



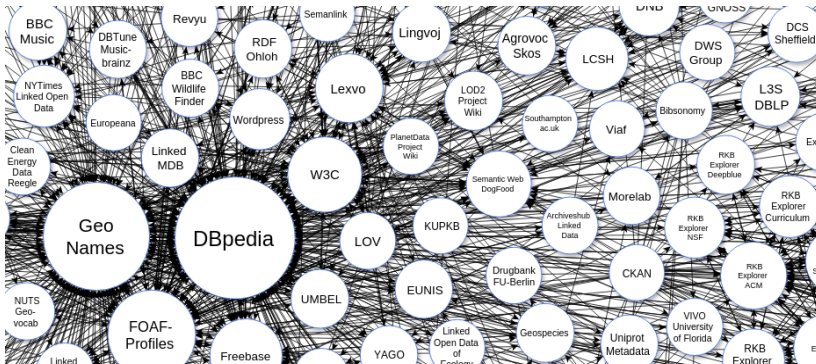
# ABSTATInf: Inference of Knowledge Patterns for Linked Data Sets Summarization

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Assignment for the Course: The Impact of Logic: from Proof Systems to Databases

# Linked Data Set Understanding



What types of resources are there in a data set? How are they described?  
What properties are used to link different types of resources? How frequently?  
Are data described as prescribed by the ontology?

## ABSTAT Linked Data set summarization framework [1]

- ▶ compact and concise representation of a data set (i.e. **summary**)
- ▶ formal modeling of **minimal type patterns** ( $C, P, D$ ) extracted from RDF data
- ▶ assertions  $\langle a, P, b \rangle$  where  $C$  min. type of  $a$  and  $D$  min. type of  $b$
- ▶ minimalization based on a **type graph** that represent the ontology (schema)
- ▶ **occurrence** statistics computed for minimal type patterns

[1] M. Palmonari, A. Rula, R. Porrini, A. Maurino, B. Spahiu and V. Ferme et al. **ASBTAT: Linked Data Summaries with ABstraction and STATistics**. *ESWC Posters and Demos*, 2015

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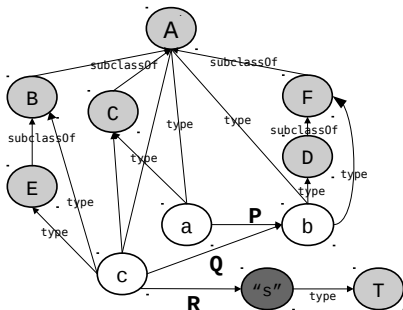
### ABSTATInf

- ▶ implementation the ABSTAT summarization model in **logic programming**
- ▶ adds **pattern inference** from the minimal type patterns
- ▶ and the computation of the respective **occurrence** statistics in the data set

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## Linked Data Set

○ = types ○ = named individuals ● = literals



### Patterns

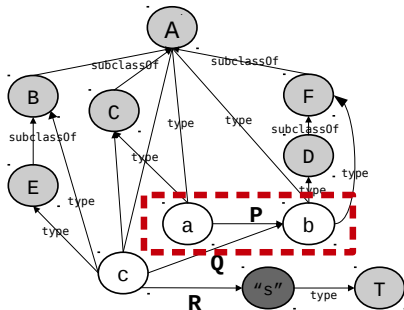
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(C, P, D) (E, Q, D) (C, Q, D) (E, R, T)  
 (C, R, T)

Minimal Type Pattern Base

Relational Assertions:  $P(x, y)$  from the triple  $\langle x, P, y \rangle$

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Patterns

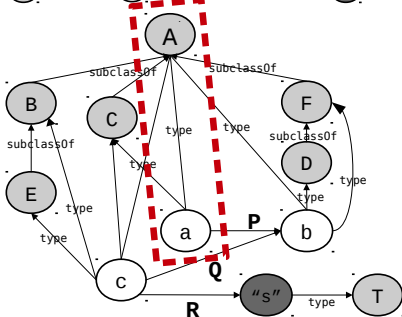
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Minimal Type Pattern Base

Typing Assertions:  $C(x)$  from the triple  $\langle x, \text{rdf:type}, C \rangle$

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Patterns

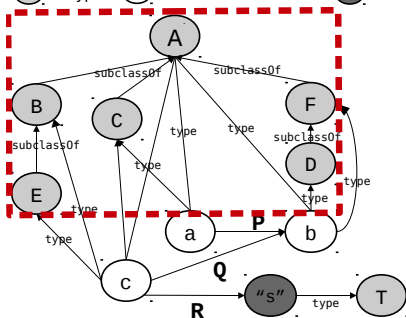
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Minimal Type Pattern Base

Type Graph:  $G = (N, \preceq^G)$ ,  $\preceq^G$  defines a partial order over  $N$

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Patterns

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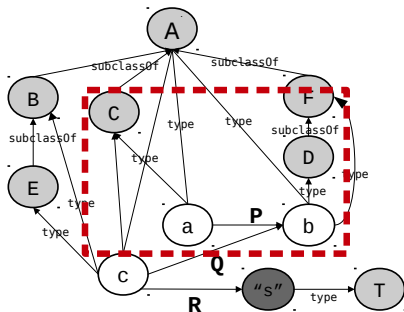
Minimal Type Pattern Base



## Abstract Knowledge Patterns and their Occurrence

$(C, P, D)$  s.t.  $\exists x \exists y (C(x) \wedge D(y) \wedge P(x, y))$  - **existential** definition  
 $(C, P, D)$  **occurs** iff ...

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### Patterns

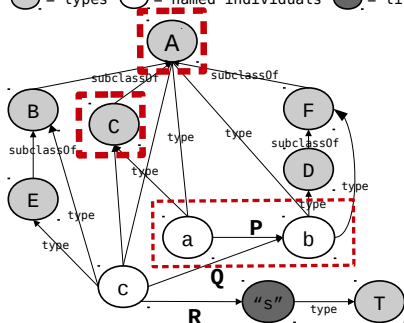
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Minimal Type Pattern Base

Subpatterns:  $(C, P, D) \preceq^G (C', P, D')$ , iff  $C \preceq^G C'$  and  $D \preceq^G D'$

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Patterns

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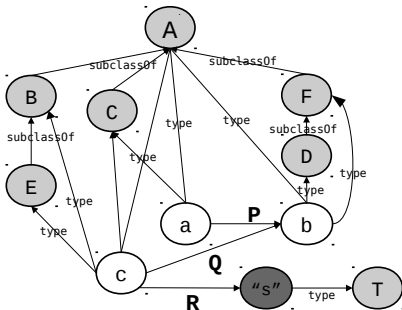
## Minimal Type Pattern Base

$(C, P, D)$  occurs as  $P(a, b)$

not exist  $C'$  s.t.  $C'(a)$  and  $C' \prec^G C$  or a  $D'$  s.t.  $D'(b)$  and  $D' \prec^G D$

ensures **compactness**

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### Patterns

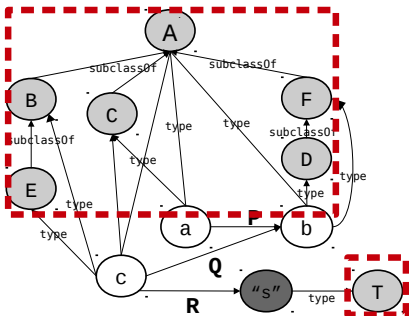
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Minimal Type Pattern Base

## Linked Data Set Summary

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### Patterns

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### Minimal Type Pattern Base

- ▶ implementation the ABSTAT summarization model in **Prolog**
- ▶ implements **pattern inference** from the minimal type patterns
- ▶ and the computation of the respective **occurrence** statistics in the data set

of the minimal type pattern base

## Relational Assertions Coverage

given  $(C, P, D)$ , all instances of type  $C$  and  $D$  linked by the property  $P$  can be retrieved by applying the existential definition of patterns as a conjunctive query.

of the minimal type pattern base

## Relational Assertions Coverage

given  $(C, P, D)$ , all instances of type  $C$  and  $D$  linked by the property  $P$  can be retrieved by applying the existential definition of patterns as a conjunctive query.

## Completeness w.r.t. Pattern Inference

the minimal type pattern base includes all and only the patterns from which all other patterns can be inferred.

# Pattern Inference and Occurrence Statistics

```
descendant(Subtype, Supertype) :-  
    rdf(Subtype, skos:broader, Supertype).  
descendant(Subtype, Supertype) :-  
    rdf(Subtype, skos:broader, X),  
    descendant(X, Supertype).  
  
minimalType(Entity, Type) :-  
    rdf(Entity, rdf:type, Type).  
  
mPattern(C, P, D, Instance) :-  
    rdf(Subject, P, Object),  
    minimalType(Subject, C),  
    minimalType(Object, D),  
    Instance = {Subject, Object}.  
  
iPattern(C, P, D, Instance):-  
    descendants(C, ICs),  
    descendants(D, IDs),  
    mPattern(IC, P, ID, Instance),  
    member(IC, ICs),  
    member(ID, IDs).  
  
occurrence(C, P, D, O) :-  
    iPatterns(C, P, D, Patterns),  
    length(Patterns, O).
```



```
descendant(Subtype, Supertype) :-  
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descendant(Subtype, Supertype) :-  
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minimalType(Entity, Type) :-  
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mPattern(C, P, D, Instance) :-  
    rdf(Subject, P, Object),  
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    minimalType(Object, D),  
    Instance = {Subject, Object}.  
  
iPattern(C, P, D, Instance) :-  
    descendants(C, ICs),  
    descendants(D, IDs),  
    mPattern(IC, P, ID, Instance),  
    member(IC, ICs),  
    member(ID, IDs).  
  
occurrence(C, P, D, 0) :-  
    iPatterns(C, P, D, Patterns),  
    length(Patterns, 0).
```

Instances of minimal type patterns are retrieved by applying their existential definition.  
(via the coverage property)

```
descendant(Subtype, Supertype) :-  
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    descendant(X, Supertype).
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minimalType(Entity, Type) :-  
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```

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mPattern(C, P, D, Instance) :-  
    rdf(Subject, P, Object),  
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iPattern(C, P, D, Instance) :-  
    descendants(C, ICs),  
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    mPattern(IC, P, ID, Instance),  
    member(IC, ICs),  
    member(ID, IDs).
```

```
occurrence(C, P, D, O) :-  
    iPatterns(C, P, D, Patterns),  
    length(Patterns, O).
```

Instances of inferred patterns  
are aggregated from minimal  
type patterns.  
(via the completeness w.r.t.  
pattern inference property)

```
descendant(Subtype, Supertype) :-  
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occurrence(C, P, D, 0) :-  
    iPatterns(C, P, D, Patterns),  
    length(Patterns, 0).
```

Occurrence statistics are trivially computed

# Demo

## Conclusions

- ▶ ABSTATInf, a Prolog implementation of the ABSTAT model

## Future work

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- ▶ pattern inference with occurrence statistics computation
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## Future work

- ▶ Consider also subproperty relations
- ▶ Experiments with large data sets

## Questions?

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<http://rporrini.info>