

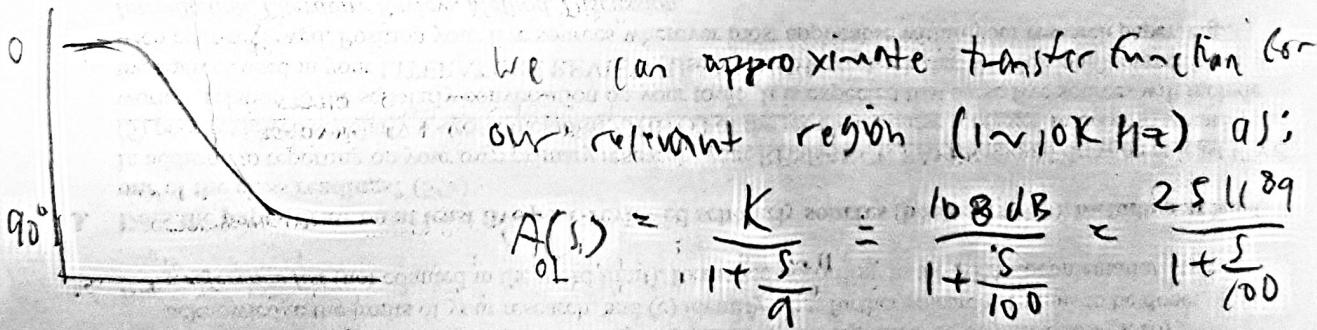
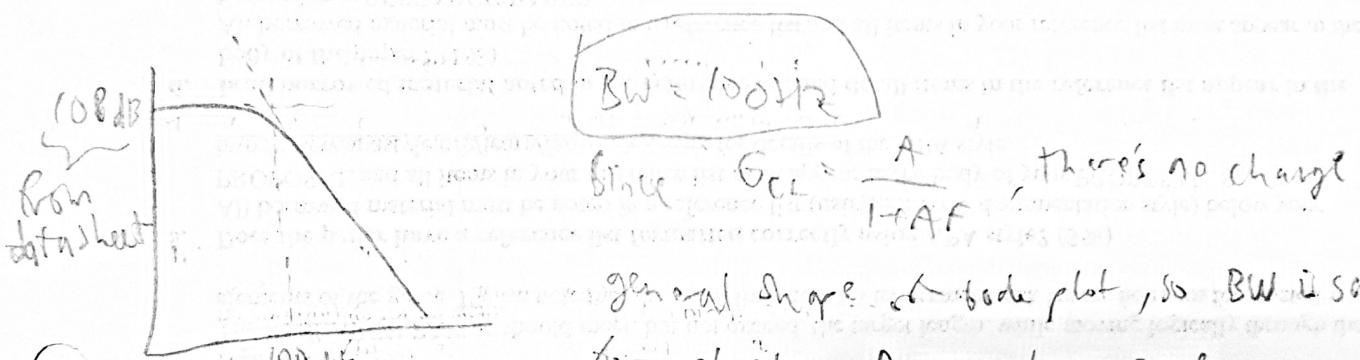
Rutherford Maxfield #63205165

1. Just looks like non-inverting op-amp

DC gain  $\approx 11 = \frac{1}{f}$  where  $f = \frac{z_1}{z_2 + z_1}$

$$\Rightarrow 11 = \frac{z_2 + z_1}{z_1} \rightarrow \boxed{10z_1 = z_2}$$

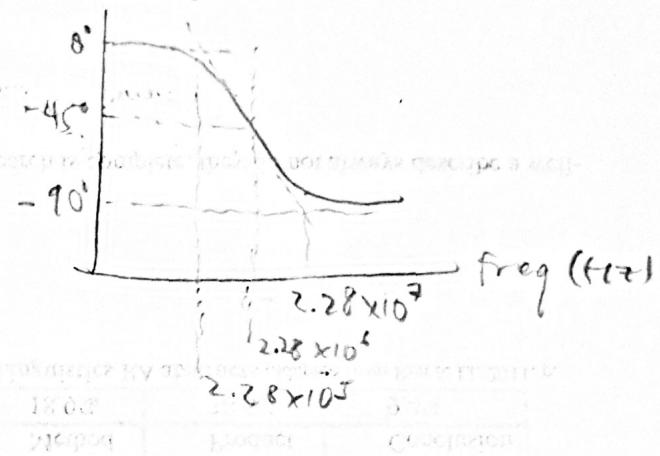
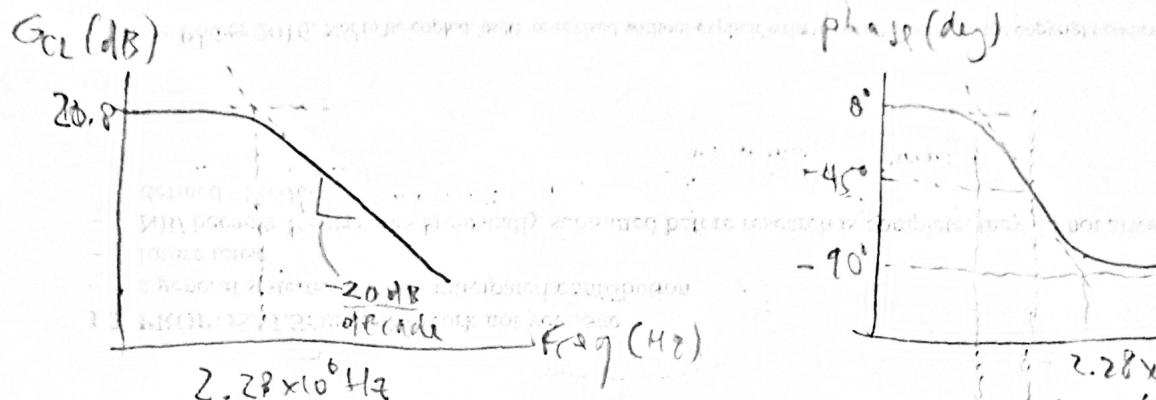
2. from fig 3



$$A(s) = \frac{K}{1 + \frac{s}{\omega_n}} = \frac{10.8 \text{ dB}}{1 + \frac{s}{100}} = \frac{251189}{1 + \frac{s}{100}}$$

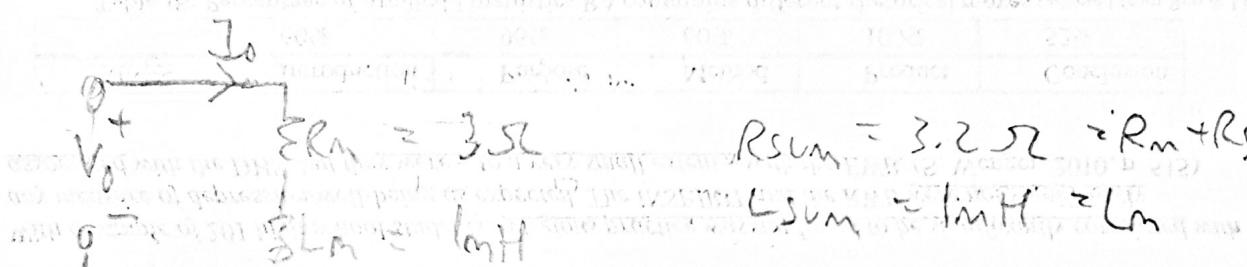
$$\frac{V_o(s)}{V_i(s)} = \frac{A}{1 + AF} = \frac{\frac{251189}{1 + s/100}}{(1 + s/100) + \frac{251189}{11}} = \frac{\frac{251189}{1 + s/100}}{\frac{11 + s}{11} + \frac{s}{100}} = \frac{\frac{251189}{11}}{1 + \frac{s}{2.28 \times 10^6}}$$

Note that  $20 \log_{10}(11) = 20.8 \text{ dB}$



3.

Given the circuit diagram, find the voltage  $V_o(t)$  across the capacitor  $C$  by expressing it in terms of the current  $I_o(t)$  flowing through the inductor  $L$ .



$$V_o(t) = -R_L I_o(t) - \frac{1}{C} \int I_o(t) dt + V_s$$

$$V_o(t) = -R_L I_o(t) - \frac{1}{C} \int I_o(t) dt + L \frac{dI_o(t)}{dt}$$

Given  $V_s = 10 \text{ V}$ ,  $R_L = 0.2 \text{ ohm}$ ,  $C = 10^{-6} \text{ F}$ ,  $L = 10^{-3} \text{ H}$ ,  $I_o(0) = 0$ . Find  $V_o(t)$ .

(a)  $V_o(t) = 10 \text{ V}$

(b)  $V_o(t) = 10 \text{ V}$

(c)  $V_o(t) = 10 \text{ V}$

$$V_o(t) = V_s - R_L I_o(t) - \frac{1}{C} \int I_o(t) dt + L \frac{dI_o(t)}{dt}$$

$$V_o(t) = V_s - R_L I_o(t) - \frac{1}{C} \int I_o(t) dt + L \frac{dI_o(t)}{dt} \quad \begin{cases} \text{Assume } I_o(0) = 0 \\ \text{due to property of inductor} \end{cases}$$

$$\frac{I_o(t)}{V_o(t)} = \frac{1}{R_L + \frac{1}{L} + \frac{1}{C}}$$

$$(a) \frac{I_o(t)}{V_o(t)} = \frac{1}{R_L + \frac{1}{L} + \frac{1}{C}}$$

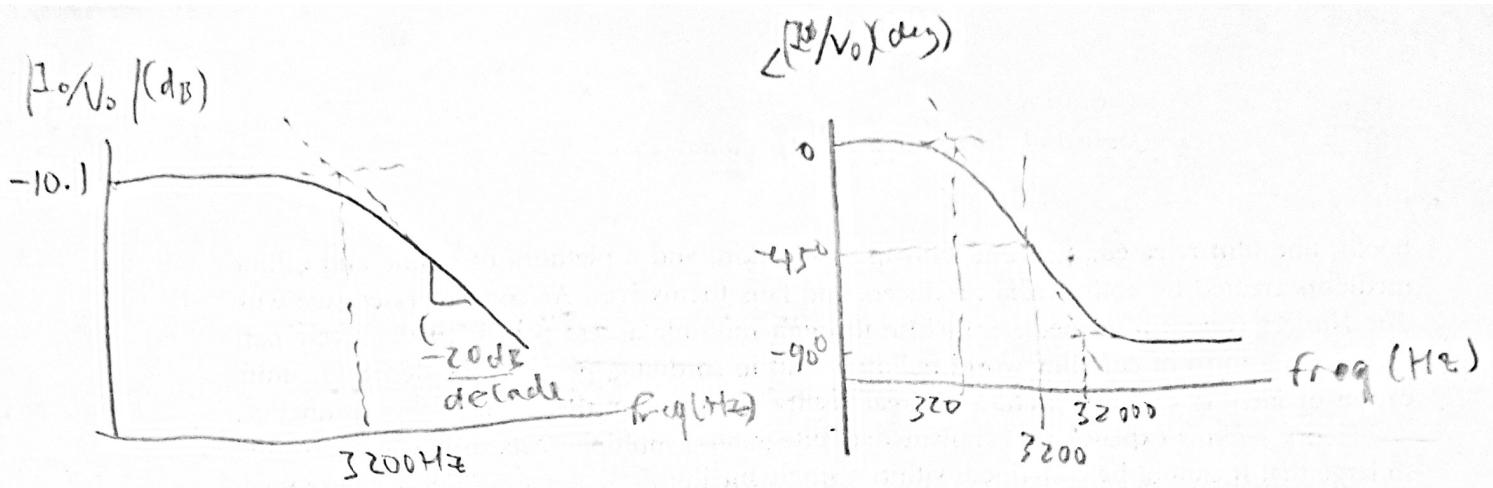
$$t = \frac{1}{R_L + \frac{1}{L} + \frac{1}{C}}$$

$$= \frac{1}{R_L + \frac{1}{L} + \frac{1}{C}}$$

$$= \frac{1}{R_L + \frac{1}{L} + \frac{1}{C}}$$

Note that

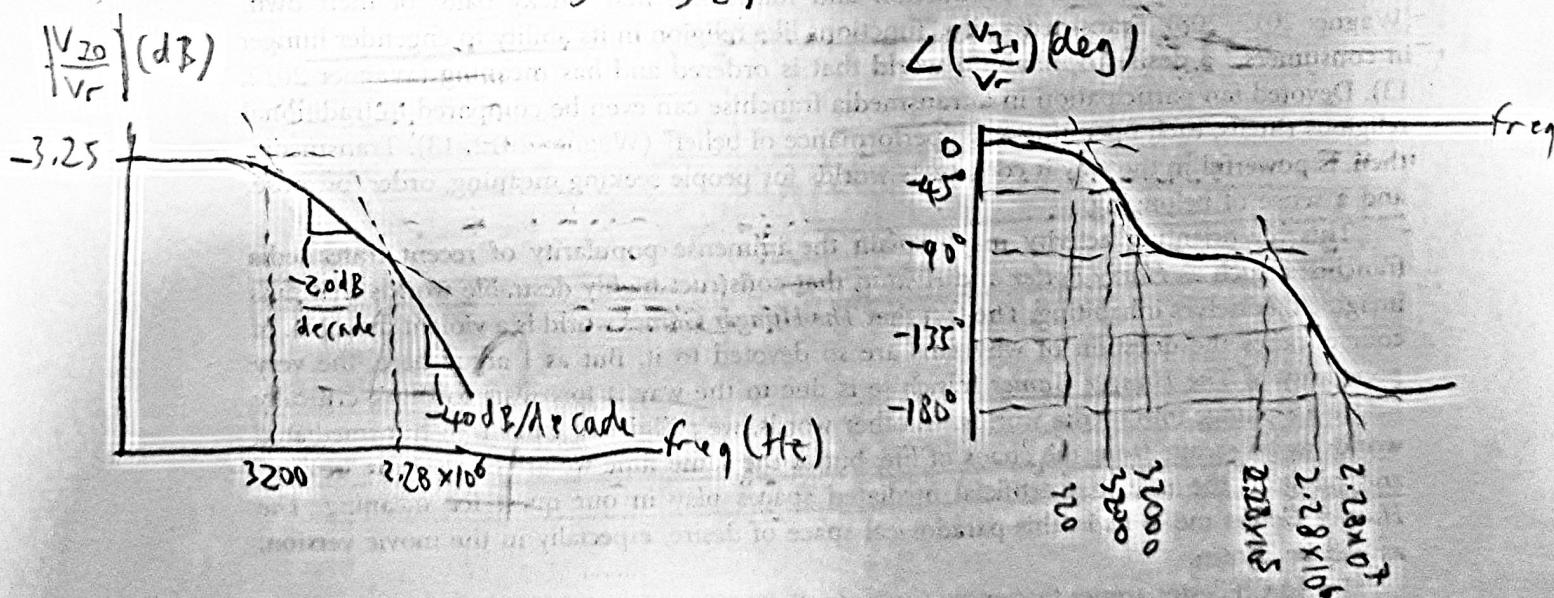
$$20 \log_{10}(1/3.2) = -10.1 \text{ dB}$$



$$4. V_{I_0} = R_S I_0 \rightarrow R_S = \frac{V_{20}(s)}{I_0(s)}$$

$$\begin{aligned} \frac{V_{20}(s)}{V_r(s)} &= \left( \frac{R_S}{R_m + R_S + sL_m} \right) \left( \frac{I_0(s)}{V_o(s)} \right) \left( \frac{V_o(s)}{V_r(s)} \right) \\ &= R_S \left( \frac{1}{R_m + R_S + sL_m} \right) \left( \frac{A_f}{1 + A_f} \right) \\ &\approx 0.2 \left( \frac{1/3.2}{1 + s/3200} \right) \left( \frac{11}{1 + s/(2.28 \times 10^6)} \right) \\ &\approx (2.2/3.2) \left( \frac{1}{1 + s/3200} \right) \left( \frac{1}{1 + s/(2.28 \times 10^6)} \right) \end{aligned}$$

Note that  $20 \log_{10} \left( \frac{2.2}{3.2} \right) = -3.25 \text{ dB}$



Get step response from MATLAB

