

CSC 466 Project Report: NFL Projections and Patterns

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Abstract

In our exploration of NFL team performance over a 20-year period, we applied K-Nearest Neighbors, Random Forest, Linear Regression, and K-Means Clustering to predict winning percentages, win-loss records, season point differentials, and to categorize teams by playing style. Our findings indicate that balanced offensive and defensive efforts are crucial for success, with our models showing significant accuracy in predicting team performances. The study emphasizes the effectiveness of data analytics in sports and contributes to the broader understanding of team strategies and their impact on game outcomes.

I. Introduction

In this project, our team embarked on an exploratory journey to analyze and predict various aspects of NFL team performances using historical data from the past 20 years. Our approach combines traditional statistical analysis with modern machine learning techniques, aiming to uncover patterns and relationships within the data. We focus on four key research questions, each addressing a different facet of team performance, from predicting winning records to understanding playing styles. Our methodology is rooted in rigorous data analysis, employing a blend of K-Nearest Neighbors, Random Forests, Linear Regression, and K-Means Clustering to extract meaningful insights from our datasets. This paper presents our findings, offering a comprehensive view of the effectiveness and applicability of these methods in sports analytics.

II. Dataset Description

We are using two primary datasets to obtain data from the NFL. The first dataset is sourced from [Fantasy Data's NFL Team Stats](#), covering offensive and defensive statistics for all 32 NFL teams from 2002 to 2022. This dataset includes comprehensive data on total yards, passing, and rushing for each season. We have manually aggregated these records into two datasets (one for offense and one for defense) for analysis. The second dataset is derived from the [NFL's official standings](#), providing win percentages for every team over the last 20 years. This dataset is crucial for correlating the statistical performances of teams with their overall success in terms of

win-loss records, thus enabling a more nuanced understanding of factors influencing team success in the NFL.

III. Research Questions

To investigate these various techniques to predict NFL season records, we asked the following research questions:

A. Can we predict the winning percentage for each team for a particular season?

We will use K-Nearest Neighbors to predict each team's winning percentage for a particular season. This method leverages similarities in team statistics to forecast outcomes, assuming teams with similar stats have similar records.

B. Can we predict whether or not a team will have a winning record given their statistics?

We will utilize random forests to help predict if a team will have a winning record based on their statistics. This approach uses multiple decision trees to enhance prediction accuracy and manage overfitting.

C. Can we predict a team's net point gains a season, given their statistics for that season?

To predict a team's net point gains a season, including the Super Bowl, we will employ linear regression. This technique models the relationship between team performance statistics and their success in crucial matches.

D. Can we group teams by their playing style, such as defensive or offensive, over the 20 year span?

We will employ K-means clustering to categorize teams into groups based on their playing style (offensive or defensive), by analyzing their statistical patterns over the 20-year span. This method will identify inherent groupings within the data, providing insights into the dominant strategies employed by different teams across seasons.

IV. Methods

A. K-Nearest Neighbors

The K-Nearest Neighbors (KNN) algorithm is a straightforward yet effective method for prediction tasks. It operates on the principle of proximity in feature space, classifying a new data point based on the majority value among its k nearest neighbors. In our experiment, we implemented Euclidean distance as our distance metric to measure the closeness of data points. The primary hyperparameter investigated in this method was the number of neighbors: k .

B. Random Forests

Random Forests are an advanced ensemble learning technique based on decision trees. By building multiple decision trees on different subsets of the dataset and averaging their predictions, Random Forests aim to improve predictive accuracy and control overfitting. In our analysis, the Random Forest classifier was constructed with specific attention to several hyperparameters: the number of trees in the forest, the number of attributes, and the number of data points.

C. Linear Regression

Linear Regression is a foundational statistical method used for modeling the relationship between a dependent variable and independent variables. It predicts the dependent variable's value based on the independent variables by fitting a linear equation to observed data. In our context, we employ it to predict the outcomes of NFL playoff games, including the Super Bowl, based on regular season performance metrics. This technique assumes a linear relationship between the input variables (team performance statistics) and the outcome (playoff results). Our implementation focuses on identifying the most significant predictors and quantifying their impact on the game outcomes. The simplicity and interpretability of Linear Regression make it a valuable tool for our analysis, allowing us to draw direct correlations between team performance and their success in high-stakes games.

D. K-Means Clustering

K-Means Clustering is a partitional algorithm, which means it simply separates the dataset into distinct clusters. In order to be able to use a k-means clustering algorithm the notion of the mean must exist for the domain of each attribute. The algorithm takes as input the dataset and an integer k which is the number of clusters to build. The algorithm has the following four steps: (1) select k initial cluster centroids, (2) on each step, for each data point, compute its distances from each of the cluster centroids and assign it to the closest centroid, (3) recompute cluster centroids, (4) steps 2 and 3 are repeated until the process converges. For our specific implementation, we are utilizing Euclidean distance as our distance measure. Additionally, to select our initial centroid, we are randomly picking k random data points from the data set.

V. Results

A. Can we predict the win percentage for each team for a particular season?

K-Nearest Neighbors is normally a categorical classification technique, and thus has no natural ordering as we would desire for winning percentage. Thus, to determine the effectiveness of our model, we used both mean absolute error and mean squared error to penalize any differences from the actual result. In tuning our k -value, we found that using the 50 nearest neighbors was most effective in predicting closest to the team's actual winning percentage for defensive statistics, and 100 nearest neighbors for offensive statistics.

Figure 1: K-Nearest Neighbors Parameter Tuning Results (Defense)

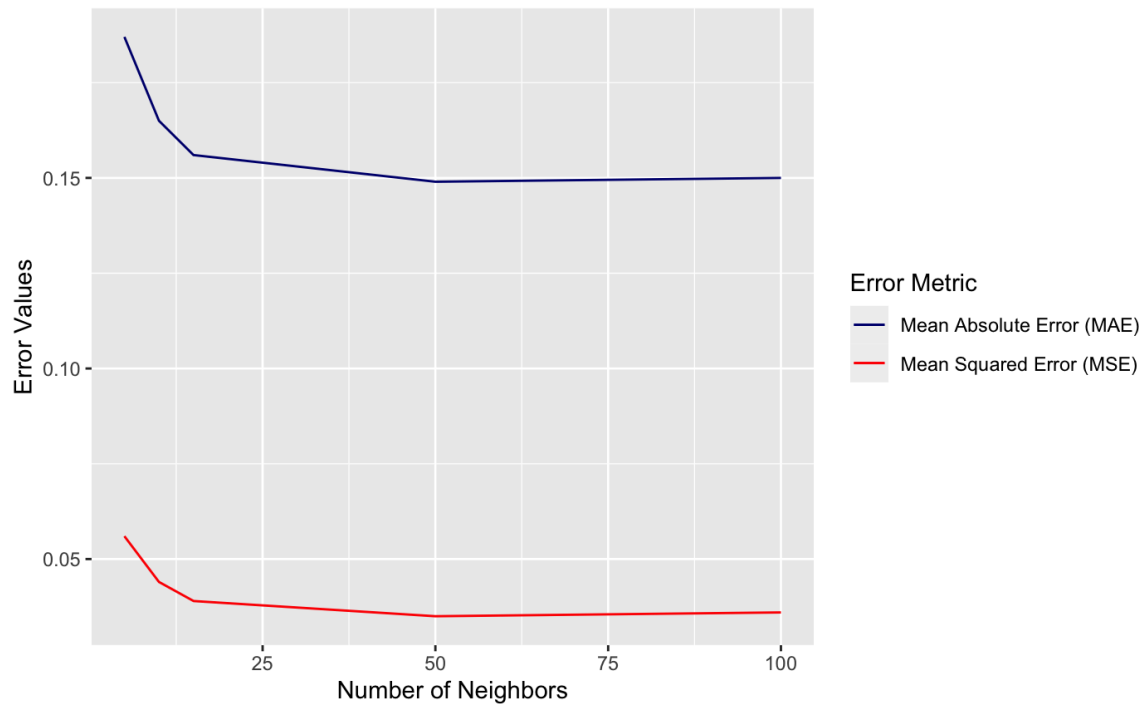
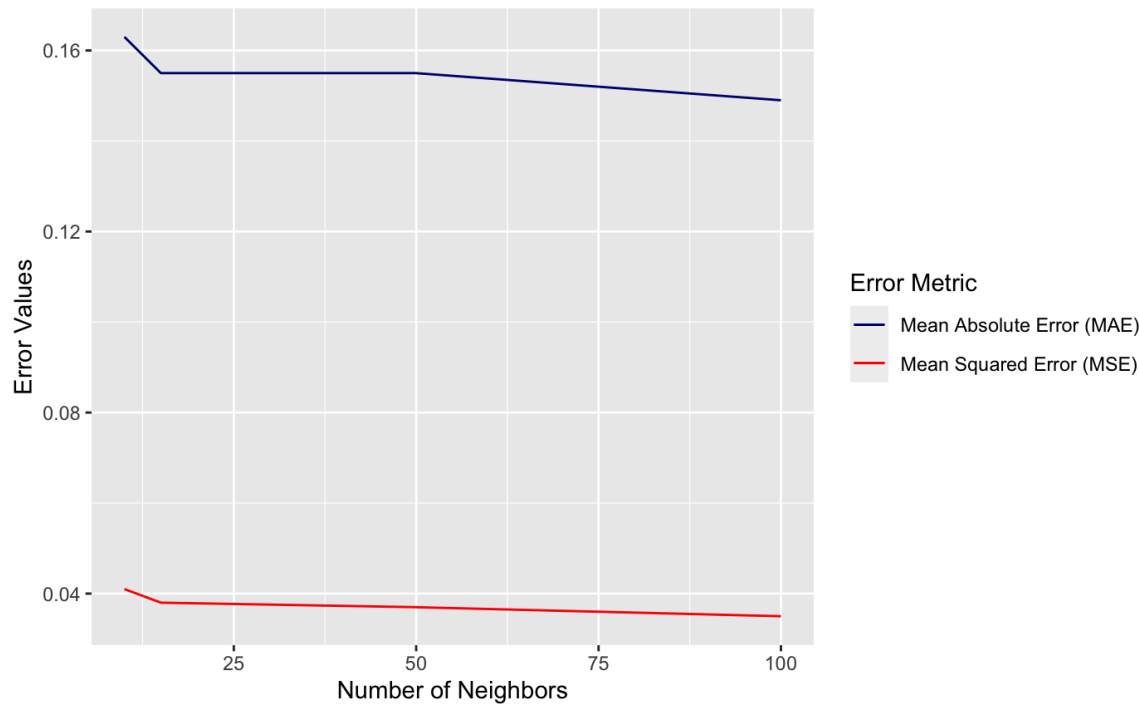


Figure 2: K-Nearest Neighbors Parameter Tuning Results (Offense)



Thus, with a mean absolute error of 0.149 for defense and 0.149 for offense, we can conclude that our model is somewhat effective at predicting the number of wins for a team in a season. On average, our model is 0.15 percentage points off the actual win percentage, which translates to about two and a half games in a seventeen game season. It was interesting to us that both offensive and defensive data were equally good at predicting the outcome of the team's season. This supports the idea that both sides of the ball are just as important as each other, and the best way to win is with a balanced team.

B. Can we predict whether or not a team will have a winning record given their statistics?

We fit a random forest with the combined offensive and defensive statistics, hoping to predict whether that team would have a winning record (1) or a losing record (0). The following table illustrates the confusion matrix results from using 10 columns, 32 rows, and 10 decision trees:

Table 1: Random Forest Confusion Matrix

	Predicted Losing Record	Predicted Winning Record
Actual Losing Record	297	71
Actual Winning Record	141	163

Thus, we were able to predict winning records with an accuracy of 68.5%. It appears that our forest is more likely to predict losing records than winning records. Our precision score is 53.6%, while our recall is 80.7%.

C. Can we predict a team's net point gains a season, given their statistics for that season?

We fit a linear regression model on a team's offensive and defensive statistics. These statistics include the number of plays a team's made, total yards traveled that season, number of yards traveled per play, number of first downs reached, etc. We then used these statistics to try and predict the net point gains of a team per season. Net point gains are defined as the number of points a team scores on offense, subtracted by the number of points that team allowed their opponents to score while on defense.

We used the years 2002 to 2015 as training data, and predicted the results of 2016 to 2022. Our results were measured in R-squared, which measures the percentage of the variation in our results that were explained by the predictors in our model. Our R-squared on this data set was 0.9417. In this case, it means that 94.17% of variation seen in net point gains are explained by the statistics of that team. Which also indicates that our model is very good at predicting net point gains a season for a NFL team.

D. Can we group teams by their playing style, such as defensive or offensive, over the 20 year span?

To try and group teams by similar playing styles, we used k-means with 10 different clusters. For k-means, it is important to standardize the data; however this makes the results quite difficult to interpret.

Our third cluster contained some of the worst teams, with high scores for points scored against them and yards gained against them, and low scores for points scored and yards gained.. These teams also all had very low winning percentages.

Similarly, the fourth cluster contained some of the best teams, with above average defensive statistics and higher points scored on offense. Nearly every single one of these teams had a winning record. Interestingly, there are a mixture of teams that are strong running teams and teams that are better at passing.

The other clusters are all somewhere in the middle, with some clusters favoring running teams, passing teams, and teams that have different defensive strengths. These teams all seem to have a wide range of records.

Overall, the best teams are strong on both offense and defense, while the worst teams are bad on offense and defense. This might sound intuitive, but we thought it was interesting that teams with good offenses and bad defenses and vice versa had such a wide range of outcomes.

VI. Conclusions

Our analysis utilizing a blend of statistical and machine learning techniques on NFL team performance data over the past two decades has yielded insightful results. The application of K-Nearest Neighbors provided a moderate accuracy in predicting a team's winning percentage, underscoring the significance of both offensive and defensive capabilities. Random Forests demonstrated a reasonable level of precision in forecasting winning records, while Linear Regression effectively captured the variance in teams' net point gains. K-Means Clustering revealed distinct groupings based on playing styles, validating the conventional wisdom that balanced teams tend to perform better. Ultimately, our results not only reinforced some existing beliefs about NFL team dynamics but also showcased the power of data-driven approaches in sports analytics.

VII. Appendix

A. K-Nearest Neighbors Results (Defense: k = 50, Offense: k = 100)

Defense MAE: 0.1487715133531158

Defense MSE: 0.03548816913946586

Offense MAE: 0.1489881305637982

Offense MSE: 0.03472488724035609

Defense Confusion Matrix:

	0.438	0.625	0.375	0.250	0.500	0.563	0.688	0.313	0.750	0.813	0.188	...	0.559	0.647	0.353	0.281	0.206	0.938	0.176	0.265	0.000	0.344	0.719
0.438	31.0	8.0	3.0	12.0	2.0	7.0	4.0	7.0	2.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.625	20.0	25.0	4.0	6.0	1.0	6.0	6.0	5.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.375	22.0	11.0	1.0	7.0	4.0	5.0	2.0	4.0	1.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.250	26.0	4.0	2.0	9.0	2.0	2.0	1.0	10.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.500	20.0	16.0	0.0	6.0	2.0	4.0	4.0	3.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.563	12.0	21.0	1.0	1.0	2.0	11.0	1.0	1.0	2.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.688	16.0	21.0	3.0	1.0	0.0	4.0	1.0	2.0	2.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.313	18.0	9.0	2.0	8.0	1.0	5.0	1.0	3.0	1.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.750	9.0	20.0	0.0	1.0	0.0	3.0	4.0	1.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.813	10.0	14.0	0.0	1.0	1.0	3.0	4.0	1.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.188	5.0	1.0	1.0	5.0	1.0	0.0	0.0	3.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.125	2.0	1.0	0.0	6.0	0.0	1.0	0.0	3.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.412	4.0	2.0	1.0	2.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.529	5.0	1.0	1.0	2.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.875	2.0	3.0	0.0	0.0	0.0	1.0	1.0	0.0	1.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.588	1.0	2.0	0.0	2.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.471	3.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.063	3.0	1.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.469	3.0	1.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.706	2.0	0.0	0.0	0.0	0.0	0.0	2.0	1.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.235	2.0	0.0	0.0	0.0	0.0	0.0	0.0	2.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.765	2.0	0.0	1.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.531	1.0	0.0	0.0	0.0	0.0	1.0	0.0	2.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.406	2.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.294	2.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.594	0.0	1.0	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
1.000	0.0	2.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.656	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.824	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.559	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.647	0.0	1.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.353	1.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.281	0.0	0.0	0.0	1.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.206	1.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.938	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.176	0.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.265	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.000	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.344	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.719	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

[40 rows x 40 columns]

Offense Confusion Matrix:

	0.438	0.625	0.375	0.250	0.500	0.563	0.688	0.313	0.750	0.813	0.188	...	0.559	0.647	0.353	0.281	0.206	0.938	0.176	0.265	0.000	0.344	0.719
0.438	21.0	15.0	10.0	5.0	11.0	4.0	0.0	0.0	1.0	9.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.625	9.0	31.0	5.0	2.0	5.0	10.0	0.0	0.0	2.0	9.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.375	22.0	13.0	9.0	0.0	8.0	3.0	0.0	0.0	0.0	2.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.250	29.0	10.0	4.0	3.0	6.0	3.0	0.0	0.0	0.0	1.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.500	6.0	20.0	8.0	1.0	10.0	6.0	1.0	0.0	0.0	3.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.563	12.0	11.0	8.0	0.0	7.0	8.0	2.0	0.0	0.0	3.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.688	8.0	21.0	0.0	1.0	7.0	8.0	0.0	0.0	1.0	4.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.313	20.0	4.0	8.0	3.0	8.0	4.0	0.0	0.0	0.0	1.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.750	3.0	18.0	1.0	0.0	6.0	8.0	0.0	0.0	0.0	5.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.813	2.0	17.0	0.0	0.0	9.0	1.0	0.0	0.0	1.0	4.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.188	8.0	2.0	3.0	2.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.125	3.0	2.0	4.0	3.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.412	2.0	5.0	1.0	0.0	0.0	2.0	0.0	0.0	0.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.529	0.0	1.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	2.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.875	1.0	3.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	3.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.588	0.0	5.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.471	1.0	3.0	0.0	0.0	1.0	0.0	0.0	0.0	1.0	0.0	0.0	...	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
0.063	2.0	0.0	1.0	0.0	0.0	1.0	1.0	0.0	0.0	0.0	0.0	...	0.0										

```

index PTS_x PLAYS_x YDS_x YDS/PLAY_x 1ST DWN_x MADE_3rd_x ATT_3rd_x PCT_3rd_x MADE_rz_x ATT_rz_x PCT_rz_x PEN_x
PEN YDS_x TO DIFF_x TOTAL PTS COMP_x ATT_x PCT_x YDS.1_x YDS/ATT_x YDS/COMP_x TD_x INT_x 1ST_x SACKS_x SACK YDS QB
RATING_x TOTAL PTS_x ATT.1_x YDS.2_x YDS/ATT.1_x TD.1_x 1ST.1_x PTS/G PTS_y PLAYS_y YDS_y YDS/PLAY_y 1ST DWN_y
MADE_3rd_y ATT_3rd_y PCT_3rd_y MADE_rz_y ATT_rz_y PCT_rz_y PEN_y PEN YDS_y TO DIFF_y PTS/G.1 TOTAL PTS_y COMP_y ATT_y
PCT_y YDS.1_y YDS/ATT_y YDS/COMP_y TD_y INT_y 1ST_y SACKS_y QB RATING_y PTS/G.2 TOTAL PTS.1 ATT.1_y YDS.2_y
YDS/ATT.1_y TD.1_y 1ST.1_y win_record predicted
0 2 417.0 1046.0 6020.0 5.8 335.0 90.0 212.0 42.5 33.0 56.0 58.9 111.0
969.0 10.0 417.0 335.0 535.0 62.6 3874.0 7.2 11.6 29.0 17.0 196.0 21.0 131.0
89.0 417.0 490.0 2146.0 4.4 17.0 117.0 16.4 262.0 1003.0 4563.0 4.5 274.0
99.0 230.0 43.0 22.0 40.0 55.0 76.0 617.0 -10.0 16.4 262.0 291.0 548.0
53.1 2740.0 5.0 9.4 18.0 22.0 148.0 41.0 61.0 16.4 262.0 414.0 1823.0
4.4 10.0 94.0 0.0 0.0
1 3 314.0 1002.0 5334.0 5.3 288.0 85.0 214.0 39.7 27.0 44.0 61.4 112.0
920.0 -12.0 314.0 285.0 514.0 55.4 3287.0 6.4 11.5 23.0 24.0 171.0 47.0 298.0
70.0 314.0 441.0 2047.0 4.6 12.0 97.0 25.1 402.0 1038.0 5535.0 5.3 317.0
90.0 215.0 41.9 28.0 60.0 46.7 105.0 931.0 12.0 25.1 402.0 268.0 479.0
55.9 3167.0 6.6 11.8 18.0 12.0 163.0 36.0 78.0 25.1 402.0 523.0 2368.0
4.5 23.0 124.0 1.0 1.0
2 4 354.0 1077.0 5353.0 5.0 316.0 95.0 236.0 40.3 25.0 53.0 47.2 104.0
874.0 1.0 354.0 360.0 573.0 62.8 3591.0 6.3 10.0 16.0 25.0 190.0 33.0 232.0
72.0 354.0 471.0 1762.0 3.7 17.0 95.0 19.8 316.0 947.0 4639.0 4.9 261.0
81.0 215.0 37.7 19.0 38.0 50.0 101.0 846.0 -1.0 19.8 316.0 262.0 479.0
54.7 2847.0 5.9 10.9 20.0 14.0 145.0 41.0 74.0 19.8 316.0 427.0 1792.0
4.2 9.0 90.0 0.0 0.0
3 5 397.0 999.0 5189.0 5.2 303.0 76.0 206.0 36.9 35.0 50.0 70.0 117.0
1053.0 12.0 397.0 281.0 495.0 56.8 3067.0 6.2 10.9 24.0 10.0 160.0 31.0 212.0
83.0 397.0 473.0 2122.0 4.5 20.0 107.0 23.7 379.0 1054.0 5591.0 5.3 355.0
90.0 212.0 42.5 31.0 58.0 53.4 112.0 1031.0 -12.0 23.7 379.0 377.0 612.0
61.6 3995.0 6.5 10.6 24.0 15.0 218.0 54.0 83.0 23.7 379.0 388.0 1596.0
4.1 17.0 90.0 0.0 0.0

```

Confusion Matrix:

```

                Predicted: 0.0 Predicted: 1.0
Actual: 0.0          297.0          71.0
Actual: 1.0          141.0          163.0

```

Overall accuracy: 0.6845238095238095

C. Linear Regression Results

R Squared: 0.9417206692058959

D. K-Means Clustering Results (k = 10)

Cluster 0:

Center:

```

0.358356509432697,0.595668460650839,0.15013299951053966,-0.1564688571445403,0.11419208413109706,0.45479671552919443,0.74601664161
12265,0.08513611371402822,0.08967469747471316,0.4256604563310005,-0.23546028311813014,0.08809916062265644,0.0032813172209569747,0
.6397997031501466,0.358356509432697,-0.24737619047370993,-0.327580813120686,-0.022943470679111105,-0.12276127587270996,0.11979979
049707726,0.15534278776826452,0.04440958633712967,-0.18764637379755603,-0.19753042297965315,-0.4709696158958576,-0.52531829984893
42,0.10975714193383837,0.358356509432697,1.0169722208848655,0.4362619883678263,-0.300027790210843,0.20476608281008868,0.381683907
7924927,-1.0034376457625565,-1.213660366736994,-1.2303884346481548,-1.1147148753031144,-1.3848843513323577,-1.1691078429983792,-1
.4017349944906101,-1.185557082622624,0.033040507834411786,-1.2876574832224537,-1.165152711185518,-1.2483989324245743,-0.773268808
1249878,0.3176916273112445,0.269653618396751,-0.6402706810593908,-1.213660366736994,-1.2303884346481548,-0.716655122816375,-0.36
414848377775466,-0.9643334388833895,-0.9445640238198401,-1.0820074557993737,-0.7099312256474676,-0.8482591090011841,0.56436871351
2296,-0.9743010527210394,0.7482597920609501,-1.080502154800067,-1.213660366736994,-1.2303884346481548,-0.8025392660907609,-0.8309
47232634985,-0.6097932743355229,-0.9196503579024058,-0.9935237675359513,-1.0034376457625565,

```

Max Dist. to Center: 9.97049336031924

Min Dist. to Center: 3.57177395974901

Avg Dist. to Center: 6.3980576132342435

SSE: 3096.049595834937

73 Points:

```

-0.9552099806941335,0.05802129976028349,-1.5031182630711257,-1.9897691404538795,-1.349191013098896,-0.575676553017995,1.700524225
2438073,-1.45972951350144,-0.9775134029976976,-1.4529684516253778,-0.04026420527704914,-0.2769206099322542,-0.5492619789070928,0.
7481949621742967,-0.9552099806941335,-1.1531679814788443,-0.513152980150352,-1.475074279936071,-1.4001453058526796,-1.48797407978

```


21137,-0.6159362074766496,-0.9807025964611038,0.4597870932379638,-1.401294532307948,1.8492934424124359,1.5770644653757366,-1.3493386412897814,-0.9552099806941335,0.2393069708865626,-0.6262408667626079,-1.1989376870546198,-0.3196570672366678,-0.24141860864397666,-0.3271796887724092,-1.3788900242810844,-1.3890780040231523,-1.1824563895634708,-1.8538400635565617,-1.651350163337201,-1.9486806117420385,-1.6251911428920855,0.8336207560336855,-2.0350531018294804,-1.0688442394627584,-1.2216028095604419,-0.5964114574364595,-0.48155708460317076,-0.46107811401312393,-0.7486918032525143,-1.3788900242810844,-1.3890780040231523,-1.6160450793471166,-1.3156276819485897,-1.52938288351827,-1.4652143827923398,-1.0286687992407166,-0.09185338336296689,-1.1286764182882454,1.4982998702852188,-1.6923205204954015,0.6652146647332837,-1.7311698438191165,-1.3788900242810844,-1.3890780040231523,0.28956805612004916,-0.7507689143779664,-1.5801428081393556,-0.48605034755815113,-0.8402412042351344,-0.3271796887724092,0.3694325096185529,1.4336442656314092,0.3015803845982011,-0.3316869373192379,0.4706347692005664,0.234278209877777,1.3845194469890298,-0.46643567413390036,-0.055563919749342744,1.390648915177585,-1.2204601946649298,0.9540292141401482,0.6439623200979706,0.7481949621742967,0.3694325096185529,-0.05460879191328175,0.03574362411081555,-0.1418355615973127,-0.16425095633902387,-0.17660544815774576,-0.24953685832559452,0.09089438698907822,-1.2058567162278668,-0.0500677770906411,-0.22822925265292648,0.19322900848890948,0.3967923779778291,0.3694325096185529,1.4643919603522029,0.759158409631813,-0.2513503589738161,-0.10697434527326101,0.5776657316896775,-1.3151469233618047,-1.0407096971581322,-1.0680662124802351,-1.002996007026962,-1.6709333917426705,-1.651350163337201,-1.3790342684827688,-1.016375411733021,-0.17899435988173246,-1.0126697619259595,-0.557533807771017,-1.112929644611459,0.4308323262929295,-0.4200115614283266,0.07912569329462495,-0.7486918032525143,-1.0407096971581322,-1.0680662124802351,-0.5332717324901753,-0.03835102090315075,-1.046808622445695,-0.8887318656838588,-1.288250261159516,-0.9658423903705896,-0.1982008011084509,0.6668733526702998,-0.9594605287670406,0.6652146647332837,-0.9022214791002577,-1.0407096971581322,-1.0680662124802351,-1.0672684176210738,-1.4544103303384686,-1.5801428081393556,-1.0686172326219043,-0.9849346583854746,-1.3151469233618047,-0.49072495162345126,1.2831855037392548,-0.33570382536003,-1.0422935958055124,-0.7106556508885584,0.9429886274115775,2.648538560081393,-0.3695289580980432,-0.8238551557896385,-0.16041510307857648,-1.1459215005983268,1.1712556536823369,0.4333933261559006,0.42740358749471735,-0.49072495162345126,-0.0807649630934142,0.6285519567128766,-0.9260936312083468,-0.35067077442208927,-0.9962108429229759,-0.4938030910929631,-0.2663046074943158,0.8761980456044215,-0.36535401997467937,-1.5725086435775728,-1.7013076289156752,-0.9384842838150494,-0.49072495162345126,0.9612320524046748,-0.08583689370095432,-0.9620408550344194,-0.7450225111634814,-0.514446722088528,-0.9840727968770605,-1.9425239028193384,-1.9613164150344395,-1.4217368996121493,-1.702743247710304,-1.4535766274679096,-1.9745736273447325,-2.842822605210215,-0.3236536621553636,-2.939469133282596,-2.2192927107691762,-2.6343539538972194,-1.7870803844046155,0.19544367032011556,0.8313082097990854,-0.42782388757286527,-1.9425239028193384,-1.9613164150344395,-1.6751054437211317,-1.2024512689445637,-1.8740787842843947,-1.5830945613607408,-1.288250261159516,-0.3103506351148721,-1.2616015064567874,0.2511600938628403,-1.8197744321003337,1.5978753254901514,-1.4824853344034588,-1.9425239028193384,-1.9613164150344395,-0.27254991157270175,-0.2622905760252213,-0.2265979170371948,-1.262806194309822,-0.5990854473179009,-0.9840727968770605,

...

Cluster 1:

Center:

0.8797926032888087,0.056694502918201016,0.8617889231455546,1.0456617711047758,0.7765010908519381,0.2792756967053199,-0.6256220591316367,0.6770037561287021,0.7848139014009068,0.500232750675664,0.7126379535150379,0.19954725951625016,0.3249796603219862,0.34951596977416105,0.87797926032888087,0.5950975835734648,0.28078191065506025,0.7030976179260146,0.9250590551940598,0.928344047007231,0.5360354087842789,0.8648255417030987,-0.5503950319473316,0.81182583204349,-0.3896634780501624,-0.34309875456378947,0.9636192230124131,0.87797926032888087,-0.1523097084475303,0.18499182396211755,0.4739633983226034,0.38928533930802145,0.22508868642671362,-0.2528291206847124,0.41638825550742686,0.40845018136370365,0.5107240097316018,0.7338328122697215,0.6315912692280847,0.7988560438771662,0.41815336574230566,-0.24150146580243725,0.562412263865578,0.48875883485745375,0.43801083293204995,0.43429105595935846,0.1187017216700012,0.0868923365626846,-0.34991768582348554,0.41638825550742686,0.40845018136370365,1.088822390275981,0.9948079098002705,0.6885862952385723,1.0558823975118283,0.5544576475233172,0.20487127950999223,0.6814022514636299,0.05100185814073013,1.0998642467015418,-0.009525023172302177,0.5550902139363533,0.41638825550742686,0.40845018136370365,-0.6941982125836116,-0.5596923274400136,-0.19317705552849873,-0.13842813219089095,-0.3329209452388803,-0.2528291206847124,

Max Dist. to Center: 9.155984869336432

Min Dist. to Center: 4.3389087617521165

Avg Dist. to Center: 6.404187210706673

SSE: 3435.803634940949

81 Points:

0.6790891956656744,-0.43634320359965234,-0.4823355904831628,-0.3316869373192379,-0.32753443356235573,-0.6769208983799666,-0.5115092225396338,-0.4906623531428651,1.1737020579151305,-0.031159768223896364,1.972280534521232,1.0988468405016072,1.5642268121410916,1.282847253306929,0.6790891956656744,-1.4670420356404337,-1.105961312752413,-1.292080730360164,-1.229835842418768,-0.6683686850168835,0.2389956072091449,0.09089438698907822,-0.9976512400446381,-0.7169000731050634,-0.7170581220800706,-0.4657402566952939,-0.11677556886558572,0.6790891956656744,0.7862199105098824,0.9098164869702134,0.6962369691069897,1.3818047084705865,0.4138488636229467,-0.0013607071525021546,0.3345569664752061,0.29972316018089057,0.6919076058178439,0.23129599512179708,-0.06916187638286442,1.0808022137731683,0.6361244299844399,-0.034335057608101335,0.6978562106049334,0.46508705561246566,0.8431873244702331,-0.0477698930491725,0.6262623325440251,1.2210755138059421,-1.2834716627185958,0.3345569664752061,0.29972316018089057,0.7857430718628258,1.0772450501365365,-0.012720920147320664,0.6356364708719008,-0.12013368252491981,-0.09185338336296689,0.06764937522863321,0.4330346445911049,1.0160751011094102,1.5978753254901514,-0.07327311438139895,0.3345569664752061,0.29972316018089057,-0.9509681484432633,-0.7216928228093507,-0.2265979170371948,0.6790834225693554,-0.4543919931675609,-0.0013607071525021546,1.3328088662095976,-1.2746134484273695,1.1118148816247462,2.273870810463769,0.43870800109004954,-1.183142625189824,-2.170534308377215,-0.12726216800839948,1.0200438107070713,0.48586157119482415,1.1026624370775304,1.0988468405016072,0.8155370559026203,0.6412645039477702,1.3328088662095976,-0.6562007290563279,-0.513152980150352,-0.5078226607491301,1.3846445692153342,2.44613181509099,3.4144566331849475,1.5196903649226543,-0.37303481149495155,0.17513668211224337,0.5050140514877897,0.1602805452296993,1.2185010929272928,1.3328088662095976,-0.8763954374906451,-0.03343408419194549,0.9331338011271901,0.9564392645437729,-0.1322073632661561,-0.3271796887724092,1.8000050506746654,1.751254739331473,1.3898090934598228,1.9872000445351519,1.5130264105714721,2.1942018846890137,0.7230981058643062,-1.408598429207597,1.6219334601331172,1.615535269188838,0.951860489419216,1.6331744744352825,0.9339899484182461,0.7560899581486393,-0.6417358313592979,1.8000050506746654,1.751254739331473,0.6479355549901242,0.25267404110720243,0.9983870554333116,1.2993180241816649,1.6969365509066738,1.3283787530244227,0.4664246397342594,0.45901672326657006,1.3347098801217412,-0.4539781281749577,0.7556752503374599,1.8000050506746654,1.751254739331473,1.1424366967573265,1.293280322895723,0.9013561588812732,3.3977288620202037,1.8607032732378805,-0.3271796887724092,0.6446828972159943,-0.027955135606661873,0.8580291342962435,1.089526379653311,1.1730236676319379,0.7404999366876346,-1.301521168176577,1.6897387576639284,1.4810185523312487,1.6491595848869454,0.5684684629335427,0.5919851482365004,0.9481175335698496,-0.10724870363791493,0.6446828972159943,0.023859721627115568,-0.030123968400524552,0.09344185928599714,0.6780904438881605,0.9708421045135768,0.9717943055112529,1.1624913704392603,-0.7894457638614093,1.5263634373295503,0.2605996167742176,-0.10330716084398205,1.013073914189927,0.6446828972159943,-0.045087763490381315,0.529889611802989494,0.9331338011271901,0.3183910986535526,0.5776657316869775,-0.

0013607071525021546,0.6952826487396887,0.6626060549685362,-0.6839553269620573,1.4209846083112803,2.10634701817935,0.9772301513623
92,-1.6798085405428362,-1.263939126933966,2.6246555819615702,0.7207422714583364,0.8431873244702331,0.3607929740477437,0.9339899484
182461,0.2158861508408905,0.10695597189321632,0.6952826487396887,0.6626060549685362,0.8448034362368407,0.10716151010202585,1.6418
194035300773,1.4769456905176113,2.086308743784871,1.3283787530244227,2.061525697756764,-0.5802664237520788,1.239119446418042,0.85
17467968846573,1.999097797415748,0.6952826487396887,0.6626060549685362,-0.9703515266395649,-0.06166554420177242,1.126946974064968
,-1.0686172326219043,-0.06854278209998732,-0.0013607071525021546,

...

Cluster 2:

Center:

-0.33540509005060937,0.4286411479313658,-0.03795540412922901,-0.27754547762504594,-0.03472036032018661,0.06650186613508137,0.5550
069040702394,-0.23316736481901487,-0.3343438825411072,-0.112405978703981,-0.37107402846787735,0.1689107969376663,-0.0164890005838
23576,-0.20195853806712408,-0.33540509005060937,0.364263606557125,0.5479425696870938,-0.05780791128184566,0.20408435618030268,-0.
21875658274567192,-0.2111521646050079,-0.1642477519276318,0.3794792667101469,0.23433328281700158,0.14013821680824282,0.0837930412
351043,-0.285519322828422,-0.33540509005060937,-0.13478148621146235,-0.35655355068231603,-0.454404786419702,-0.42903675281784837,
-0.31084575749130544,0.0005161302992253686,-0.18978357881638047,-0.1835890029868308,-0.37061180189831167,-0.3212866456873747,-0.1
9065133413114357,-0.4110053851649061,-0.43613674550591264,-0.09736518217018347,-0.4267654632889406,-0.2635303095482658,-0.3134056
4534394205,-0.05810903499203305,-0.08502807100524591,-0.0913364484326846,0.2016884041414936,-0.18978357881638047,-0.1835890029868
308,-0.8184489204675619,-0.7964020157586896,-0.4966083084609094,-0.6965710266476984,-0.27773671297561914,0.06421608217410915,-0.5
229178022058895,-0.013114763521901872,-0.7327746431268397,0.06298235235884904,-0.4060366722185408,-0.18978357881638047,-0.1835890
029868308,0.5814263506757928,0.6668982359604002,0.4952926915506254,0.32122090745876414,0.41859184687282425,0.0005161302992253686,

Max Dist. to Center: 8.615853422347058

Min Dist. to Center: 4.359115752421403

Avg Dist. to Center: 6.222380089866412

SSE: 2779.383217238254

70 Points:

-0.06064622100244917,1.2401972860557822,-0.17403290483965278,-0.8054247096434215,0.08751355187436377,1.246721663497492,1.85852661
43711958,0.33304473316192323,-0.3628804141654611,0.356606236340144,-0.8601898400096814,0.15753226915212312,0.16823237082144207,0.
10661221281513798,-0.06064622100244917,0.5992954875900293,0.6065960925424299,0.276435408861904,-0.023860722967826466,-0.504447606
0638381,-0.8602024402440183,-1.3379015909444978,2.1254309027037945,0.17513668211224337,-0.47264368736649853,-0.13625562410319222,
-1.2466250519210984,-0.06064622100244917,0.7424668750361844,-0.2692467269824852,-1.1989376870546198,0.7437565425803662,-0.2414186
0864397666,-0.3271796887724092,-0.5447118840444692,-0.5795700079584045,-1.441676942116206,-1.2828531489375452,-0.8602560198600319
,-1.3531412528800748,-0.14663865293435743,0.18265389580234537,-0.24588225699831692,-1.0688442394627584,-1.3302759745094248,-0.444
6595353718909,-0.05073842237926128,-0.043958718497014035,-0.10695597189321632,-0.5447118840444692,-0.5795700079584045,-1.47823756
2474415,-1.0731067969399621,-1.5983220636714943,-1.2181504468887052,-0.8988780682813164,0.23589249426489284,-0.46405097744553503,
-0.16455316494461927,-1.3099587856806045,0.38541646650622335,-0.8193266426283718,-0.5447118840444692,-0.5795700079584045,-0.19501
639878749472,-0.15180142806448135,-0.001007101853500006,-0.8744282709339867,-0.4543919931675609,-0.3271796887724092,
-0.7315690407712124,0.48790347659501027,-0.20787100448345266,-0.5685558234813307,0.3429276967584989,0.031789519153834,-0.03750205
5157467885,0.06655126406331653,-0.2092221669574019,0.356606236340144,-0.6241506421321054,-0.42173823629371326,-1.0561873346935577
,-1.2834837441297058,-0.7315690407712124,-0.603888386696063,-0.5790205726616922,-0.324829111732214,-0.7764444330068683,-0.504447
6060638381,-0.3716699747092788,-0.8021030992194068,-0.16482933531172272,0.08505489843108958,-0.10602203529614046,-0.2680494771400
329,-0.4249163369716346,-0.7315690407712124,1.092491158825769,0.74372825316602478,0.22244330506658685,0.10570837669014578,0.686876
9770674981,-0.6582538152571534,-0.38689439805375836,-0.41208559497949115,-1.2023964320675273,-0.9456686756806327,-0.4647089481214
49,-0.9906390344423578,-0.106375411733021,-0.3959833132921792,-0.9143636715506208,0.08160423184365968,0.08247516982735287,0.12732
84785637916,-0.7892847004773919,-1.1448804017444516,1.2834716627185958,-0.38689439805375836,-0.41208559497949115,-1.3601168337263
851,-1.3479637999497402,-0.8399910819860205,-1.3554081890573912,-0.7690873373219174,-0.4195992609908247,-0.7299011537826191,-1.20
38363119632682,-0.9594605287670406,0.4786825325819101,-0.32195762379750566,-0.38689439805375836,-0.41208559497949115,0.3477181907
0895443,0.7117584915234074,0.9013561588812732,1.067461345945191,0.2690752775841395,-0.6582538152571534,
0.1629947189204719,0.788821000379319,1.106175198350776,0.8526574934912202,0.4067812329795326,0.031789519153834,0.4365051122246980
7,-0.109994220503529192,0.2517525746667756,-0.16041510307857648,0.6305840413223786,0.08512345597139356,0.012255338271760563,-0.321
109620090679,0.1629947189204719,0.9916380552920159,1.3530954743376178,0.015016052324892622,1.596380658889927,0.8069210255605298,
0.9717943055112529,0.44809338147247224,0.4597870932379638,0.8507500597208968,0.2605996167742176,-0.1527298557327973,0.19136519924
04632,0.1629947189204719,-0.5920007069116074,-0.3445757656516854,-0.014453526953613549,0.3183910986535526,-0.45984109939961776,-0.
0013607071525021546,-0.31925833262916775,-0.34230042290494395,0.1734665007123739,-0.191775089247725,-0.26693541225215583,-0.0067
04441539982867,-0.40755968057395653,-0.17899435988173246,-0.36384956544872354,0.33725944768953037,-0.13487116007061292,0.86274163
93382412,-0.1122839455541055,-0.3243176564668584,0.32086791567964895,-0.31925833262916775,-0.34230042290494395,-0.257656698744772
15,-0.11919131590602663,-0.33443709419570344,-0.6675046812472708,-0.8988780682813164,-0.9658423903705896,-0.8628262419511612,0.25
11600938628403,-0.6408257497547099,-1.200106656780452,-0.736431806156486,-0.31925833262916775,-0.34230042290494395,0.560935350868
2737,0.8513237310527632,0.9013561588812732,1.067461345945191,0.8478490941854998,-0.0013607071525021546,

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Cluster 3:

Center:

-0.9273572629015353,-0.2459668110014162,-0.4438425141687873,-0.3768048203977317,-0.19678671653833424,-0.43104177392946436,-0.2857
9152378622147,-0.3522241873773539,-0.44336806746492063,-0.369685645224249,-0.29464228820275734,-0.10796671251055187,-0.0672186735
5117242,-0.8863134707168934,-0.9273572629015353,0.6304337866139965,0.7404232122480097,0.15319485506588487,-0.010651191105203845,
-0.6527571536880222,-0.889281753668705,-0.4278946288082322,0.14252160572066272,0.21588796520609868,0.848381383473313,0.906327891
8846723,-0.3222027476029517,-0.9273572629015353,-1.1399553892726835,-0.7717522395956591,-0.08213833610224282,-0.5525952865299228,-
0.6444601094430763,1.0193886215937351,1.2578429389378694,1.2707339830467335,0.15637503570889683,0.7974356935933649,0.90087022811
89022,0.8009110451154752,0.6609740516644016,-0.53719834646460572,0.9993282210893052,1.3720543689704354,1.0501838291349623,1.138452
0911478606,-0.182621686325356,-0.12341003192865402,0.886206624258078,1.2578429389378694,1.2707339830467335,-0.38796448680807505,-
0.9314438037920657,0.768589788255895,-0.004130708312144995,1.0232608521174094,0.7561240460551445,0.5677008973864818,-1.085061095
1611368,-0.09459470001928558,-0.6493927428097299,1.1622546863662333,1.2578429389378694,1.2707339830467335,1.403650793402726,1.465
2446358872508,0.8906137391106219,1.7887346322145998,1.5873934153983493,1.0193886215937351,

Max Dist. to Center: 8.031241599192779
 Min Dist. to Center: 4.174703859274756
 Avg Dist. to Center: 6.1714447352404935
 SSE: 819.9968852021509

21 Points:

-0.7659753392208926,-0.608296074333543,-0.16087364386706396,0.14205083500494575,0.2152206243164313,-1.3856313159137672,-1.3015211
 68176577,-0.9025158962952584,-0.055563919749342744,0.48586157119482415,-0.5123426010322011,0.5195763350557708,0.682956578235391,-
 1.6042751188092852,-0.7659753392208926,0.9131695417516186,1.3530954743376178,-0.11569362594361306,1.0394226838763243,0.1512367097
 483466,0.2389956072091449,-0.8021030992194068,1.709019950337337,0.6255456005180123,-0.9614725567936426,-1.61893647076765,-0.83577
 06944463665,-0.7659753392208926,-1.795209182438305,-1.759451622394924,-1.1989376870546198,0.3183910986535526,-1.1151085716665412,
 1.3124255090568004,1.2814618824194721,1.2348444659798234,-0.4646148594174354,0.15336184800109565,0.5241587312250116,0.38169079250
 042826,1.2449401611435045,-0.3236536621553636,1.5039661516827105,2.126845958610625,1.3865531492151475,1.8666389699192347,0.380080
 2398446482,0.154343945045071,1.6043395783982448,1.2814618824194721,1.2348444659798234,-0.9663810712329519,-1.5419805079566422,0.5
 387925210784786,-0.3946039938765893,1.177736270690753,1.1098815012725156,0.7322748160713435,-1.4116929413669979,-0.8320066171621
 083,-1.4799048550075122,1.4188339421125469,1.2814618824194721,1.2348444659798234,1.7045546644500773,0.990888970582119,-0.00100710
 1853500006,2.0384061543847793,1.5230852135537536,1.3124255090568004,
 -1.901383188060338,-1.425072210319524,-1.0011864516880942,-0.3316869373192379,-1.41304454931993,-0.6769208983799666,-0.4325080279
 759395,-0.5391157111607928,-1.284829897413816,-1.4529684516253778,-0.6738431048431739,1.2436644668630663,0.035651893154212785,-1.
 2834837441297058,-1.901383188060338,0.1546405775277777,-0.7985792143661591,1.4789644489321583,-1.0365115866289225,-0.66836868501
 68835,-1.837267371313497,-1.159302093702801,0.6679925694211927,-1.040967397583333,1.1160501382717198,1.280528296042845,-0.4249163
 369716346,-1.901383188060338,-0.854518919753796,-0.2692467269824852,0.4593401370867894,-0.9577052331268882,-0.45984109939961776,1.
 .9693186171614518,1.1687351067118212,1.1371452250754572,-0.38485468940120926,0.5621184971851828,0.9197058029635962,1.287946338594
 721,0.7230981058643062,-1.8425763360284904,1.916851731259133,1.2320527031500776,1.1692068193171818,0.8043755154672532,-0.48155708
 460317076,-1.1106902873578852,1.2834716627185958,1.1687351067118212,1.1371452250754572,0.195139428122676,-0.49105667291925575,1.3
 201032294816961,0.7987309645076336,1.826727281866073,1.21913012714847,0.9981249924084276,-0.7881230531558086,0.9842116232081772,-
 1.573170921083199,1.5846236150563187,1.1687351067118212,1.1371452250754572,0.541551972671972,-0.41057864302516184,-1.128961177771
 968,0.873272384257273,0.7996179428020531,1.9693186171614518,
 -1.488507606664176,0.4664093677532739,-0.7079229214418287,-1.0422935958055124,-0.5829485784464908,0.639255591325663,1.70052422524
 38073,-0.22416888404425664,-1.284829897413816,-0.41892577278793675,-1.7049617060978492,1.5332997195859845,0.441192177833847,-1.0
 69622827676653,-1.488507606664176,-0.15923347663381152,0.5626843642015364,-0.9783775025157497,-0.09750805850681526,-0.66836868501
 68835,0.11686249082546059,-0.9807025964611038,0.251581617054735,0.35530024947455097,1.604879007698864,1.0169405899691637,-0.93848
 42838150494,-1.488507606664176,-0.373235529543117,-1.0945909767493742,-1.4358345190748212,-1.8084361209805153,-1.1697141943554514
 ,1.6434996355415443,1.3490979478440626,1.31858667246928,0.013946160679921576,0.7466156617974555,0.9197058029635962,1.2361603073389
 3328,-0.5815070323336893,-1.4809280803444127,0.12768088642796963,1.9990183506876897,1.060533654368199,2.08843024062899,-0.4815570
 8460317076,-0.043958718497014035,1.0695597189321633,1.3490979478440626,1.31858667246928,-0.5923320968641904,-1.153947091942838,0.
 7226303348204112,-0.2315095002408565,0.918192165150276,0.6728869977687052,0.20057446339717527,-0.9959796825595384,0.1876246756773
 5028,-0.9203084585533916,0.9214649232812315,1.3490979478440626,1.31858667246928,1.5882543952722668,1.7817586612484682,1.126946974
 064968,3.009350962824368,2.053627878771667,1.6434996355415443,

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Cluster 4:

Center:

0.3044906212947816,1.0338538411751135,1.014389353066969,0.6453972180993898,1.223308327406002,0.38361361928668497,-0.1816792352362
 1005,0.5377601707876729,0.7012029477503485,0.39861422016791503,0.7166141173909159,-0.02711020445873724,0.017714534410999416,-1.00
 01180298294108,0.3044906212947816,1.281317651119826,1.2894234682433223,0.5633431526612747,1.2161187521890076,0.38072622028261077
 ,0.028315981447288217,0.6043679415589571,0.34527408133718795,1.333813624711084,0.12311649724783331,0.2257656159573796,0.330028544
 88818517,0.3044906212947816,-0.2545554208207109,0.03665467352635379,0.370503825079213,0.20141560157367885,0.4561682212068522,0.80
 26764571675908,1.3457161445728332,1.4232644305811009,0.44963608939355704,1.2574819486376454,1.3103085363054485,1.1785483476733385
 ,0.21430210196708796,-0.8480436328972765,0.6904832538267831,1.3726630718653066,1.1474721863273853,1.0398828252866896,-0.352311485
 9359979,-0.2485865531006138,1.0000383372015726,1.3457161445728332,1.4232644305811009,0.5204636018828752,0.14717745612844943,0.896
 1272715393612,0.9355042675863124,1.23942422427479,0.929621268577194,1.3370839672382098,-0.944015525208606,0.8432157334952208,-0.3
 257372873208884,1.4022549748181696,1.3457161445728332,1.4232644305811009,0.32833481251265273,0.6143535847685445,0.703964195595541
 9,0.7713231793711162,0.7767081458949161,0.8026764571675908,

Max Dist. to Center: 9.295953448044502

Min Dist. to Center: 4.685853084715728

Avg Dist. to Center: 6.6170199616990475

SSE: 1807.3062574285868

40 Points:

0.7134954941153546,1.3261737214227276,1.5084726052270634,1.089526379653311,1.7157787255107249,0.43676690060172,-0.590510417103328
 2,0.8418049923501754,0.5590690690828939,1.2613935803229048,-0.3011496345101589,-0.13210298357079509,-0.19831365567030945,-1.71120
 55770358117,0.7134954941153546,1.7240108483357242,1.550698251871638,0.9561257358581357,1.3340120260322794,0.31515778870139205,-0.
 3716699747092788,0.6266928787141692,0.6679925694211927,1.8416496802135884,-0.3504364700097125,-0.41631756180647866,0.294078788609
 14616,0.7134954941153546,-0.1325938344377775,0.7296818292829956,1.4069274651675931,1.1691219865071798,1.1237219585787803,-0.00136
 07071525021546,1.574551499259364,1.5279421886929219,-1.08275617770431882,0.8818075496598968,1.7107999464407653,0.7700860265408394,
 -0.4945333564538229,-1.9872356383021217,0.5209052479293241,1.8711907427647543,1.4952263141641304,1.3763635294029348,-1.6509220249
 252108,-1.0423100585847525,1.71129550291461,1.574551499259364,1.5279421886929219,-0.8876339187342652,-1.1054429149411125,-0.1046
 3982701828695,0.033317202296372916,1.3075643580284744,1.8746218824041876,0.4664246397342594,-0.37240979434834903,-0.2266005370386
 7977,-1.0135745246290784,0.672780413865574,1.574551499259364,1.5279421886929219,0.48340183808306675,1.5520575378564037,2.02931023
 4799741,2.426784077760615,1.957165576004774,-0.0013607071525021546,
 -0.11225566867696943,0.48790347659501027,0.9087862837619434,0.8526574934912202,0.5664150735321171,0.8417442820490606,0.35750391766
 100376,0.7206715973053536,-0.8238551557896385,-0.548181076426168,-0.785651145943079,1.0264380273208777,0.19162892570389422,-2.03
 1996951715391,-0.11225566867696943,0.703920172310559,0.2553022658152826,0.9561257358581357,0.6688845269457869,0.6429999466074844,
 -0.005270625558225895,0.44809338147247224,0.8761980456044215,1.0309136270832044,0.9938429209149338,1.642961391894157,0.2940787886

0914616,-0.11225566867696943,0.06429482519386391,0.631426561453604,0.9331338011271901,-0.3196570672366678,0.19542637286730558,1.3124255090568004,2.3410935740713894,2.2955790815129413,-1.0229360495310185,1.6372916288911863,2.699667625787226,1.702234588237826,-1.1033490876128875,-3.5061583121752484,0.7371786467550694,1.8711907427647543,1.8212458090110792,1.0378400109512054,0.19544367032011556,-0.3516697479761115,2.03216346597111,2.3410935740713894,2.2955790815129413,0.31326015687070596,-0.29703996491235357,1.228184322610728,1.6497289659534866,2.86505312954127,2.639362263535858,3.6566267557792687,-0.9959796825595384,1.653344659134072,-2.13276731753732,2.9109409986064927,2.3410935740713894,2.2955790815129413,-0.19501639878749472,0.022655121347213352,0.22458371333019278,-0.6802393092460689,-0.2614673876337741,1.3124255090568004,-0.18106826557632977,0.4664093677532739,0.28842112362561223,0.14205083500494575,0.8218292184162521,0.1330338645158055,-0.4325080279759395,0.4057247701888174,0.09809432745871641,0.356606236340144,-0.1644953620547208,-1.7250968735468453,-1.1263769993409145,-0.4280400783174943,-0.18106826557632977,1.9332602177767837,1.3091837459967244,1.609674127200664,0.8207821564949513,-0.17660544815774576,-1.3487349057787577,0.26949388423077525,0.04337614087150613,1.211077194445512,-1.0836797741504287,-1.7836787870637008,0.4995059673465121,-0.18106826557632977,-0.6357537423853056,-0.6655429738943645,-0.4882471909940165,-0.5323397892000745,-0.07760174057724582,0.9866065274368931,1.1687351067118212,1.1371452250754572,-1.9002979197095062,0.22016254553312545,1.3152528747021808,-0.31742062877231175,0.549150754105735,-1.3362687780707816,1.366337625157236,1.2320527031500776,1.6038994791131134,0.3607929740477437,-0.4200115614283266,-0.7140849604737152,0.42782388757286527,1.1687351067118212,1.1371452250754572,-0.49389815624083205,-1.0892748559405374,0.8375289684091195,0.41440928643531283,1.956518012825472,1.8746218824041876,1.3969002569140538,-0.7881230531558086,0.1557611977761172,-0.1068405907047651,1.6675184515282044,1.1687351067118212,1.1371452250754572,-0.31131666796530527,-0.34370363241734553,-0.2265979170371948,-0.09767242418231564,-0.35792969040066747,0.9866065274368931,

...

Cluster 5:

Center:

-1.4738616823241095,-0.8264322329841375,-1.456756001922526,-1.3623866852137452,-1.3453080277881575,-0.7275430710609524,0.25288071404962476,-0.9591539431675676,-1.3180533022155585,-1.4302614333409063,-0.7754104695060003,-0.0958985769804303,-0.08512491718493248,-0.8283067935708432,-1.4738616823241095,-0.5671283623347957,0.013787759940368861,-1.0592767195281933,-0.9756156900979512,-1.2974712042420875,-0.7446711139351271,-1.024145717411787,0.8424349954125466,-0.8766290084352819,0.7097937130045662,0.6754342207824854,-1.3646068775472884,-1.4738616823241095,-0.9819348541400383,-1.1496050749079032,-0.9332290781670973,-1.0008165956870378,-1.1962790918797859,0.8473451885187071,0.36807033222612945,0.3359360062303854,0.10340689191433741,-0.004354856789777812,-0.042435722887013694,-0.0703872636979602,0.2847037666320068,0.3224260594856511,0.13193196060636234,0.1351536351627272,0.32331840025482844,-0.04713890792624273,-0.0374312822334902,-0.04303466135143117,0.8310768086792713,0.36807033222612945,0.3359360062303854,-0.6386226527249047,-0.7440649475498782,-0.16177860696510457,-0.3902833209116608,0.19031171449958986,0.39386010195039206,-0.08323856269241453,-0.3583654274967457,-0.4061555408875202,-0.2989548021302351,0.11155996694104928,0.36807033222612945,0.3359360062303854,1.0546876197875819,0.6947843407698371,0.06606043779570575,0.3746791042477545,0.5877919401044832,0.8473451885187071,

Max Dist. to Center: 10.410757533328567

Min Dist. to Center: 4.147210189549247

Avg Dist. to Center: 6.264034271613067

SSE: 2991.397234046991

74 Points:

-0.9724131299189736,-0.9736959246430608,-1.4843193188245702,-1.279162481967605,-0.9022162595516597,-1.4868756612757386,-0.9065151953581054,-1.241689402420761,-1.4384881446218751,-0.8066917773519772,-1.6428461277090134,0.3023498955135822,-0.20611250729779354,-0.00031824541138847156,-0.9724131299189736,-1.127011810298712,-0.5570647084912455,-1.3705065373212668,-1.149284069172999,-0.9962108429229759,-0.1274037419419102,-0.6235036019777098,1.2926089979708792,-1.0860082894239098,1.2382573556285057,1.428796380709291,-1.4520522306584644,-0.9724131299189736,-0.6576302601221545,-0.9504832505996,-0.9620408550344194,-0.9577052331268882,-0.7328692128441692,0.3297134193322418,0.31201161133367644,0.28576612576598115,-0.18545426436064383,-0.08521207175615365,-0.06916187638286442,0.1227606364734875,-0.5815070323336893,-0.9746205223867037,-0.1475761666229783,1.1042250952271424,0.6258409945722673,1.2246116073383664,0.07235262397042715,0.04493557890805857,0.0,0.31201161133367644,0.28576612576598115,-1.30105646935237,-1.4611402129537665,-0.4723154545021537,-1.148714177321017,-0.24992441348431887,0.01739524251298571,-0.7299011537826191,0.04330346445911049,-0.991324006682737,-1.1068405907047651,-0.48774729674082834,0.31201161133367644,0.28576612576598115,1.801471555431586,1.9126010733072394,1.126946974064968,2.0384061543847793,1.9089344246213271,0.3297134193322418,-2.0046020834093787,-0.22140211518228892,-1.3000896652083265,-1.516031368129696,-1.3172642449883791,-1.6893643519996817,0.04149913940622644,-1.9200364146717628,-1.7458046390379933,-1.582223786480058,-1.493768739575807,0.7368027745979595,0.9091232754324292,-1.4973446605827587,-2.0046020834093787,-0.10692113427354664,0.3870374508379628,-0.6908162103250369,-1.1676959030577463,-1.815816237688206,-1.7151342549298105,-0.9807025964611038,0.04337614087150613,-1.1760900731050634,2.3381223118395797,1.7747552449309976,-1.0411978731837324,-2.0046020834093787,-1.0295310616485884,-0.6033146376024165,0.22244330506658685,-1.8084361209805153,-0.8966860809109,1.3124255090568004,0.8305547795888691,0.8021763991176306,1.0707684133949182,0.25197240150075867,-0.26693541225215583,-0.05849047274537102,0.6361244299844399,1.3399283139913944,0.009713577977562969,-0.04622337607927566,0.7345141595212502,-0.7481633795010288,0.5647168093691809,0.3047804482459631,1.4973836065050286,0.8305547795888691,0.8021763991176306,-0.37577742749280213,0.04248927409972514,-0.8399910819860205,-0.35100447577594784,-0.5095058754031181,-0.09185338336296689,0.4664246397342594,-0.7881230531558086,-0.704552705557175,-0.80891386387221056,-0.009621722090486921,0.8305547795888691,0.8021763991176306,1.0067530493832142,1.0926552910722742,0.6757653436975803,0.29070549919351985,1.1854671538696266,1.3124255090568004,-0.21547456402600992,-0.8017430539091701,-1.147818216811227,-1.0422935958055124,-1.093776868214761,1.5504546995834065,0.9895134741705583,1.1325251404577485,-0.6701969085815793,-1.1944577819160176,0.2454674553115962,0.3023498955135822,0.581571507078098,-0.00031824541138847156,-0.21547456402600992,-0.028452620733149313,0.6065960925424299,-0.8215258885935426,-0.32535450283056183,-0.9962108429229759,-0.4938030910929631,-0.8021030992194068,0.8761980456044215,-0.36535401997467937,1.604879007698864,1.1981571378948197,-1.1439114625524154,-0.21547456402600992,-1.7077031114909087,-1.5367396819816364,-0.9620408550344194,0.5310738206169593,-1.2243198170443617,0.8184418917621028,0.492374452465917,0.45325053874489446,1.5493294334922751,0.805463895337577,0.12861165948642875,0.7700860265408394,0.9840191335039054,0.7612911048986699,0.638872563797308,0.08160423184365968,1.1692068193171818,-0.9232617511139929,-0.72773917733025477,-0.9602537840569931,0.0,0.492374452465917,0.45325053874489446,0.254199792496691,0.09099345110145067,0.4233988748977036,0.3724245653013618,0.5288199722720778,0.23589249426489284,0.3334995515657173,1.4982998702852188,0.4425324988872149,-0.2674459960235841,-0.07327311438139895,0.492374452465917,0.45325053874489446,1.4525707478981547,0.8018943753861163,-0.2265979170371948,0.29070549919351985,0.9443113969523933,0.8184418917621028,

...

Cluster 6:

Center:

-0.4161176097220395,-0.23927616358752224,-0.4754294520178494,-0.45136805874850566,-0.4932175564937749,-0.2559575676644008,0.21530176744635393,-0.40599648544837863,-0.5521226765164392,-0.3645024739017556,-0.48710406076052687,0.10417840680842769,0.01750930147343403,0.22479850874971988,-0.4161176097220395,-0.39601565784343146,-0.3643153325106921,-0.23814795611094924,-0.5515535725435678,-0.4026439886087882,-0.29196204612203236,-0.5276238718795356,-0.20427879395696613,-0.5407764408274526,0.19370724516839788,0.093334314092414601,-0.2919292686311293,-0.4161176097220395,0.08478966812628037,-0.04339751310517151,-0.15160432443899366,-0.23458397845130513,-0.15232522425680725,-0.17090827568646064,-0.7174805002869318,-0.7134106221897994,0.10189224288202357,-0.5459024963147663,-0.7041190178579599,-0.4177219944753794,0.02547767407000968,0.6569841343100938,-0.29948494627665995,-0.6517225715037063,-0.5100795611576276,-0.5719591234357722,0.019876967368717875,-0.004154227432232519,-0.22517046714361333,-0.7174805002869318,-0.7134106221897994,0.05256563623031704,0.17013184515689755,-0.13197360721939072,-0.28394790700127703,-0.5614221677868784,-0.6472963970270222,-0.5046281096233005,0.13301000978072022,-0.19809110944283964,0.2607344623839894,-0.41968627311127993,-0.7174805002869318,-0.7134106221897994,-0.15910614023434622,-0.48669679011058,-0.6516585056464694,-0.6679747432447267,-0.48028450601551664,-0.17090827568646064,

Max Dist. to Center: 8.744292140608358

Min Dist. to Center: 3.9098664819774474

Avg Dist. to Center: 6.104253126394358

SSE: 3632.863145813882

95 Points:

-0.645553294647012,0.10100951744375616,-0.18343237696293055,-0.3316869373192379,-0.6787288827780414,0.841744282049606,1.0685146687342526,0.33304473316192323,-1.284829897413816,0.6151169060495043,-2.437925531086112,-0.7113734890166314,-0.9859976700462011,0.21354267104166444,-0.645553294647012,-0.9962309543980497,-0.7107557576843723,-0.899951695554647,-0.7649370368289012,-0.3405265271107912,0.2389956072091449,-0.6235036019777098,0.4597870932379638,-0.9959265057427559,-1.0836797741504287,-1.1247095218794974,-0.8357706944463665,-0.645553294647012,1.0049850878783728,0.7689839364147523,0.22244330506658685,-0.3196570672366678,0.468454486311857,0.3297134193322418,-0.1614408466384569,-0.18877304434094003,-0.524434986929605,-0.6657419431654603,-0.464708948121449,-0.8870669720315815,0.6361244299844399,0.6889614537600544,0.3046318491035789,-0.557533807771017,-0.7869101497645102,-0.03609666827497473,0.318534716669804,-0.05079674137432731,-0.21391194378643263,-0.1614408466384569,-0.18877304434094003,0.01795833500063108,0.10716151010202585,-0.10463982701828695,-0.305790160708616,-0.5095058754031181,-0.6380965127427318,0.4664246397342594,1.4982998702852188,-0.4815083602485444,-0.17417992994789736,-0.40485246026894245,-0.1614408466384569,-0.18877304434094003,-0.6020673409098316,-0.6664482488289807,-0.45218873222088757,-0.6802393092460689,-1.081396961152368,0.3297134193322418,0.1974010173701521,-1.618519189895151,-0.7906382761266728,-0.09481805115714712,-0.9979965638832103,-1.183142625189824,-1.2225199736128827,-0.7087024642235441,-0.5165386613735202,-0.16041510307857648,-0.6365737578098728,-0.20451179675152464,-0.7598309728491629,2.031360460892614,0.1974010173701521,-1.1793241526589768,-1.8524606945476008,0.40714508713040964,-0.9030257909645052,0.6429999466074844,0.3611287235928292,-1.516501088186195,-0.5812402876781804,-1.7165807751919862,0.1383923994174316,-0.0044617710663515334,-0.014061979496902749,0.1974010173701521,0.17367741387810914,-0.09238724488958042,-0.2513503589738161,0.5310738206169593,0.30463761824512614,-0.3271796887724092,-0.5447118840444692,-0.5795700079584045,0.09370633069614774,0.1804002255735839,0.12861165948642875,0.045081589665405285,-0.14663865293435743,-0.4683129644289947,0.06869723220276559,0.08160423184365968,0.08247516982735287,0.1273284785637916,1.1186265179427788,0.4552169515468552,-2.03216346597111,-0.5447118840444692,-0.5795700079584045,1.3960335037276472,1.4491104071497656,0.607731701231703,0.8923891885756782,-0.12013368252491981,-0.5288478868667792,0.06764937522863321,2.537583017303868,1.0479385790106435,0.8517467968846573,-0.48774729674082834,-0.5447118840444692,-0.5795700079584045,-1.8232201672768422,-1.2770461717699122,-0.2265979170371948,-0.48605034755815113,-1.1296281125358145,-0.3271796887724092,-1.3508824128654555,-0.7372607273839611,-0.9335102524004946,-0.8054247096434215,-1.5088248536514806,-0.17069917157010903,0.7525098904794754,-0.5875690691787222,-0.9775134029976976,-0.8066917773519772,-0.7980742616208455,1.316073280043796,0.34760595825357576,0.21354267104166444,-1.3508824128654555,-0.6823569002364603,-0.09599156091186466,-1.1090871807842555,-1.1101589221679111,-1.3240530008290683,-0.8602024402440183,-1.159302093702801,-0.7894457638614093,-1.0860082894239098,0.01618518206064556,-1.602805452296993,-0.8357706944463665,-1.3508824128654555,-0.6576302601221545,-0.0465347865691977,0.6962369691069897,-0.3196570672366678,-0.6782635901552589,0.6555324009521492,-0.4996211737614091,-0.5237418702987667,0.7916078183381267,0.6050618027414877,0.3263851953557202,0.2522257144869579,0.11428237470524166,0.037994593528714225,0.0883584502778336,-0.6853614156939524,0.951860489419216,-1.927159081694987,0.6878078557188693,0.7013857751301331,-0.21391194378643263,-0.4996211737614091,-0.5237418702987667,0.01795833500063108,0.058657333100300316,-0.012720920147320664,0.5645854043375222,0.788401434190877,1.1098815012725156,-0.5969760656140771,-0.16455316494461927,0.2832151093810495,-1.200106656780452,0.00962172209486921,-0.4996211737614091,-0.5237418702987667,0.9486029147943089,0.08953013195502965,-0.6777795474045814,0.0965165375056021,-0.21323623625032742,0.6555324009521492,

...

Cluster 7:

Center:

1.2129358583131054,0.09666496352893712,0.6807190920728808,0.7871405675314925,0.5667547200013778,0.4023007404784957,-0.2997187860497299,0.625053534408271,0.9922545532332734,0.8516266676984935,0.6753865542453895,-0.20374149022832538,-0.1592364310262137,1.0109708754756541,1.2129358583131054,-0.2274064759862844,-0.7252372851159433,0.5893043196109875,0.19255177664291886,0.9725859457790341,0.6976444378840458,0.7292925898955698,-0.6964177851412431,0.14063727559605685,-0.6442538223781555,-0.5899980250505068,1.0152593097084095,1.2129358583131054,0.9363300588106018,0.9119418668771614,0.49210246491936943,0.9134502037213821,0.8140964597150657,-1.0153800428803461,-0.8569890371750253,-0.8425264754988793,-0.1877876735898419,-0.4617697018410887,-0.45629305297807415,-0.4364183174995867,-0.4704768078062003,0.07954566971369337,-0.5458204135903082,-0.6744824703388089,-0.6400857673334377,-0.49644394740210795,0.12866023027932716,0.07570668185596834,-1.011530415032652,-0.8569890371750253,-0.8425264754988793,-0.18267935673804395,0.09391746177176746,-0.5248754677395416,-0.39982631598163065,-0.6613886456747563,-0.47887245162565095,-0.6266720959496025,0.6867745193153376,-0.3703251607633907,0.5272999500043426,-0.7743517845425614,-0.8569890371750253,-0.8425264754988793,-0.4047280543793977,-0.12424100509891044,0.26538205224639305,-0.4096142668937579,-0.21785411244661482,-1.0153800428803461,

Max Dist. to Center: 10.318598845837979

Min Dist. to Center: 4.630422880676113

Avg Dist. to Center: 6.716324886853627

SSE: 4380.232315748691

94 Points:

1.6940749999312392,-0.9307077069595882,-0.33946361420934107,0.14205083500494575,0.05558678376384688,0.031789519153834,-1.0645175844854942,0.6722182392874259,0.712727316290953,1.0028829106135446,0.13365504142116919,-0.05969417039006553,0.11364040942905354,1.60

36386279865085, 1.6940749999312392, -1.3101050085596389, -2.0061517437407277, 0.38100315147671, -0.781047391478055, 0.9708421045135768, 0.8496611891275686, 1.16249137043392603, -1.2058567162278668, -0.1851904526123718, -1.5725086435775728, -1.437719922841994, 1.4239282716 646589, 1.6940749999312392, 1.3331328539311085, 0.5200705912469603, -0.4882471909940165, 0.5310738206169593, 0.25003199555621586, -1.972 0400314664561, -1.085800407441193, -1.095980281310054, 0.6919076058178439, -0.38104373225514276, -0.8602560198600319, 0.045081589665405 285, 0.37520340234484073, 0.7612911048968699, 0.009713577977562969, -1.0688442394627584, -0.8955833147134932, -1.004974324533758, -0.17 382946872894972, 0.2158861508408905, -1.6043395783982448, -1.085800407441193, -1.095980281310054, 0.254199792496691, 0.7377158111244578 , -0.56423436137312, -0.20244315484042888, -0.8988780682813164, -0.856593764494637, -0.8628262419511612, 1.4982998702852188, -0.00355619 17300482053, 0.012352202203476216, -1.1509059885159154, -1.085800407441193, -1.095980281310054, -0.21439977698379648, -0.33207319578989 92, -0.2265979170371948, -0.09767242418231564, 0.2690752775841395, -1.9720400314664561, 1.4532309107834782, -1.2101311219021604, 0.6080031758170555, 1.5632641519774946, 0.05558678376384688, -0.7781652437419381, -1.538524751 8676601, -0.006128772963577624, 0.40541082187483474, 0.356606236340144, 0.30758303370043205, -0.13210298357079509, -0.2217102105527617, 1.9244300026660879, 1.4532309107834782, -0.05460879191328175, -0.07403569674141795, 0.015016052324892622, 1.1544966456559942, 1.6265264 2032576, 1.8267261201970453, 1.6982898621643514, 0.251581617054735, 0.5354638168368585, -1.2058869915072146, -0.7128537311393702, 0.9103 60324821244, 1.4532309107834782, -0.9420249907011922, -0.5836635840365382, -0.014453526953613549, 0.3183910986535526, -0.8966860809109 , -0.6582538152571534, 0.492374452465917, 0.45325053874489446, 1.210348710923314, 1.187182166949176, 0.7219322670943048, 0.95133713575969 79, 0.8100717817441726, -0.251324011018548, 0.9927744817309493, 1.1042250952271424, 1.4952263141641304, 0.279080400628361, 2.16490041191 51303, 1.959581984555776, -1.9252074940778938, 0.492374452465917, 0.45325053874489446, -0.0017284531240405801, 0.2041698641054769, -0.28 847764076022114, 0.1350494111978696, 0.00965704843447924, 0.23589249426489284, -0.5969760656140771, 1.7061564996889487, 0.1557611977761 172, 1.1315449951177176, -0.8193266426283718, 0.492374452465917, 0.45325053874489446, 0.696618998242386, 1.9271391190915472, 2.480491865 167129, 2.426784077760615, 1.9089344246213271, -0.6582538152571534, 1.625262403031879, -0.563078566500703, 0.10983115328333508, 0.37891972116703654, 0.4067812329795326, 0.9429886274115775, -1.0645175844 854942, 1.7624187946908225, 1.4810185523312487, 1.2613935803229048, 0.9411619332665576, -1.1458263681010088, -0.767629824476647, 1.38977 77115334555, 1.625262403031879, -0.6823569002364603, -1.0620495844115196, 0.22415153755450282, -0.028463681439013264, 0.970842104513576 8, 0.9717943055112529, 0.9838918731975632, -0.37303481149495155, -0.095108668931218, -1.9391302956479308, -2.360276894099879, 0.91036032 4821244, 1.625262403031879, -0.8299729459835805, 0.23185513894741172, -0.4882471909940165, 0.7437565425803662, 1.1237219585787803, -1.315 1469233618047, -1.8297971271116877, -1.8496601397151642, -0.7637154969782836, -1.5198365758964127, -1.4535766274679096, -1.482060330893 545, 0.027308698825375295, 0.6889614537600544, -0.30486591122352097, -1.1966718473856937, -0.7869101497645102, -1.390190742081897, -0.23 537499190379393, -0.6251906630686426, -1.390427634611812, -1.8297971271116877, -1.8496601397151642, -0.671079249362877, -0.183863551909, 32734, -1.1387275293166612, -1.0372931866193777, -1.418040992118915, -0.9658423903705896, -0.7299011537826191, 1.4982998702852188, -1.24 62318298781383, 0.6652146647332837, -1.399590497931573, -1.8297971271116877, -1.8496601397151642, -0.6602174754987369, -0.9106874180053 534, -0.9033703625882752, -1.6511841176856576, -0.9367035070020279, -1.3151469233618047,

...

Cluster 8:

Center:

-0.2793127563302357, -0.40733910492164666, -0.19978519352439206, -0.003495107094653559, -0.279836611324957, -0.0743340717677506, -0.293 5420712735375, 0.07705922122383045, -0.14812912891082414, -0.13705570521327282, -0.05837501246993823, -0.3702669912616284, -0.281282161 538604, -0.5504303618297836, -0.2793127563302357, -0.5544122556685834, -0.38882459267914776, -0.4870350974582344, -0.44464322176457166, -0.23980393642879966, 0.1227484241451553, -0.3717428649020646, 0.5149740869250846, -0.4885381458519198, -0.14135906200171716, -0.139629 8643164848, -0.5424800838394042, -0.2793127563302357, -0.0018618730223904307, 0.28469200787253435, 0.47931938798005863, 0.1518323404894 388, 0.2677952704068252, 0.5999418323819433, 0.6545380310140316, 0.645285879737057, 0.21646972490786937, 0.493574006344084, 0.5003305943 732903, 0.43534860796625213, 0.6403159324364815, -0.03346361602813968, 0.6926448034043131, 0.5128298971258511, 0.631078255533664, 0.2595 312651631381, -0.33770369308606507, -0.3366755291367016, 0.5502433734747395, 0.6545380310140316, 0.645285879737057, 0.2703287273458196, 0.13423813903069992, 0.3729508788624876, 0.4046037723243526, 0.47721642863761765, 0.3569873566816115, 0.37353722872491674, -0.20963050 626109078, 0.3722792885748577, -0.6461286980417341, 0.4500629616579769, 0.6545380310140316, 0.645285879737057, 0.18377684741011308, 0.17 378073463276575, 0.08868563189423308, 0.5316869817700924, 0.2806972417729219, 0.5999418323819433,

Max Dist. to Center: 9.732789125313404

Min Dist. to Center: 4.635664739498042

Avg Dist. to Center: 6.437607235657886

SSE: 3537.233380810226

83 Points:

-0.7487721899960526, -0.3718608770744433, -0.20975089890810822, -0.09481805115714712, -0.806435955220109, 0.234278209877777, 0.12050033 396992077, 0.1876846591081384, -0.055563919749342744, -0.8066917773519772, 0.9038925862332556, 0.7368027745979595, 0.5269795456857045, -1.2834837441297058, -0.7487721899960526, -1.36241735091990366, -0.6887989935139256, -1.6580678295119795, -0.7235104105882201, 0.3045265 271107912, 0.9717943055112529, -0.08770511025261879, 1.9172254265205657, -0.6806402628587176, 1.2382573556285057, 0.9510436634507434, -1 .4520522306584644, -0.7487721899960526, 0.08617134293071295, 0.6641783173967346, 0.9331338011271901, -0.3196570672366678, -0.1322073632 661561, 0.4926229101421955, 0.6501919384566286, 0.6207349517238079, 0.3728669257529393, 0.14222839841242402, -0.06916187638286442, 0.096 86762087079344, 0.6361244299844399, 0.18265389580234537, 0.5798889021545268, 0.08160423184365968, 1.060533654368199, -0.829875952920411 6, 0.19544367032011556, 0.5372732260746145, 1.2834716627185958, 0.6501919384566286, 0.6207349517238079, -1.3601168337263851, -1.07310679 69399621, -1.3225653430585955, -0.7014154175477697, 0.00965704843447924, 1.21913012714847, -0.7299011537826191, -0.5802664237520788, -0. 7364161834584091, -0.08091386387221056, -0.48774729674082834, 0.6501919384566286, 0.6207349517238079, 1.6657879080574738, 1.52298144628 77878, 0.6757653436975803, 1.8442171926968618, 1.1854671538696266, 0.4926229101421955, -0.23267771325085002, -0.7372607273839611, -1.164737266633127, -1.0422935958055124, -0.4871682741149402, 1.4492103542214352, 0.59450750 1520867, 1.2536585355025704, 0.40541082187483474, -0.41892577278793675, 1.2020473624996675, -0.20451179675152464, -0.1827159524153413, 0.53433940457212438, -0.23267771325085002, 0.5992954875900293, 0.45290504334930287, 0.48557089409151416, -0.6084364488085501, -1.1601319 218760213, -1.7151342549298105, -1.516501088186195, -1.2058567162278668, -0.45543580365583314, 0.38280683413100364, 0.1767547768593044, -0.21948915823426868, -0.23267771325085002, -1.2701727567539278, -1.1633696442299485, -0.7251440230142179, 1.5944874304339933, 0.031609 504808574735, 0.3297134193322418, 0.5149198076074474, 0.48116460757471335, 0.7517277333300136, 1.0249519015142643, 0.9197058029635962, 1 .1325882449785565, -0.4945333564538229, -0.7576315689762569, -0.1672373846980463, 0.8485698793812717, 0.8431873244702331, 0.55923779520 91033, 0.13389814714527135, 0.16801999069969756, -0.5347798594660816, 0.5149198076074474, 0.48116460757471335, 0.43138088561873594, 0.13 94976281031762, 0.7226303348204112, 0.3590561895678384, 0.3990292413126787, 0.01739524251298571, -0.33112588927699294, 1.0825866114775 94, 0.41066902098598185, 0.8517467968846573, -0.15616795085328483, 0.5149198076074474, 0.48116460757471335, 0.38648494710155795, 1.22640 53122879068, 1.8037194196160484, 1.4558392693210263, 1.2336983052530734, 0.3297134193322418, -0.5079281008482913, -0.6942725097004884, -0.5685558234813307, -0.5829485784464908, -1.790608697361653, -1.6175259 464313543, -1.2174627234117963, 0.40541082187483474, 0.6151169060495043, 0.04669760446732137, -0.2769206099322542, 0.7219508363728114, -1 .8181360352623381, -0.5079281008482913, -1.3101050085596389, -0.31555020261633165, -2.024054928663795, -1.41395418126624, -1.651895158 7351605, 0.3761699747092788, 0.9089438698907822, 1.9172254265205657, -1.9417852343948707, 0.7494284862013617, 0.012012460563253552, -1

.7601929987645133,-0.5079281008482913,-0.5263711537010604,0.5036947132753951,1.4069274651675931,0.10570837669014578,1.232933203956601,1.3124255090568004,0.6051012281735677,0.5649068140641701,0.771667758340701,0.18199071837196557,-0.06916187638286442,0.1227606364734875,0.37520340234484073,0.905950407170501,-0.049270076247639655,0.33725944768953037,0.7345141595212502,-0.1411556912427530.3800802398446482,0.41418881428297555,1.8182515221846773,0.6051012281735677,0.5649068140641701,0.47075446186807923,0.559867162181308,0.125157440159125036,-0.041391187129825036,-0.37971514444371907,-0.7473451386186845,0.7322748160713435,0.2511600938628403,0.34694206518351567,-0.9203084585533916,0.0925165585623728,0.6051012281735677,0.5649068140641701,0.2701846779237474,0.2581714630530012,0.22458371333019278,-0.29186138587023336,-0.2614673876337741,1.3124255090568004,

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Cluster 9:

Center:

-0.24773046882258506,-0.15584508321499307,-0.12205382399792689,-0.07113116254093756,0.051595937750032274,-0.5250543803370092,-0.3989325202863695,-0.3828536315529732,0.06736267801710458,-0.02146561810979536,0.18459418849053694,0.38380981034190303,0.43339332615590054,-0.3184363586353046,-0.24773046882258506,0.6725327668944001,0.7487603130460723,0.22088379559778976,0.34736787773338895,-0.20938966394835495,-0.41136323753397697,0.25609892193764794,-0.1440087876933998,0.4374998770836038,0.9174634100669425,1.0552431785079956,0.13230488535347046,-0.24773046882258506,-0.10689087935749169,-0.7069739451624246,-0.020375947754119102,-0.39409601992386023,-0.64413507597469,1.0086781358692094,1.409406772847656,1.3963971393324004,0.6839315888162213,1.3281793535257103,1.2311991219577316,1.330669814339166,0.673088242233383,-0.576807441134218,1.0355376310442217,1.3407061698845726,1.0768346291105462,1.0661475810286343,0.23698689846313536,0.4555588526907209,0.3181940163823186,1.409406772847656,1.3963971393324004,1.1661902523721055,0.8577636492037284,1.0564108653956092,1.4025439202773502,1.1583050174251652,0.6701557821218056,1.5165328362657415,-0.46594527758002735,1.389674379501368,-0.7640877978766162,1.2696232364631523,1.409406772847656,1.3963971393324004,-0.20470808788564562,-0.09735644660224829,0.07230991308119993,0.45576611662824995,0.1340280537104888,1.0086781358692094,

Max Dist. to Center: 9.317178093132988

Min Dist. to Center: 4.389678785708287

Avg Dist. to Center: 6.226288649968521

SSE: 1609.601821688544

40 Points:

-0.9208036822444533,-0.479331421283125,-0.877113419660828,-0.8054247096434215,0.15136708809539753,-0.7781652437419381,-1.301521168176577,-0.1514888470173642,0.8663855634990122,0.8736275757588645,0.46908353751140486,0.08512345597139356,-0.5102677207696724,-1.2834837441297058,-0.9208036822444533,0.2331090910681751,0.5407285000310897,-0.27254523986581836,-0.17345687328139744,-0.6683686850168835,-0.6159362074766496,-0.44490410473601283,1.2926089979708792,0.13009579027166648,0.7494284862013617,0.34149709315535526,-0.9384842838150494,-0.9208036822444533,-1.1607901680696826,-1.2812759856252183,-0.9620408550344194,0.10570837669014578,-0.18681298595506637,0.9866065274368931,1.326552592702533,1.2906726036394611,0.9910082433786921,1.2587543428763508,0.9197058029635962,1.36562585402803,0.8100717817441726,-0.7576315689762569,1.2876927528569653,0.8485698793812717,1.060533654368199,0.337446524499349,1.6725362265163768,1.6518709550766786,1.2834716627185958,1.326552592702533,1.2906726036394611,1.5929013849743638,1.1904214631405627,1.3430829561994364,1.410739014883304,0.788401434190877,0.01739524251298571,0.3334995515657173,-0.9959796825595384,1.270982924319275,-0.08091386387221056,1.0043597597531175,1.326552592702533,1.2906726036394611,-0.44700031533941753,-0.2390297027703287,0.22458371333019278,1.4558392693210263,0.654924488651713,0.9866065274368931,0.386635658843393,-1.1241546865352152,0.1793872469955904,0.8526574934912202,-0.1998273611202882,-1.3856313159137672,-1.2225199736128827,-0.9509692543131878,0.09809432745871641,-0.8066917773519772,1.1772011311441337,0.7368027745979595,0.6985542814903591,1.496708169759982,0.386635658843393,-0.603888386696063,-0.6009764368321389,-0.2986871755195199,0.14184578199489833,0.8069210255605298,1.2160605382786216,1.6982898621643514,-1.4140621924110959,-0.23023134445294868,0.38280683413100364,0.6545074941178519,1.3212146822959758,0.386635658843393,-0.6138772246484565,0.11067364195782879,0.9331338011271901,-0.3196570672366678,-0.4052354767107075,0.6555324009521492,0.9658269104380504,0.9277897088518157,0.6719675633137874,1.4496134786821502,1.3152528747021808,1.0549091981704741,1.3319138370233707,-0.3959833132921792,1.6415946782081838,0.33725944768953037,0.19114833477633575,0.454178772241325,0.8724444252434019,0.6671956607435667,-1.4973836065050286,0.9658269104380504,0.9277897088518157,0.8841770124861841,0.8508922241284841,0.5158127943607367,1.368754293749353,1.0479828961096762,1.000632875396563,1.6627504332511378,0.8747299820740295,1.3347098801217412,-2.13276731753732,0.7556752503374599,0.9658269104380504,0.9277897088518157,0.07635089596072986,0.18548123413146175,0.22458371333019278,-0.8744282709339867,-0.06854278209998732,0.6555324009521492,-0.5595375485228116,-0.24289622402402528,-0.9842674018661943,-1.0422935958055124,-0.29560766545183886,0.234278209877777,0.2785027230973094,0.11500462208124423,-0.8238551557896385,-0.8066917773519772,-0.5123426010322011,-1.2182351812817382,-0.5258654240246406,-0.5349705365440208,-0.5595375485228116,0.12848440634764532,0.7822430059060034,-0.7431000816324399,-0.44272994384582526,-1.1601319218760213,-0.8602024402440183,-0.8021030992194068,0.8761980456044215,0.4003411413151279,1.1160501382717198,1.2970025276724502,-1.1439114625524154,-0.5595375485228116,-1.2264197212802297,-1.0847654499664352,-0.4882471909940165,-0.3196570672366678,-0.7328692128441692,1.6434996355415443,1.3941886581271228,1.3604577757140084,-0.8833557520026227,0.6448241227010292,1.3152528747021808,0.2263326988842638,0.11428237470524166,-0.9746205223867037,0.6388725563797308,0.33725944768953037,0.6258409945722673,-0.024423443500776958,0.13389814714527135,-0.2559374276937256,0.5347798594660816,1.3941886581271228,1.3604577757140084,0.09670548749931772,-0.2323677289100529,0.6307114279494466,0.8132641372078474,1.4373550889878746,1.4376273789003753,1.6627504332511378,0.8747299820740295,0.9842116232081772,-1.1068405907047651,1.0043597597531175,1.3941886581271228,1.3604577757140084,-0.3500834243579088,-0.28555144928011394,-0.001007101853500006,0.0965165375056021,-0.7920100528516877,1.6434996355415443,

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