Chapter 1

Data Analysis

The signature of GGM SUSY particle production in this search is an excess of two-photon events with high $\not{E}_T$. $\not{E}_T$ is reconstructed using the particle flow algorithm as described in Sec. **??**. Candidate two-photon events, as well as control events, are selected according to the offline object criteria presented in Secs. **??** and **??**, the event quality criteria in Sec. **??**, and the trigger requirements in Sec. **??**. These are summarized in Table 1.1.

Table 1.1: Selection criteria for $\gamma\gamma$, $e\gamma$, ee, and ff events.

Variable	Cut			
	$\gamma\gamma$	$e\gamma$	ee	ff
HLT match	IsoVL	IsoVL	IsoVL	IsoVL || R9Id
E_T	$> 40/$ > 25 GeV	$> 40/$ > 25 GeV	$> 40/$ > 25 GeV	$> 40/$ > 25 GeV
SC $|\eta|$	< 1.4442	< 1.4442	< 1.4442	< 1.4442
H/E	< 0.05	< 0.05	< 0.05	< 0.05
$R9$	< 1	< 1	< 1	< 1
Pixel seed	No/No	Yes/No	Yes/Yes	No/No
$I_{\text{comb}}, \sigma_{i\eta i\eta}$	< 6 GeV && < 0.011	< 6 GeV && < 0.011	< 6 GeV && < 0.011	< 20 GeV && $(\geq 6$ GeV || $\geq 0.011)$
JSON	Yes	Yes	Yes	Yes
No. good PVs	≥ 1	≥ 1	≥ 1	≥ 1
ΔR_{EM}	> 0.6	> 0.6	> 0.6	> 0.6
$\Delta\phi_{\text{EM}}$	≥ 0.05	≥ 0.05	≥ 0.05	≥ 0.05

This search utilizes 4.7 fb^{-1} of CMS data collected during the period April-December 2011, corresponding to the following datasets [**?**]:

- `/Photon/Run2011A-05Jul2011ReReco-ECAL-v1/AOD`

- `/Photon/Run2011A-05Aug2011-v1/AOD`

- `/Photon/Run2011A-03Oct2011-v1/AOD`

- `/Photon/Run2011B-PromptReco-v1/AOD`

The search strategy is to model the backgrounds to the GGM SUSY signal using $\not{E}_T$ shape templates derived from the control samples, and then to look for a high-$\not{E}_T$ excess above the estimated background in the $\gamma\gamma$ sample. There are two categories of backgrounds: QCD processes with no real $\not{E}_T$ and electroweak processes with real $\not{E}_T$ from neutrinos. The relevant QCD background processes are multijet production with at least two jets faking photons, photon + jet production with at least one jet faking a photon, diphoton production, and Z production with a radiated photon where at least one of the Z decay products (typically a jet) fakes a photon. The relevant electroweak background processes, which are small compared to the QCD background, involve $W \rightarrow e\nu$ decay with a recoiling jet that fakes a photon or a real radiated photon. In both cases, the electron is misidentified as a photon due to a small inefficiency in reconstructing the electron pixel seed. The main diagrams contributing to the QCD(electroweak) backgrounds are shown in Figure **??**(**??**). **Generate these Feynman diagrams.**

Figure **??** shows the $\not{E}_T$ spectrum of the $\gamma\gamma$ search data sample overlaid on the $\not{E}_T$ spectra of MC simulated background components. The MC spectra are normalized to the integrated luminosity of the $\gamma\gamma$ data sample. **Make this plot.** The dominant background components are QCD inclusive photon processes. The MC is not used in the actual background estimation. It is just shown here to illustrate the breakdown of backgrounds.

Data control samples are used to model all of the backgrounds. The primary control sample used to model the QCD background is the ff sample, which is similar to the candidate $\gamma\gamma$ sample but with combined isolation or $\sigma_{i\eta i\eta}$ cuts inverted. The cuts on these variables are used to distinguish between photons and jets, so by inverting those cuts, the resulting ff sample becomes enriched with QCD dijets. Because the fake photons are still required to pass a tight cut on H/E, they are guaranteed to be very electromagnetic jets, with an EM energy scale and resolution similar to that of the candidate photons. This insures that the resulting estimate of the $\not{E}_T$ shape does not have too long of a tail from severe HCAL mis-measurements that are actually rare in the $\gamma\gamma$ sample, as shown in Figure **??**. **Plot the $\gamma\gamma/ff$ $\not{E}_T$ agreement for different values of the ff H/E cut in MC. Make the same plot in data for a restricted $\not{E}_T$ range?**

As a cross-check, the ee sample is also used to model the QCD background. This sample of Z decays should have no true $\not{E}_T$, just like the ff sample, and the electron definition (differing from the photon definition only in the presence of a pixel seed) insures that the electron energy scale and resolution is similar to that of the photon.

Finally, the $e\gamma$ sample is used to model the electroweak background from $W \to e\nu$ decays. The $e\gamma$ $\not{E}_T$ distribution is scaled by the electron→photon misidentification rate to predict the number of $W\gamma$ and W + jet events in the $\gamma\gamma$ sample.

The remainder of this chapter describes the data analysis procedures and the final results of the search. Sec. 1.1 addresses the QCD background estimation. Sec. **??** addresses the electroweak background estimation. The chapter concludes with a discussion of systematic errors in Sec. 1.3 and a presentation of the final results in Sec. 1.4.

1.1 Modeling the QCD Background

1.1.1 Outline of the Procedure

Due to the fact that the CMS ECAL energy resolution is much better than the HCAL energy resolution, the energies of the two candidate photons in the events of the $\gamma\gamma$ sample are typically measured to far greater accuracy and precision than the energy of the hadronic recoil in those events. Therefore, fake $\not{E}_T$ in the $\gamma\gamma$ sample is almost entirely the result of hadronic mis-measurement in QCD dijet, photon + jet, and diphoton events. The strategy employed to model this background is to find a control sample in data consisting of two well-measured EM objects, just like the candidate $\gamma\gamma$ sample, and assign each event a weight to account for the underlying kinematic differences between the control and candidate samples. Once the reweighted $\not{E}_T$ spectrum of the control sample is created, it is then normalized in the low-$\not{E}_T$ region, the assumption being that GGM SUSY does not predict a significant amount of events at low $\not{E}_T$. There are three aspects to this QCD background estimation procedure that bear highlighting:

Choice of control sample Since the underlying cause of $\not{E}_T$ in the candidate sample is mis-measured hadronic activity, a control sample with similar hadronic activity to the candidate sample should be chosen. Hadronic activity refers to number of jets, jet E_T, pileup, etc.

Reweighting The control sample is reweighted so that its $\not{E}_T$ spectrum appears as it would if the control sample had the same kinematic properties as the candidate sample (i.e. particle p_T and η distributions, etc.). By choosing an appropriate control sample and reweighting it, the control $\not{E}_T$ distribution should now match both the hadronic activity and the kinematics of the candidate sample.

Normalization Finally, the control $\not{E}_T$ distribution is normalized in a region of

low $\not{E}_T$, where contamination from the expected GGM SUSY signal is small. This implies an extrapolation of the low-$\not{E}_T$ QCD background prediction to the high-$\not{E}_T$ signal region.

As explained in the beginning of this chapter, the ff sample is used as the primary QCD control sample, while the ee sample is used as a cross-check. Both samples have two well-measured EM objects per event, no real $\not{E}_T$,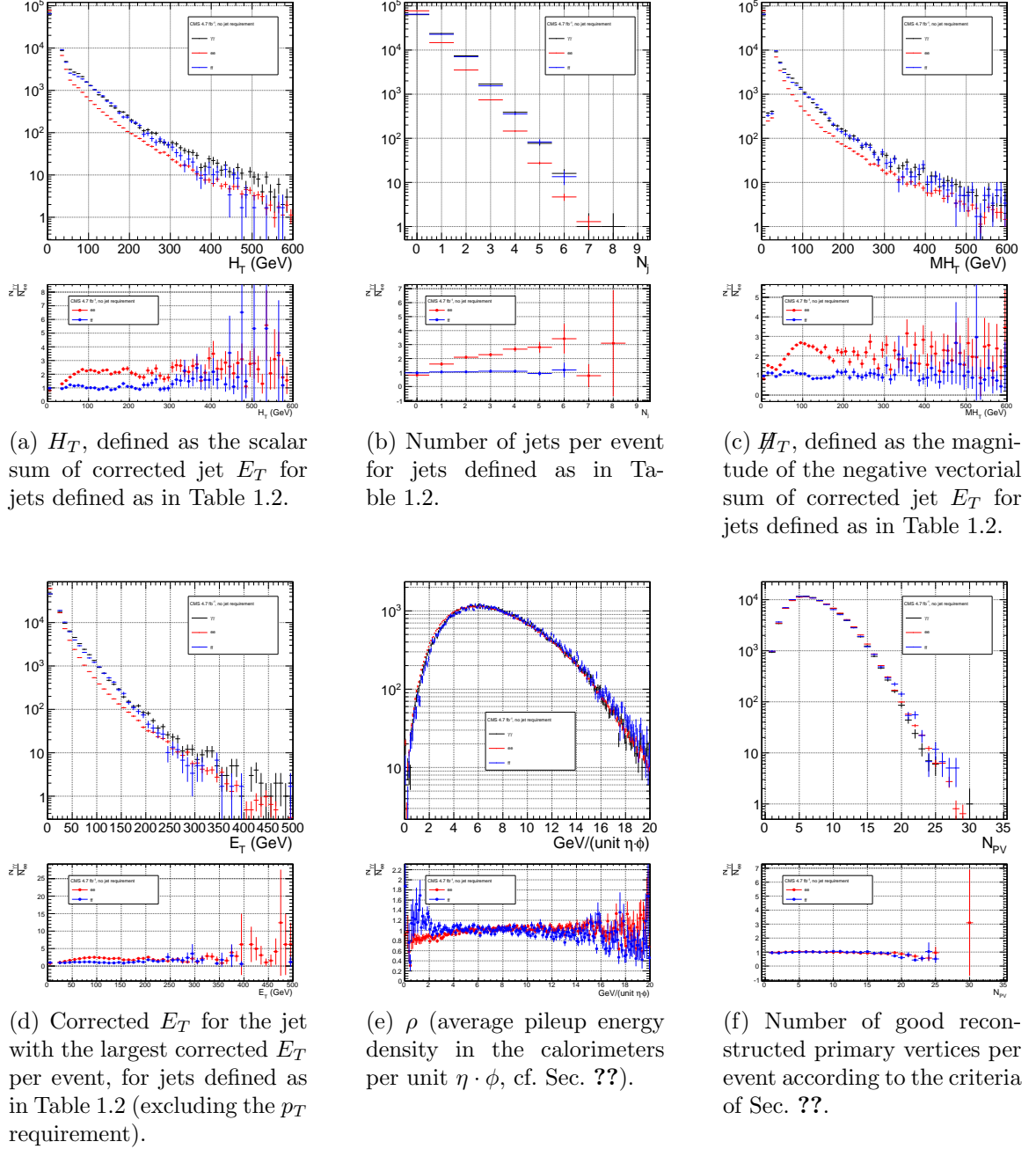 and similar hadronic activity to the $\gamma\gamma$ sample. Figure 1.1 shows a comparison of the shapes of some distributions relevant to hadronic activity between the $\gamma\gamma$, ee, and ff samples. In general, the ee sample has less hadronic activity than the $\gamma\gamma$ and ff samples, as shown by the more steeply falling ee distributions in Figs. 1.1a, 1.1b, 1.1c, and 1.1d. In addition to the kinematic reweighting, there is also a reweighting by number of jets per event, which attempts to correct for this difference (see Sec. 1.1.2).

Table 1.2: Definition of HB/HE/HF hadronic jets. **Add a footnote describing the PF electron and PF muon definitions, with references.**

Variable	Cut
Algorithm	`L1FastL2L3Residual` corrected PF (cf. Sec. **??**)
p_T	> 30 GeV
$\|\eta\|$	< 5.0
Neutral hadronic energy fraction	< 0.99
Neutral electromagnetic energy fraction	< 0.99
Number of constituents	> 1
Charged hadronic energy	> 0.0 GeV if $\|\eta\| < 2.4$
Number of charged hadrons	> 0 if $\|\eta\| < 2.4$
Charged electromagnetic energy fraction	< 0.99 if $\|\eta\| < 2.4$
ΔR to nearest electron, muon, or one of the two primary EM objects	> 0.5

(a) H_T, defined as the scalar sum of corrected jet E_T for jets defined as in Table 1.2.

(b) Number of jets per event for jets defined as in Table 1.2.

(c) $\not{H}_T$, defined as the magnitude of the negative vectorial sum of corrected jet E_T for jets defined as in Table 1.2.

(d) Corrected E_T for the jet with the largest corrected E_T per event, for jets defined as in Table 1.2 (excluding the p_T requirement).

(e) ρ (average pileup energy density in the calorimeters per unit $\eta \cdot \phi$, cf. Sec. **??**).

(f) Number of good reconstructed primary vertices per event according to the criteria of Sec. **??**.

Figure 1.1: Comparison of the shapes of some distributions relevant to hadronic activity between the $\gamma\gamma$, ee, and ff samples. The ee and ff distributions are normalized to the number of events in the $\gamma\gamma$ distribution. Errors are statistical only.

EM objects (well measured kinematics, no fake ME$_T$)

di-EM p$_T$ (well-measured handle on the kinematics of the jet system)

Most energetic EM object

2nd most energetic EM object

z (beam direction)

y

x

Jets (poorly measured kinematics, source of fake ME$_T$)
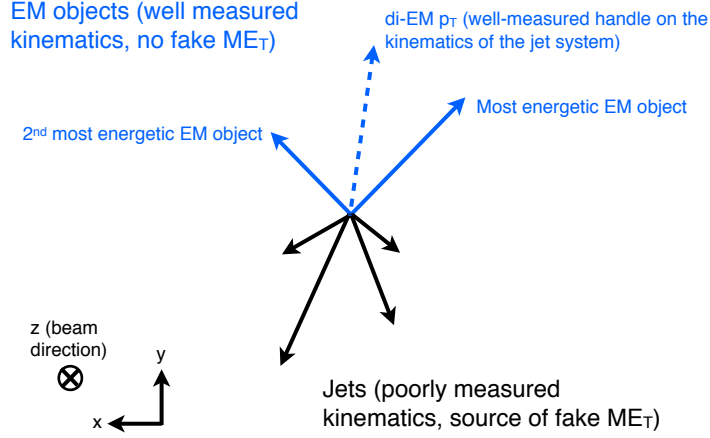
Figure 1.2: Cartoon showing the di-EM system in blue and the hadronic recoil in black. The di-EM p_T (dashed blue line) is used to reweight the control sample kinematic properties to match those of the candidate $\gamma\gamma$ sample.

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1.1.2 Reweighting

To reweight the control sample events to match the kinematics of the candidate sample events, a weight based on the p_T of the di-EM-object system and the number of jets in the event is used. As explained in Sec. 1.1.1, $\not{E}_T$ in the $\gamma\gamma$, ff, and ee samples is due to the poorly measured hadronic recoil off the well-measured di-EM system. Therefore, the p_T of the di-EM system is a good handle on the true magnitude of the hadronic recoil, which affects the measured $\not{E}_T$. The di-EM system is depicted in Figure 1.2.

Whereas the di-EM p_T reweighting accounts for differences in production kinematics between the control and $\gamma\gamma$ samples, a simultaneous reweighting based on the number of jets in the event accounts for differences in hadronic activity between the samples, especially between ee and $\gamma\gamma$ (cf. Fig. 1.1). Jets are defined as in Table **??**. Figure 1.3 shows the effect of reweighting by number of jets per event, which is to increase(decrease) the tail of the $ee(ff)$ $\not{E}_T$ spectrum.

Although the electron and photon energies are well measured by the ECAL, the ECAL-only measurement of the fake photon energy (cf. Sec **??**) is biased slightly
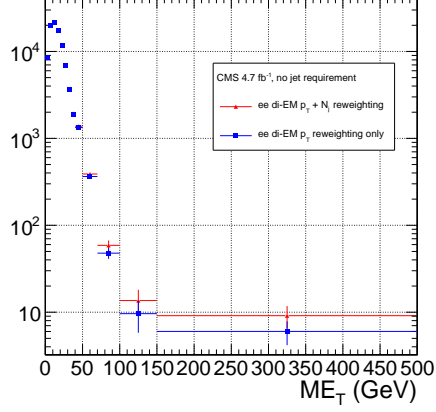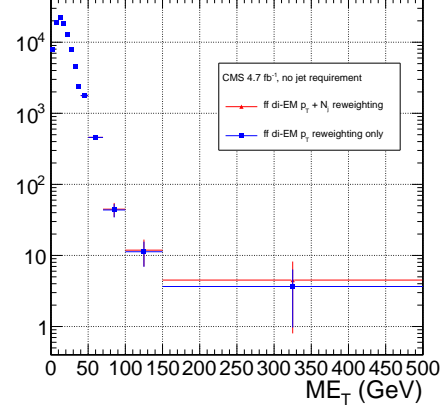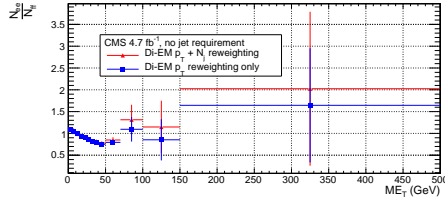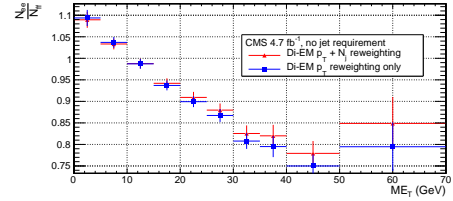
(a) *ee* $\not{E}_T$ spectra.

(b) *ff* $\not{E}_T$ spectra.

(c) Ratio of *ee* to *ff* $\not{E}_T$ spectra.

(d) Ratio of *ee* to *ff* $\not{E}_T$ spectra, zoomed x-axis.

Figure 1.3: $\not{E}_T$ spectra of the reweighted *ee* and *ff* control samples. Blue squares indicate di-EM p_T reweighting only; red triangles indicate di-EM p_T + number of jets reweighting. PF p_T (cf. p. 10) is used to calculate the di-EM p_T. The full normalization procedure is employed, along with *ee* sideband subtraction (discussed in at the end of this section). Error bars include statistical, reweighting, and normalization error (see Sec. 1.3).

low due to the fact that fakes (which are really jets) tend to deposit some energy in the HCAL. This can be seen in Figs. 1.4 and 1.5, which show the relative difference between the ECAL-only E_T measurement and the PF E_T measurement vs. EMF for electrons, photons, and fakes. PF E_T is defined as the `L1Fast`-corrected E_T of the nearest PF jet with $p_T \geq 20$ GeV (i.e., the E_T of the PF jet object reconstructed from the same ECAL shower as the fake photon). On average, the fakes tend to deposit a few percent more energy in the HCAL than the electrons or photons, which is recovered by the PF algorithm. For this reason, the PF p_T is used in the calculation of di-EM p_T rather than the ECAL-only p_T. This leads to a modest improvement in the agreement between the ee and ff $\not{E}_T$ spectra, as shown in Figure 1.6.

The control sample event weights are defined as

$$w_{ij} \;\; = \;\; \frac{N_{\text{control}}}{N_{\gamma\gamma}} \frac{N^{ij}_{\gamma\gamma}}{N^{ij}_{\text{control}}} \tag{1.1}$$

where i runs over the number of di-EM p_T bins, j runs over the number of jet bins, N_{control} is the total number of events in the control sample, $N_{\gamma\gamma}$ is the total number of events in the $\gamma\gamma$ sample, $N^{ij}_{\gamma\gamma}$ is the number of $\gamma\gamma$ events in the ith di-EM p_T bin and j^{th} jet bin, and N^{ij}_{control} is the number of control sample events in the ith di-EM p_T bin and j^{th} jet bin. The effect of the reweighting is more significant for the ee sample than for the ff sample, as shown in Figure 1.7.

The ee sample contains a non-negligible background of $t\bar{t}$ events in which both W bosons decay to electrons. These events have significant real $\not{E}_T$ from the two neutrinos (unlike the $\gamma\gamma$ events), and therefore inflate the background estimate at high $\not{E}_T$. In order to remove the $t\bar{t}$ contribution from the ee sample, a sideband subtraction method is employed.

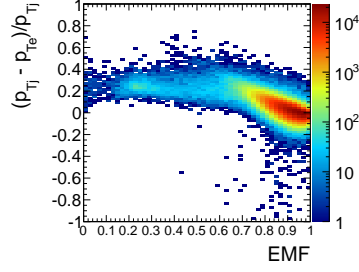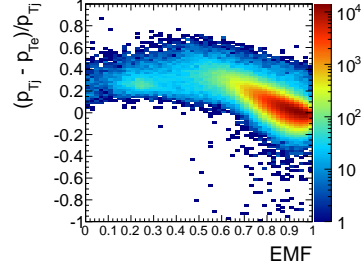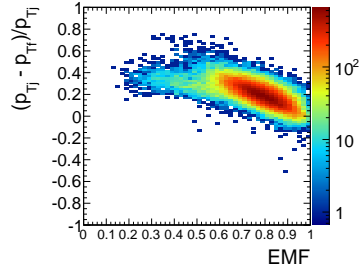Only events in the ee sample with 81 GeV $\leq m_{\text{ee}} < 101$ GeV, where m_{ee} is the
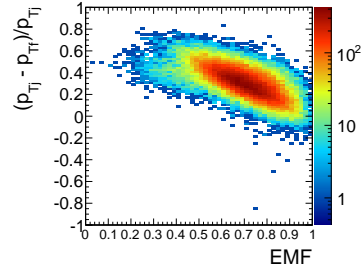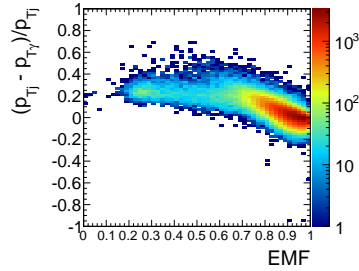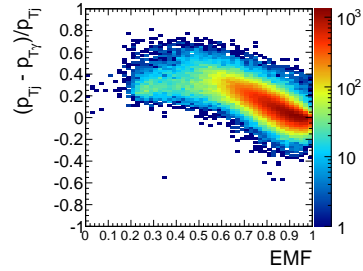
(a) Leading electron in *ee* events.

(b) Trailing electron in *ee* events.

(c) Leading fake in *ff* events.

(d) Trailing fake in *ff* events.

(e) Leading photon in $\gamma\gamma$ events.

(f) Trailing photon in $\gamma\gamma$ events.

Figure 1.4: Relative difference between the ECAL-only E_T measurement and the PF E_T measurement vs. EMF. PF E_T is defined in the text.
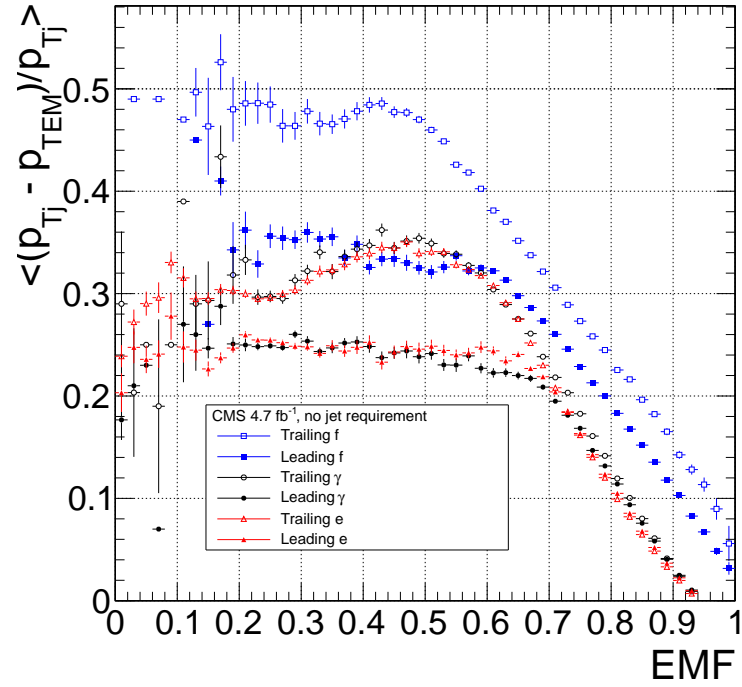
Figure 1.5: Average relative difference between the ECAL-only E_T measurement and the PF E_T measurement vs. EMF for the leading (filled marker) and trailing (open marker) electrons in *ee* events (red triangles), fakes in *ff* events (blue squares), and photons in $\gamma\gamma$ events (black circles). These are nothing more than profile histograms of Fig. 1.4. PF E_T is defined in the text. Error bars are statistical only.
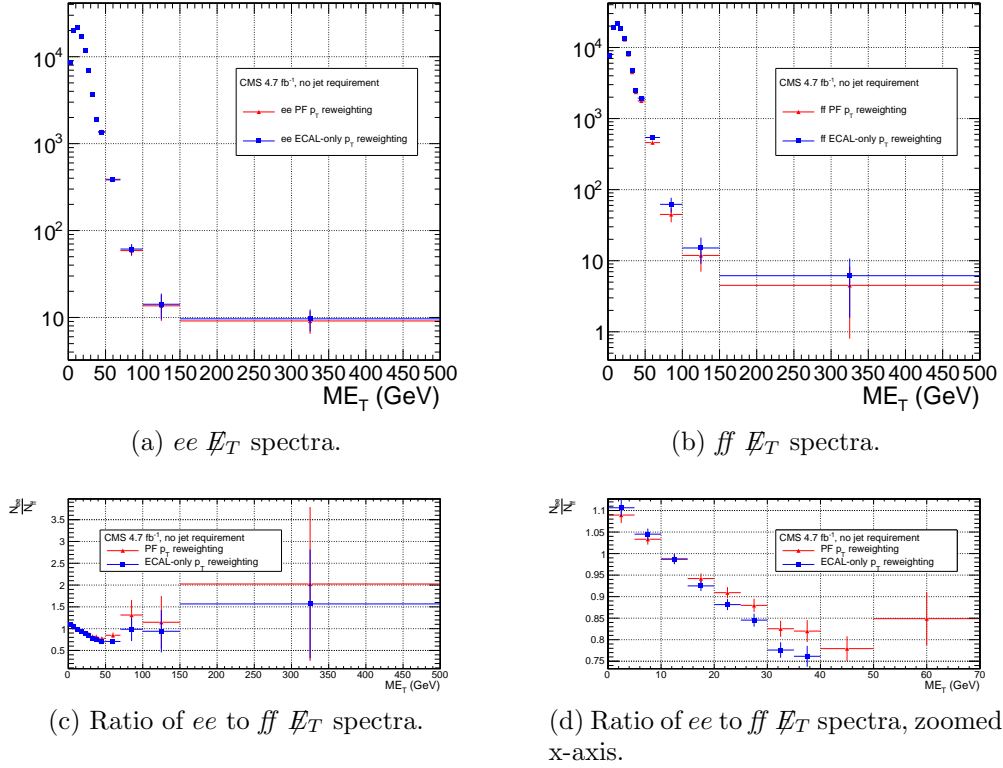
(a) *ee* $\not{E}_T$ spectra.

(b) *ff* $\not{E}_T$ spectra.

(c) Ratio of *ee* to *ff* $\not{E}_T$ spectra.

(d) Ratio of *ee* to *ff* $\not{E}_T$ spectra, zoomed x-axis.

Figure 1.6: $\not{E}_T$ spectra of the reweighted *ee* and *ff* control samples. Blue squares indicate reweighting using the ECAL-only p_T estimate; red triangles indicate reweighting using the PF p_T estimate. The full reweighting and normalization procedure is employed, along with *ee* sideband subtraction (discussed at the end of this section). Error bars include statistical, reweighting, and normalization error (see Sec. 1.3).
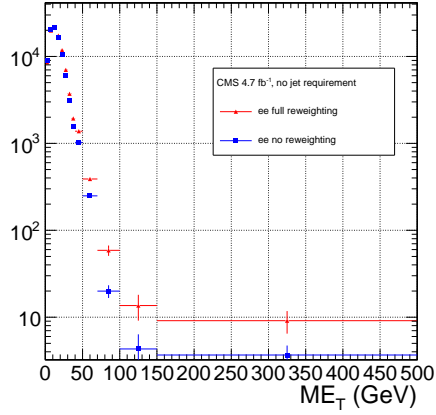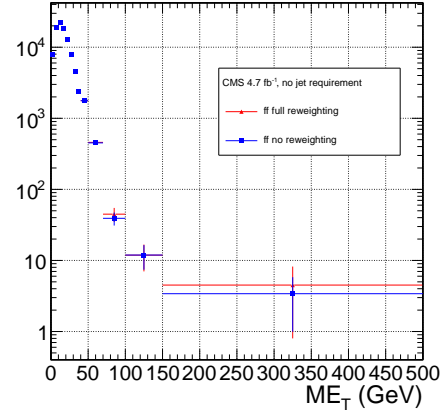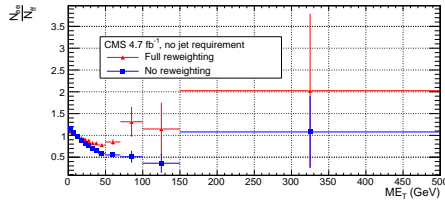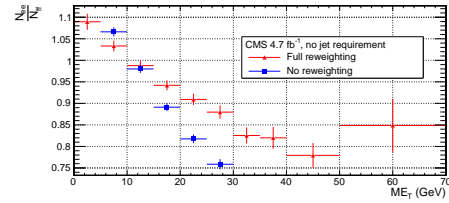
(a) *ee* $\not{E}_T$ spectra.

(b) *ff* $\not{E}_T$ spectra.

(c) Ratio of *ee* to *ff* $\not{E}_T$ spectra.

(d) Ratio of *ee* to *ff* $\not{E}_T$ spectra, zoomed x-axis.

Figure 1.7: $\not{E}_T$ spectra of the *ee* and *ff* control samples. Red triangles indicate full di-EM p_T + number of jets reweighting; blue squares indicate no reweighting. PF p_T (cf. p. 10) is used to calculate the di-EM p_T. The full normalization procedure is employed, along with *ee* sideband subtraction (discussed at the end of this section). Error bars include statistical, reweighting (where appropriate), and normalization error (see Sec. 1.3).

di-electron invariant mass, are used in the QCD background estimate. This choice maximizes the ratio of Z signal to background. The sidebands used to estimate the background contribution within the Z window are defined such that 71 GeV $\leq m_{\text{ee}} <$ 81 GeV and 101 GeV $\leq m_{\text{ee}} <$ 111 GeV.

The full reweighting procedure is applied to the Z signal region and the two sideband regions independently. Only Z signal events are used in the calculation of the di-EM p_T weights for the Z signal region, and likewise only the events within a given sideband region are used in the calculation of the weights for that region. Assuming a constant $t\bar{t}$ background shape, the resulting reweighted sideband $\not{E}_T$ distributions are added together and subtracted from the reweighted Z signal $\not{E}_T$ distribution. The sideband subtracted Z signal $\not{E}_T$ distribution is then normalized as discussed in Secs. 1.1.1 and 1.1.3. The statistical and reweighting error from the sideband regions is propagated to the error on the final ee QCD $\not{E}_T$ estimate.

The di-EM p_T weights for the two ee sideband regions are shown in figure **??**. The overall scale of the weights, as well as the trend with di-EM p_T, is similar for the two regions (except at high di-EM p_T, where the statistics are poor anyway). Figure 1.9 shows the $\not{E}_T$ spectra for the two sideband regions and the Z signal region after subtraction. The shapes of the spectra indicate that the high-$\not{E}_T$ $t\bar{t}$ tail, present in the sideband distributions, was successfully subtracted from the Z signal distribution.

The ee (81 GeV $\leq m_{\text{ee}} <$ 101 GeV), ff, and $\gamma\gamma$ di-EM p_T spectra for events with 0, 1, or ≥ 2 jets (as in Table **??**) are shown in Figure 1.10. Broad humps in the ff and $\gamma\gamma$ spectra are due to kinematic ΔR and p_T turn-ons that are suppressed in the ee sample due to the invariant mass cut. Figure 1.11 shows the weights applied to the ee (81 GeV $\leq m_{\text{ee}} <$ 101 GeV) and ff $\not{E}_T$ spectra as a function of di-EM p_T and number of jets per event.

(a) 71 GeV $\leq m_{ee} < 81$ GeV, 0 jets.

(b) 71 GeV $\leq m_{ee} < 81$ GeV, 1 jet.

(c) 71 GeV $\leq m_{ee} < 81$ GeV, ≥ 2 jets.

(d) 101 GeV $\leq m_{ee} < 111$ GeV, 0 jets.

(e) 101 GeV $\leq m_{ee} < 111$ GeV, 1 jet.

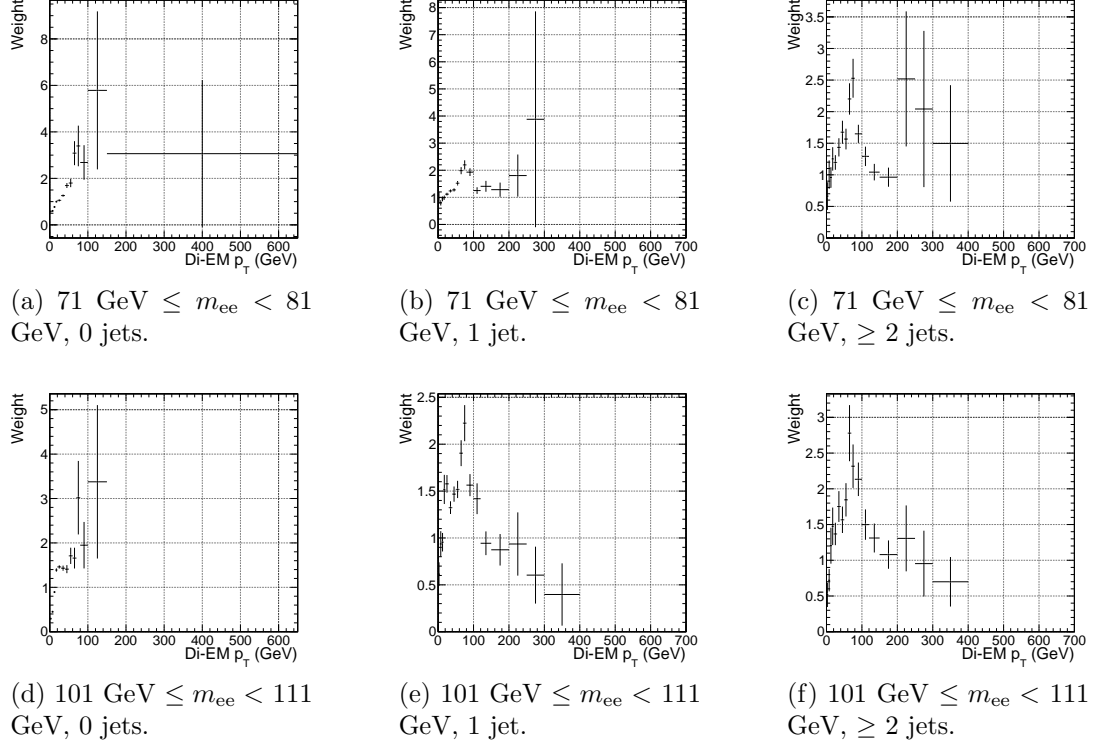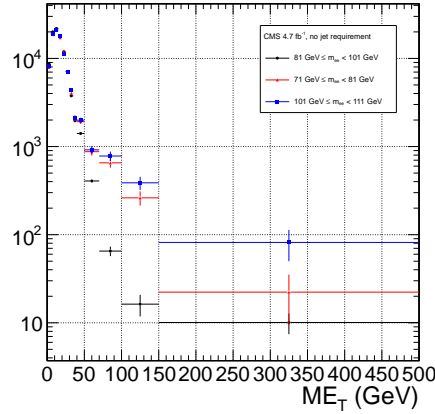(f) 101 GeV $\leq m_{ee} < 111$ GeV, ≥ 2 jets.

Figure 1.8: ee sideband di-EM p_T weights for events with 0, 1, or ≥ 2 jets (as in Table **??**). Errors are statistical only.
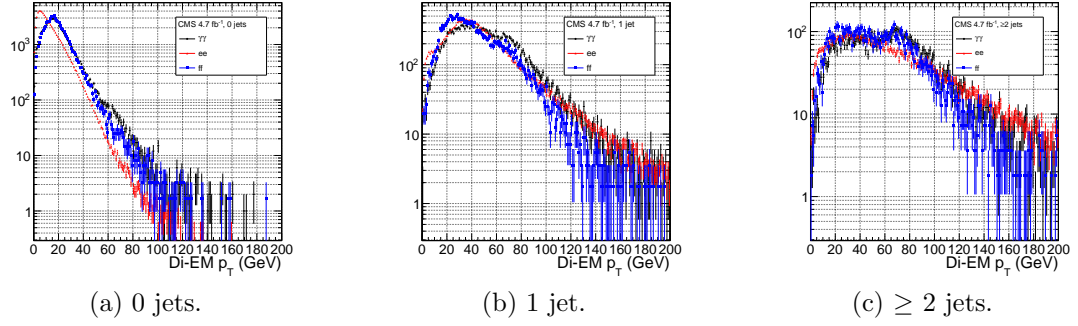

Figure 1.9: $\not{E}_T$ spectra of the ee sample for 71 GeV $\leq m_{ee} < 81$ GeV (red triangles), 81 GeV $\leq m_{ee} < 101$ GeV (black circles), and 101 GeV $\leq m_{ee} < 111$ GeV (blue squares). The two sideband distributions (red and blue) are normalized to the area of the Z signal distribution (black). Errors on the sideband distributions are statistical only, while the error on the Z signal distribution includes statistical, reweighting, and normalization error (see Sec. 1.3).

(a) 0 jets.   (b) 1 jet.   (c) ≥ 2 jets.

Figure 1.10: ee (81 GeV $\leq m_{ee} < 101$ GeV) (red triangles), ff (blue squares), and $\gamma\gamma$ (black circles) di-EM p_T spectra for events with 0, 1, or ≥ 2 jets (as in Table **??**). Errors are statistical only. **Zoom out the x-axis to show the full tail out to 500 GeV?**
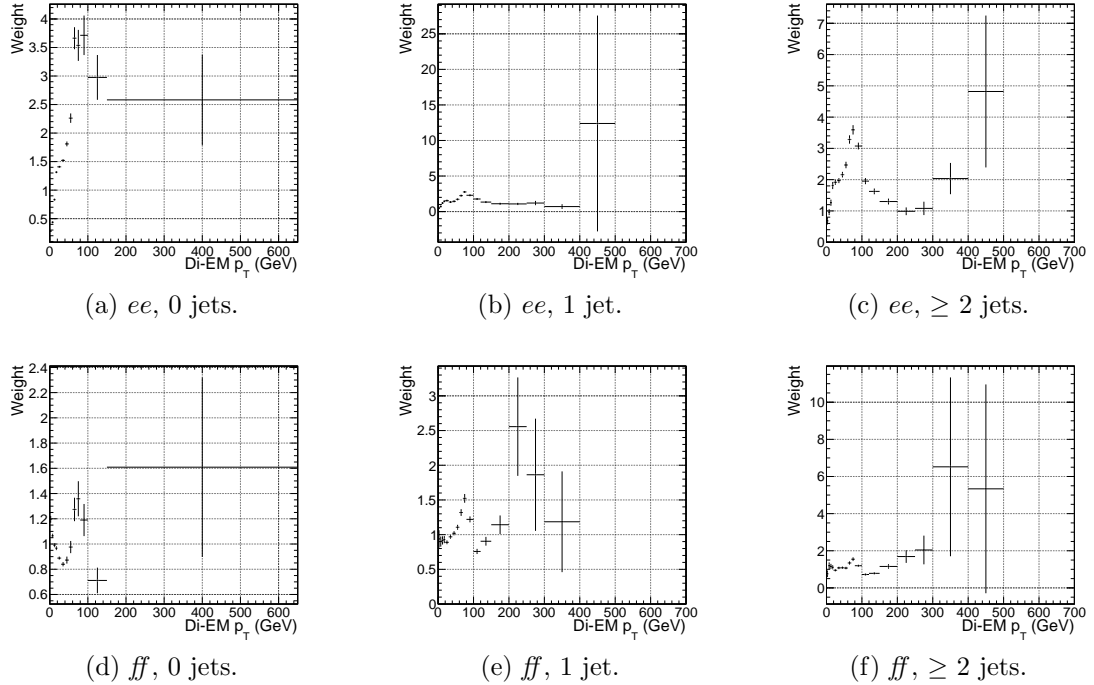

(a) ee, 0 jets.   (b) ee, 1 jet.   (c) ee, ≥ 2 jets.

(d) ff, 0 jets.   (e) ff, 1 jet.   (f) ff, ≥ 2 jets.

Figure 1.11: ee (81 GeV $\leq m_{ee} < 101$ GeV) and ff di-EM p_T weights for events with 0, 1, or ≥ 2 jets (as in Table **??**). Errors are statistical only. **Zoom in the x-axis to hide large weights with large statistical errors?**

1.1.3 Normalization

After reweighting, the $\not{E}_T$ distributions of the QCD control samples are normalized to the $\not{E}_T < 20$ GeV region of the candidate $\gamma\gamma$ $\not{E}_T$ spectrum, where signal contamination is low. The normalization factor is $(N_{\gamma\gamma}^{\not{E}_T<20\mathrm{GeV}} - N_{e\gamma}^{\not{E}_T<20\mathrm{GeV}})/N_{\mathrm{control}}^{\not{E}_T<20\mathrm{GeV}}$, where $N_{e\gamma}^{\not{E}_T<20\mathrm{GeV}}$ is the expected number of electroweak background events with $\not{E}_T < 20$ GeV (discussed in Section 1.2).

1.2 Modeling the Electroweak Background

1.3 Systematic Errors

1.4 Results