



Algorithms: Design  
and Analysis, Part II

# Introduction

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Motivating Application:  
Sequence Alignment

# Sequence Alignment

Sequence alignment: fundamental problem in computational genomics.

Input: two strings over the alphabet  $\{A, C, G, T\}$ .  
(portions of one or more genomes)

Problem: figure out how "similar" the two strings are.

Example  
AGGGCT  
AGGCA

Example applications

- ① Extrapolate function of genome substrings
- ② Similar genomes can reflect proximity in evolutionary tree

# Measuring Similarity

Question: what does "similar" mean?

Intuition: AGGGCT, AGGCA are similar because they can be "nicely aligned".

Idea: measure similarity via quality of "best" alignment.

Assumption: have experimentally determined penalties for gaps and the possible matches.

Example

AGGGCT  
AGGCA

AGGGCT  
AGGCA

insert  
are "gap"

one  
mismatch

# Problem Statement

Input: 2 strings over  $\{A, C, G, T\}$ .

- penalty  $\text{pen}_{\text{gap}} \geq 0$  for each gap
- penalty  $\text{pen}_{\text{AT}} \geq 0$  for mismatching A & T
- etc.

Output: alignment of the strings that minimizes the total penalty.

$\Rightarrow$  called the Needleman-Wunsch score [1970]

Small  
NW Score  $\approx$  similar  
strings

# Algorithms Are Fundamental

Note: this measure of genome similarity would be useless without an efficient algorithm to find the best alignment.

Brute-force search: try all possible alignments, remember the best one.

Question: Suppose each string has length 500. Roughly how many possible alignments are there?

Point: need a fast, clever algorithm

Solution: straightforward dynamic programming.

- (A) # of students in this class  $\approx 10^4 - 10^5$
- (B) # people on earth  $\approx 10^9 - 10^{10}$
- (C) # atoms in known universe  $\approx 10^{80}$
- (D) more than any of the above  $\geq 2^{500} \geq 10^{125}$