Measurement and Mathematics

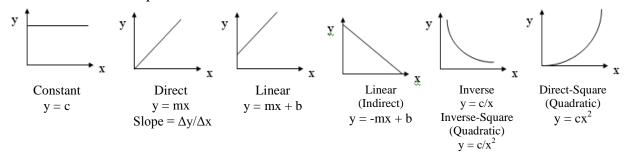
Estimation: 1 kg = 2.2 lbs 1 apple = 1 N 1 quarter = 5 g = 0.005 kg

Order of magnitude: power of ten (thickness of paper = 10^{-4} m)

Fundamental units

Quantity	Units	Symbol
Length	meter	m
Mass	kilogram	kg
Time	second	S
Electric current	ampere	A

General Relationships:

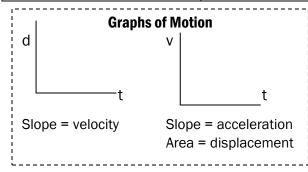


Scalars (magnitude only)	Vectors (magnitude and direction) – only 9!
Distance	Displacement
Speed	Velocity
	Acceleration
	Force (weight, normal force, etc.)
Anything else!	Momentum
	Impulse
	Fields (gravitational, electric, magnetic)

$$\sin \theta = \frac{opp}{hyp}$$

$$\cos \theta = \frac{adj}{hyp}$$

$$\tan \theta = \frac{opp}{adj}$$



Constant Velocity

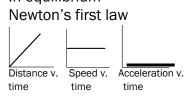
Projectiles

Forces are balanced

F_{net} = 0, a = 0

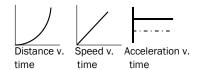
In equilibrium

Newton's first law



Two Types of Motion <u>Constant Acceleration</u>

Forces are unbalanced $F_{net} \neq 0$, $a \neq 0$ not in equilibrium Newton's second law



Horizontal Launch

	Х	Υ
d		h
t	the same	
а	0	9.81
Vi	Vi	0
Vf	Vi	
Vavg	Vi	

Horizontal – constant speed Vertical – constant acceleration

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	•
,vi ∕¹↑ _{vv}	•
• ^{VI} ∕ _{Vy}	•
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Angle Launch

	Х	Υ
d		
t	whole	half
а	0	9.81
Vi	Vx	Vy
Vf	Vx	0 (top)
Vavg	Vx	

Mechanics

Equilibrium: no net force, no acceleration, constant velocity or at rest, forces form a closed figure

Concurrent vectors: placed tail-to-tail

Component vectors: must be head-to-tail to find resultant

Resultant force = F_{net} : head-to-head and tail-to-tail with components

Range of possible resultants:

Maximum = sum of vectors Minimum = difference of vectors

Equilibrant: equal and opposite to resultant

Box on a Hill in Equilibrium: $mgsin\theta = F_f \text{ or } F_A \text{ or } F_T \text{ and } mgcos\theta = F_N$

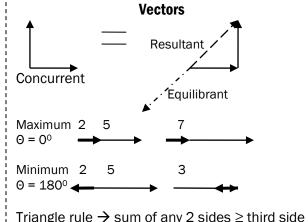
Mass (m): = inertia, amount of matter, constant from place to place, units: kg

Weight (F_g) : = force of gravity, changes from place to place, units: N Formula: $F_g = mg$

Two names for little "g":

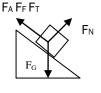
1) acceleration due to gravity, units: m/s^2 , formula: $g = GM/r^2$

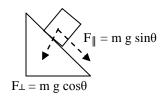
2) gravitational field strength, units: N/kg, formula: $g = F_g/m$



Triangle rule \rightarrow sum of any 2 sides \geq third side for forces to be in equilibrium







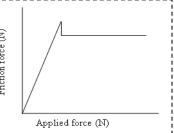
Friction

Static friction (at rest) = applied force until motion starts

Kinetic friction (in motion) is constant

Maximum static friction is greater than kinetic friction

$$F_f = \mu F_N$$



 $F_{c} = ma_{c} = 0$

Circular Motion

Newton's Third Law: Whenever A exerts force on B, B exerts equal/opposite force on A. (Action/reaction pairs: bat and ball, Earth and Moon, hammer and nail)

Forces are the same but the effects of the forces are not: $m\mathbf{a} = \mathbf{m}$

Newton's Law of **Universal Gravitation**

$$F_g = \frac{Gm_1m_2}{r^2}$$

Conservation Laws: electric charge, momentum, mass and energy

Energy

Work: force and displacement must be parallel

W = Fd

Mechanical Energy: PE_g + PE_s + KE

Total Energy: $PE_g + PE_s + KE + Q$

Internal Energy = Q: thermal energy, heat due to

friction/air resistance

Power: rate of change of energy, rate of dong work

(units: Watts (W) = J/s)

 PE_{g} increases if height increases. KE increases if speed increases. PEs increases if spring is stretched or compressed.

Formulas for springs: $PE_s = \frac{1}{2} kx^2$ $F_s = kx$

k = spring constant (units: N/m)

Conservation of Energy: $E_T = E_T$

 $PE_g + PE_s + KE + Q = PE_g + PE_s + KE + Q$

Work-Energy Theorem: $W = \Delta E_T$

Electricity

Conductors (metals) have free electrons, insulators do not.

Objects become charged by losing or gaining electrons (not protons).

Elementary Charge: proton or electron

1 Coulomb of charge = 6.25×10^{18} elementary charges

 $q = -1.60 \times 10^{-19} C$ Charge of Electron: q = -1eOR

Mass of Electron: $m = 9.11 \times 10^{-31} \text{ kg}$

 $OR_{a} = +1.60 \times 10^{-19} C$ q = +1eCharge of Proton:

 $m = 1.67 \times 10^{-27} \text{ kg}$ Mass of Proton:

If two or more identical charged spheres touch, the final charge on each is the average charge (total charge/# of spheres). The total charge is conserved.

A neutral object will be attracted (never repelled) by any charged object. If two objects attract, they could have opposite charges or one could be neutral. If two objects repel, they must have the same type of charge.

Charging by conduction: direct contact - electroscope gets same charge as rod Charging by induction: no direct contact - electroscope gets charge opposite of rod

Collisions

Conservation of Momentum: $p_{before} = p_{after}$

Isolated System: no external forces

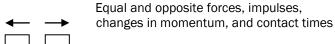
Elastic Collision: total KE is conserved

<u>Sticky</u> $m_1v_1 + m_2v_2 = (m_1 + m_2) \cdot v_f$ (inelastic)

Bouncy $m_1v_1 + m_2v_2 = m_1v_1 + m_2v_2$ (elastic)

Remember - Moving to the left gets a NEGATIVE sign!

Explosion



Different speed based on mass

m**a=M**a

mV=Mv

Coulomb's Law (electric force, electrostatic force) $F_e = \frac{kq_1q_2}{r^2}$

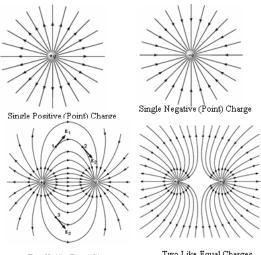
Electric Field (units: N/C or V/m)

Lines go from + to -.

Lines never cross.

Lines show direction of force on small positive test

Field is most intense where field lines are most dense.



Two Unlike Equal Charges

Two Like Equal Charges

Electric potential difference (voltage): work done per unit charge (V = W/q)

Resistance of a wire: $R = \rho L/A$ where $A = \pi r^2$

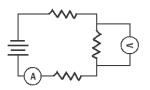
Least resistance (best conductor): short, fat, cold Most resistance (worst conductor): long, skinny, hot

Voltmeter: connect in parallel, infinite internal resistance

Ammeter: connect in series, zero internal resistance



Series Circuit



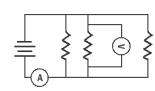
$$R_{eq} = R_1 + R_2 + R_3$$
$$V_T = V_1 + V_2 + V_3$$

Control: current stays the same

Resistance adds up (greater than greatest)

Adding extra resistor increases total resistance and decreases total current.

Parallel Circuit



Potential difference	V	Volt	V = J/C
Current	ı	Amps	A = C/s
Resistance	R	Ohms	$\Omega = V/A$
Power	Р	Watts	W = J/s
Charge	q	Coulombs	С
Energy	W	Joules	J = N·m

$$I_T = I_1 + I_2 + I_3$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

Control: voltage stays the same

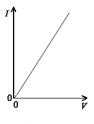
Resistance adds down (less than least)

Adding extra resistor decreases total resistance and increases total current.

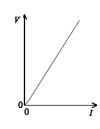
Resistance: R = V/I

Ohmic Device: follows Ohm's law (V\alpha I at constant T) = constant resistance

Non-Ohmic Device: resistance not constant (eg. filament lamp)



Slope = 1/R



Slope = R

Mechanical Power: P = W/t = Fd/t = FvElectrical Power: $P = VI = I^2R = V^2/R$

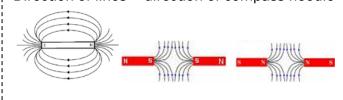
1 electronvolt (eV) = $1.60 \times 10^{-19} \text{ J}$

1 kilowatt hour = $(1000 \text{ W})(1 \text{ hr}) = 3.6 \text{ x } 10^6 \text{J}$

Three units of energy: joules, electronvolts, kilowatt hours

Magnetic Fields

From N to S, density = strength (intensity)
Direction of lines = direction of compass needle

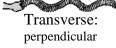


Two Principles of Electromagnetism:

- 1) An electric current (or moving charged particle) generates a magnetic field.
- 2) A changing/moving magnetic field induces an electric current (electromagnetic induction).

Waves

Mechanical: needs medium Electromagnetic: no medium





Radio Wave: electromagnetic wave – speed = $3.00 \times 10^8 \text{ m/s}$

Period (T): seconds/cycle

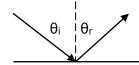
Frequency (f): cycles/second

Wave equation: $v = f\lambda$

In one medium : $f \alpha 1/\lambda$

Control: speed - you can only change the speed of the wave by changing the properties of the medium)

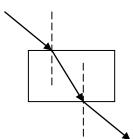
Law of Reflection: $\theta_i = \theta_r$



Refraction: changing direction when changing speed when crossing a boundary

FAST:

into fast, bend away from normal (high n to low n) into slow, bend towards normal (low n to high n)



Light slows down, bends towards the normal, and has a shorter wavelength when it enters a medium with a higher index. The frequency stays the same.

Sound

Longitudinal, mechanical

Speed = 331 m/s (STP) 340 m/s (room temp)

Amplitude = loudness (volume)

Frequency = pitch

Energy α amplitude

Speeds up when going from air to water

Can't be polarized

Light

Transverse, electromagnetic

Speed = $c = 3.00 \times 10^{8} \text{ m/s (vacuum)}$

Amplitude α brightness (intensity)

Frequency α energy (E =hf)

Slows down when going from air to water

Can be polarized

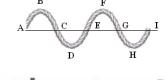
Red: long wavelength, low frequency

Blue: short wavelength, high frequency

In Phase: A, E, I

Out of Phase by 180^{0} or $\lambda/2$: A, C

Amplitude



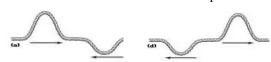
Hard reflection: out of phase



Soft reflection: in phase



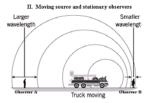
Constructive interference: in phase



Destructive interference: out of phase

Doppler Effect: apparent change in frequency due to relative motion

Constant low frequency, Decreasing amplitude



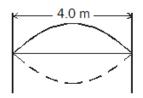
Constant high frequency, Increasing amplitude

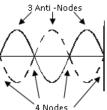
Doppler Shift for Light:

"blue shift" = object moving towards

"red shift" = object moving away

Standing Wave: Two identical waves traveling in opposite directions in the same medium interfere

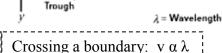




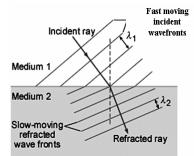
Fundamental Wave:

lowest frequency (f₁), $\lambda_1 = 8.0 \text{ m}$

Visible Light: 400 nm (violet) – 700 nm (red)

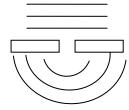


Control: frequency stays the same, so does period and phase



Diffraction: bending around obstacle or spreading through opening

Noticeable diffraction: when size of opening approx, equal to size of wavelength – as opening gets smaller, more diffraction effects

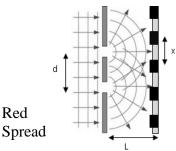


Resonance: energy is transferred to a system by making it vibrate at its natural frequency resulting in large amplitude standing waves

Examples: guitar strings, bridges, swings, wine glasses

Order of Electromagnetic Spectrum: Source – accelerating charged particles Radioactive Monkeys In Virginia Use X-ray Guns lowest to highest frequency and energy

Double Slit Diffraction and Interference: equally spaced bright and dark bands

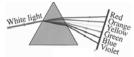


Single Slit Diffraction: wide and bright central maximum

Red

Dispersion: spreading out of light into components due to refraction – each color has slightly different index and speed

Blue Bends Best - slowest Red Resists Refraction - fastest



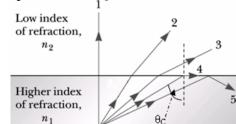
Total Internal Reflection

Critical Angle (θ_C): incident angle for which the refracted angle is 90°

Formula: $\sin \theta_C = n_2/n_1$

Total Internal Reflection: all light is reflected at surface, none is refracted - only occurs when light travels from high to low index and incident angle is greater than θ_C

Major use: fiber optic cables



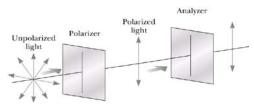
Polarization

Only transverse waves can be polarized - light = yes, sound = no.

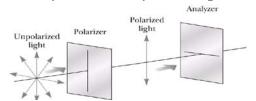
Polarized Light: vibrates in only one direction

Natural Polarization: light is partially polarized when it reflects off a surface

50% of unpolarized light transmits through a single polarizer.



Parallel polarizers: 50% passes through both



Perpendicular polarizers: 0% passes through second

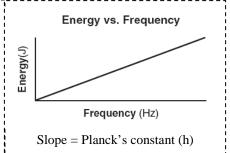
Modern Physics

Wave-Particle Duality		
	Wave Nature	Particle Nature
Light (Energy)	 Diffraction Interference Doppler Effect 	Photo-electric Effect
Matter	- Electron Diffraction - Matter Waves	Collisions (e.g. Alpha particle scattering)

Photon – quantum (particle) of light

Higher frequency = higher energy (E = hf)

Higher intensity = more photons



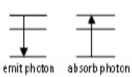
Ground state: lowest energy level $E = mc^2$ (only use if E is in Joules and m is in kg)

 $1 u = 9.31 \times 10^2 \text{ MeV}$

 $E_{photon} = |\Delta E_n|$

 $(E_{photon} = E_i - E_f)$

Excited state: higher energy level Ionization: zero energy level



Atomic Spectra

Hadrons made of quarks, leptons don't break down further...

Antimatter = same mass, opposite charge

Alpha particle = helium nucleus (2 protons and 2 neutrons)

Positron = anti-electron = positive electron

Proton = uud

Neutron = udd

Fundamental forces:

EM and gravity – long-range; Strong and weak – short-range