

# Image Features: Descriptors

Slides adapted from Lana Lazebnik, Kirill Dyagilev, Ayelet Dominitz, Matthew Brown  
and Robert Pless

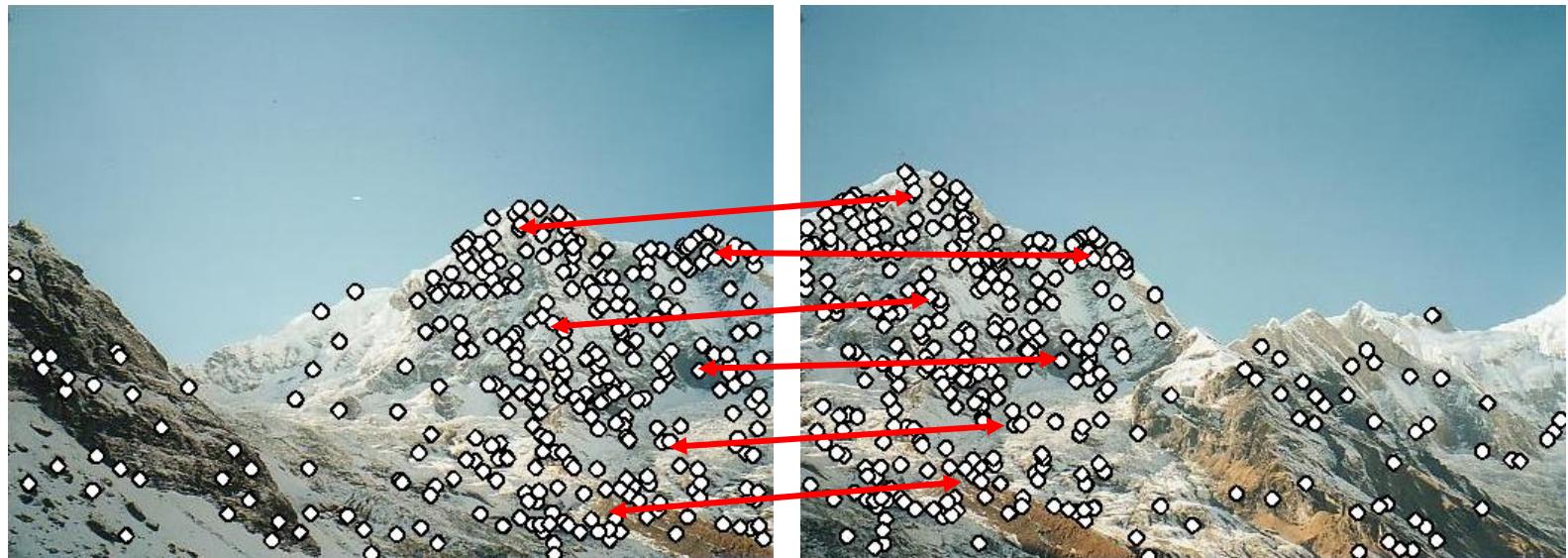
# Recall: Image Feature Motivation

- Motivation: panorama stitching
  - We have two images – how do we combine them?



# Image Feature Motivation

- Motivation: panorama stitching
  - We have two images – how do we combine them?

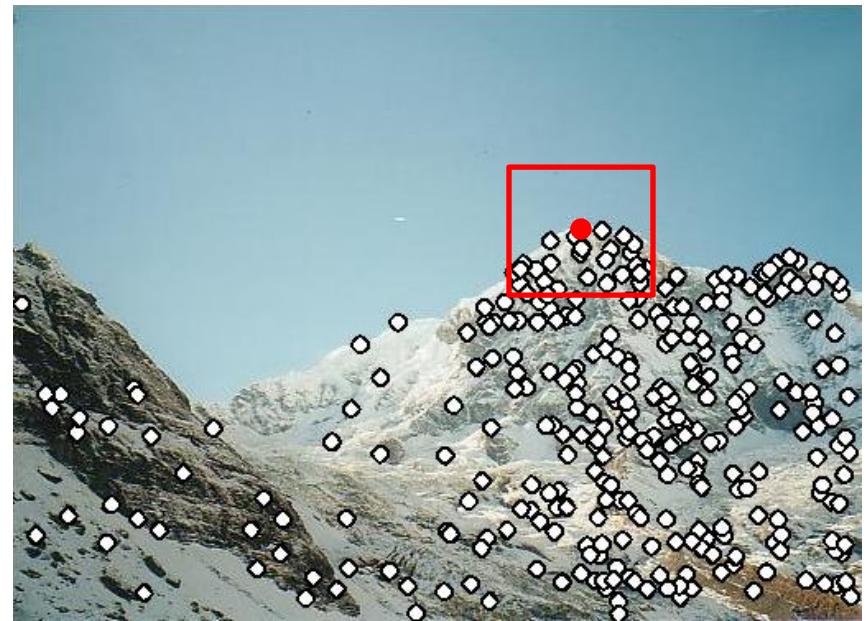


Step 1: find features

Step 2: match features (how?)

# Image Features

- One characteristic of good image features is *locality*
  - A feature occupies a relatively small area of the image; robust to clutter and occlusion
- We describe the feature by a patch of the image centered at the interest point



# Image Features

- Sparse image features have:
  - a location (interest point)
  - descriptor
- So far, we've focused on location
  - edge points
  - corner points
  - blobs
- Today, we'll cover 2 feature descriptors
  - MOPS (Brown et al., 2005)
  - SIFT (Lowe, 2004)

# But First...

## Scale Invariance → Affine Invariance

- “Same” region may be rotated or stretched in two images
  - In addition to translation & scale invariance, we want *affine invariance*



# Recall: 2<sup>nd</sup> Moment Matrix

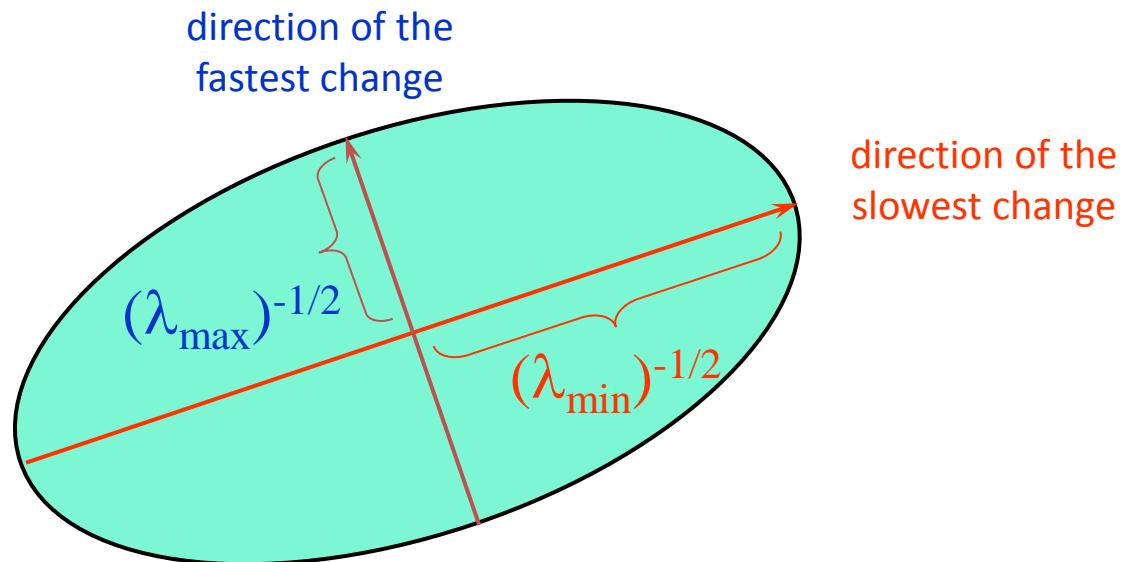
$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

We can visualize M as an ellipse with axis lengths determined by the eigenvalues and orientation determined by R

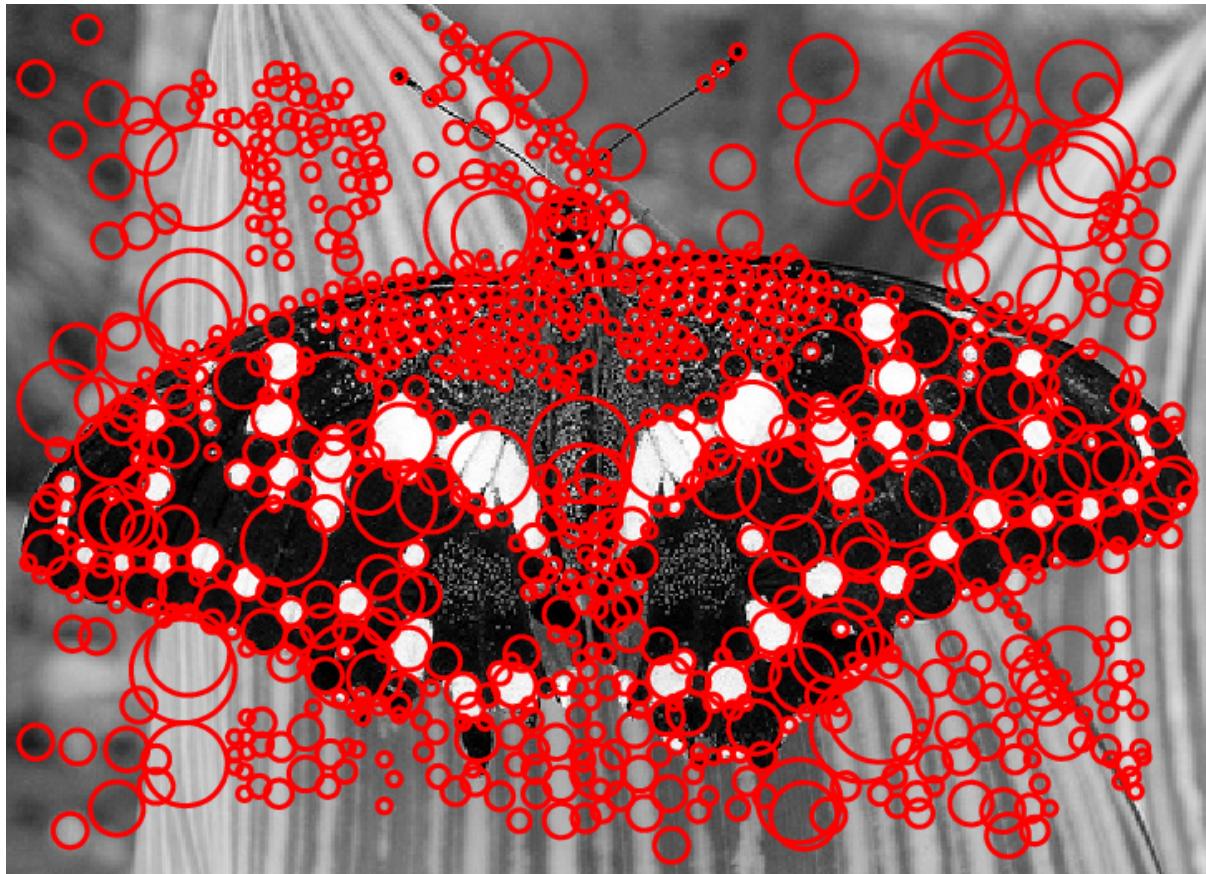
Rotation Matrix

Ellipse equation:

$$[u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$$

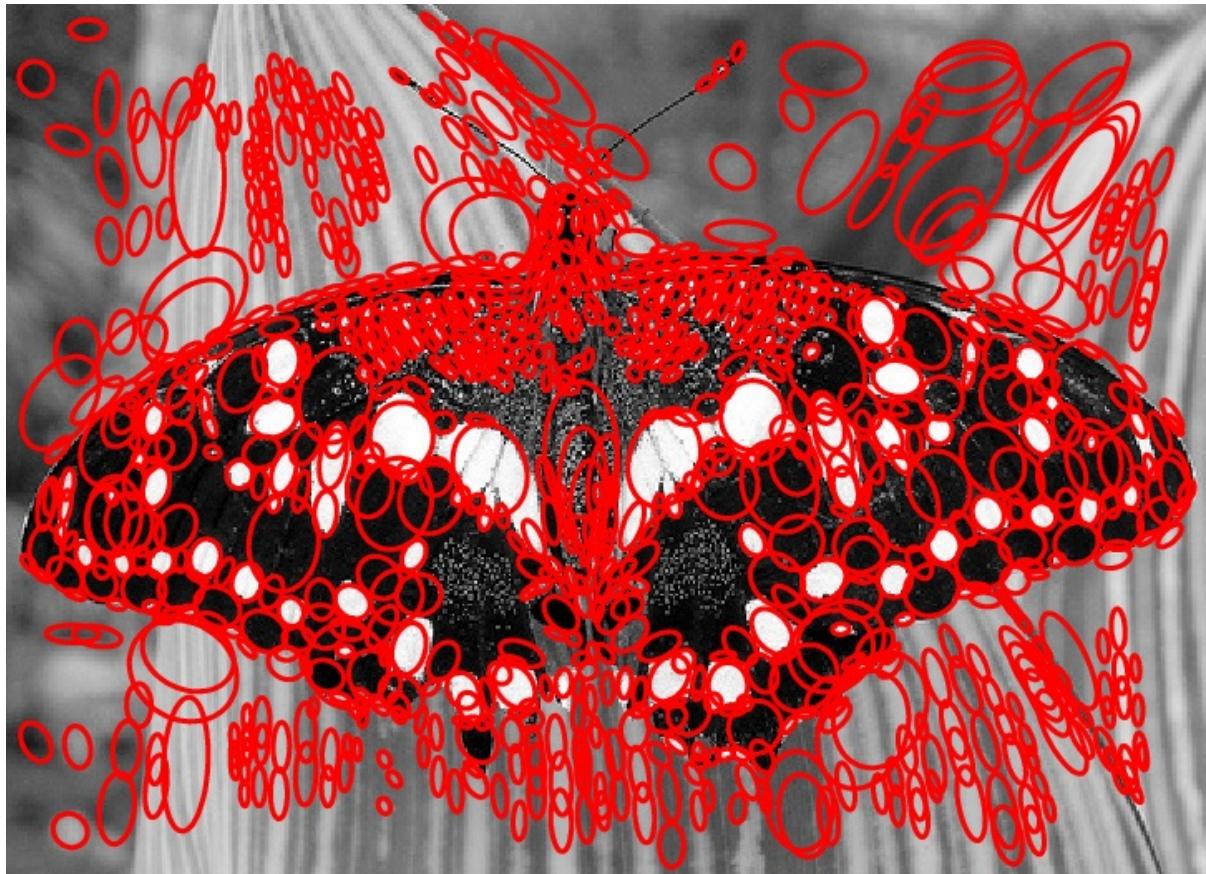


# Affine adaptation example



Scale-invariant regions (blobs)

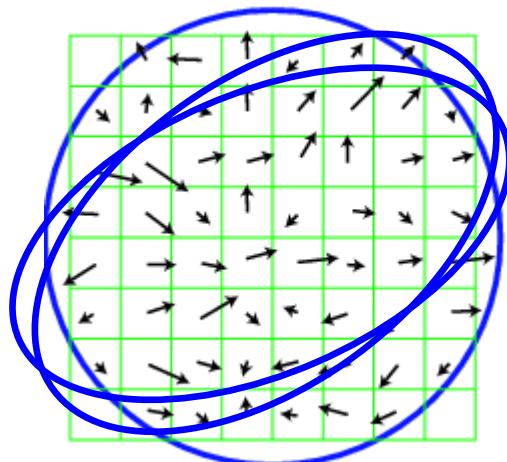
# Affine adaptation example



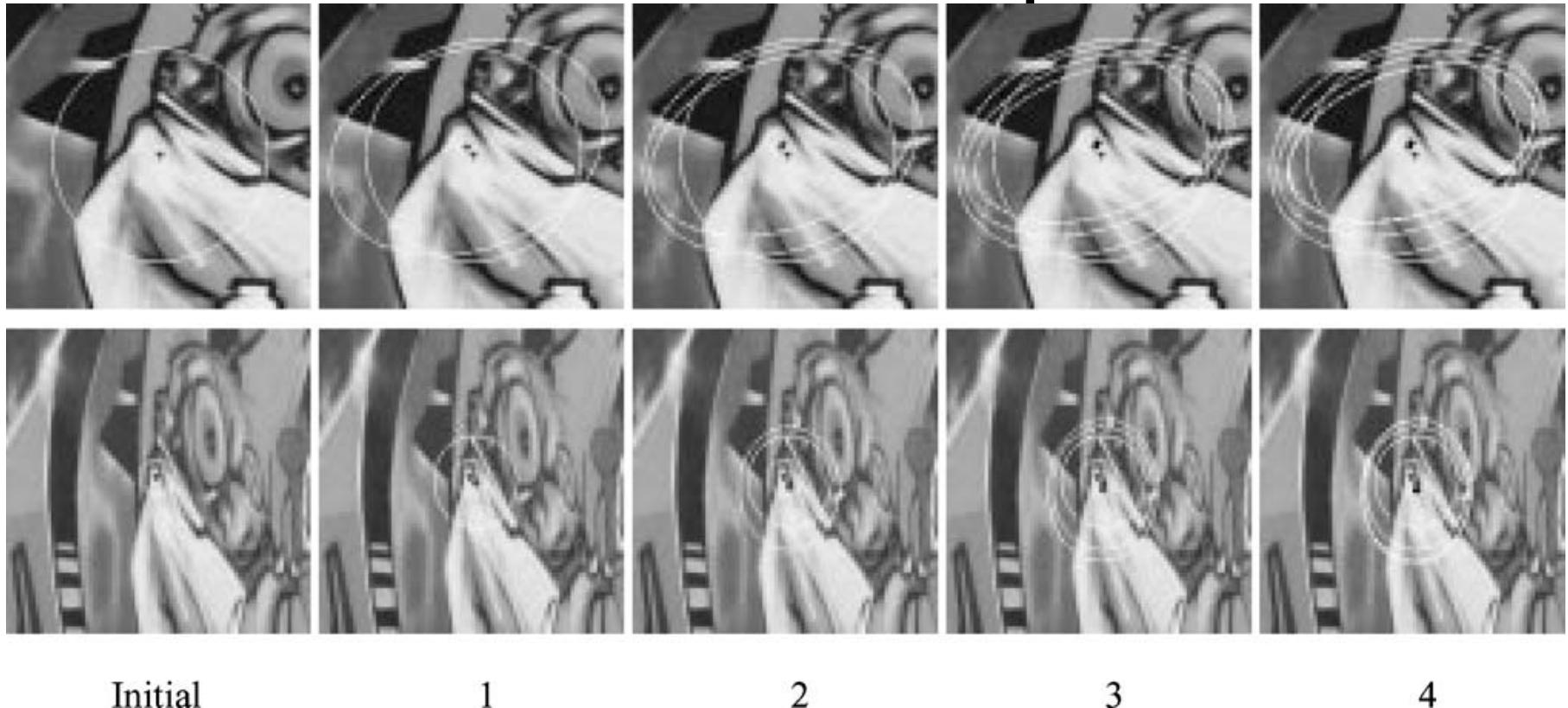
Affine-adapted blobs

# Affine adaptation

- Problem: the second moment “window” determined by weights  $w(x,y)$  must match the characteristic shape of the region
  - *“Chicken an egg” problem: Pixels “vote” for shape. Shape determines which pixels get to vote.*
- Solution: iterative approach
  - Use a circular window to compute second moment matrix
  - Perform affine adaptation to find an ellipse-shaped window
  - Recompute second moment matrix using new window and iterate



# Iterative affine adaptation

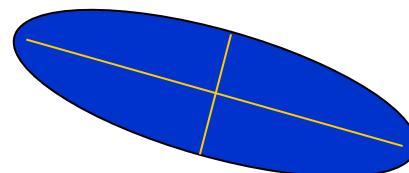
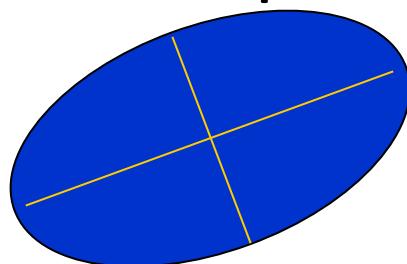


K. Mikolajczyk and C. Schmid, [Scale and Affine invariant interest point detectors](#), IJCV 60(1):63-86, 2004.

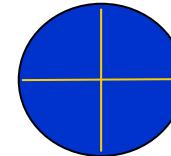
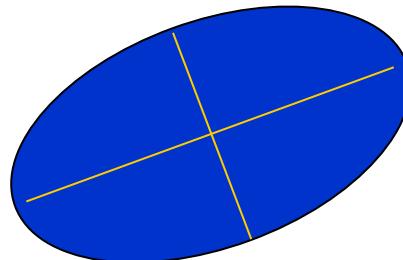
<http://www.robots.ox.ac.uk/~vgg/research/affine/>

# Affine normalization

- The second moment ellipse can be viewed as the “characteristic shape” of a region
- How do we compare two regions of different shape?



- We can normalize the region by transforming the ellipse into a unit circle



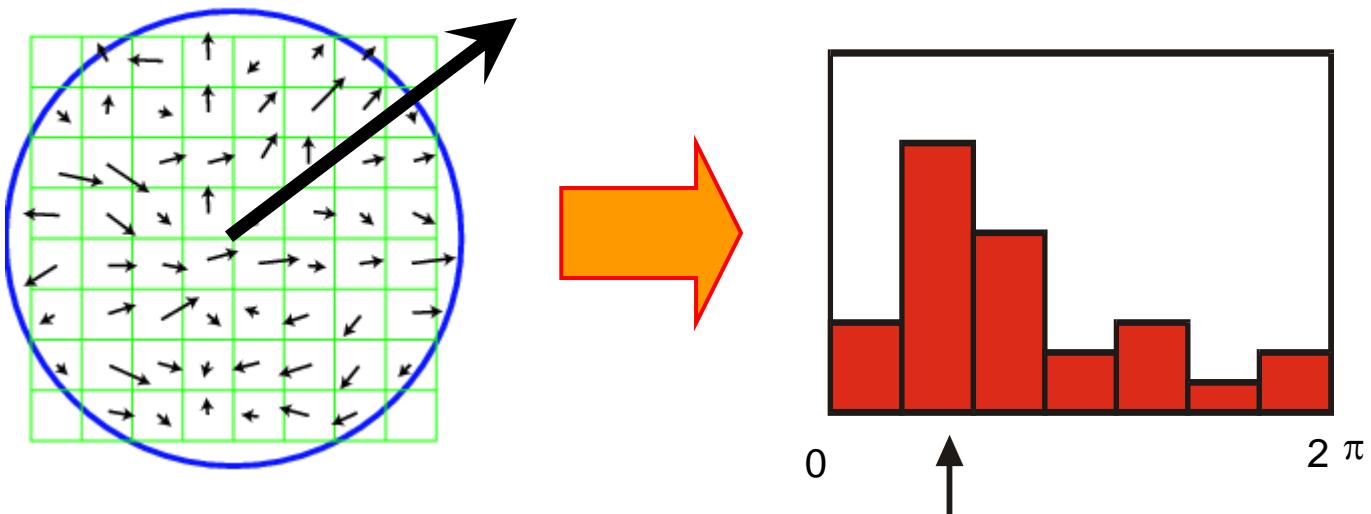
# Orientation ambiguity

- There is no unique transformation from an ellipse to a unit circle
  - We can rotate or flip a unit circle, and it still stays a unit circle



# Orientation ambiguity

- There is no unique transformation from an ellipse to a unit circle
  - We can rotate or flip a unit circle, and it still stays a unit circle
- So, to assign a unique orientation to keypoints:
  - Create histogram of local gradient directions in the patch
  - Assign canonical orientation at peak of smoothed histogram



# Ok, What's Left?

- We have:
  - Interest point location
  - Scale
  - Orientation
- We need to describe the image patch in that region
- Two methods: MOPS & SIFT

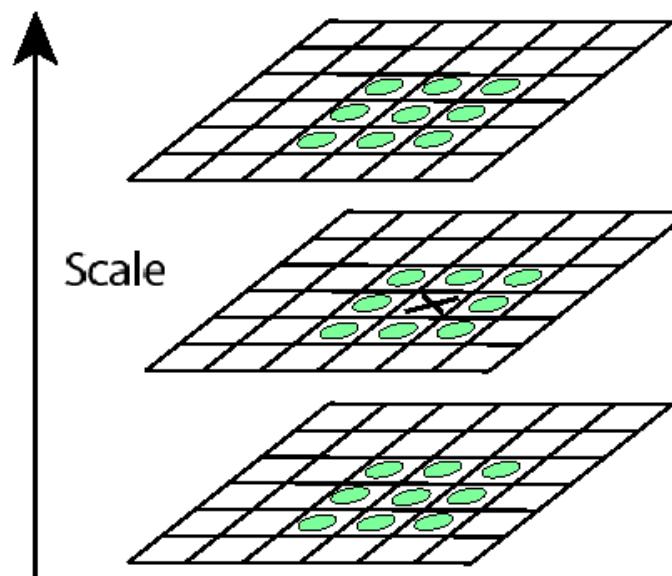


# Scale-Invariant Feature Transform (SIFT) Algorithm

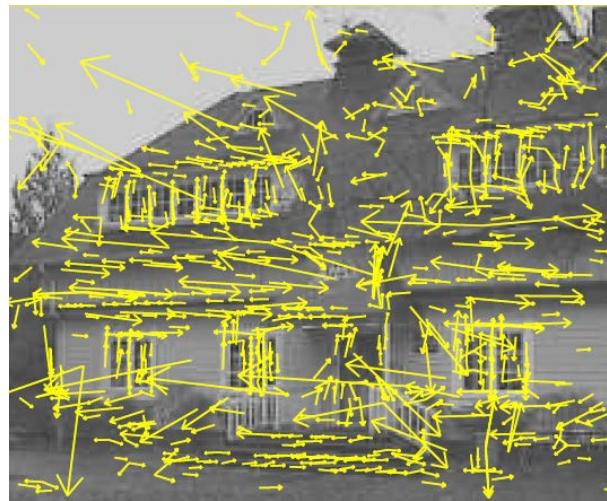
1. Interest-point detection
2. Feature localization
3. Orientation assignment
4. Feature descriptor

# Step 1: Interest Point Detection

- Calculate Difference of Gaussian at varying scales
- X is selected if it is larger or smaller than all 26 neighbors

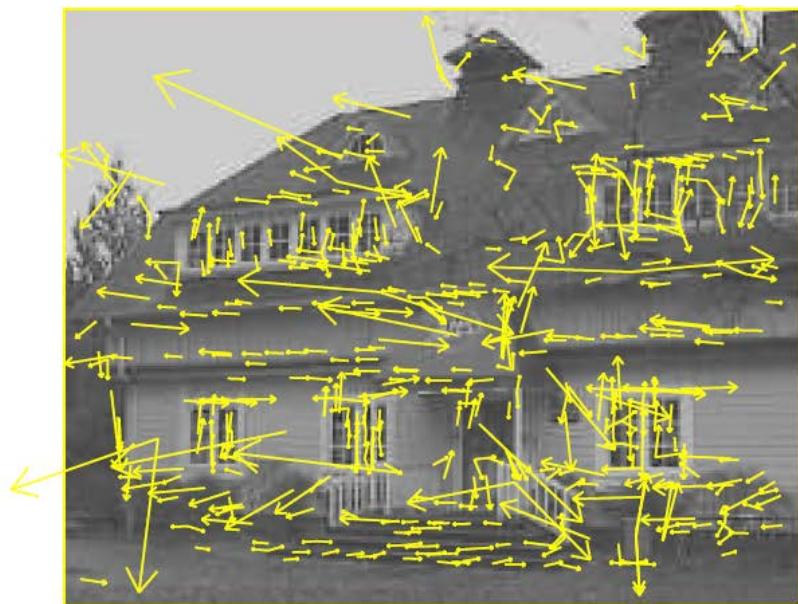
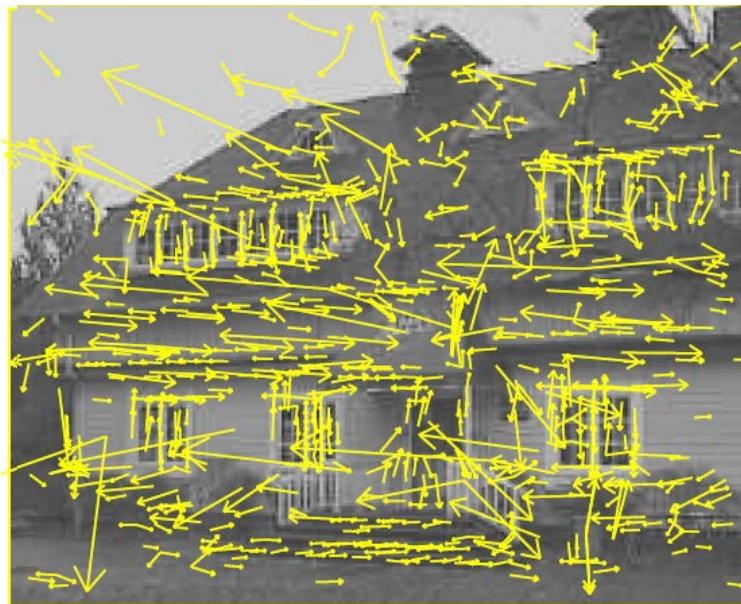


# Step 2: Feature Localization



- Too many keypoints, some are unstable:
  - points with low contrast (sensitive to noise)
  - points that are localized along an edge
    - prefer points on corners

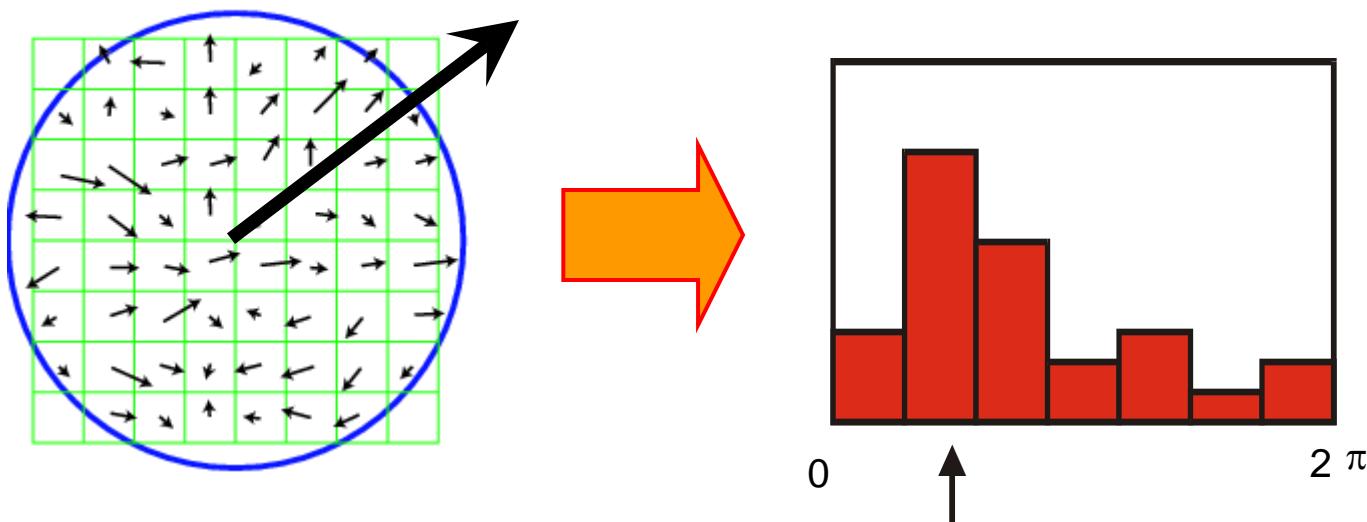
# Step 2: Feature Localization



536 out of 832 are left after contrast thresholding  
and cornerness thresholding

# Step 3: Orientation assignment

- Required: Rotation invariance of features
- Solution:
  - Assign orientation to feature based on local gradients
  - Transform relative data accordingly
  - For location of multiple peaks multiply key point

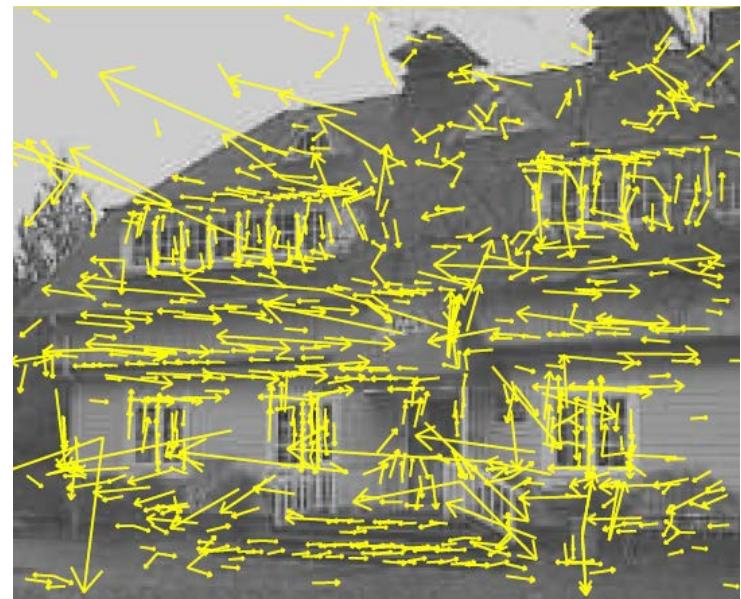


# Step 4: Feature Descriptor

- So far, we have assigned location, scale, and orientation to each keypoint:
  - Impose a repeatable local 2D coordinate system
  - Provide invariance to these parameters

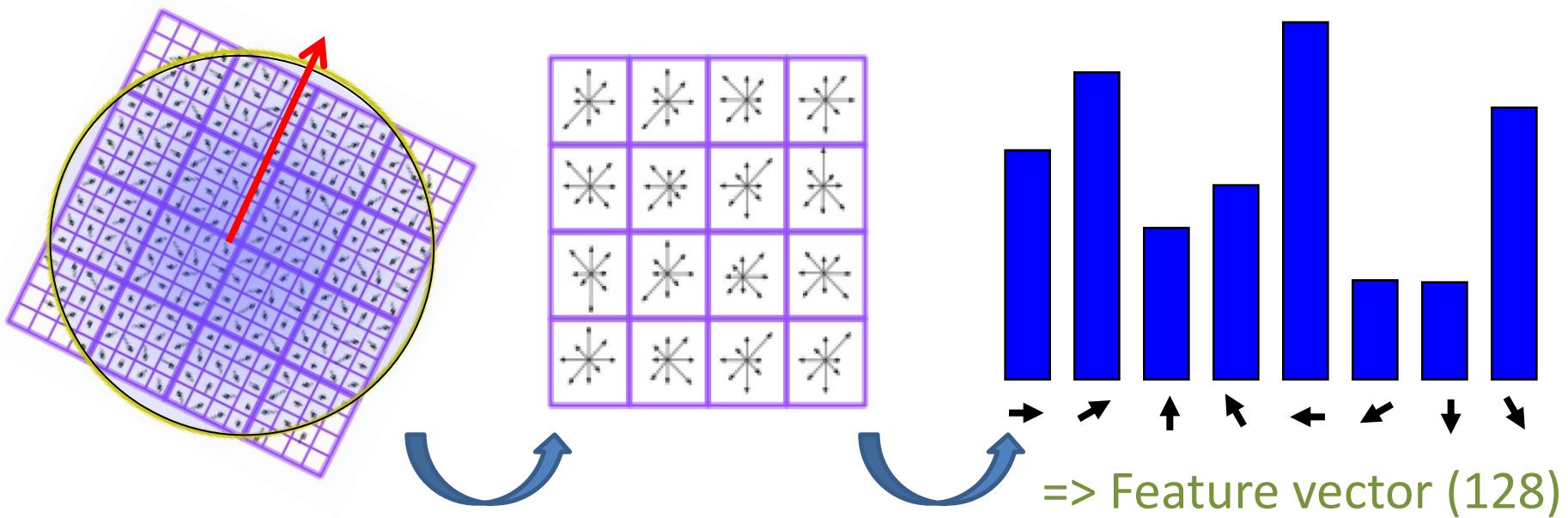
**Remaining goal:**

- Define local descriptor invariant to remaining variations:
  - Illumination
  - 3D Viewpoint



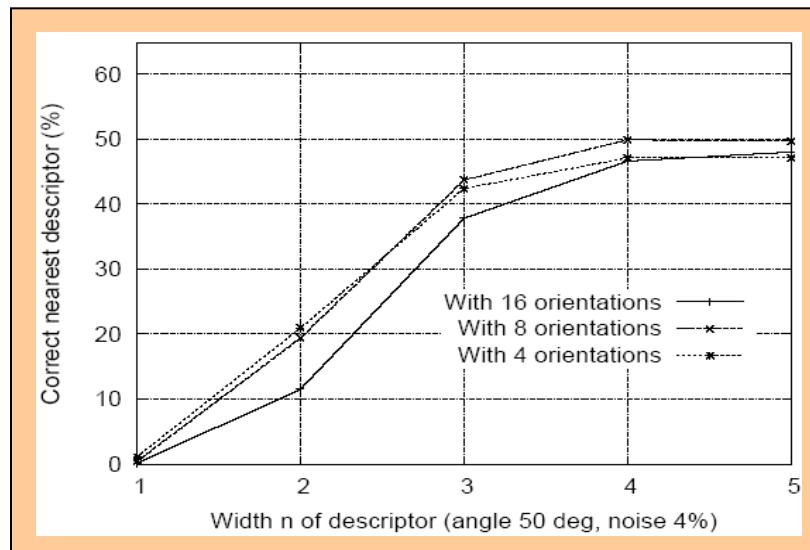
# Step 4: Keypoint descriptor

- Create 16 gradient histograms
  - 8 bins each
  - Weighted by magnitude
  - Histogram and gradient values are interpolated and smoothed



# Step 4: Keypoint descriptor

- Justification:
  - Inspired by the human visual system
  - Parameters  $r$  (# of bins) and  $n \times n$  (# of histograms) chosen empirically



# Matching SIFT Features

- Nearest Neighbor algorithm based on L2 distance
  - Euclidean distance in 128-D
- How to discard bad matches?
  - Threshold on L2 → bad performance
  - Solution: threshold on ratio

**best match**  
—————  
**second best match**

# SIFT for Recognition / Detection

For set of database images:

1. Compute SIFT features
2. Save descriptors to database

For query image:

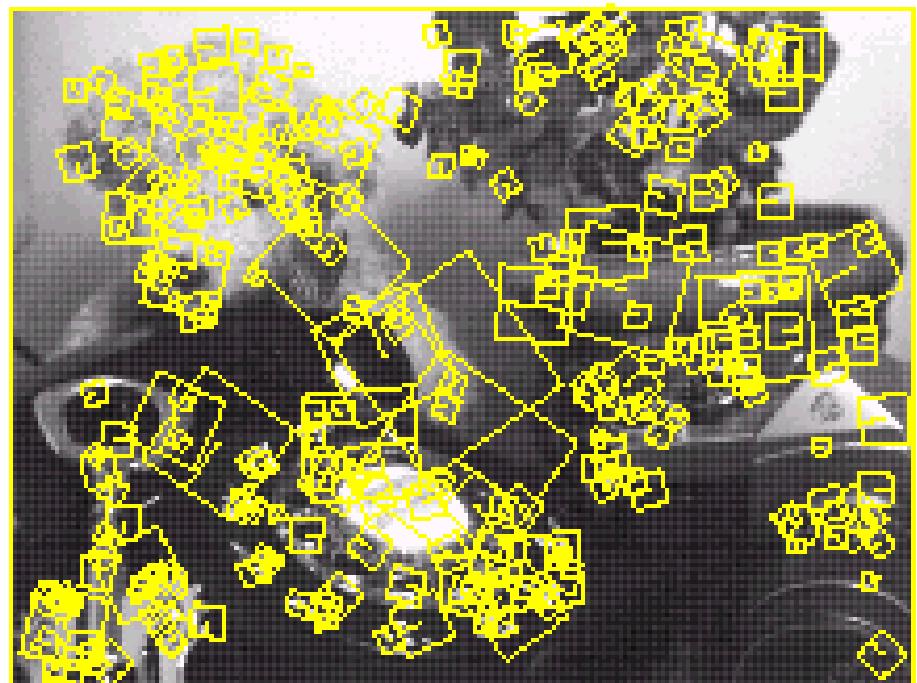
1. Compute SIFT features
2. For each descriptor find its match in the database
3. Check to see if you have “enough” matches at the correct relative scale, orientation, and location
  - *We'll see how to do this next class*
4. Verify (with affine transform)

# Recognition under occlusion



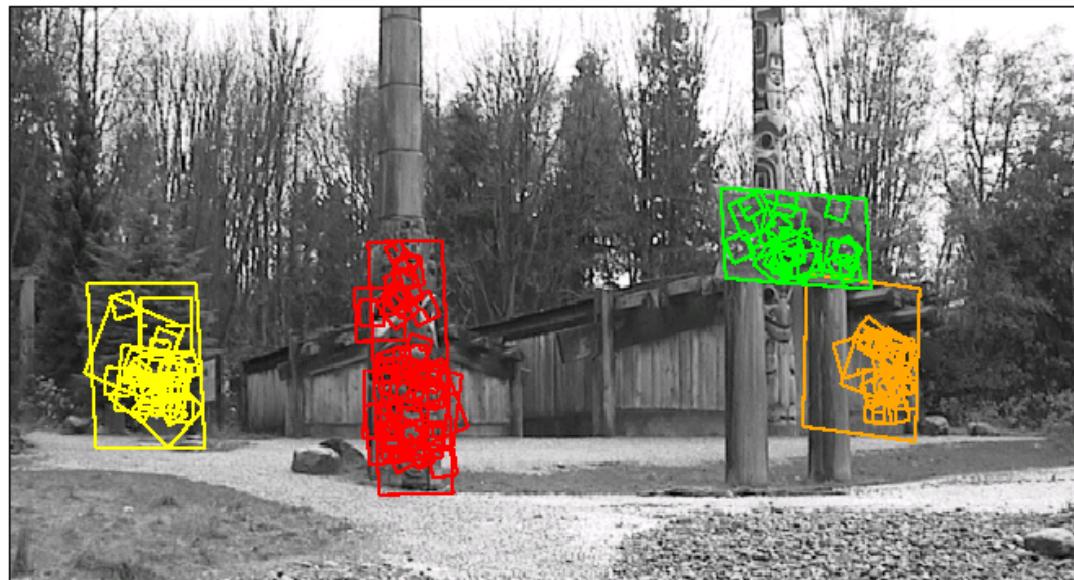
# Test of illumination Robustness

- Same **image** under differing illumination



273 keypoints verified in final match

# Location recognition



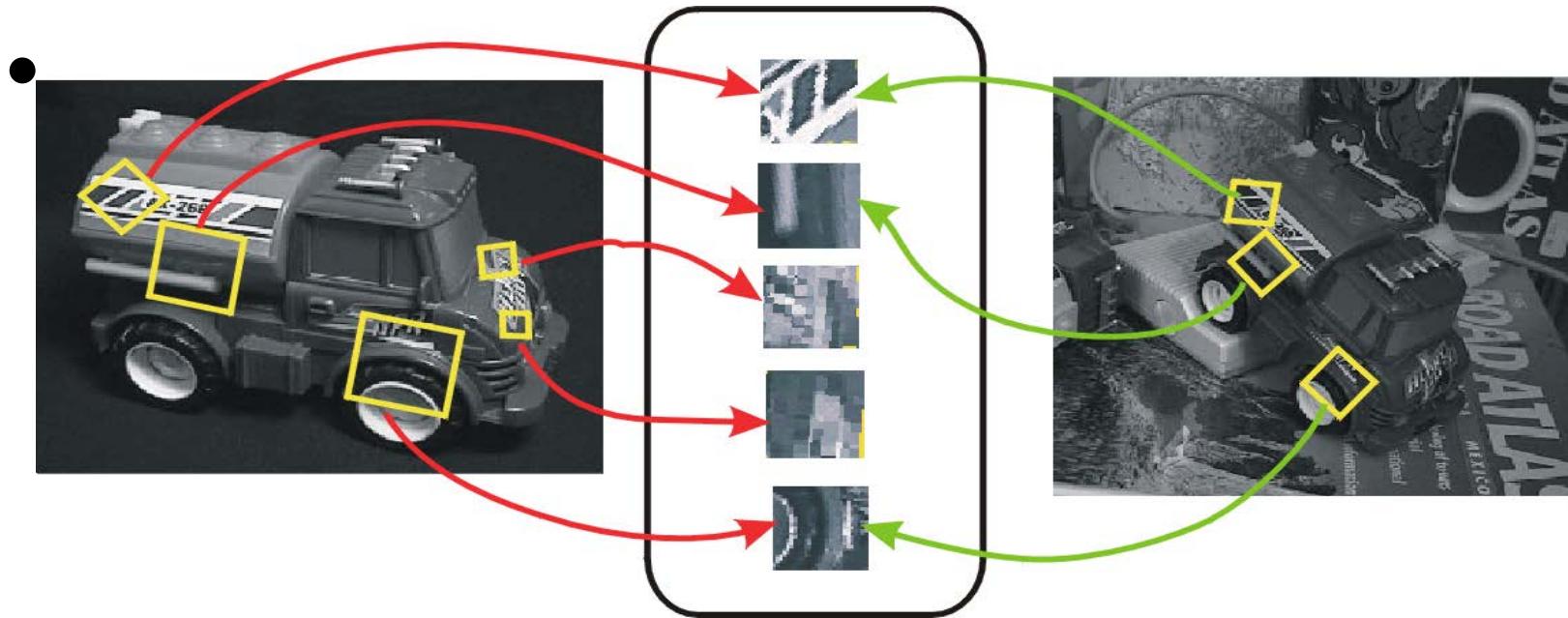
# Image Registration Results



[Brown & Lowe 2003]

# Invariance vs. Covariance

- **Invariance:**
  - $\text{features}(\text{transform}(\text{image})) = \text{features}(\text{image})$



Covariant detection => invariant description

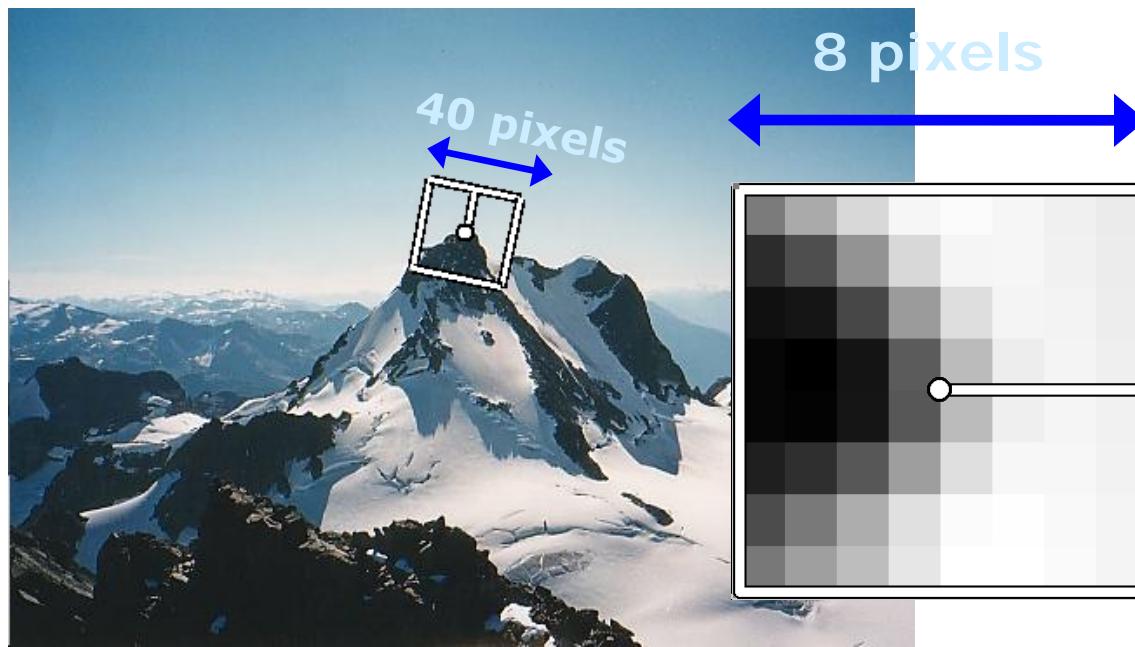
# SIFT Summary

- Most widely used image feature in computer vision
  - >36,000 citations (as of 2016)
- Robust to Viewpoint, Lighting, Scale
- Many Extensions
  - PCA-SIFT
  - SURF (More efficient implementation)
- Weak point [Lowe]: key point detection
  - Many papers use a different interest point operator + SIFT feature descriptor

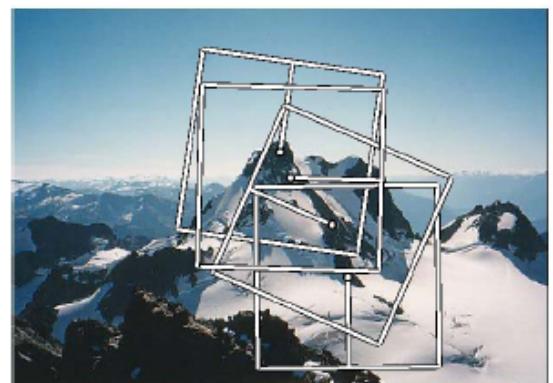
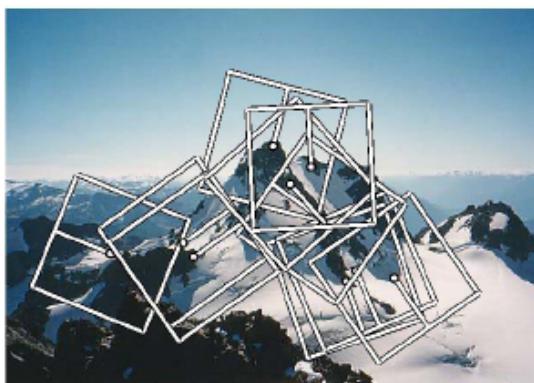
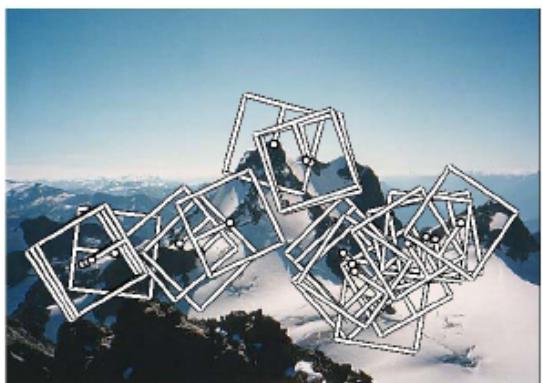
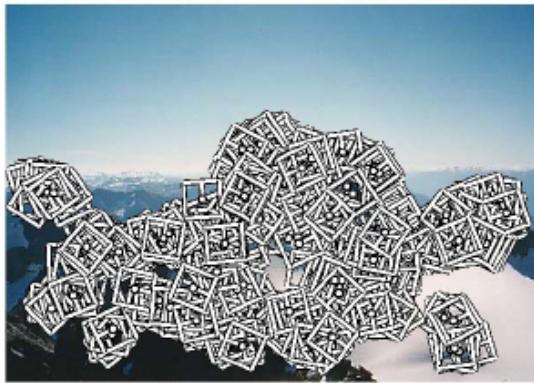
# Multiscale Oriented Patches Descriptor

Take square window around detected feature

- Rotate to horizontal
- Sample 8x8 square window centered at feature
- Intensity normalize the window by subtracting the mean, dividing by the standard deviation in the window



# Detections at multiple scales



*Figure 1. Multi-scale Oriented Patches (MOPS) extracted at five pyramid levels from one of the Matier images. The boxes show the feature orientation and the region from which the descriptor vector is sampled.*

# MOPS & SIFT Comparison

## SIFT

- 1. Interest-point detection:**  
Local max blobs in scale space.
- 2. Feature localization:** Get rid of low-contrast, non-corners
- 3. Orientation assignment:**  
Max gradient direction
- 4. Feature descriptor:**  
Histogram of gradient directions

## MOPS

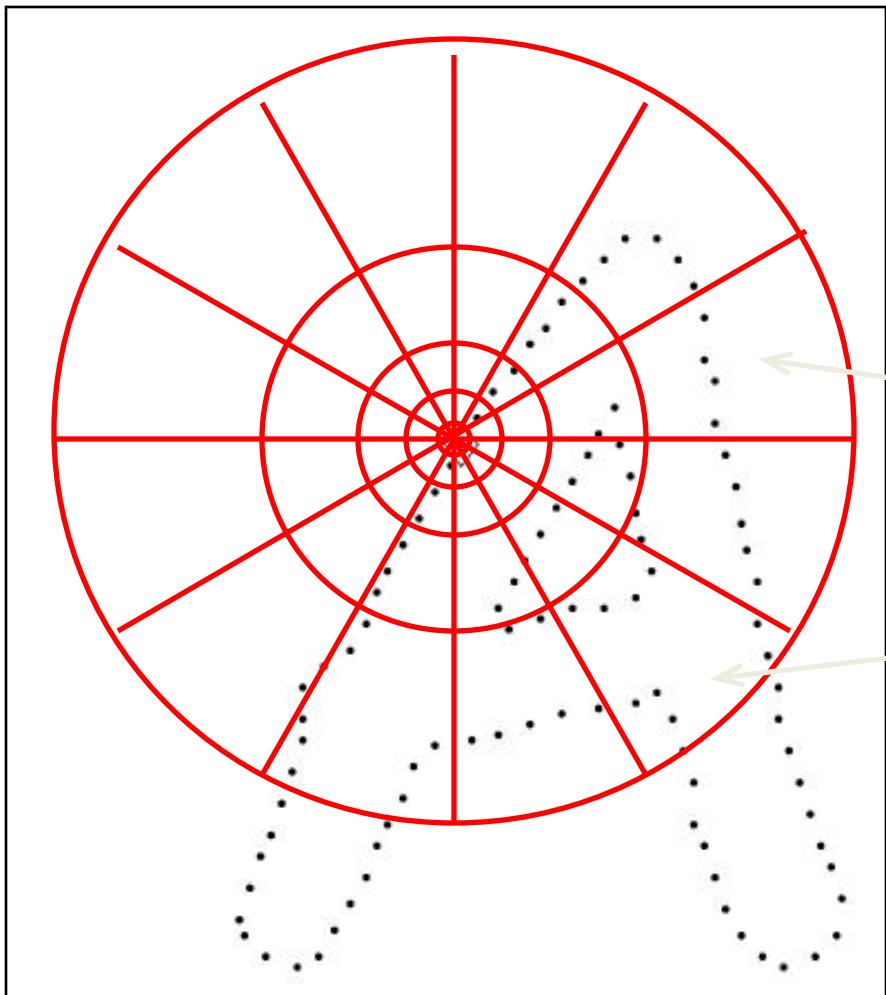
- 1. Interest-point detection:**  
multi-scale Harris corners
- 2. Feature localization:**  
Adaptive thresholding
- 3. Orientation assignment:**  
Pixel gradient direction
- 4. Feature descriptor:**  
Normalized image patch

# Shape Contexts

- Local image feature
  - Different Approach than SIFT / MOPS
- Interest Point: Edge points
- Feature Descriptor: Spatial histogram of neighboring edge points

"Shape Matching and Object Recognition Using Shape Contexts", Belongie et al. PAMI April 2002

# Shape Context



Count = 4

Count = 10

Compact representation of  
distribution of points  
relative to each point

# Trademark Similarity



query



1: 0.086



2: 0.108



3: 0.109



query



1: 0.066



2: 0.073



3: 0.077



query



1: 0.046



2: 0.107



3: 0.114



query



1: 0.046



2: 0.107



3: 0.114



query



1: 0.117



2: 0.121



3: 0.129



query



1: 0.096



2: 0.147



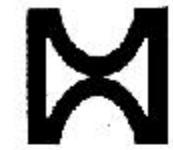
3: 0.153



query



1: 0.078



2: 0.116



3: 0.122



query



1: 0.092



2: 0.10



3: 0.102

# Shape Contexts

- Translation-Invariant: **Yes**
- Scale-Invariant: **Yes** (if radial distances are normalized)
- Rotation-Invariant: **Yes** (if angles are measured relative to common direction, e.g., tangent)
- *Robust to small deformations, noise, outliers*
- Applications:
  - Digit Recognition (.63% error on 20,000 example MNIST data)
    - Note in this case, rotation invariance is NOT desirable ‘6’ vs. ‘9’
  - Trademark Retrieval

# Next time: Fitting Models to Sets of Features

- Local features describe the region around 1 pixel
- Objects take up  $>1$  pixel (and therefore multiple local features)
- How do we match sets of features to a given model?

