

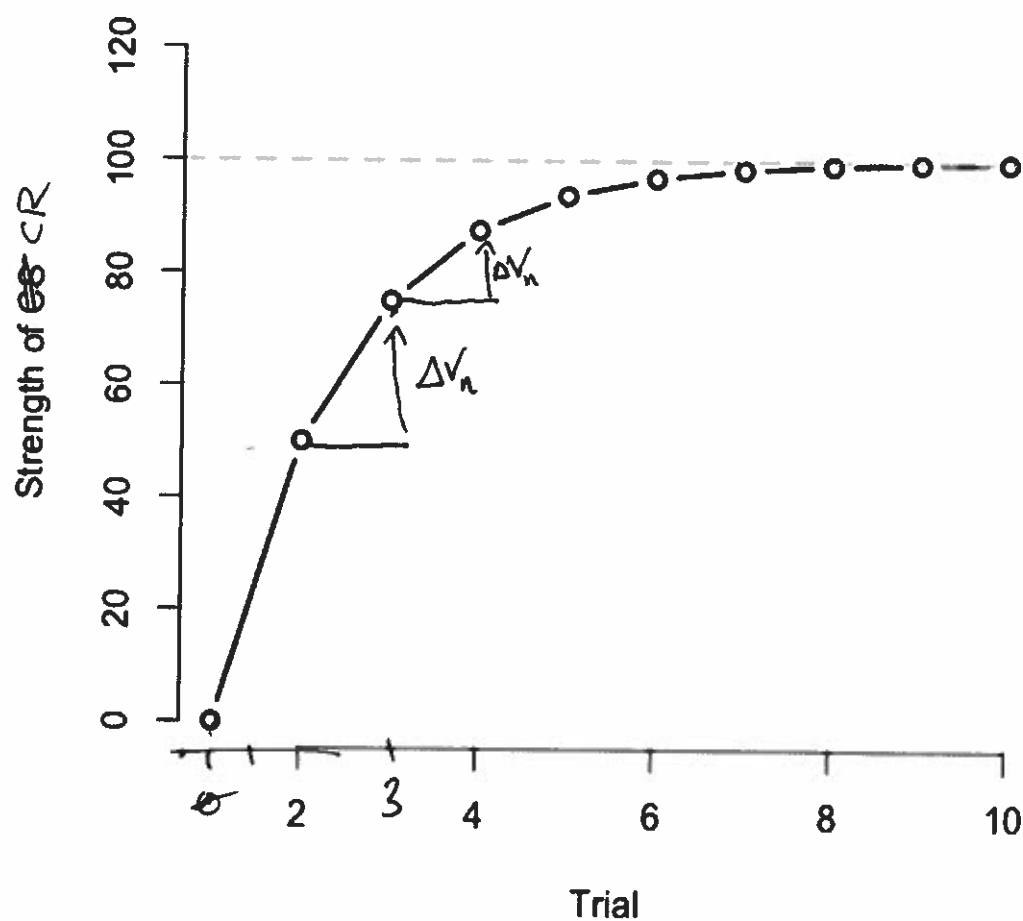
# PSYC 5303 – Lecture 4

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# Mathematical model of conditioning

We know that conditioning looks like this:



Goal – construct a mathematical equation to produce this curve.

## Rescorla-Wagner Model

- uses a "difference equation"
- $V_n$  represents associative strength of CS at trial  $n$
- Equation:

$$\Delta V_n = \alpha \beta (\lambda - \sum V)$$

$$V_n = V_{n-1} + \Delta V_n$$

where  $\Delta V_n = c(V_{\max} - V_{\text{tot}})$

- Parameters:
  - $c$  = "learning rate" (depends on salience of CS, strength of US, etc.)
  - $V_{\max}$  = maximum possible associative strength
  - $V_{\text{tot}}$  = total associative strength of *all* CS
- today, we'll use this equation to generate some standard phenomena in classical conditioning
  - acquisition
  - extinction
  - blocking

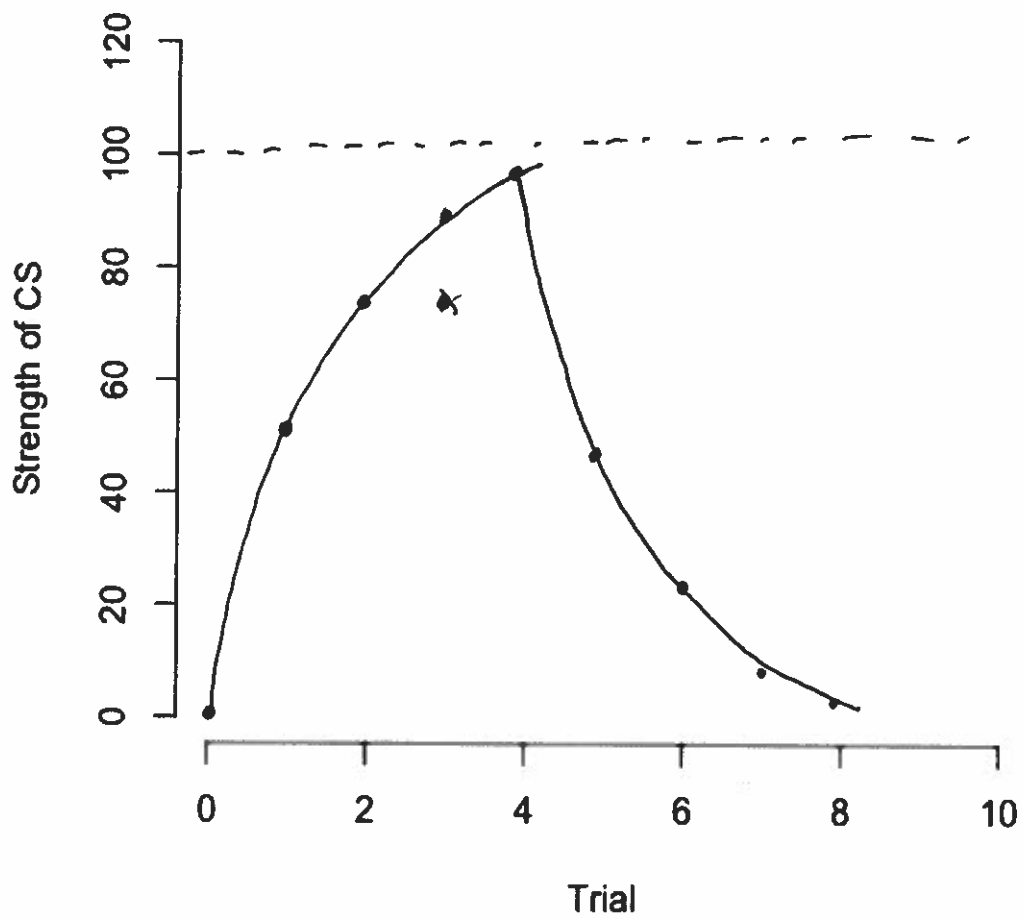
## Acquisition

Set  $c = 0.5$  and  $V_{\max} = 100$

Trial ( $n$ )	Associative strength $V_n = V_{n-1} + c(V_{\max} - V_{\text{tot}})$
1	$\begin{aligned} V_1 &= V_0 + c(V_{\max} - V_{\text{tot}}) \\ &= 0 + 0.5(100 - 0) \\ &= 0 + 50 = \textcircled{50} \end{aligned}$
2	$\begin{aligned} V_2 &= V_1 + 0.5(100 - 50) \\ &= 50 + 0.5(50) = 50 + 25 = \textcircled{75} \end{aligned}$
3	$\begin{aligned} V_3 &= V_2 + 0.5(100 - 75) \\ &= 75 + 0.5(25) = \textcircled{87.5} \end{aligned}$
4	$\begin{aligned} V_4 &= V_3 + 0.5(100 - 87.5) \\ &= 87.5 + 0.5(12.5) = \textcircled{93.75} \end{aligned}$

# Acquisition

Let's plot our numbers here:



## Extinction

Keep  $c = 0.5$  but now  $V_{\max} = 0$  "asymptote"

Trial ( $n$ )	Associative strength $V_n = V_{n-1} + c(V_{\max} - V_{\text{tot}})$
5	$V_5 = V_4 + c(V_{\max} - V_{\text{tot}})$ $= 93.75 + 0.5(0 - 93.75)$ $= 46.88$
6	$V_6 = V_5 + 0.5(0 - 46.88)$ $= 46.88 + 0.5(0 - 46.88) =$ $= 23.44$
7	$V_7 = 23.44 + 0.5(0 - 23.44)$ $= 11.72$
8	$V_8 = 11.72 + 0.5(0 - 11.72)$ $= 5.86$

# Blocking

Recall from lecture 2 – **blocking** happens when presence of an established CS interferes with conditioning a *new* CS

Training phase 1:

- $CS_a$  (noise) +  $US$  (shock)  $\rightarrow UR$  (fear response)
- (repeat)
- $CS_a$  (noise)  $\rightarrow CR$  (fear response)  $\checkmark_{max}$  is attained!

Training phase 2:

- $CS_a$  (noise) +  $CS_b$  (light) +  $US$  (shock)  $\rightarrow UR$  (fear response)
- (repeat)
- $CS_a$  (noise) +  $CS_b$  (light)  $\rightarrow CR$  (fear response)

Test phase:

- $CS_b$  (light)  $\rightarrow$  no CR!

Interpretation: previous learning blocks learning of  $CS_b$

# Blocking

Let's see how Rescorla-Wagner would predict this:

Phase 1:

- $CS_a$  (noise) +  $US$  (shock)  $\rightarrow UR$  (fear response)
- (repeat)
- $CS_a$  (noise)  $\rightarrow CR$  (fear response)

After Phase 1, we can assume the following:

- $V_{\text{noise}} = V_{\text{max}} = 100$
- $V_{\text{light}} = 0$

Thus, at the beginning of Phase 2, we have

- $V_{\text{tot}} = V_{\text{noise}} + V_{\text{light}} = 100 + 0 = 100$



## Blocking

Now, at the beginning of Phase 2, here's what happens:

$$\begin{aligned} V_n &= V_{n-1} + c(V_{\max} - V_{\text{tot}}) \\ &= V_{n-1} + c(100 - 100) \\ &= V_{n-1} + 0 \end{aligned}$$

That is, there is no learning that occurs! (i.e.,  $\Delta V_n = 0$ )