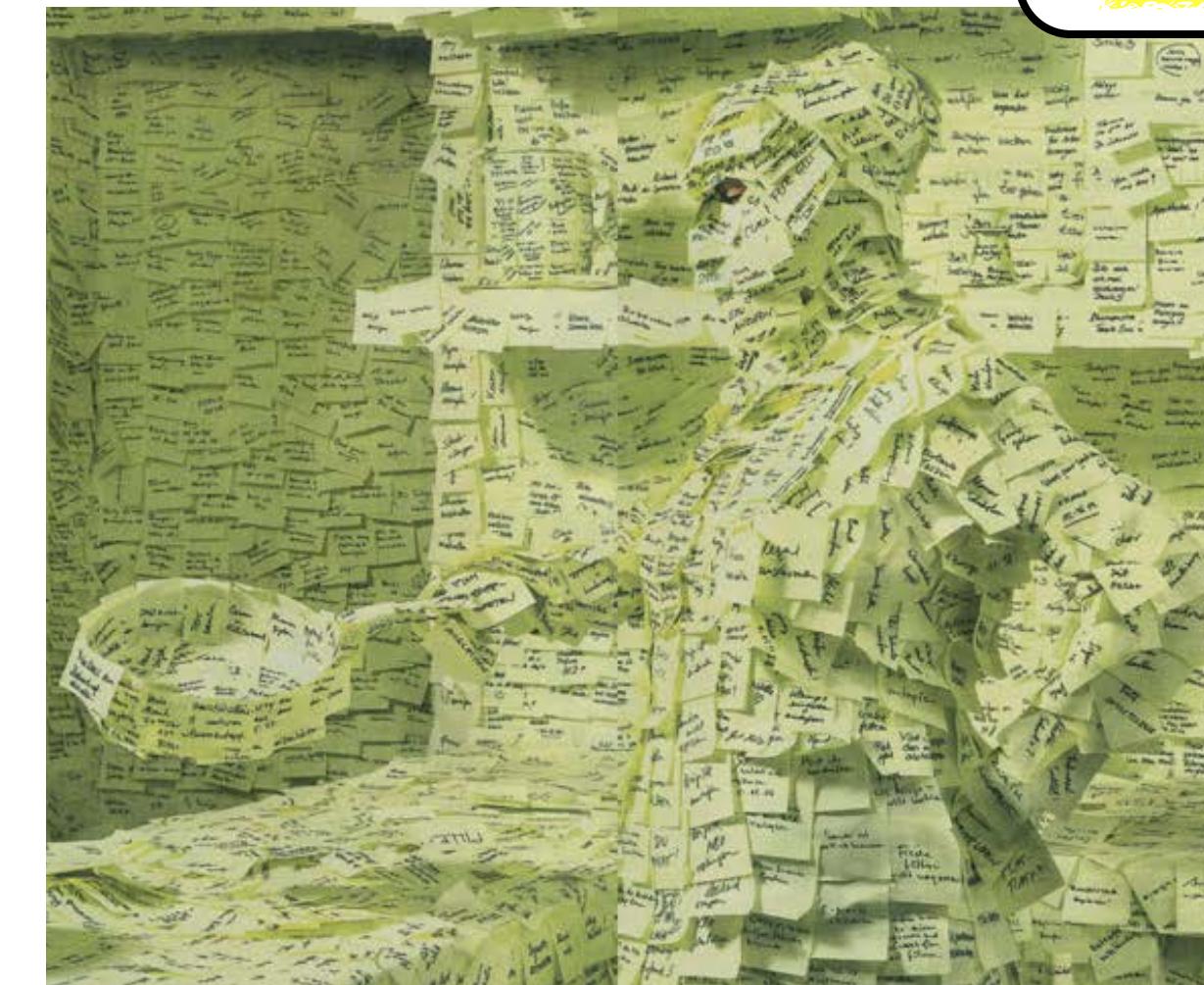
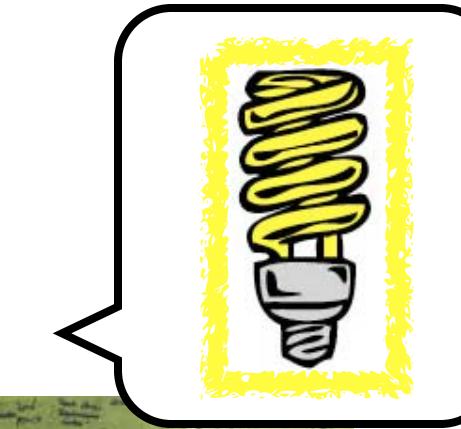
# Robot Decision Making



# Should your robot's decision making



OR

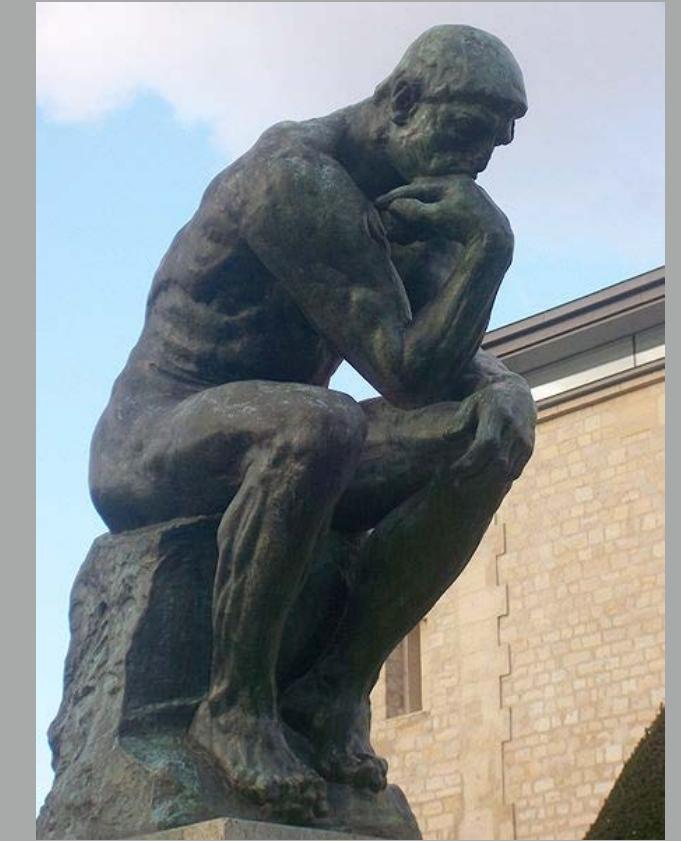
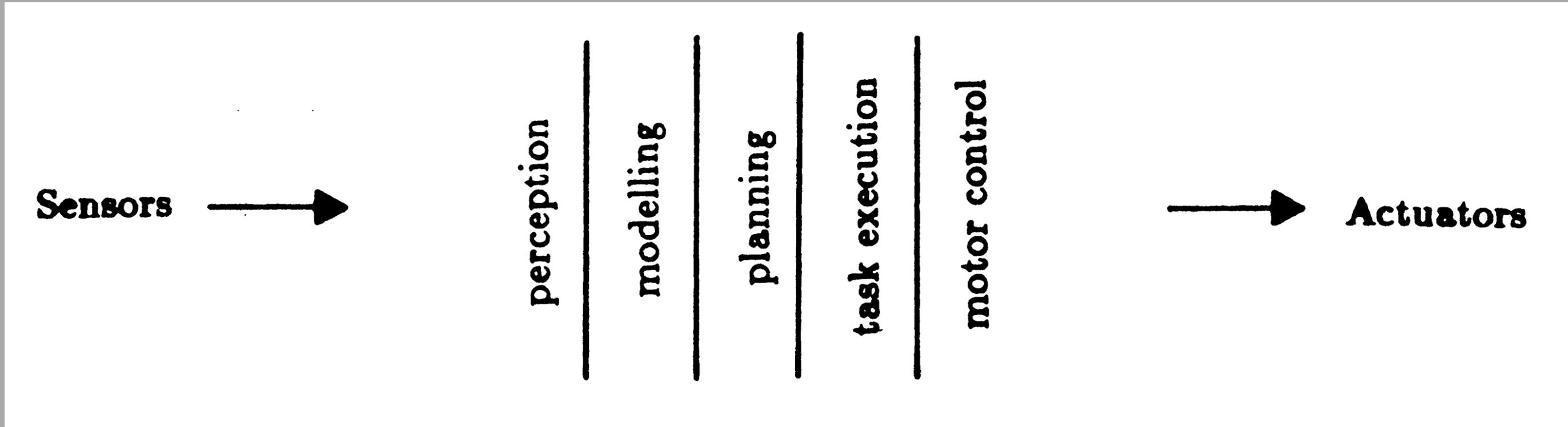


fully think through  
solving a problem?

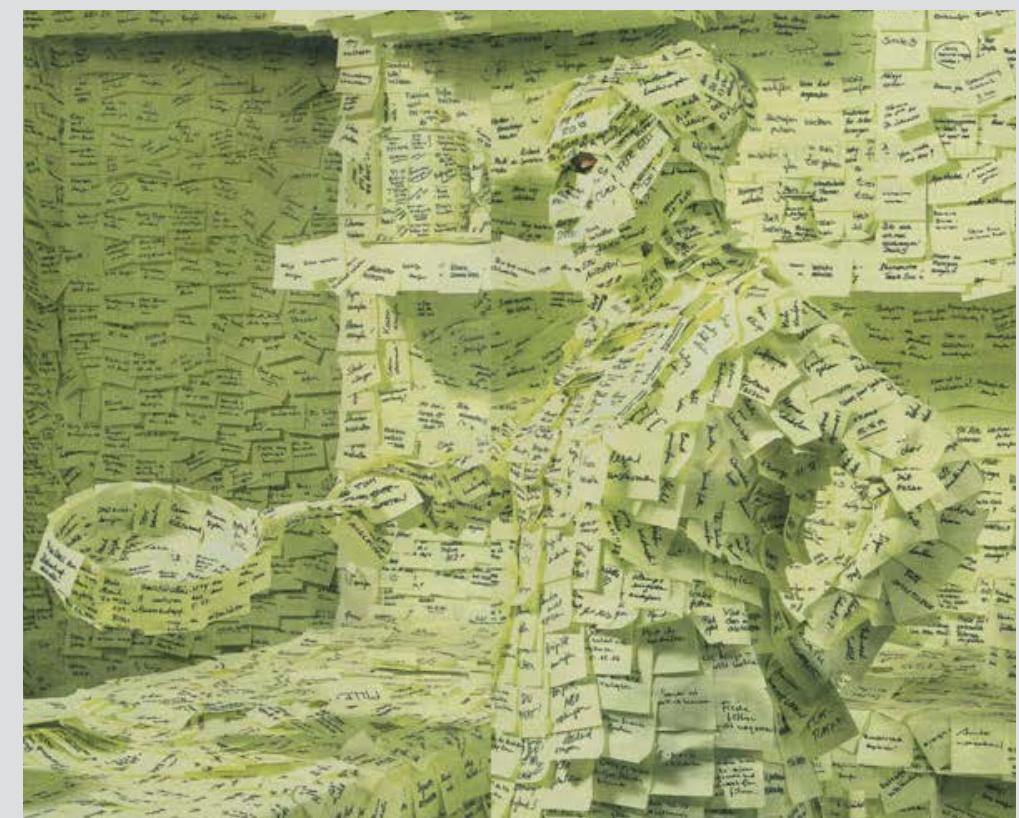
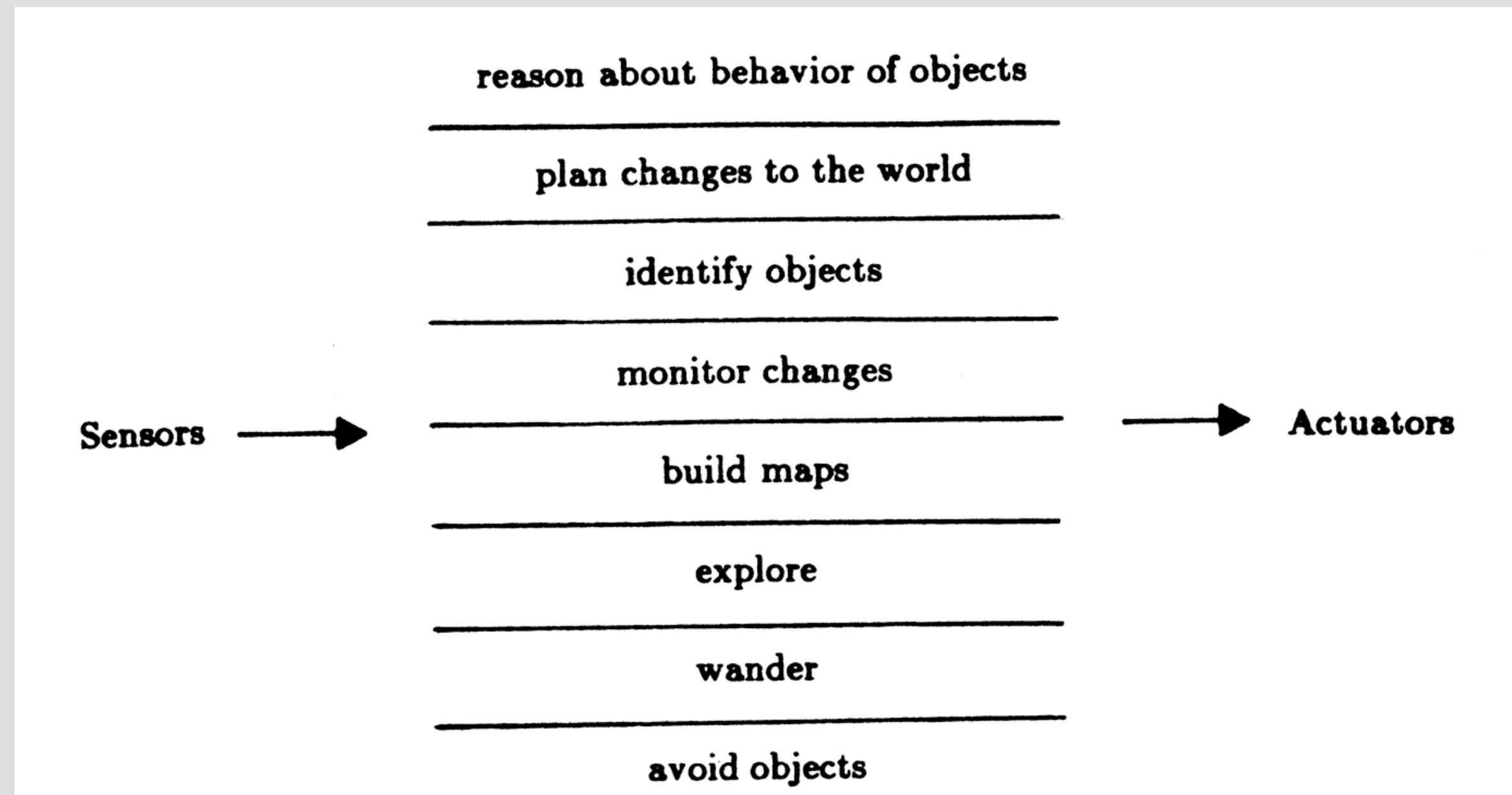
react quickly to  
changes in its world?

# Deliberation v. Reaction

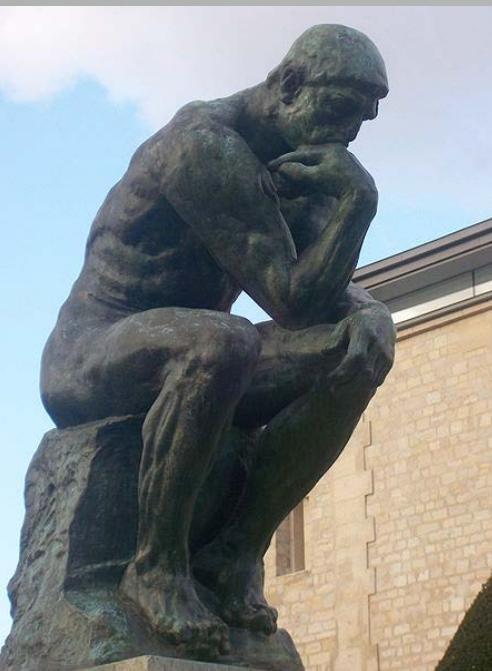
**deliberative:**  
sense-plan-act,  
path planning  
motion planning



**reaction:**  
controllers acting in parallel  
subsumption,  
Finite State Machine



# Deliberation-Reaction spectrum



**DELIBERATIVE**

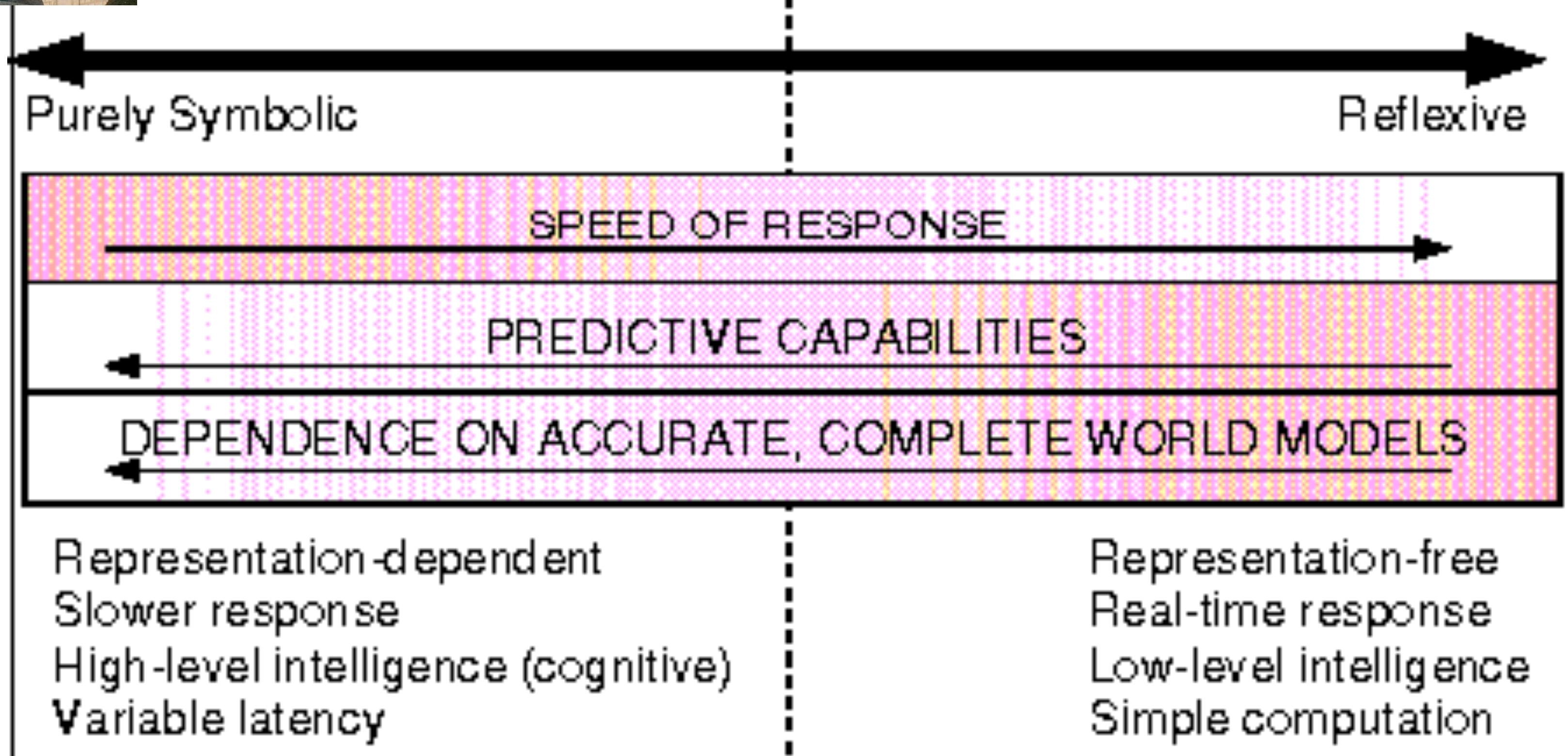
**REACTIVE**

Complete  
Adaptive  
Optimal  
Slower

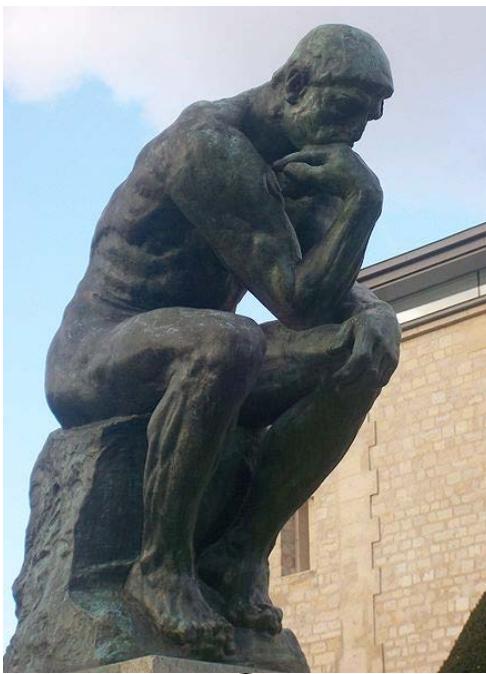
Faster  
Cheaper  
More robust  
Forgetful

Requires  
complete model  
of the world

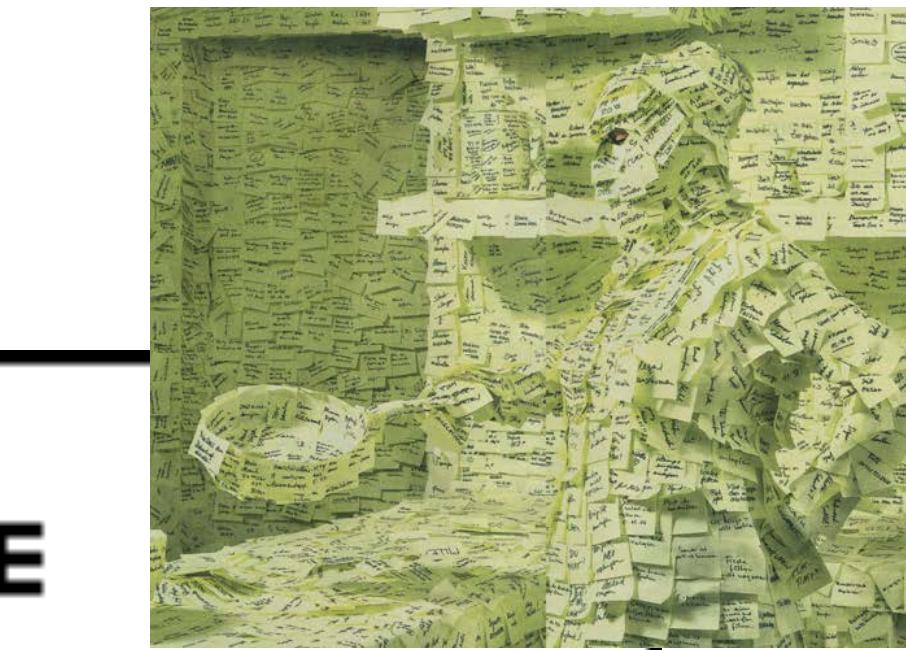
Requires a  
complete design  
of the problem



# Examples?



**DELIBERATIVE**



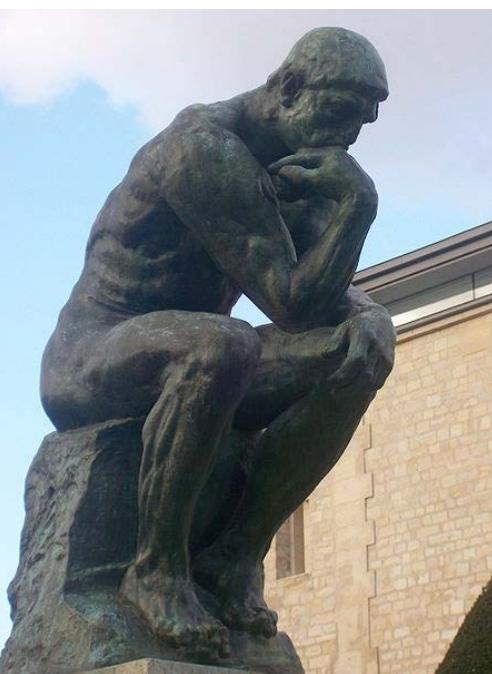
**REACTIVE**

← Purely Symbolic

→ Reflexive

example???

# Examples?



**DELIBERATIVE**



**REACTIVE**

← Purely Symbolic

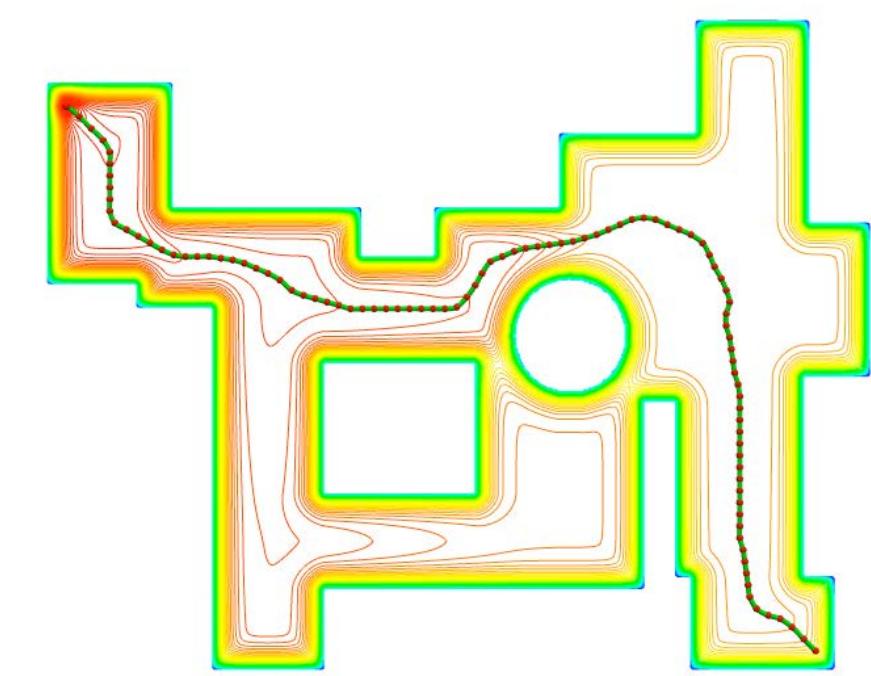
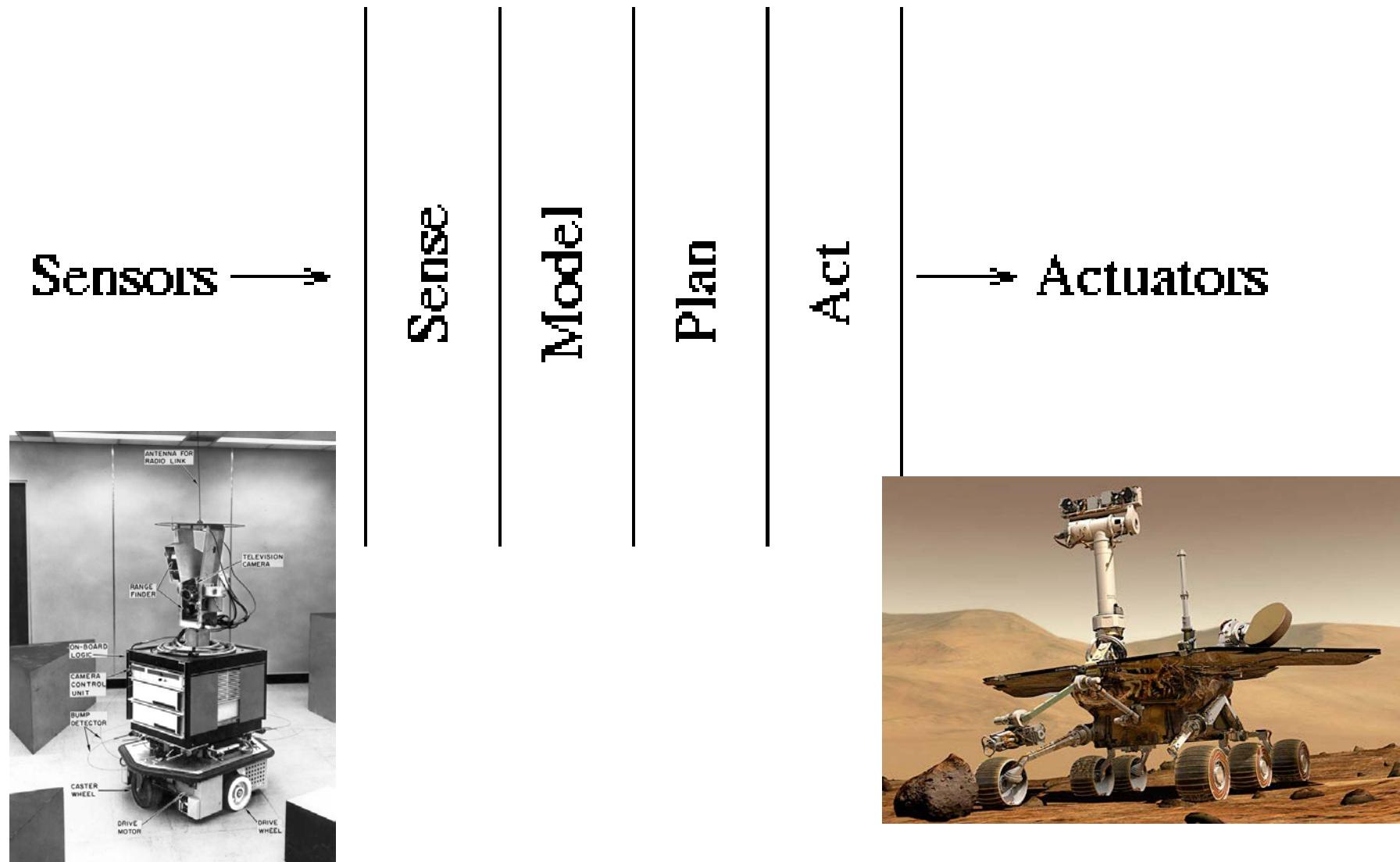
→ Reflexive



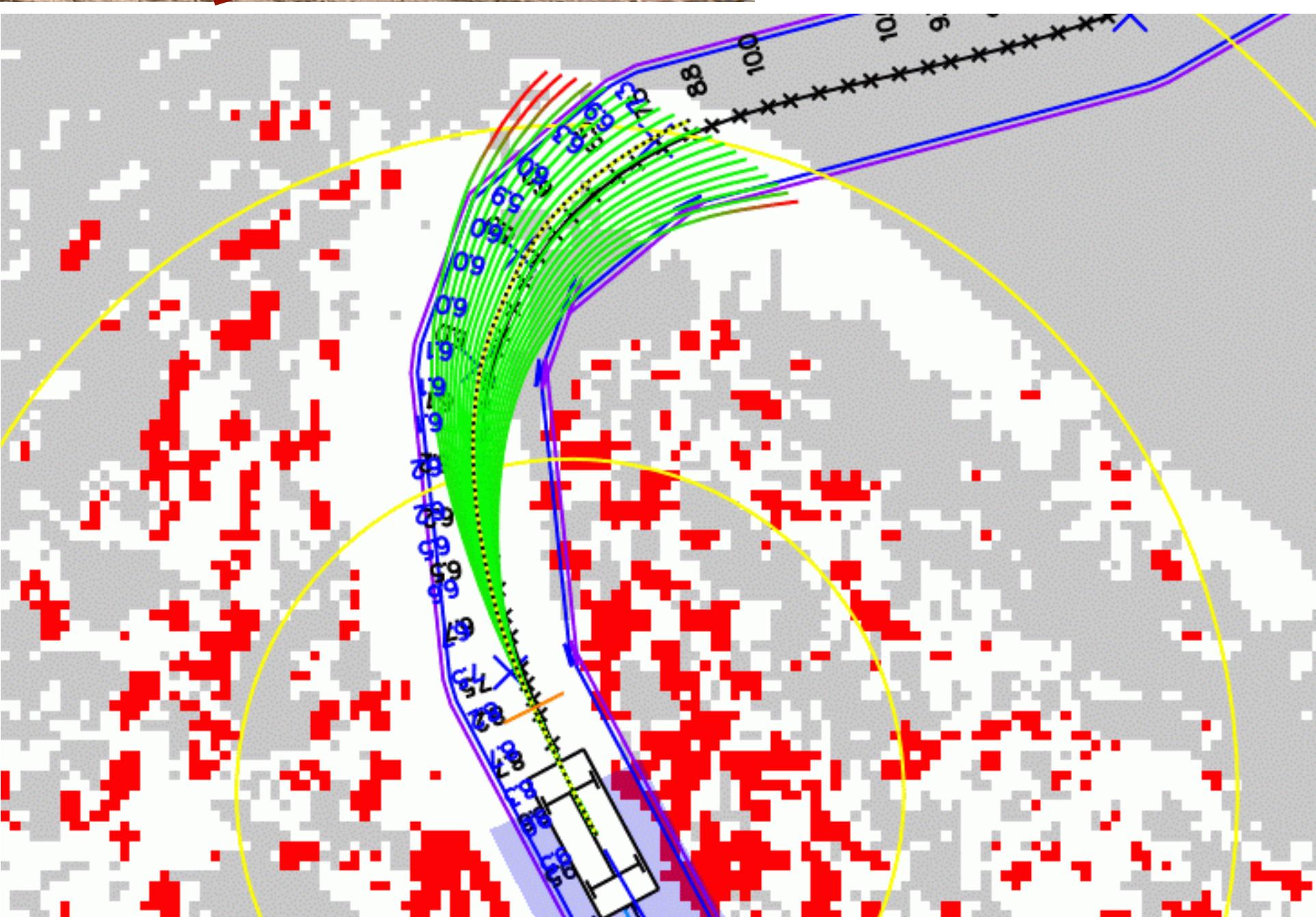
# Deliberation

## “Sense-Plan-Act” paradigm

- sense: build most complete model of world
  - GPS, SLAM, 3D reconstruction, affordances
- plan: search over all possible outcomes
  - Graph search, Roadmap planning
- act: execute plan through motor forces
  - PID control, Model predictive control



# Stanley (Grand Challenge)



Navigation



Road detection

2005



# MIT Talos (Urban Challenge)



2007





2013



Deliberation  
requires a model of the world



Color+Depth Camera



Laser Rangefinder





# Simultaneous Localization and Mapping

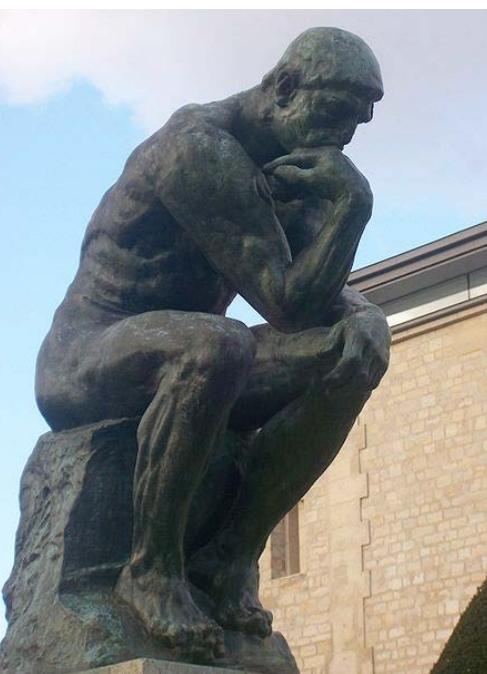




Autonomous robot navigation  
from previously built map



# Examples?



**DELIBERATIVE**



**REACTIVE**

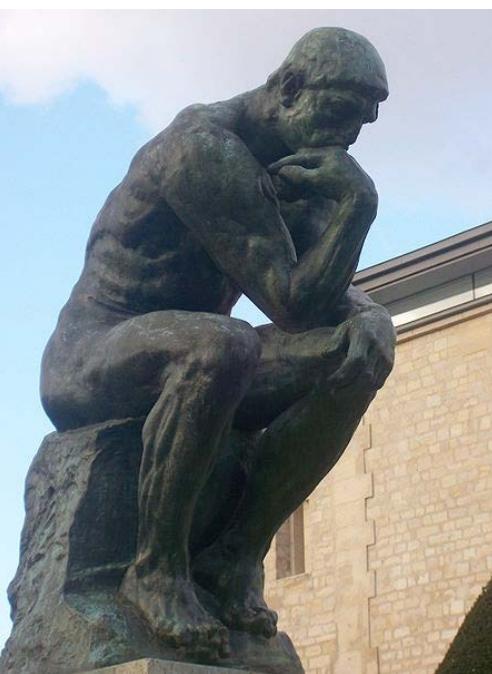
Purely Symbolic

Reflexive

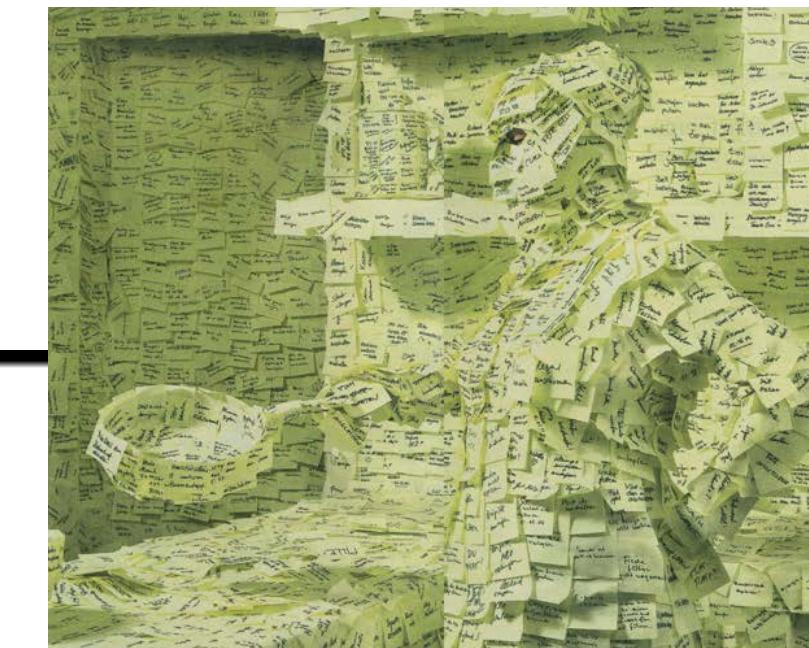


more common  
example???

# Examples?



**DELIBERATIVE**



**REACTIVE**

← Purely Symbolic

→ Reflexive



# Reaction

- No representation of state
  - Typically, fast hardcoded rules
- Embodied intelligence
  - behavior  $\leftarrow$  control + embodiment
  - Stigmergy (e.g, ant scouts using pheromones)
- Finite State Machines
  - most common
- Subsumption architecture
  - prioritized reactive policies

Sensors → → Actuators

Avoid Obstacles

Avoid Collision

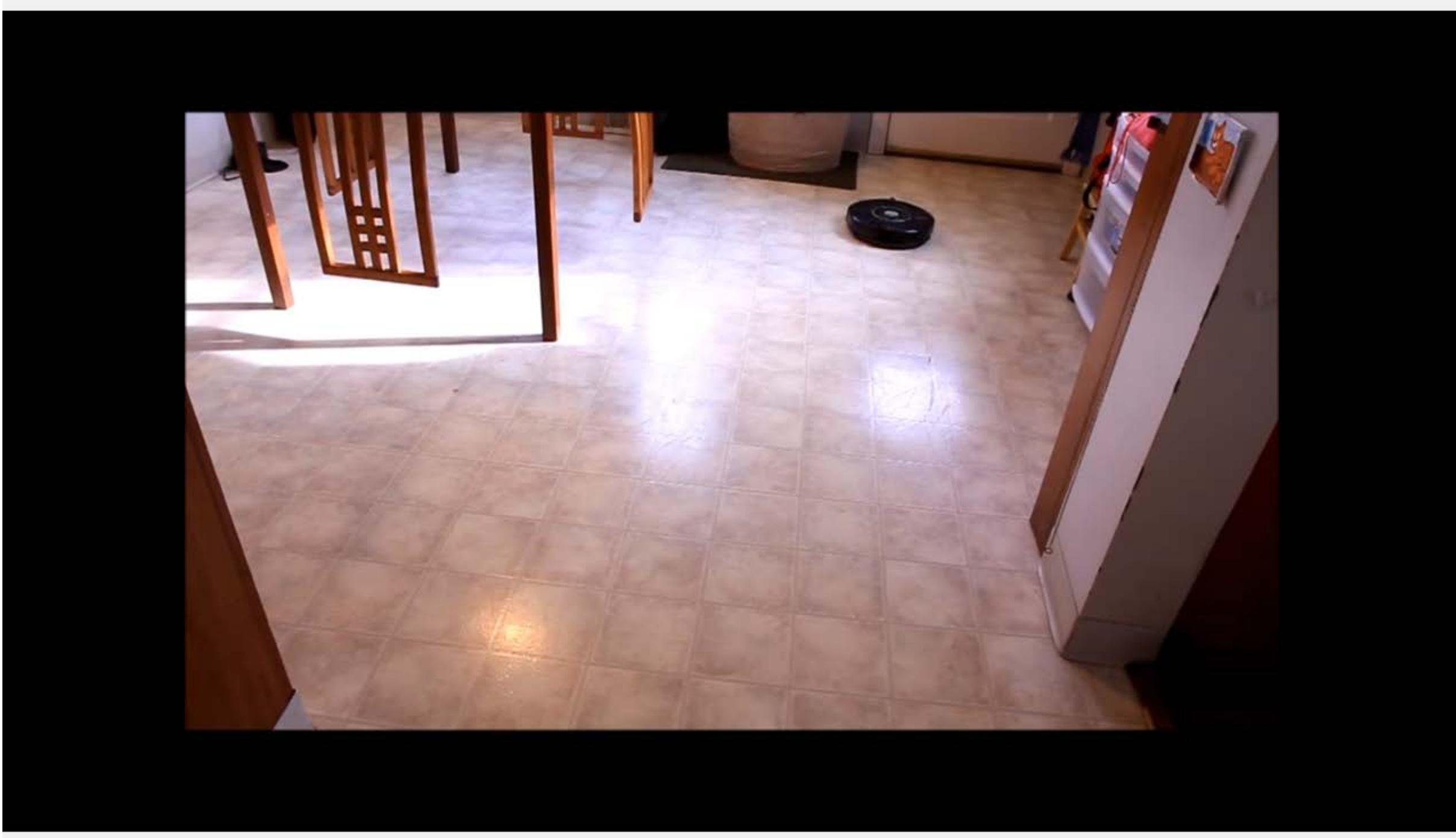


Explore

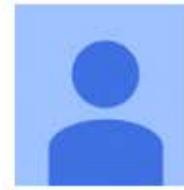
Wander Around

Sensors →

# Roomba cleaning pattern



roomba cleaning "pattern"

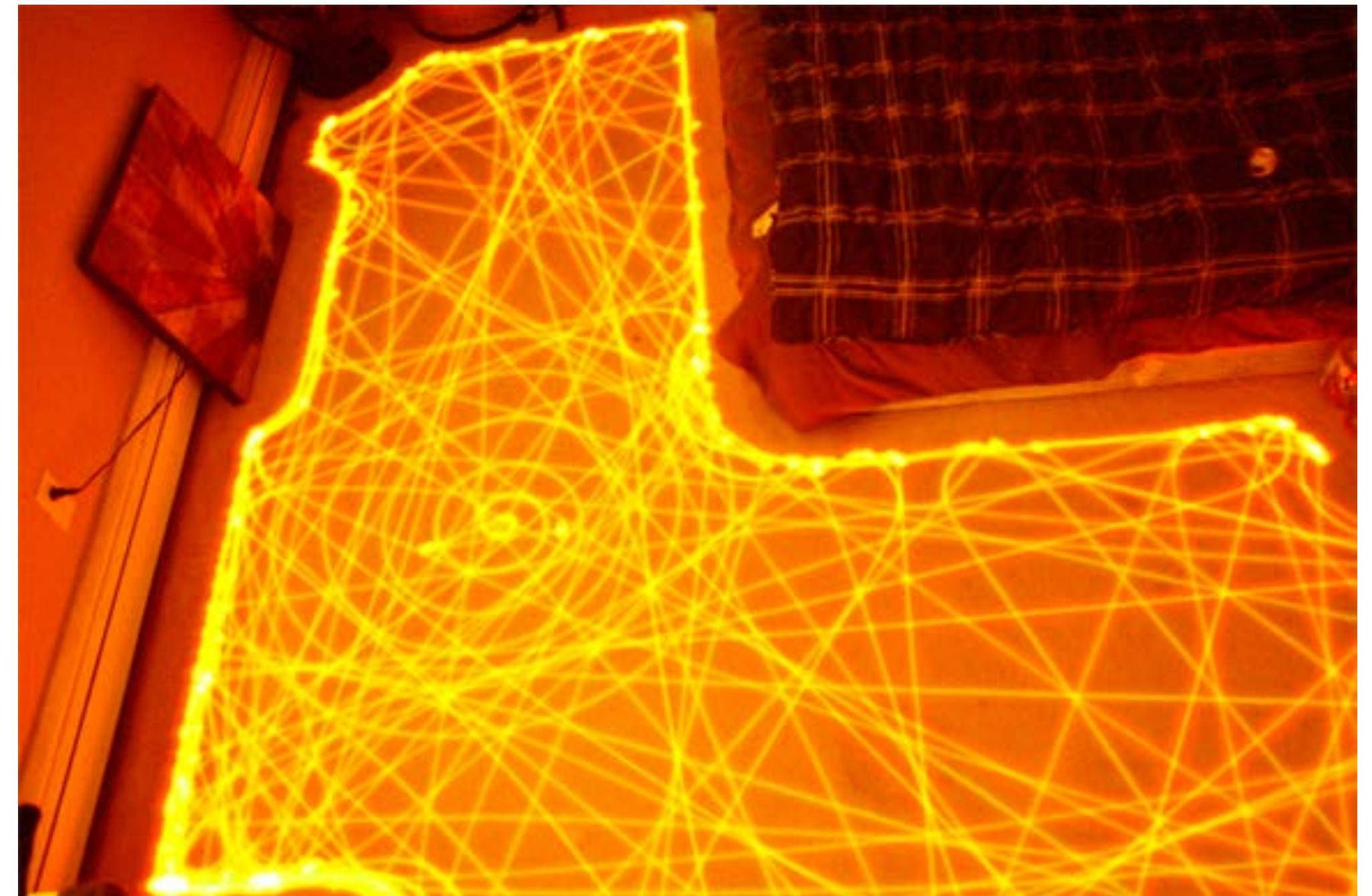


miro ledajaks



21

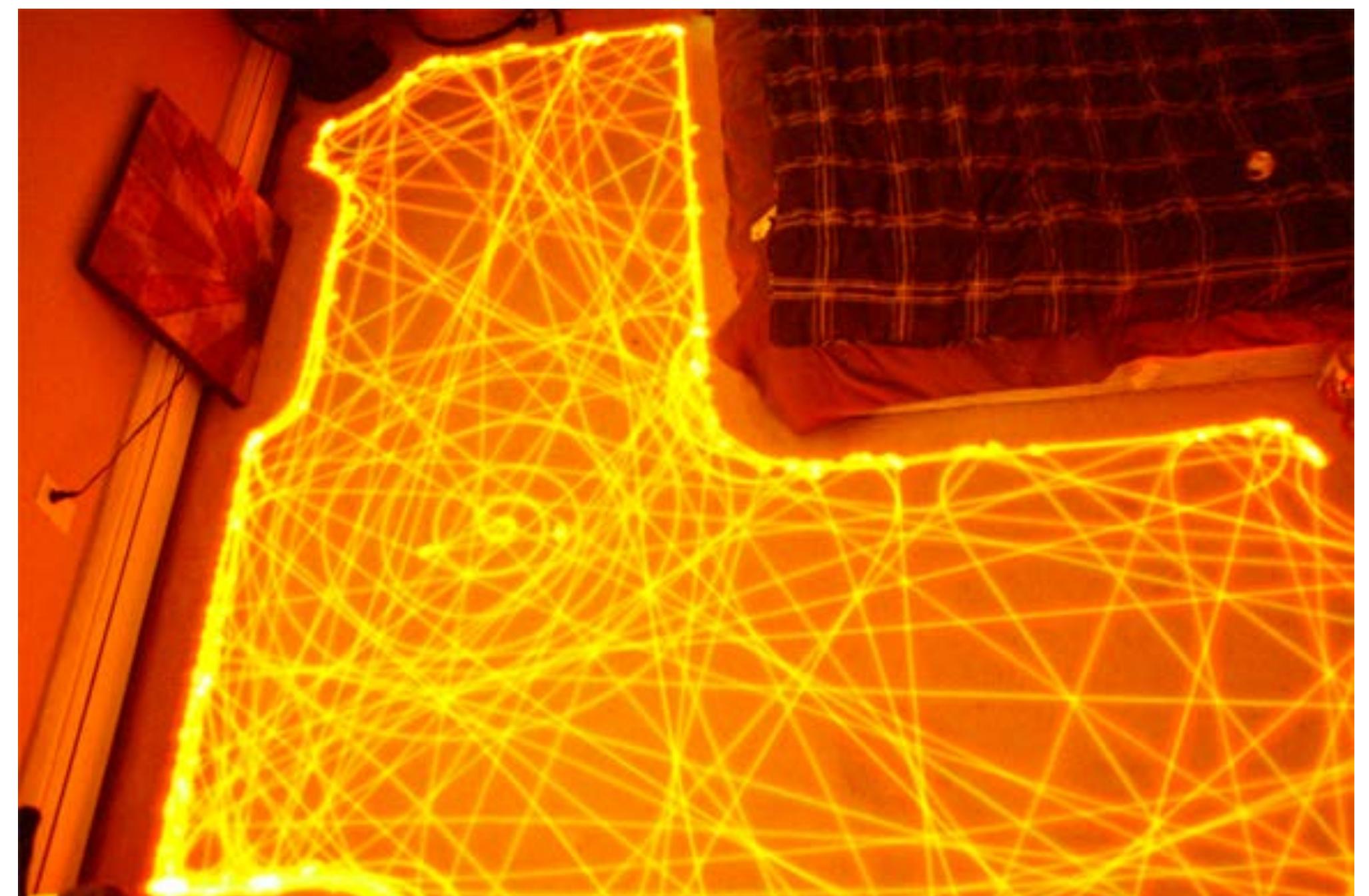
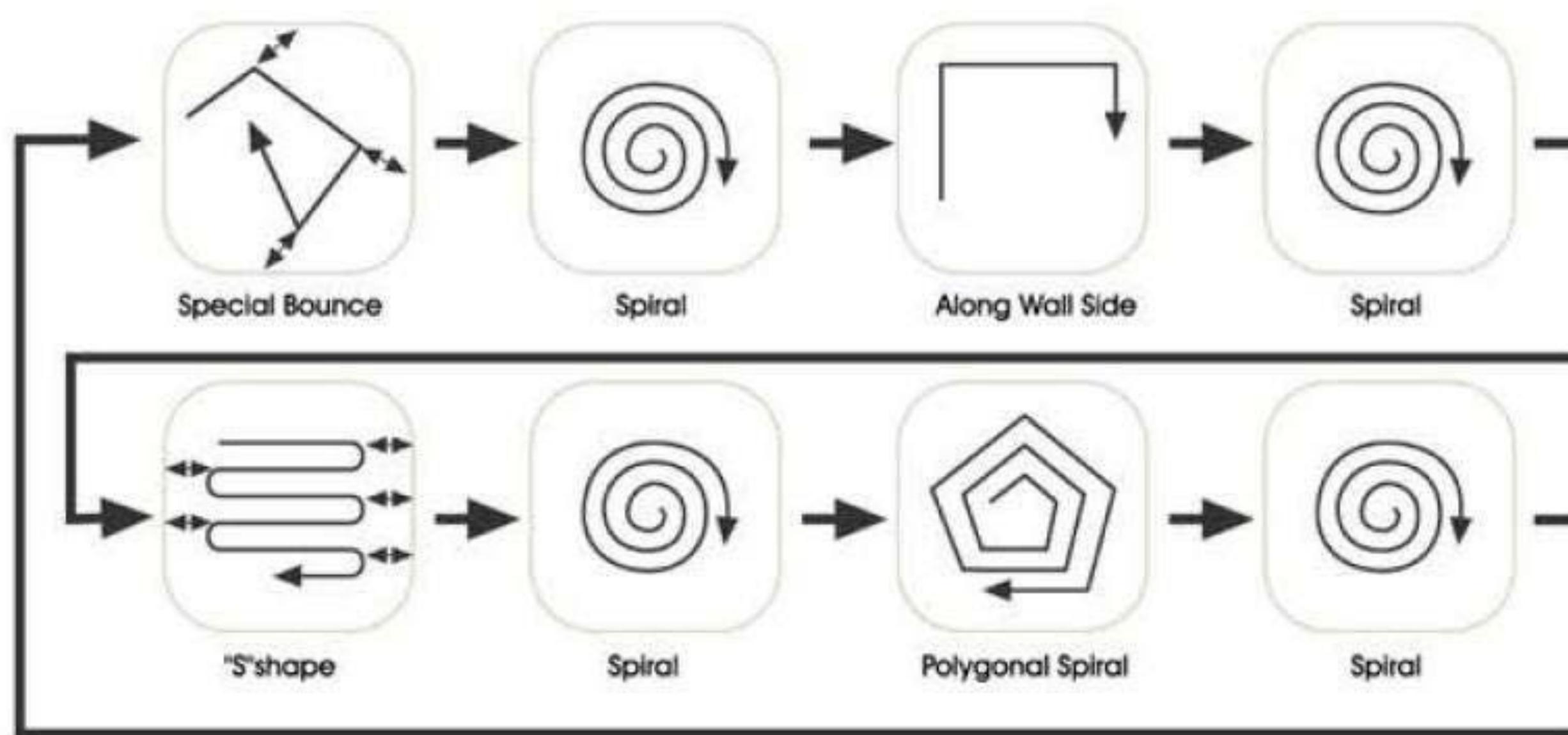
196 views



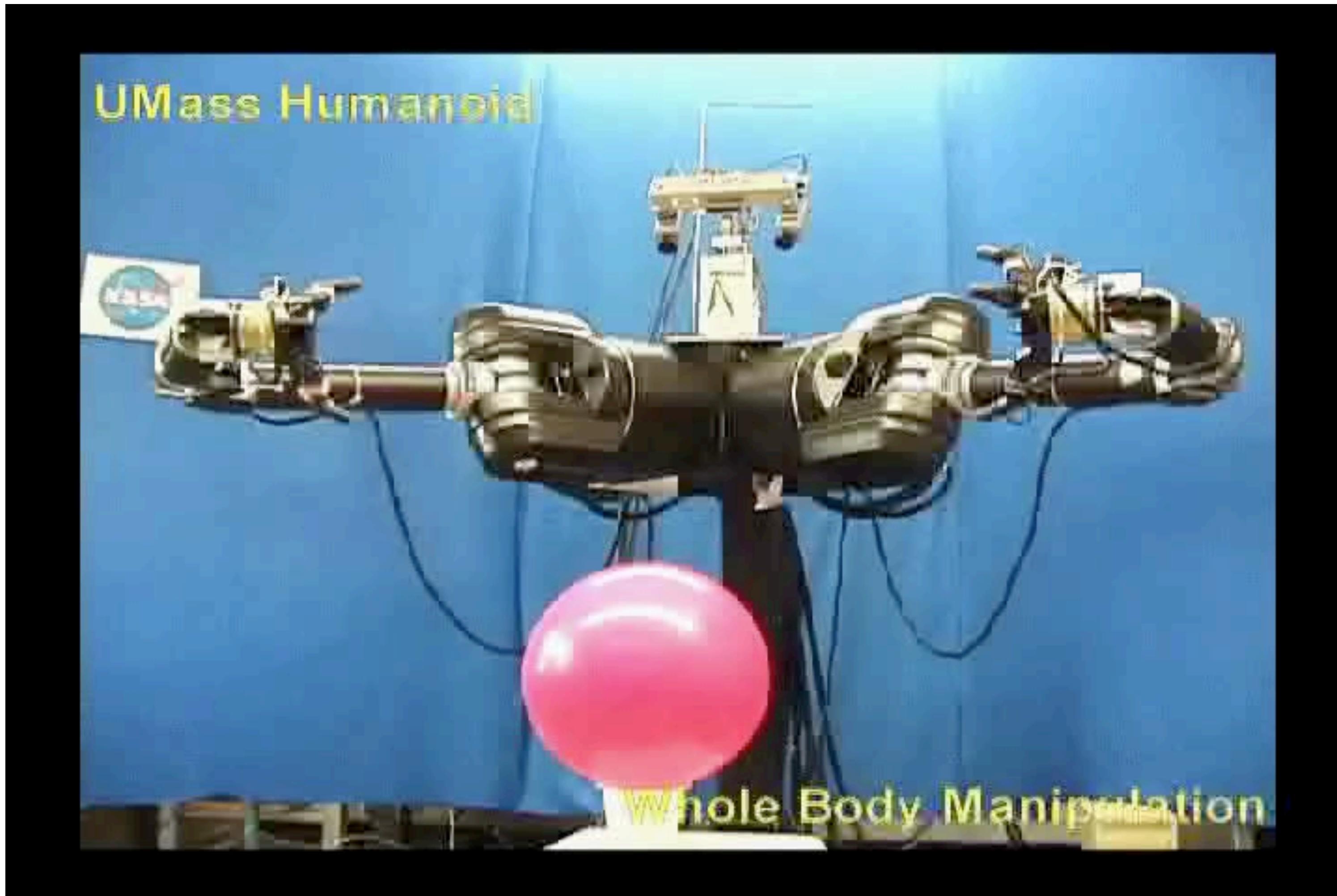
<https://www.youtube.com/watch?v=G4ocrevf4ng>



# Vacuuming Finite State Machine



# Manipulation Gaits



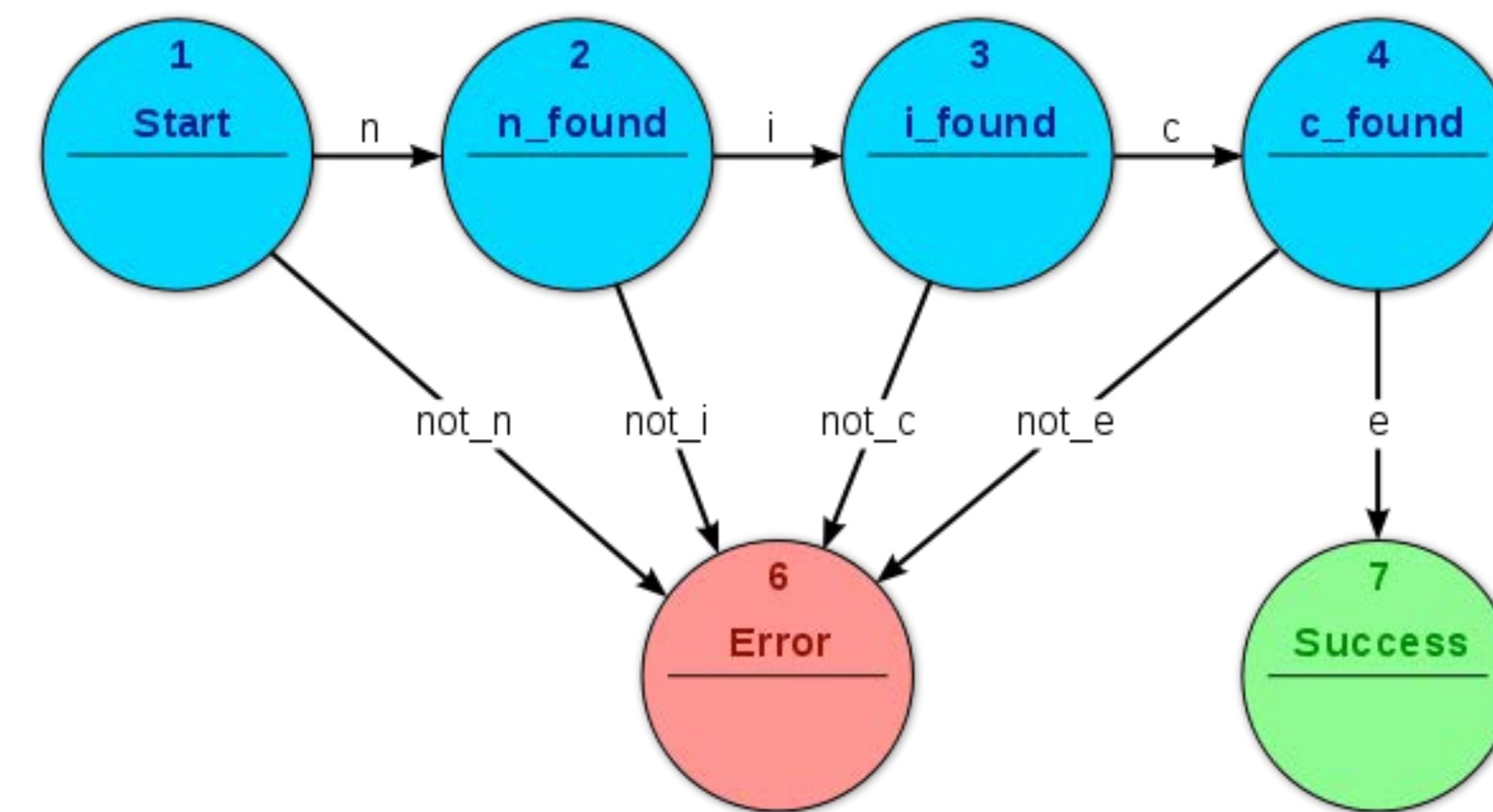
Collections of robust  
manipulation controllers

# How do we computationally represent reactive control?

# “nice” recognizer

- recognize the string “nice” from input

- if input is “nice”
    - output **success**
  - if input not “nice”
    - output **error**



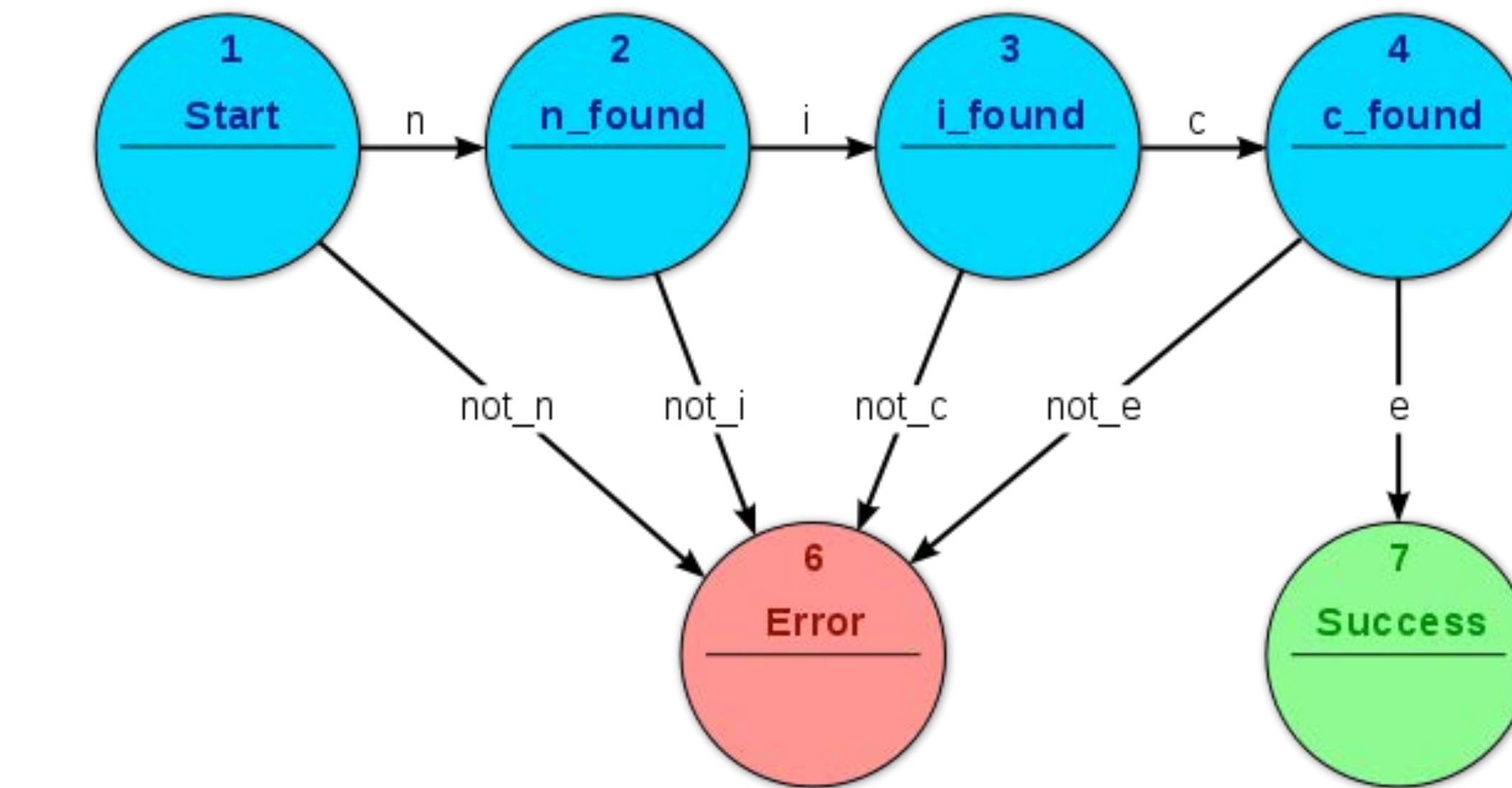
- robotics uses
  - preconditions (enter state)
  - postconditions (exit state)

```

state ← start
while state != success and state != error
    token ← <next string character from input>
    switch (state):
        case start:
            if token = "n" then state ← n_found
            else state ← error
            break
        case n_found:
            if token = "i" then state ← i_found
            else state ← error
            break
        case i_found:
            if token = "c" then state ← c_found
            else state ← error
            break
        case c_found:
            if token = "e" then state ← success
            else state ← error
            break
    end while loop
    output ← state

```

“nice” recognizer



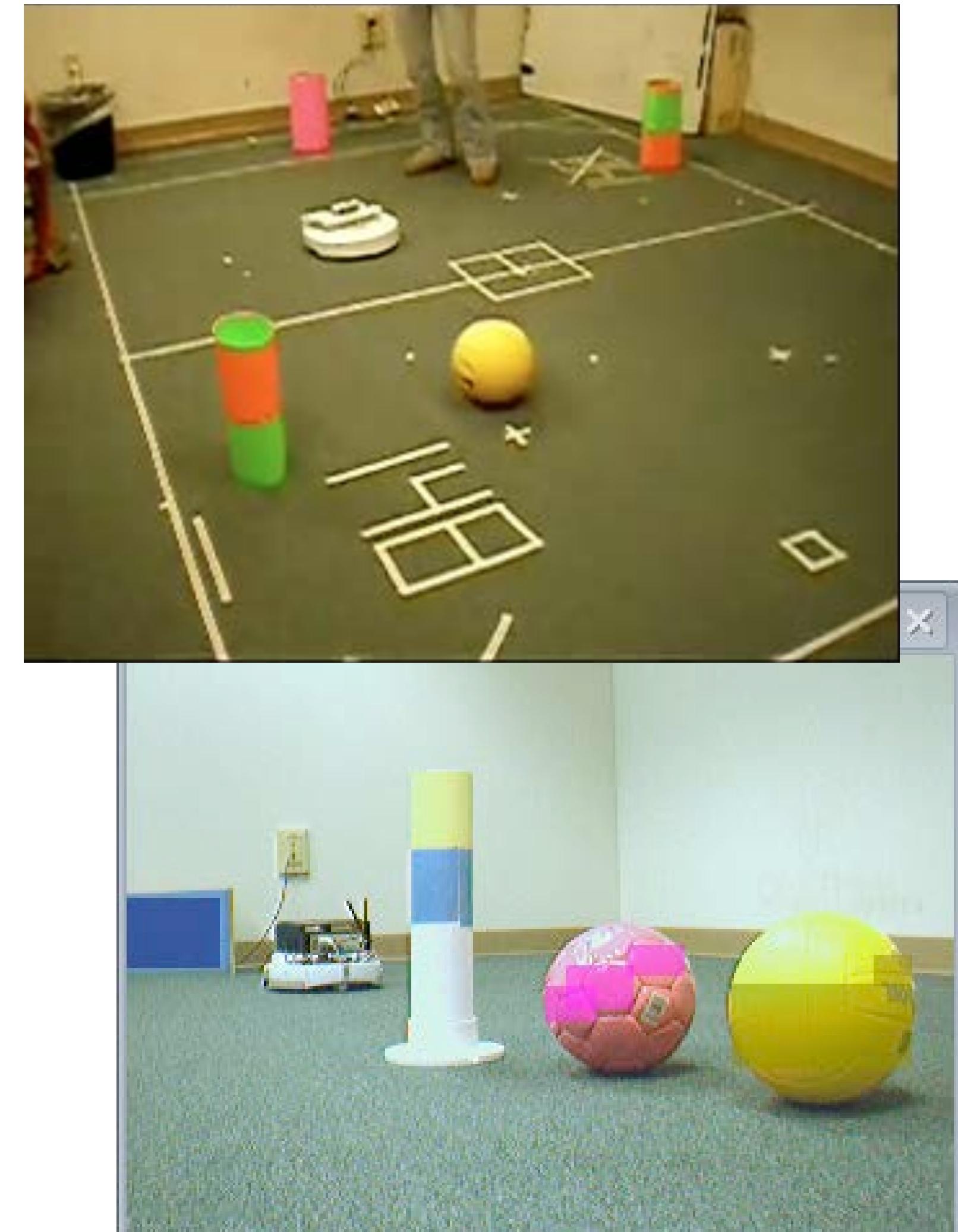
Consider input: “nice”

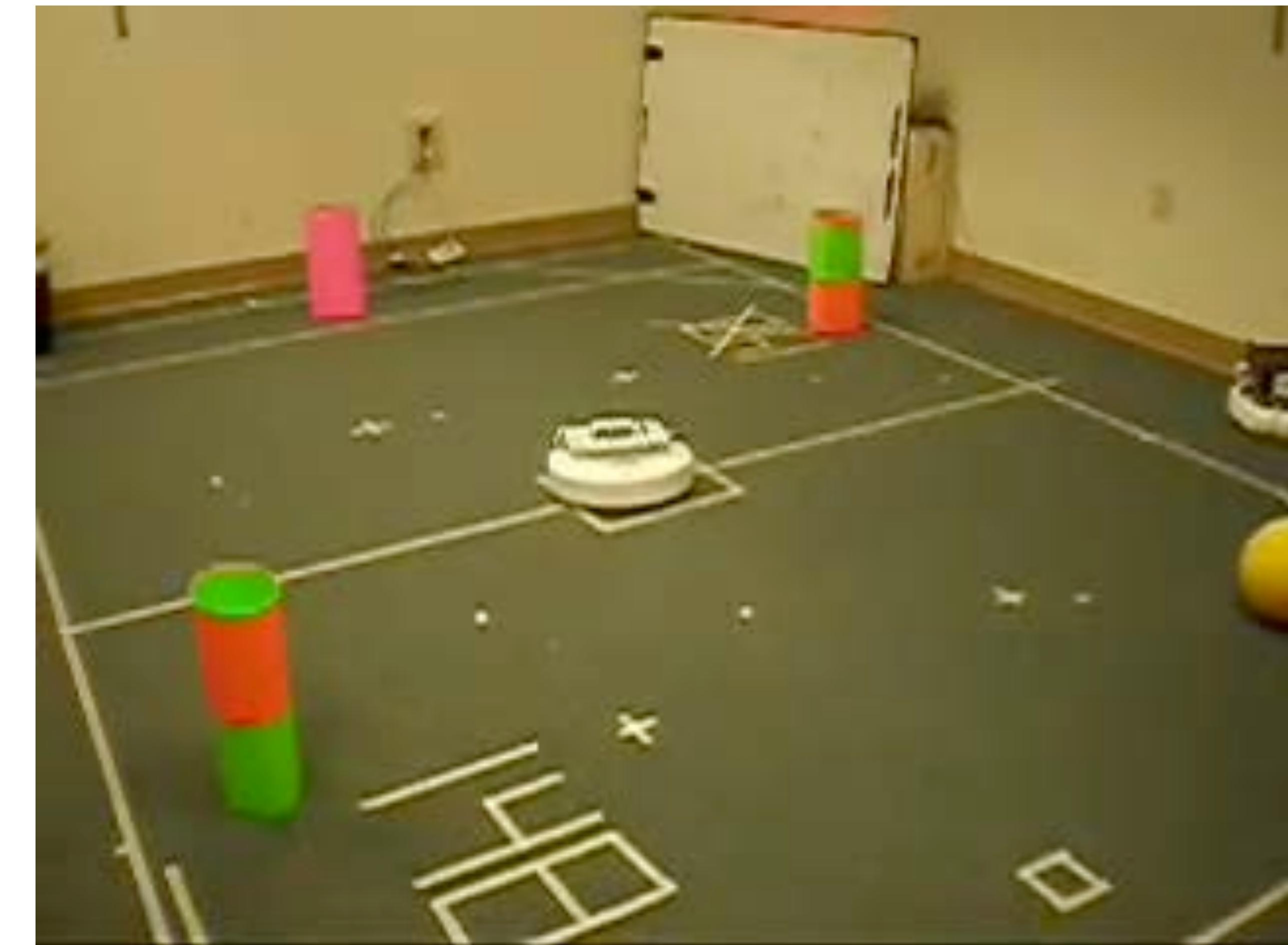
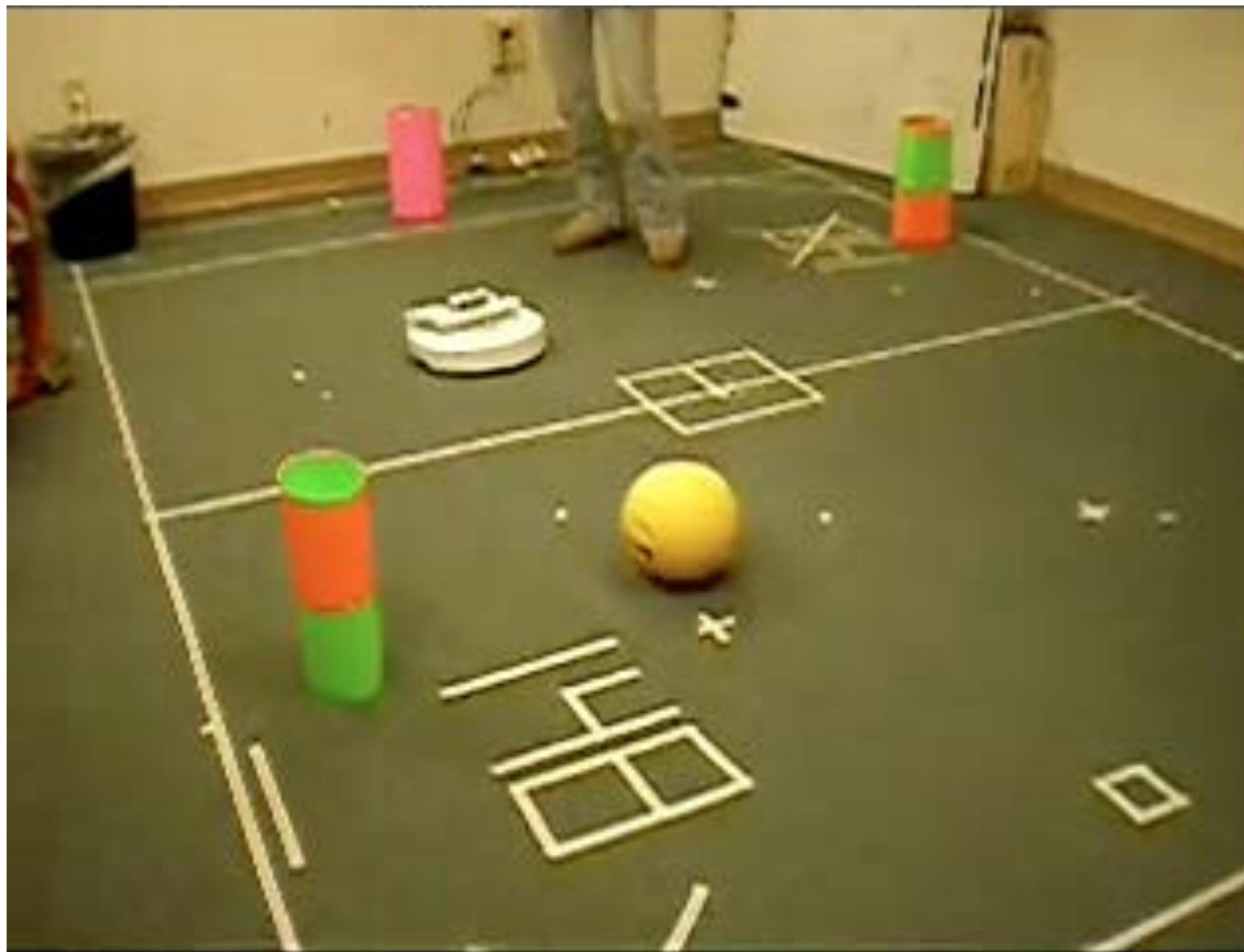
Consider input: “robotics”

Consider input: “niece”

# Move to objects in sequence?

- How to move a mobile robot to a given sequence of objects?
  - yellow ball
  - green/orange landmark
  - pink landmark
  - orange/green landmark



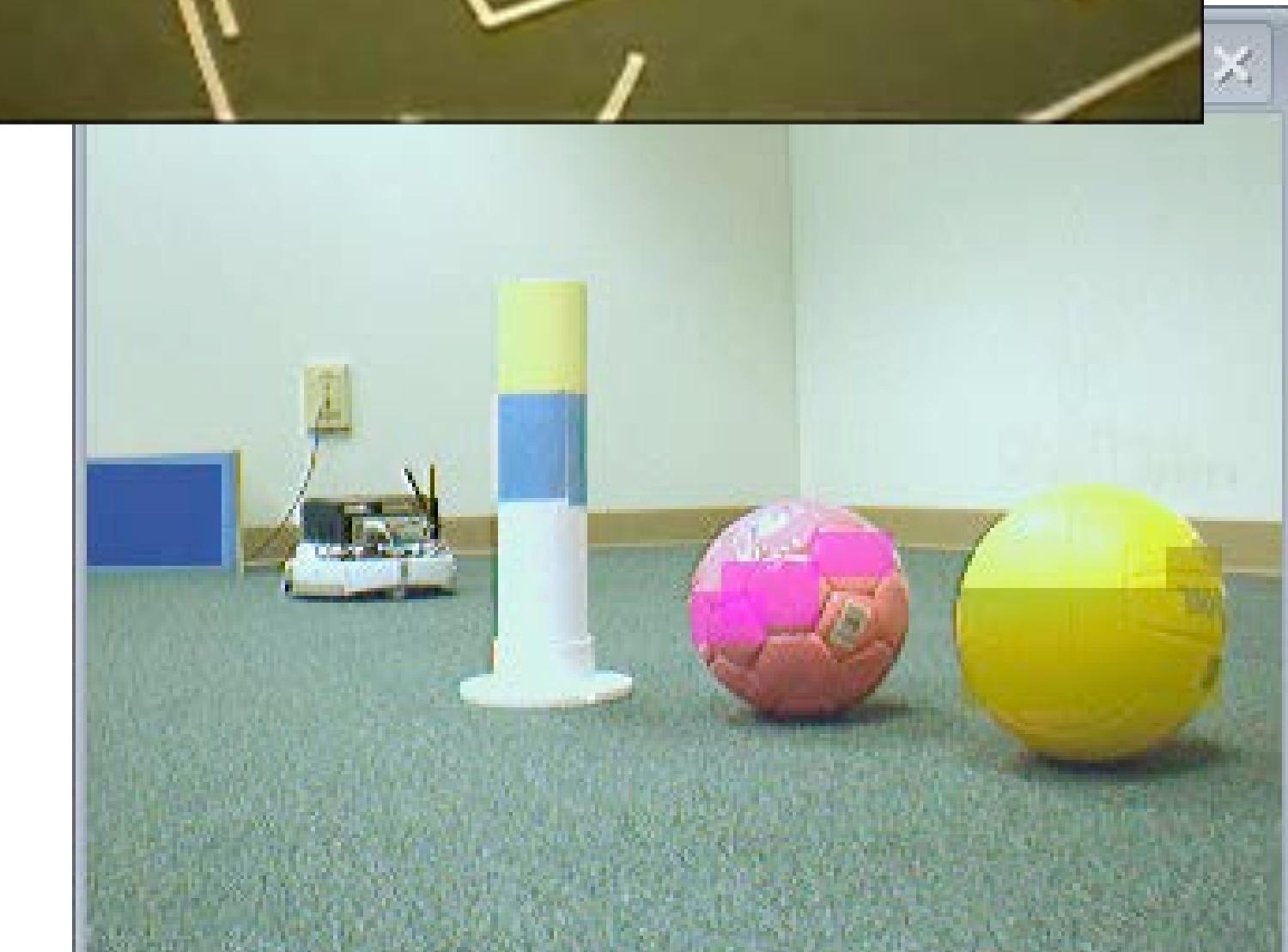
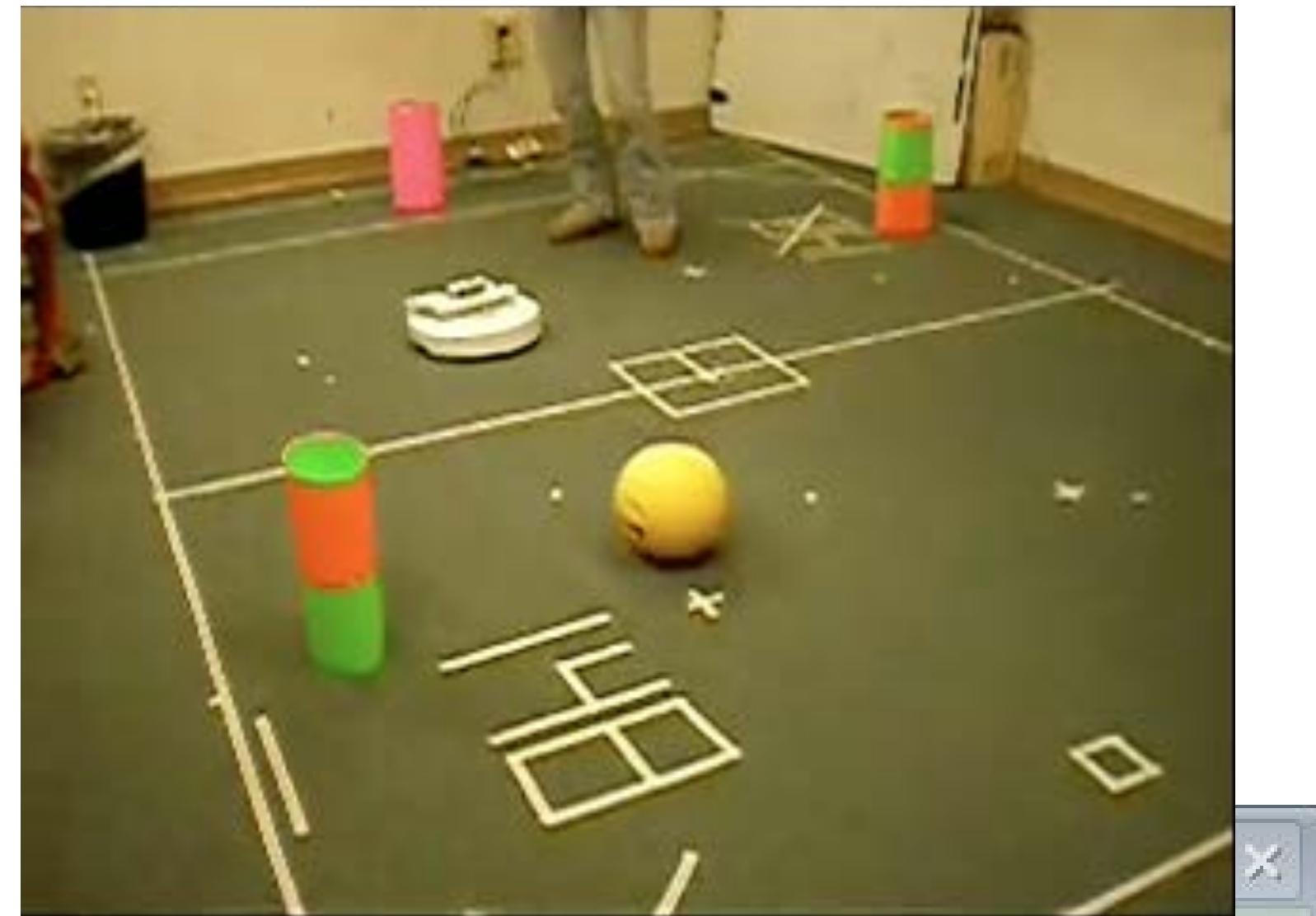


# Object Seeking

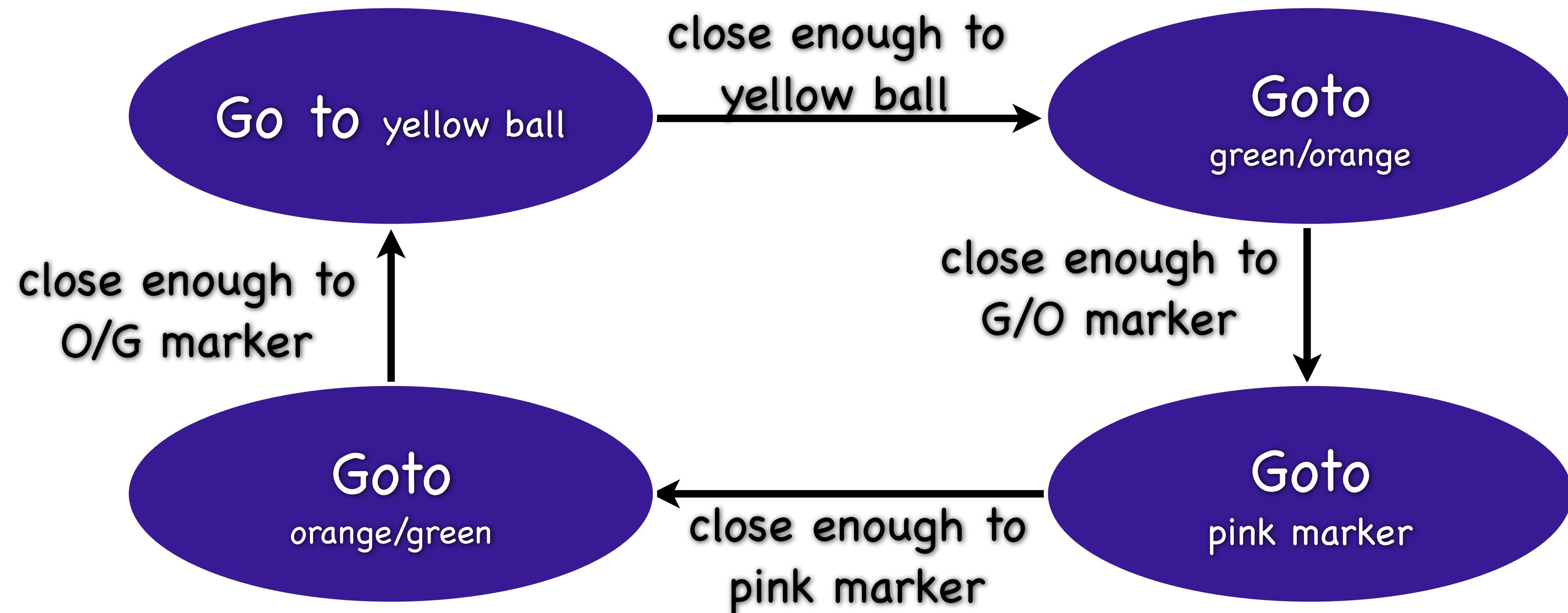
<http://www.youtube.com/watch?v=-hOA0jMUggg>

# Move to objects in sequence?

- What are the states?
- What are the transitions?
- Preconditions for states?
- Postconditions for states?

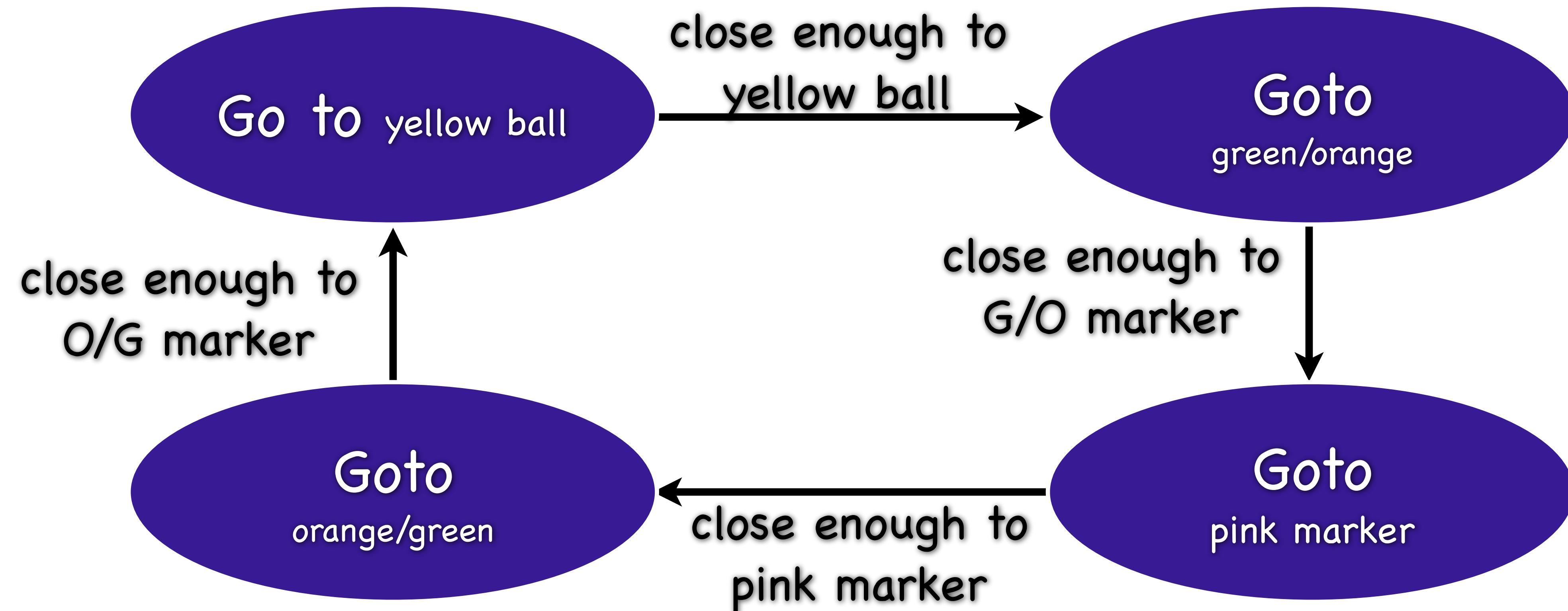


# Object seeking FSM



# Object seeking FSM

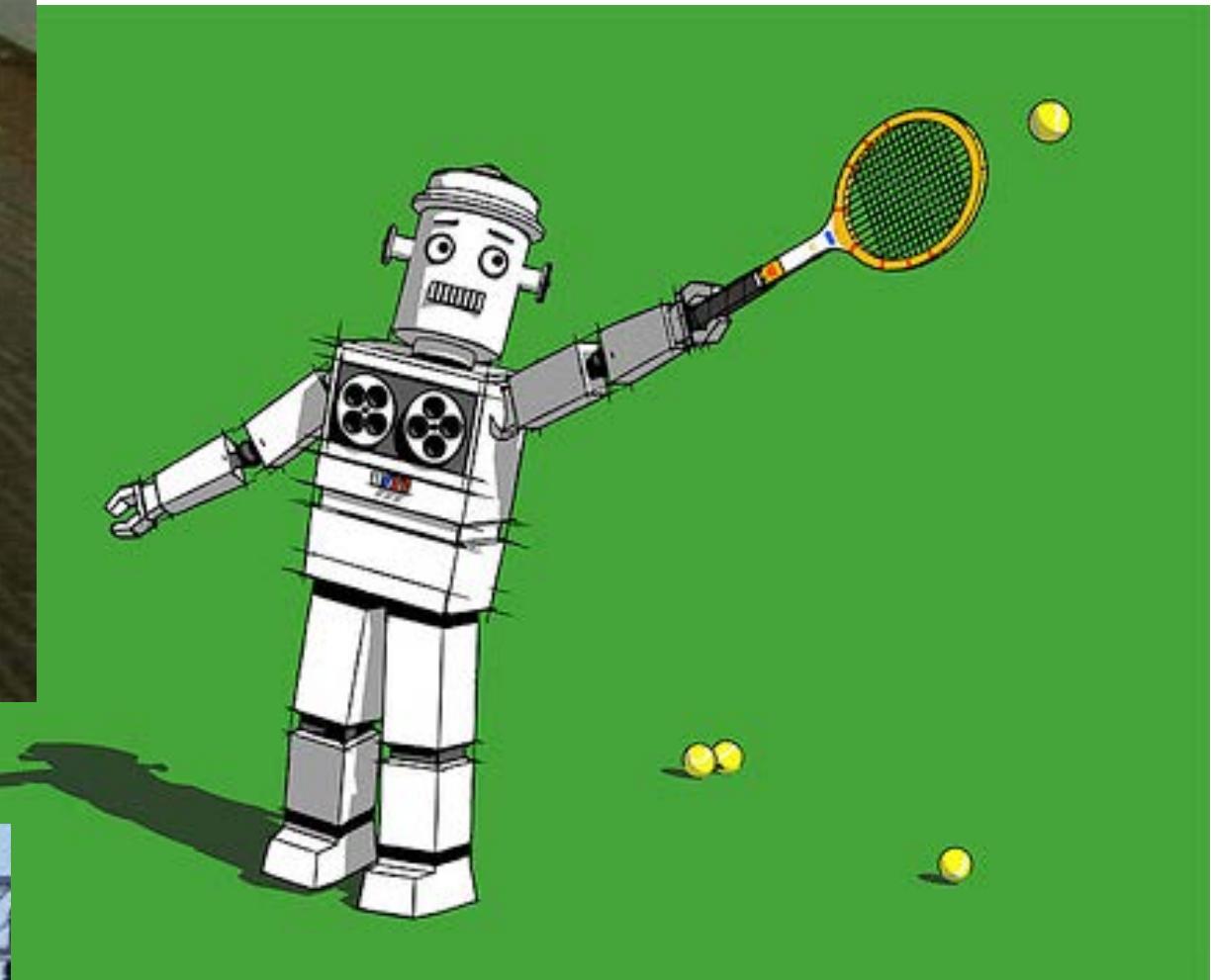
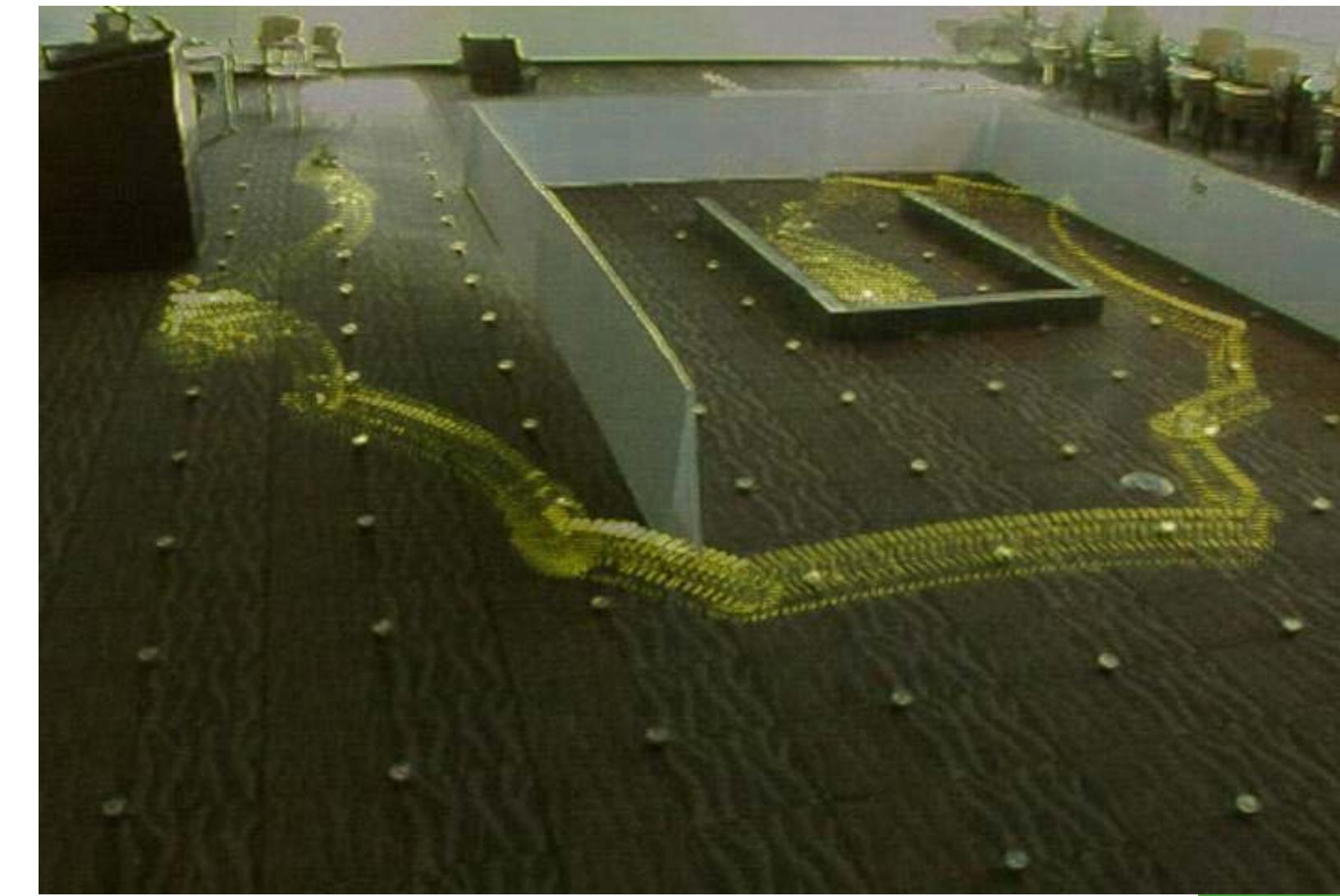
How to implement state?



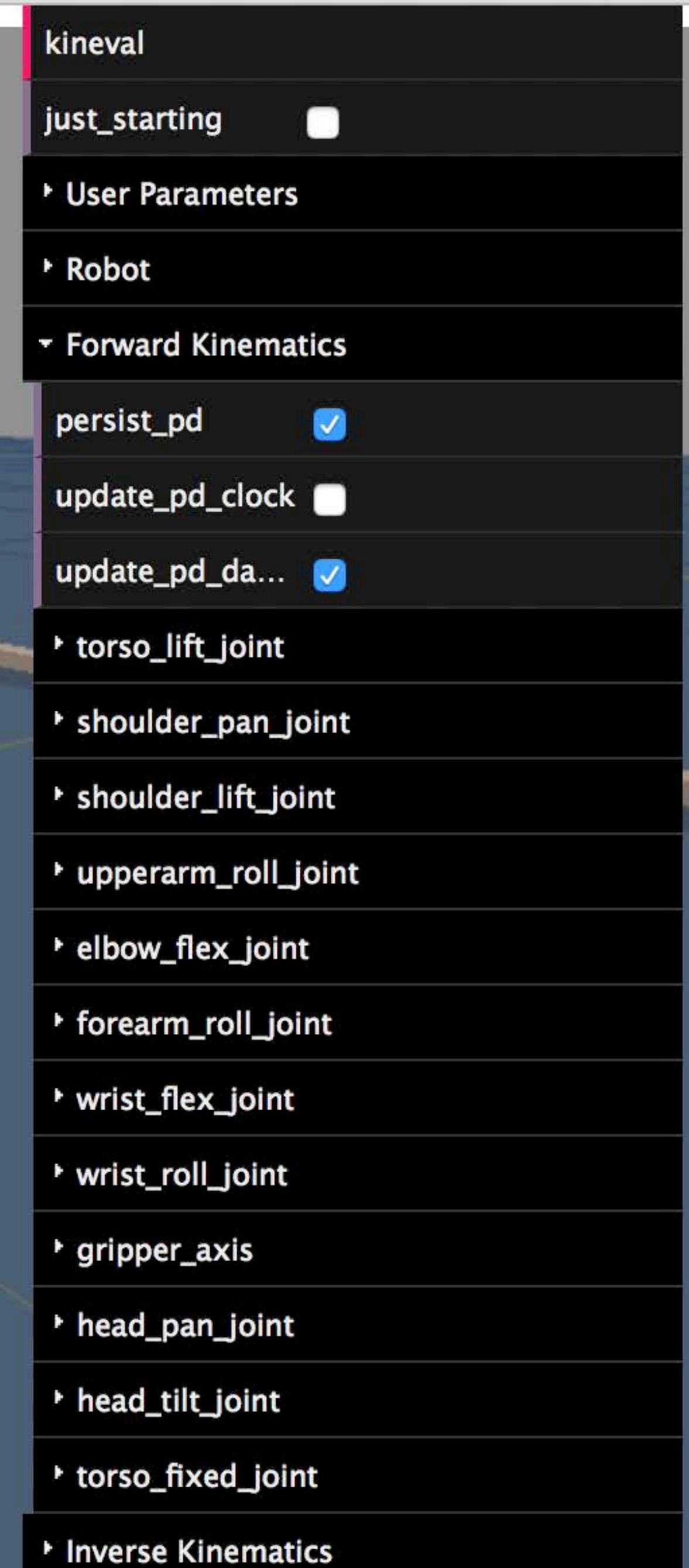
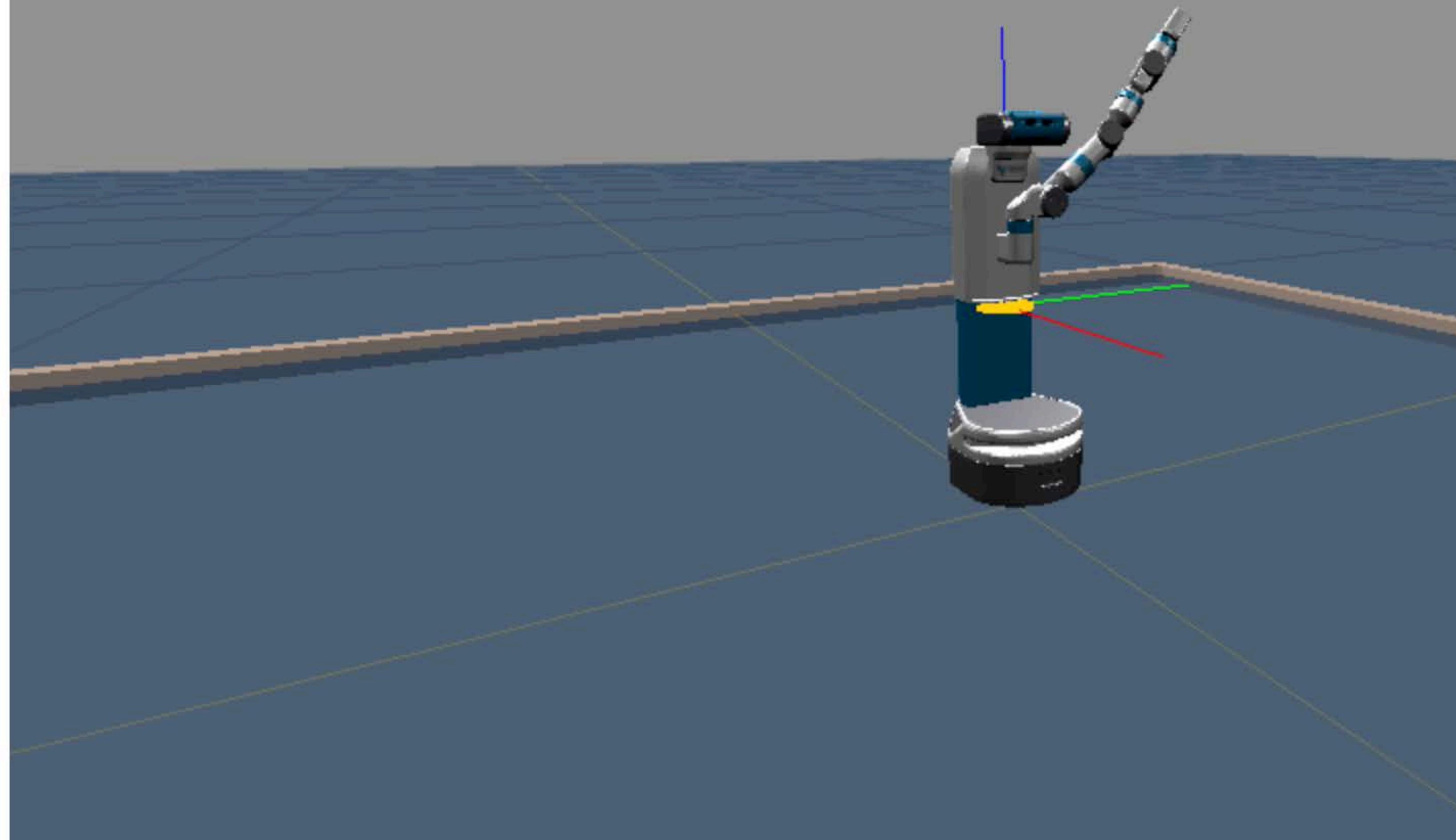
How to detect “close enough”?

# FSMs for Other Tasks

- Robot foraging?
- Robot tennis/pong?
- Pushing a ball into a goal?
- Vacuuming a room
- Driving a car?
- Robot dancing!



joint servo controller has been invoked  
executing dance routine, pose 2 of 10



P3 robot dance (by ohseejay)

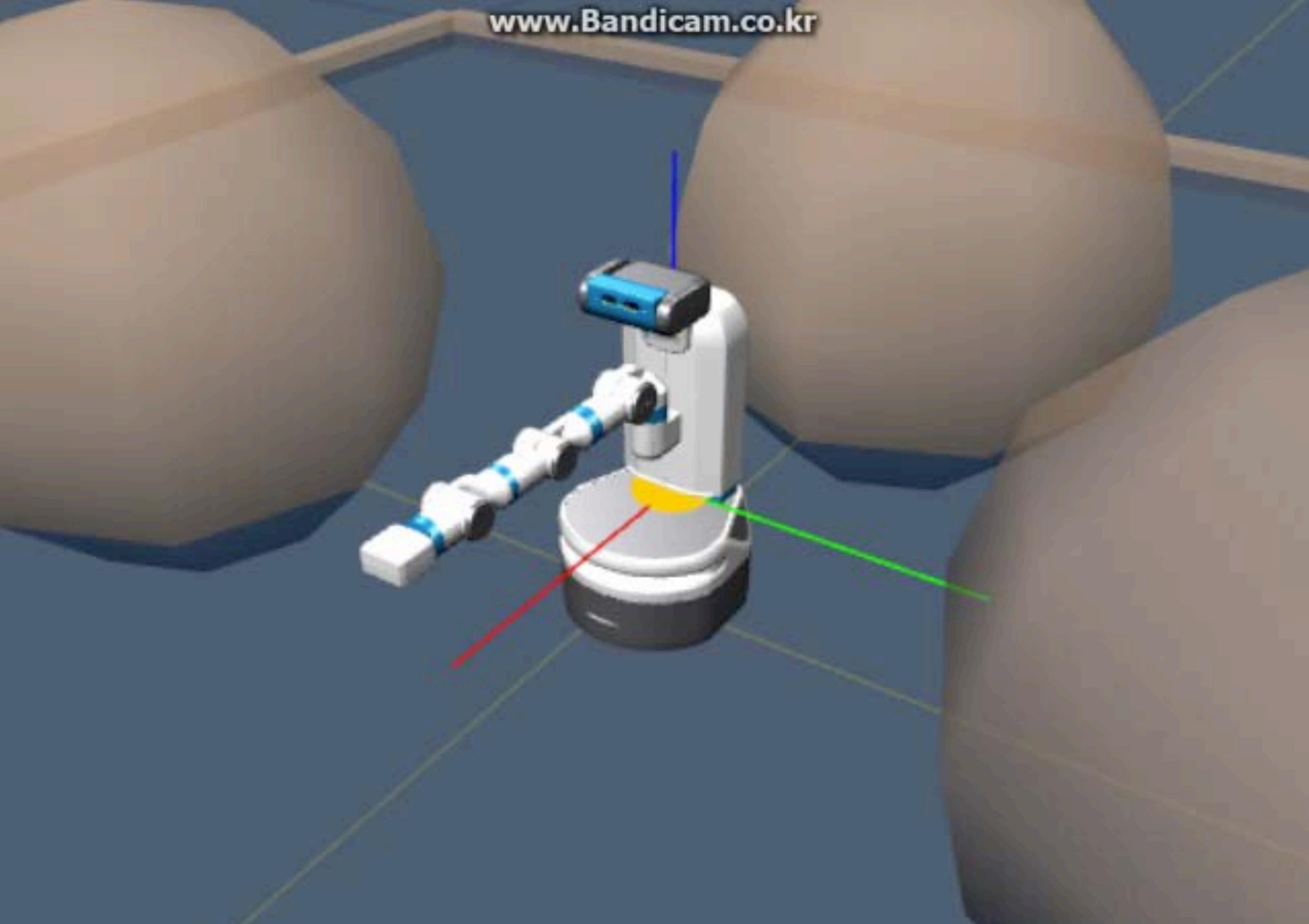
<https://www.youtube.com/watch?v=WyQ9aoB3bpl>



An aerial photograph of a small white boat with a grey stripe docked at a wooden pier. The pier extends from the bottom left towards the center of the frame. The water is a clear blue. In the background, there are some buildings and trees under a clear sky.

sreesha

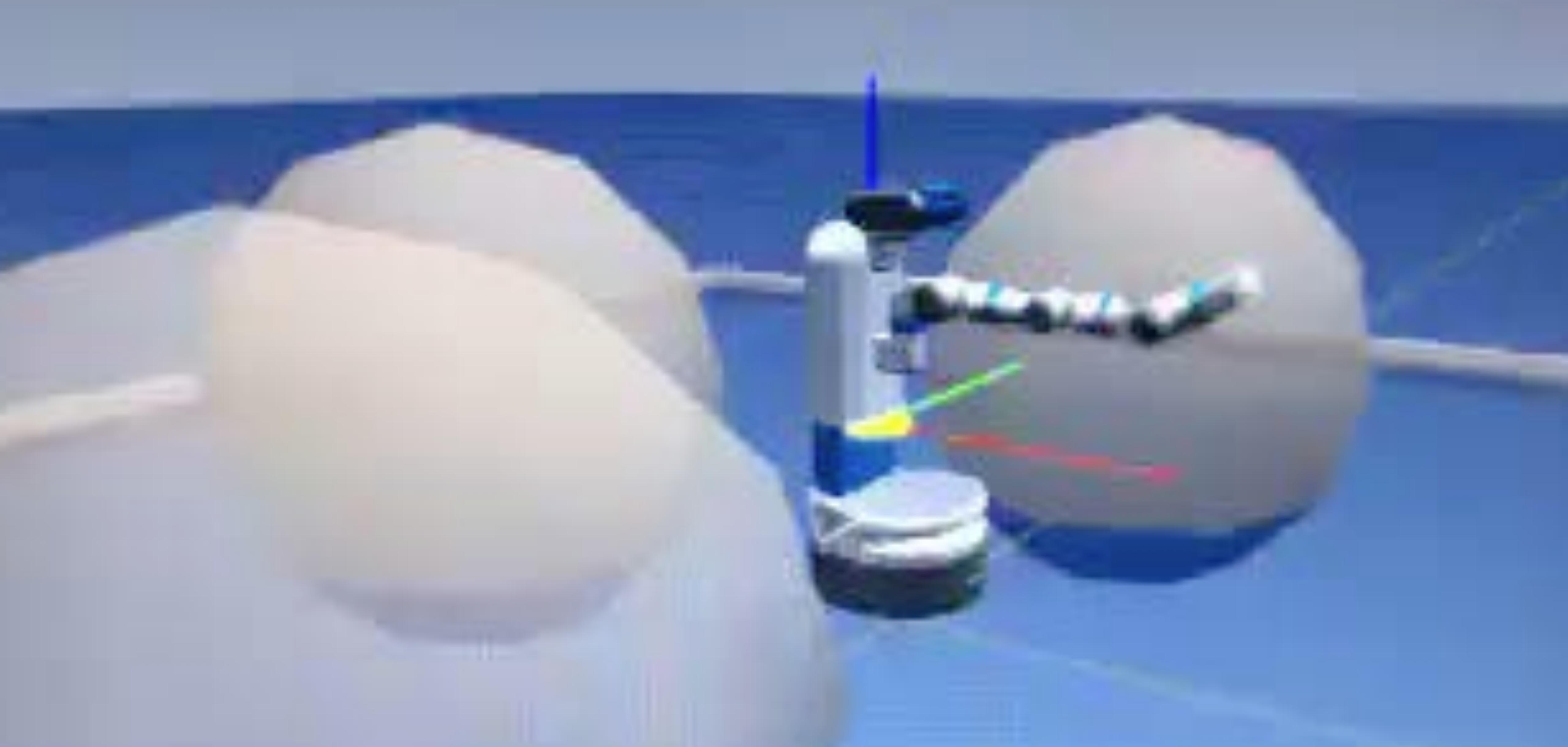




heostar

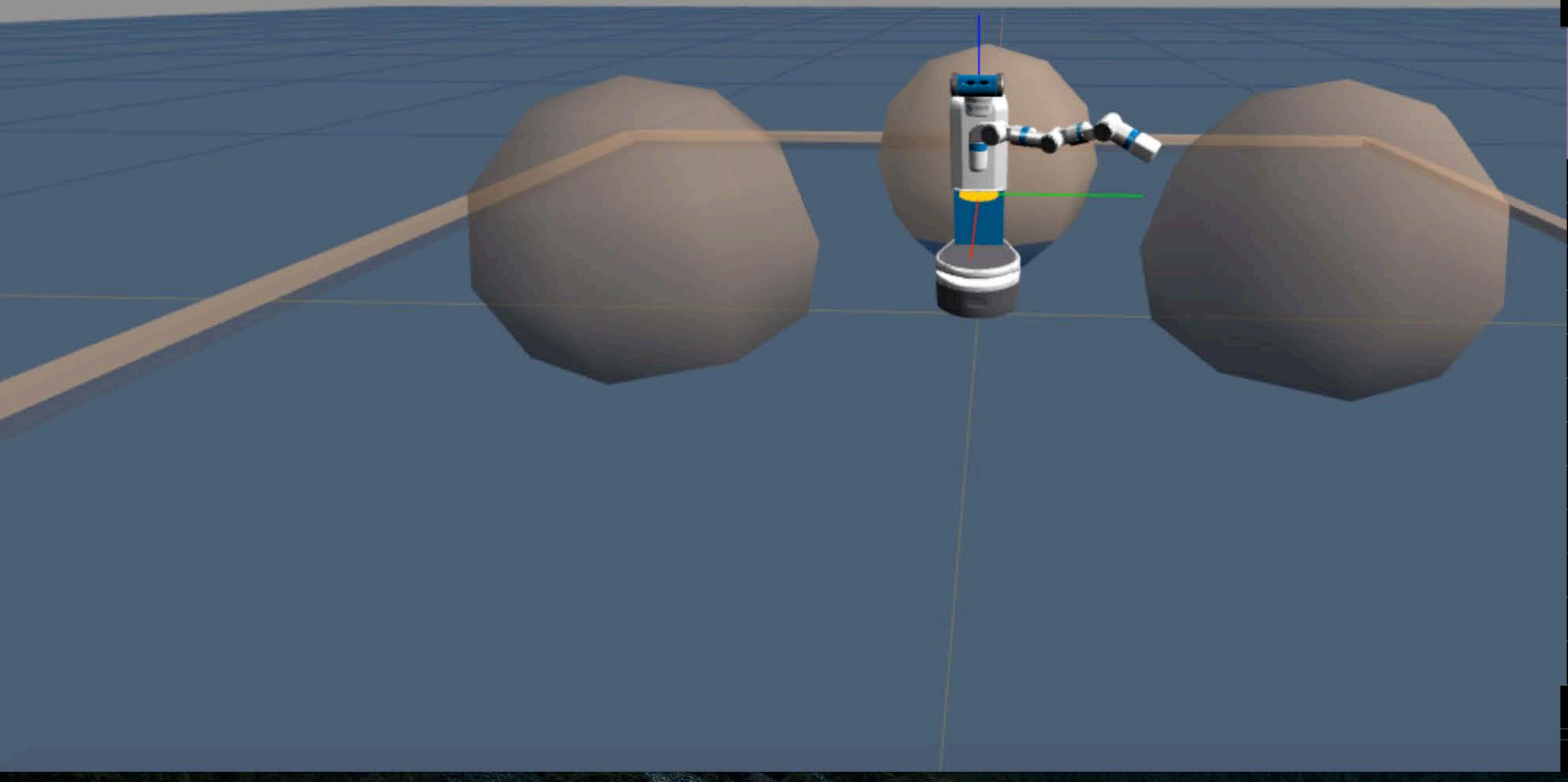


noah



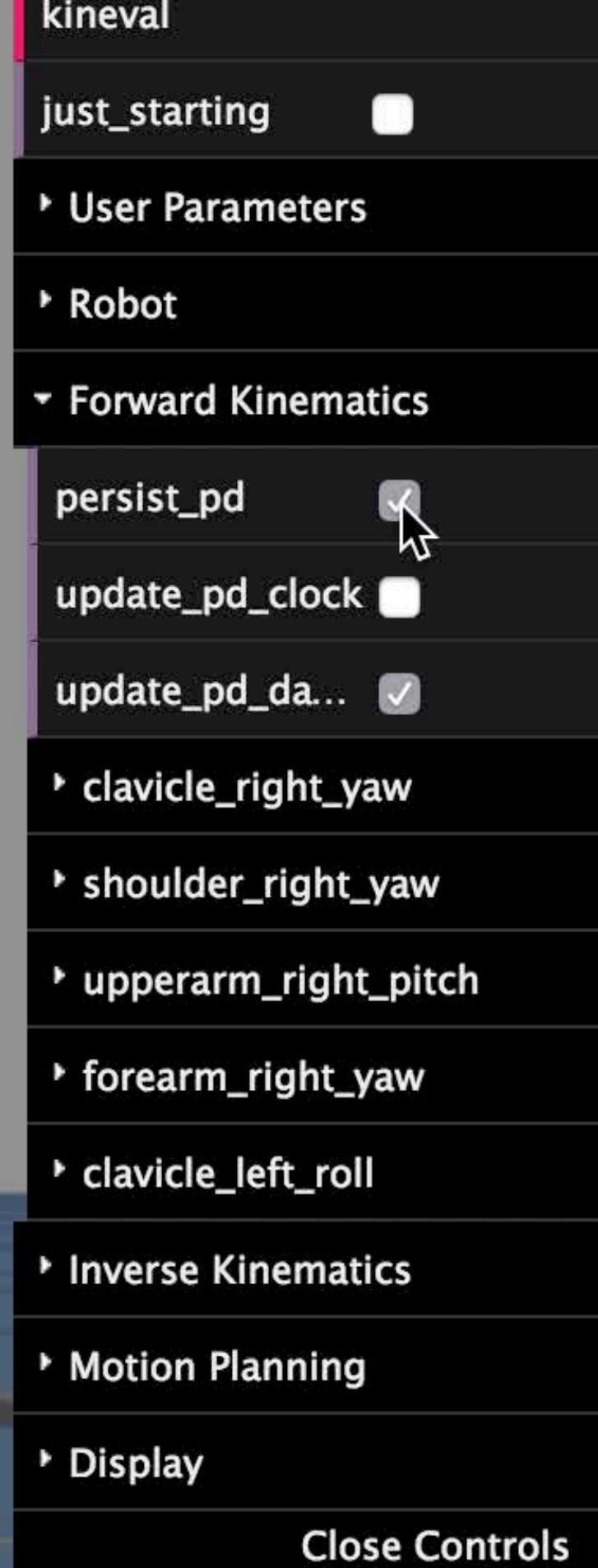
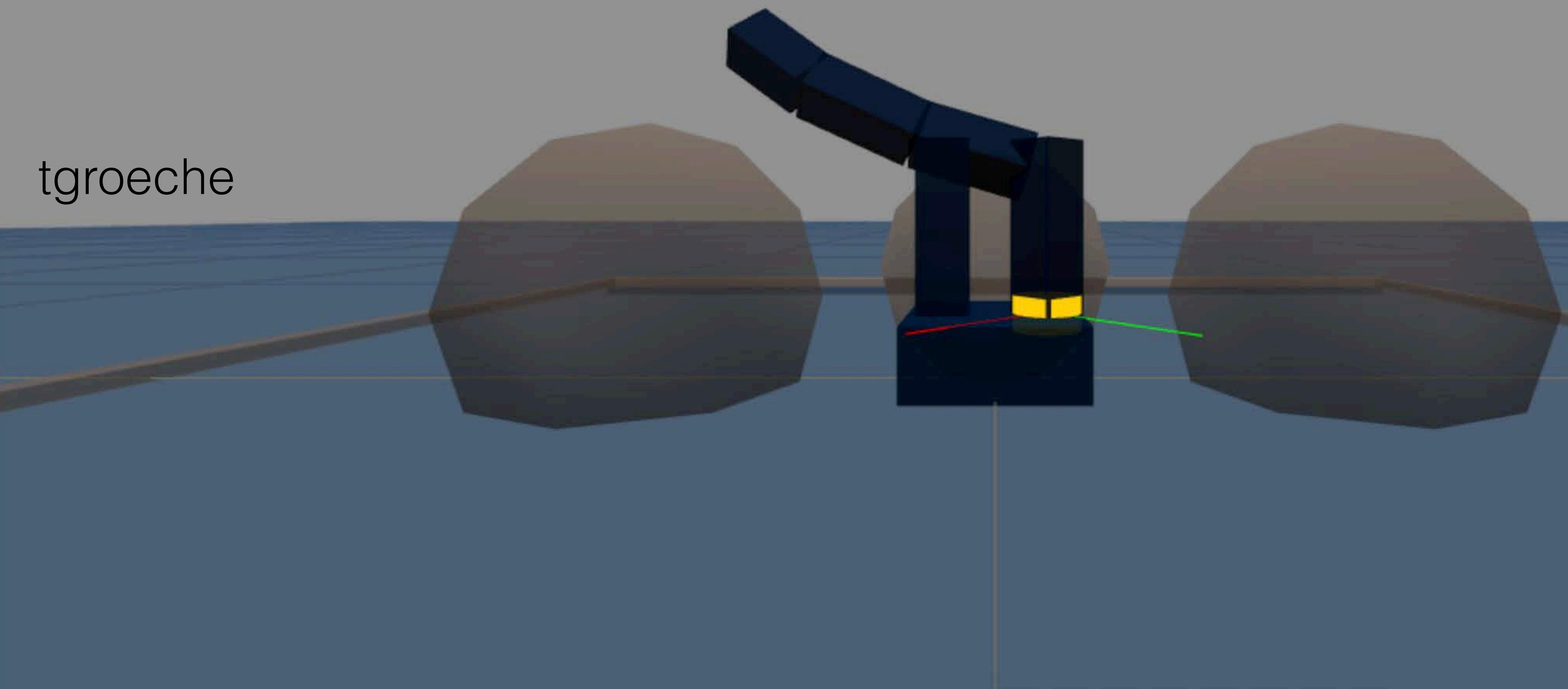
oint servo controller has been invoked  
ecuting dance routine, pose 4 of 10

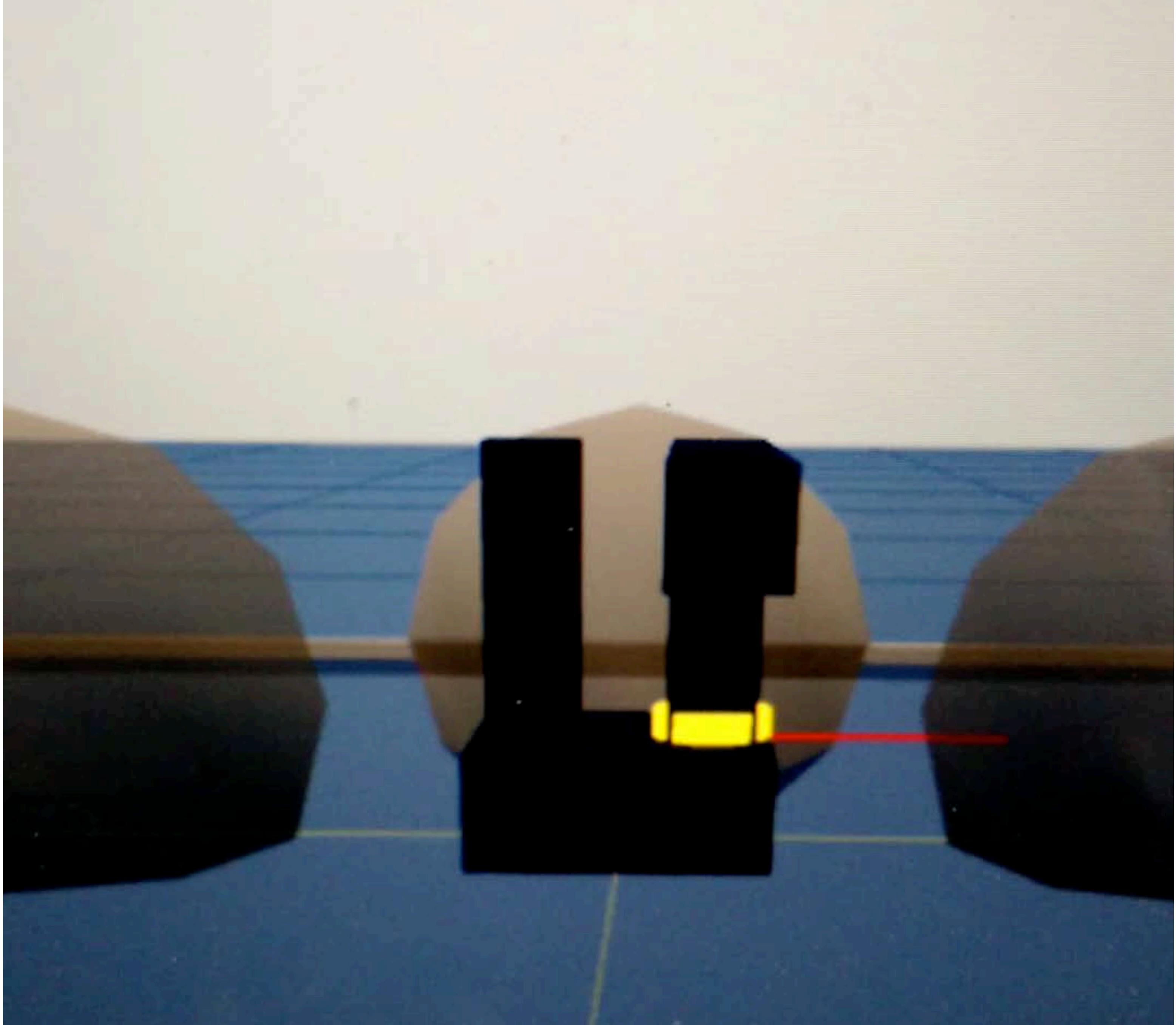
cneeruko



joint servo controller has been invoked  
executing dance routine, pose 9 of 10

tgroeche



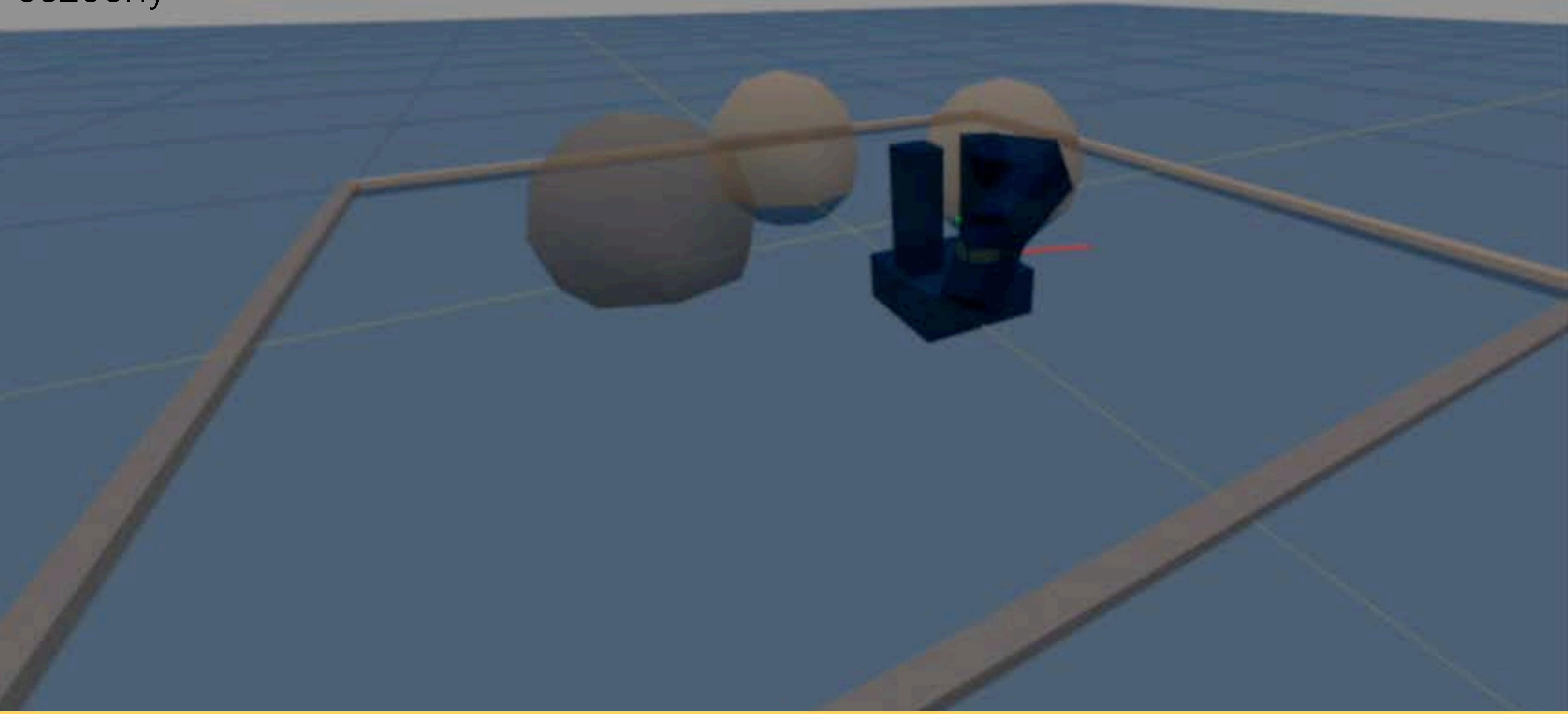


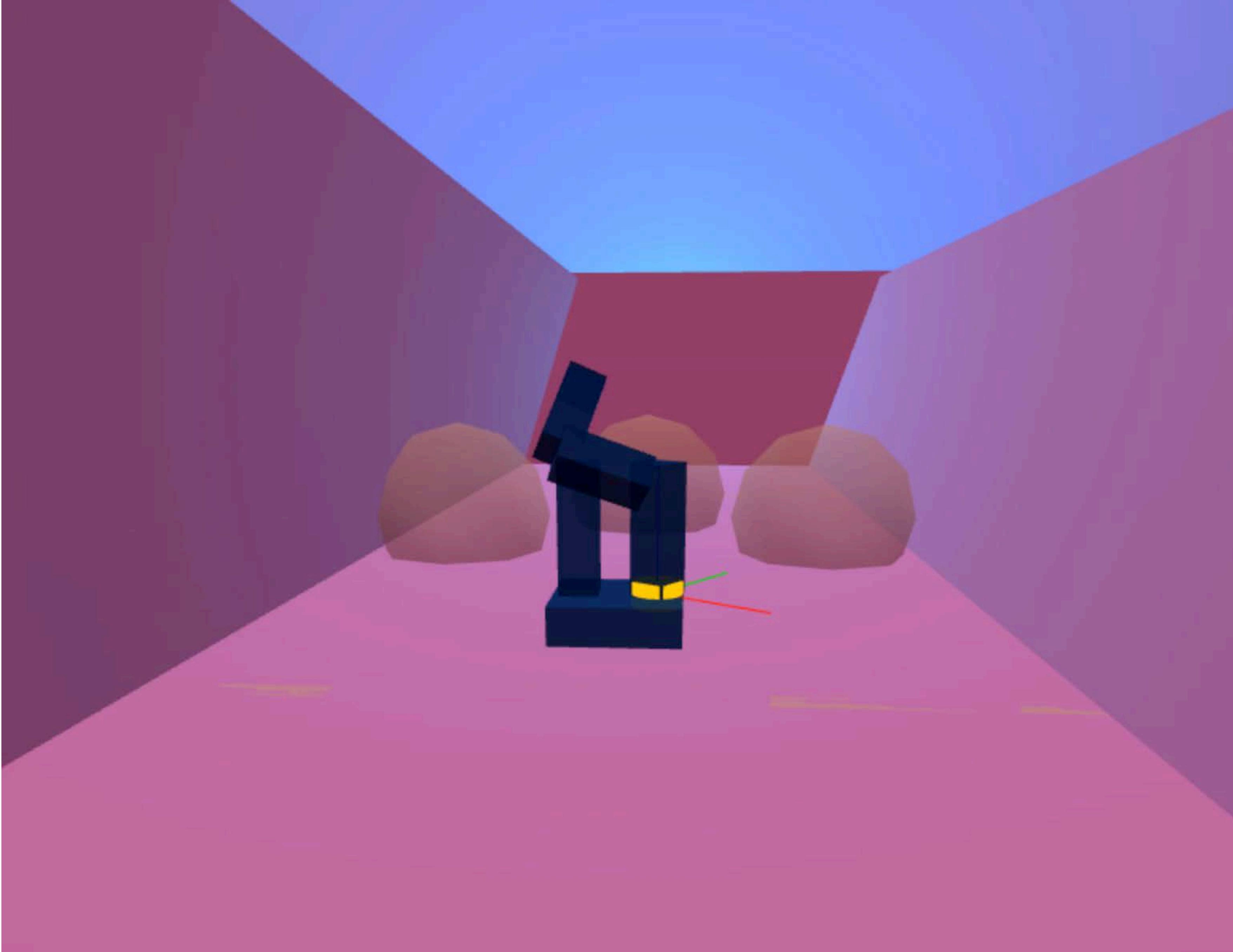
ankit





cszechy





cszechy  
ohseejay



# Let's generalize FSMs for robot control



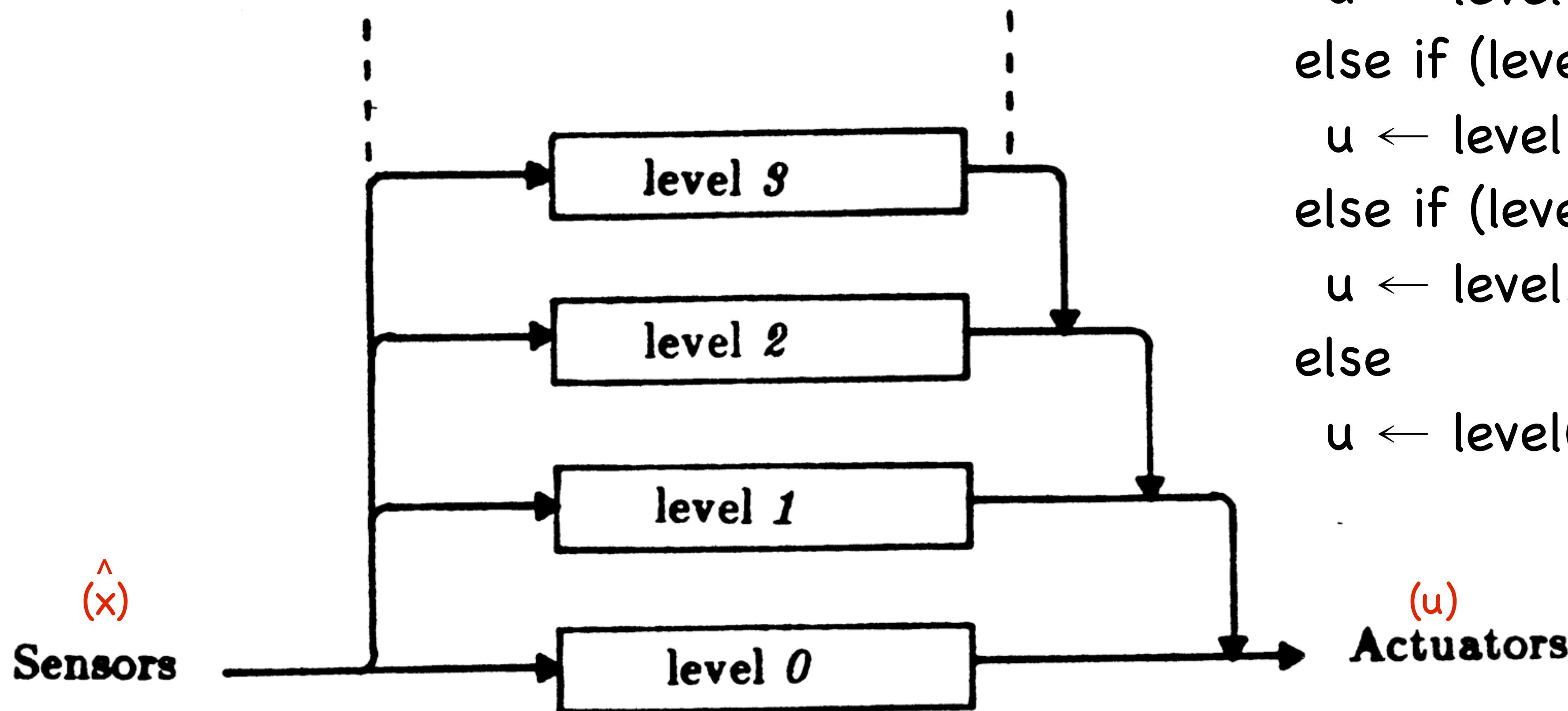
# Subsumption Architecture

[Brooks 1986]

- Generalization of FSM-based control
- Collection of modular reactive controllers in a priority hierarchy
- Controllers can be FSMs
- Large nested if-else statement
- Most robots are controlled by some form of subsumption



# Subsumption Architecture



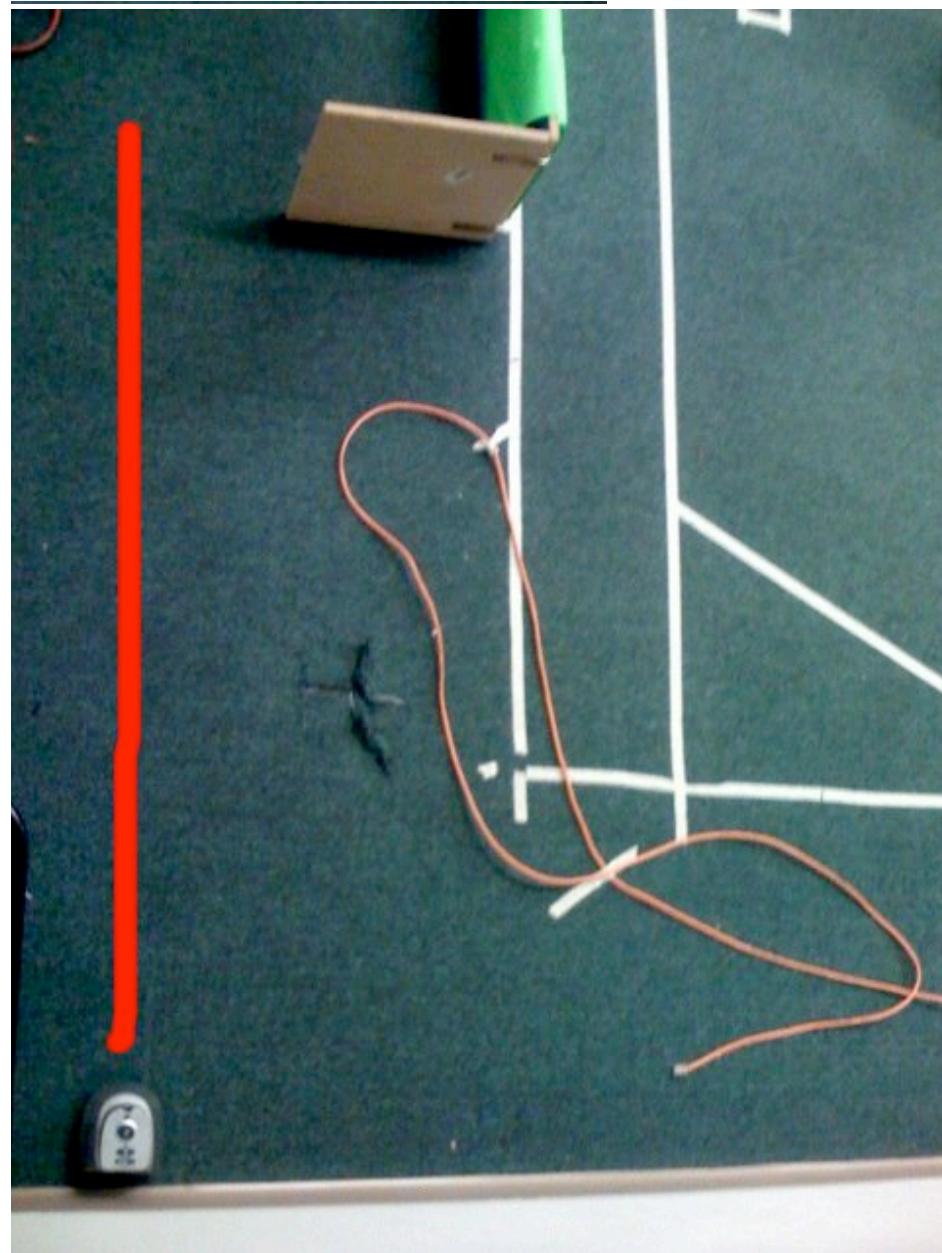
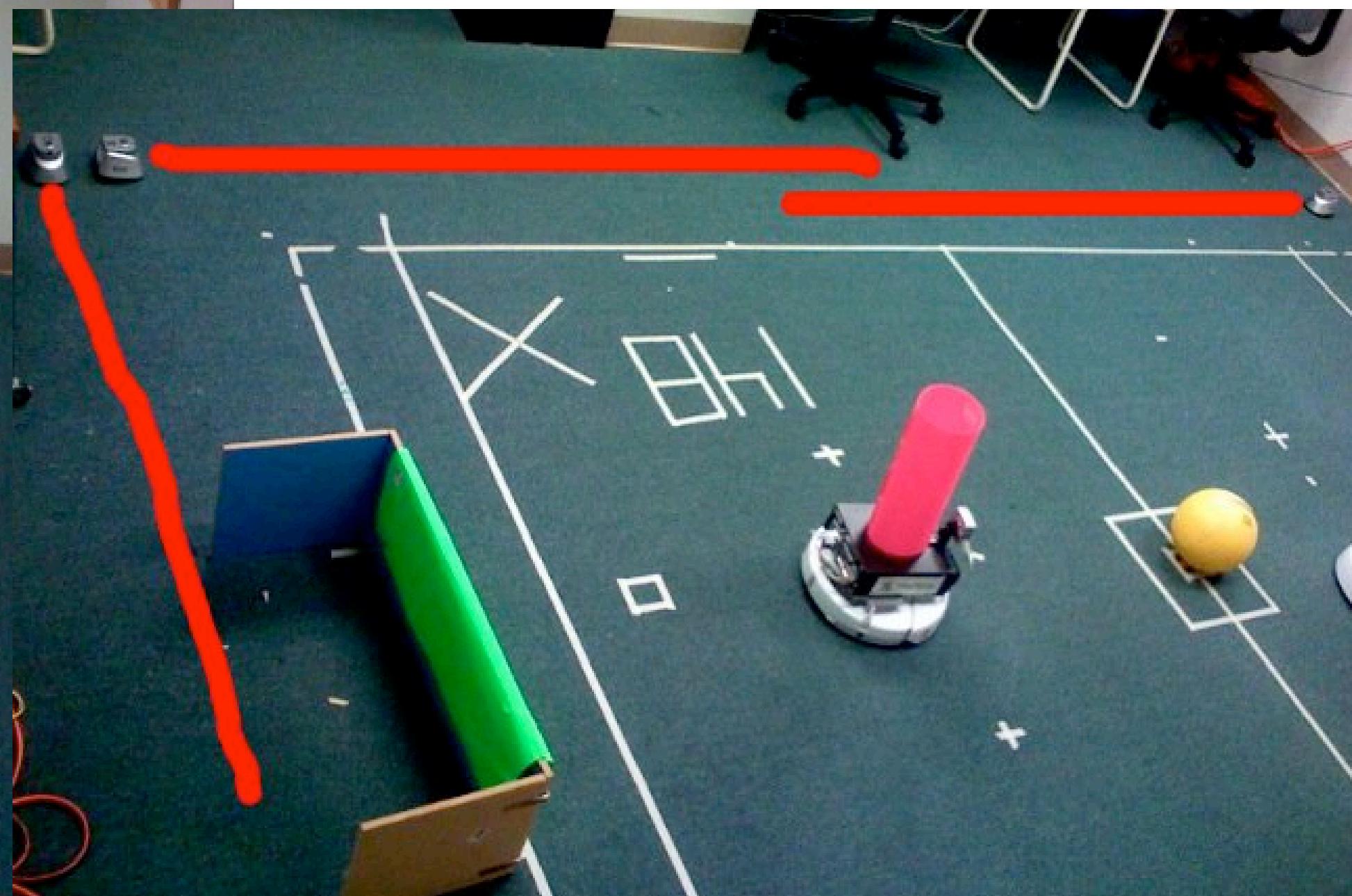
```
if (level3_condition)  
    u ← level3_control  
else if (level2_condition)  
    u ← level2_control  
else if (level1_condition)  
    u ← level1_control  
else  
    u ← level0_control
```

# Subsumption Design Process

- 1. Divide your problem into basic competencies** ordered simple to more complex.  
Designate a level for each basic competency.
- 2. Subdivide each level into multiple simple components** that interact through shared variables. Limit the sharing of variables among levels to avoid incomprehensible code.
- 3. Implement each module as a separate light-weight thread.** You might think of setting the priorities for these threads s.t. modules in a given level have the same priority.
- 4. Implement "arbitration" processes** for suppression and inhibition as one or more separate that serve to control access to shared variables. You might want to control access using semaphores.

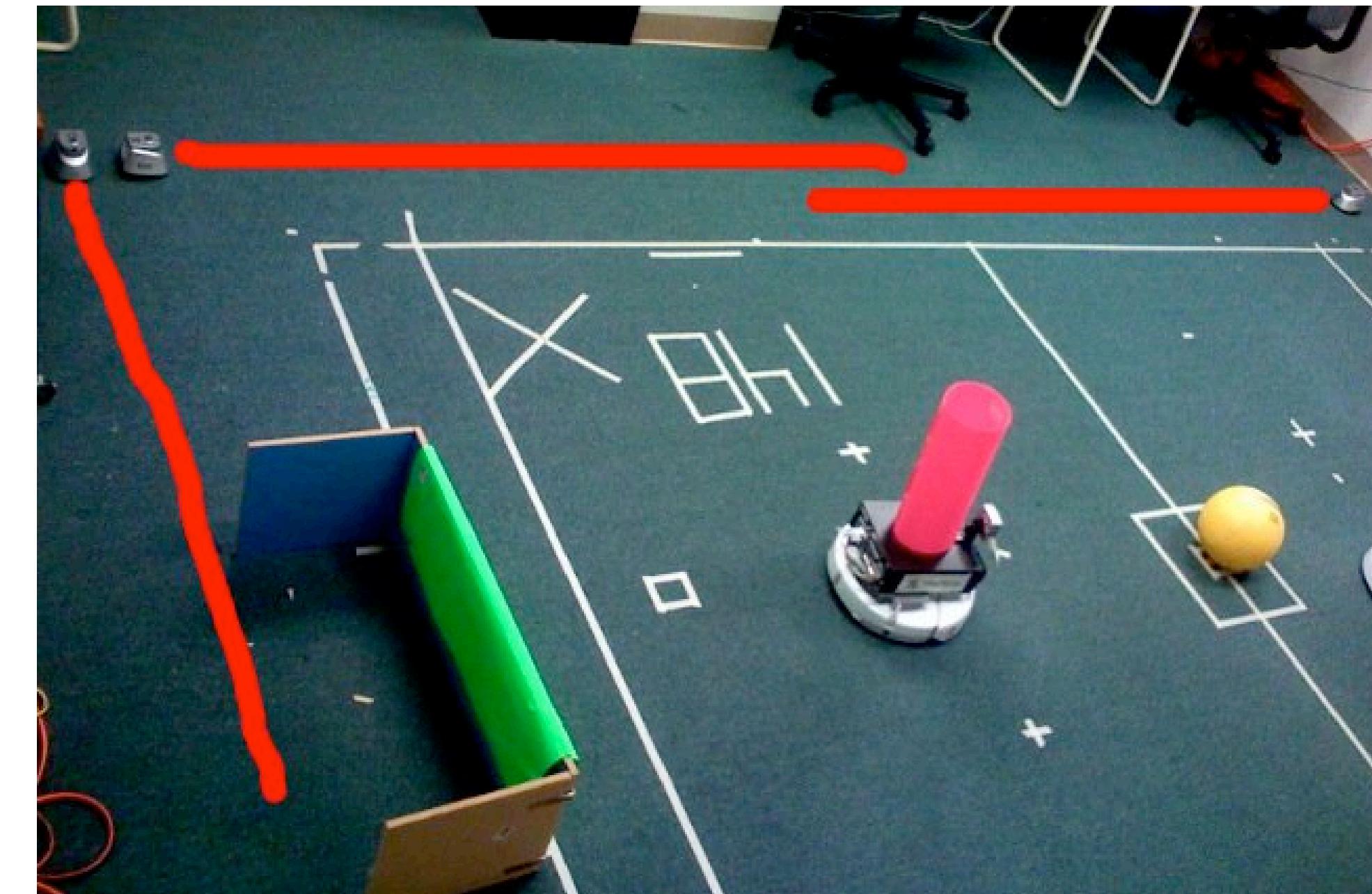
# Subsumption for robot soccer

- Propose modules and priority?



# What behavior will result?

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball



# Snappy's Subsumption: Goal Scoring

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball

Goal Scoring Challenge - Put ball into the orange post



# Snappy's Subsumption: Navigate to Ball

1. Avoid IR Wall
2. Avoid Robot
3. Avoid Fiducial
4. Bumper Hit
5. Go To Opposite Goal
6. Go To Any Goal
7. Line Up On Ball
8. Go To Ball
9. Score Goal
10. At Ball
11. Look For Ball



Are there other methods of  
decision making?

# Types of Decision Making

- Deliberative (Planner-based) Control
  - “Think hard, act later.”
- Reactive Control
  - “Don’t think, (re)act.”
- Hybrid Control
  - “Think and act separately & concurrently.”
- Behavior-Based Control
  - “Think the way you act.”

# Next lecture: Inverse Kinematics

