

## PART 2

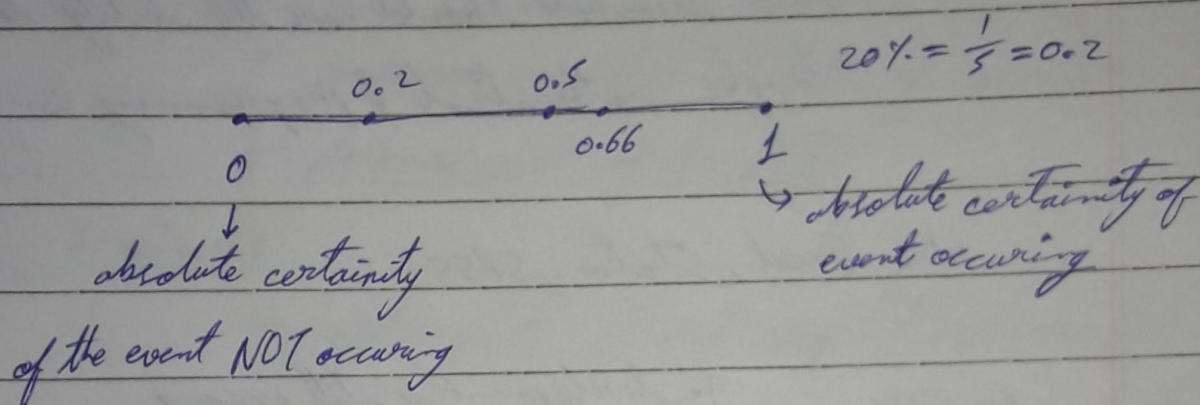
### Probability

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- Prediction of outcome (likelihood of an event occurring)

Event : specific outcome / combination of outcomes



Definition :-

$A \rightarrow$  event

$P(A) \rightarrow$  probability of A

$$P(A) = \frac{\text{preferred (favourable)}}{\text{all (sample space)}}$$

independent events

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

$$\text{Eg : } P(\text{ace of spade}) = P(\text{ace}) \cdot P(\text{spade})$$



## Expected Values

- average outcome we expect if we run an experiment many times.

Ex: flipping a coin

trial: flip & record outcome

experiment  $\rightarrow$  multiple trials

Ex: coin toss  $\times$  20 times = 20 outcomes

= 1 experiment with 20 trials

## Experimental Probabilities vs Theoretical (True) Probabilities

- |   |   |
|---|---|
| <ul style="list-style-type: none"> <li>• Done when true probability is not known.</li> <li>• easy to compute</li> </ul> | <ul style="list-style-type: none"> <li>• approx equal to experimental probability</li> <li>• too many cases/conditions to take care of</li> </ul> |
|---|---|
- $P(A) = \frac{\text{successful trials}}{\text{all trials}}$

Expected value of  $A = E(A) =$  outcome we expect to occur when we run an exp.



## → Categorical Outcomes

$$E(A) = P(A) \cdot n$$

Ex: drawing ~~card~~ spade from 20 trials from a deck of cards

$$P(A) = 0.25$$

$$n = 20$$

$$E(A) = 0.25 \times 20 = 5$$

We expect 5 spades in 20 trials. (no guarantee)

## → Numerical Outcomes



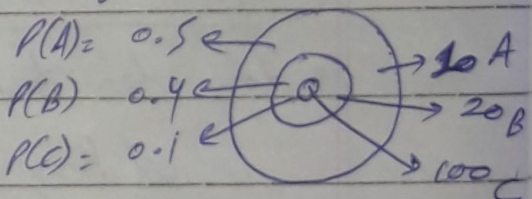
$$E(A) = \sum P(A) \cdot n(A) = \sum x_i \cdot f_i$$

Ex:

$$E(X) = A \cdot P(A) + B \cdot P(B) + C \cdot P(C)$$

$$= 0.5 \times 10 + 0.4 \times 20 + 0.1 \times 100$$

$$= 5 + 8 + 10 = 23$$



- We can use expected values to make predictions about future based on past data.



Frequency

$P(A)$  = sum of top numbers of 2 dice

	1	2	3	4	5	6	
1	2	3	4	5	6	7	→ 6 favourable outcomes
2	3	4	5	6	7	8	
3	4	5	6	7	8	9	possible outcomes = 36
4	5	6	7	8	9	10	
5	6	7	8	9	10	11	
6	7	8	9	10	11	12	

$$P(7) = \frac{6}{36} = \frac{1}{6}$$

$$E(A) = P(2) \cdot 2 + P(3) \cdot 3 + P(4) \cdot 4 + \dots + P(12) \cdot 12 = 7$$

$$P(E(A)) = P(7) = \frac{1}{6}$$

- most probable
- very unlikely

## Probability Frequency Distribution

- a collection of probabilities for each possible outcome

Sum ( $A_i$ )	Frequency ( $f_i$ )	Probability ( $x_i$ )
2	1	$1/36$
3	2	$1/18$
4	3	$1/12$
5	4	$1/9$
6	5	$5/36$
7	6	$1/6$
8	5	$5/36$
9	4	$1/9$
10	3	$1/12$
11	2	$1/18$
12	1	$1/36$

