## **MECH421 Midterm Exam**

## Feb. 25<sup>th</sup> 2019, 3pm-4pm

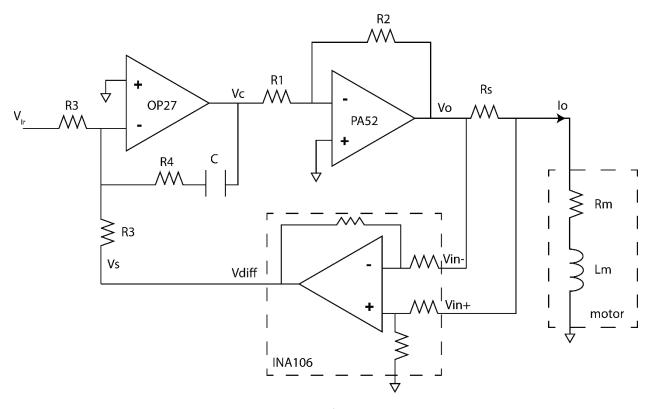


Figure 1: A motor power amplifier with a current controller.

In Figure 1, OP 27 is considered as an ideal op-amp to implement current controller. PA52 is a high power op-amp to drive the motor, and Figure 2 describes its frequency response. In this circuit PA52 is not an ideal op-amp. INA106 is a difference op-amp with a fixed gain of 10 ( $K_g$ =10), and its functions follow the equation:  $V_{diff} = K_g(V_{IN+} - V_{IN-})$ . Lm and Rm are motor's inductance and resistance. Rs is the current sensing resistor. Lm=6mH, Rm=3.9 $\Omega$ , Rs=0.1 $\Omega$ .

- 1). (30 marks) Draw a block diagram for the whole circuit in Figure 1. Clearly label the following signals:
  - a) V<sub>Ir</sub> (reference current command).
  - b) V<sub>c</sub> (input voltage of PA52).
  - c) V<sub>o</sub> (output voltage of PA52).
  - d) I<sub>o</sub> (motor current).
  - e) V<sub>s</sub> (current sensing signal).

- 2). (30 marks) Consider voltage stage only, which is an inverting amplifier circuit; the input is  $V_c$  and the output is  $V_o$ . PA52 frequency response is shown in Figure 2 below.
  - a) Design resistors R1 and R2 to set the DC gain from  $V_c$  to  $V_o$  is 9. (i.e.  $|V_o/V_c|=9$ ).
- b) Is this voltage stage stable? If yes, what is the negative loop transmission (NLT) crossover frequency, and what is the phase margin.
- 3). (40 marks) Consider the current controllor design with following objectives: 10kHz closed loop bandwidth; no steady-state error; at least 60 degree phase margin.
- a) Select R3, R4 and C in the circuit to design a PI ( $C(s) = K(1 + \frac{\omega_I}{s})$ ) controller to achieve above objectives. Make sure to show K and  $\omega_I$  clearly.
  - b) Draw Bode plots of the controller only.
  - c) Draw Bode plots for the NLT of the whole system, and label the corner frequencies.

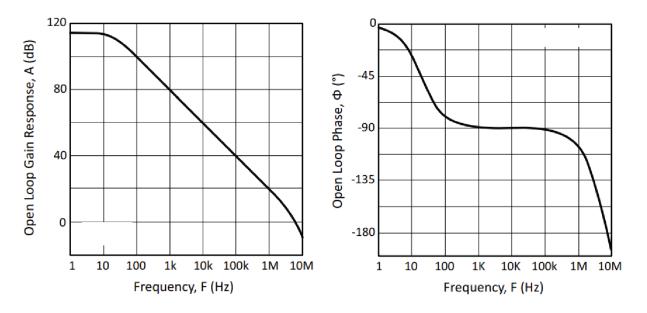


Figure 2: PA52 frequency response.