Problem session 4 PSYC 4301

Given the assumptions of classical test theory, answer the following:

1. If the observed score X is 85 and the error score E is 7, what is the true score T?

- 2. If the true score T is 32 and the observed score X is 28, what is the error score E?
- 3. If the true score variance  $\sigma_T^2$  is 10 and the observed score variance  $\sigma_X^2$  is 12, what is the error score variance  $\sigma_E^2$ ?
- 4. If the observed score variance  $\sigma_X^2$  is 16 and the true score variance  $\sigma_T^2$  is 9, calculate the correlation between observed scores X and true scores T.
- 5. If the error score variance  $\sigma_E^2$  is 3 and the true score variance  $\sigma_T^2$  is 8, calculate the reliability coefficient  $\rho_{XX'}$ .
- 6. If the observed score variance  $\sigma_X^2$  is 15 and the error score variance  $\sigma_E^2$  is 2, calculate the reliability coefficient  $\rho_{XX'}$ .

Suppose we have a test X with reliability coefficient  $\rho_{XX'} = 0.75$  and we calculate an observed score variance of 32.

1. Calculate and interpret the values of  $\sigma_T^2/\sigma_X^2$ ,  $\sigma_E^2/\sigma_X^2$ ,  $\rho_{XT}$ , and  $\rho_{XE}$ 

2. Calculate the true-score variance and the error variance.

3. Calculate the expected measurement error of our test X.

Suppose we have a test X with reliability coefficient  $\rho_{XX'} = 0.40$  and we calculate an observed score variance of 84.

1. Calculate the true-score variance and the error variance.

2. Calculate expected measurement error for our test X.

3. Suppose someone scores 75 on this test. Calculate a 95% confidence interval for their true score.