

1. Consider the data set given in the table below:

$x$	5	8	9	7	14
$y$	3	1	6	7	19

- Use the `lm` function in R to find the equation of the least-squares regression line  $y = a + bx$
  - Plot the data and regression line together
  - Construct a density plot of the residuals. Comment on the overall fit of the model.
- 2.
3. Consider the following data relating GPA to SAT score:

SAT	500	530	590	660	610	700	570	640
GPA	2.3	3.1	2.6	3.0	2.4	3.3	2.6	3.5

- Assume a linear model  $SAT \sim a + b \cdot GPA$ , and compute maximum likelihood estimates for the parameters  $a$  and  $b$ .
  - Based on your model, what  $SAT$  score would you predict for someone with a  $GPA$  of 3.2?
  - Construct 95% confidence intervals for the parameters  $a$  and  $b$ .
  - Based on your 95% CIs, can you conclude that  $GPA$  is a significant predictor of  $SAT$ ? Explain.
4. This exercise illustrates the importance of looking at your data before fitting a model. Consider the following data:

$x$	1	2	3	4	5
$y$	0.74	2.22	6.04	16.20	44.55

- Construct a scatter plot of the data. Does it look linear?
- Use `lm` to fit a linear model  $y = a + bx$ .
- Construct a new scatter plot of  $x$  versus  $\log y$ . Describe the shape. (Hint: just type `plot(x, log(y))` in the R console). What do you notice?
- Use `lm` to fit a linear model for  $\log(y) = a + bx$
- Construct residual plots for both models. Based on these plots, which do you think is the better model? Explain.