

CSC 466 Lab 7 Report:

PageRank and Link Analysis

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CSC 466: Knowledge Discovery from Data, Fall 2023

Abstract

This lab report examines the PageRank algorithm's efficacy across diverse datasets: NCAA Football, Dolphins, and Les Miserables. Using directed graphs, adjacency, and transition matrices, the algorithm's performance in identifying central nodes was analyzed. The results varied: with the NCAA Football dataset, PageRank didn't align with the actual season outcomes, suggesting limited suitability for sports ranking. With the Dolphins dataset lacking a ground truth, this presented challenges to verify the accuracy of the rankings. With the Les Miserables dataset, PageRank identified central figures but not the main characters, indicating its limitations in narrative contexts. The study highlights PageRank's effectiveness in networks where centrality is key and its limitations in datasets with complex dynamics.

I. Introduction

This lab report focuses on the implementation and analysis of the PageRank algorithm, a fundamental technique in link analysis and web search optimization. Utilizing datasets like NCAA Football, Dolphins, and Les Miserables, the assignment involves building a system to compute PageRank scores for various nodes. Our approach includes constructing directed graphs from the datasets, formulating adjacency and transition matrices, and iteratively computing the PageRank values. The aim is to gain insights into the significance of nodes within each network and understand the performance implications of different aspects of the PageRank algorithm, such as convergence behavior and the impact of the damping factor.

II. Description of Datasets

A. NCAA Football Dataset

This dataset includes detailed records of 1,537 games from the 2009 NCAA Division I football season. The data captures game outcomes, which can be used to analyze team performance, predict future outcomes, and understand the dynamics of college football competitions.

B. Dolphins Dataset

This dataset tracks the social interactions of a dolphin group, providing a network structure illustrating relationships and hierarchies. Analyzing this data can reveal social patterns, dominance structures, and interaction frequencies within the dolphin community.

C. Les Miserables Dataset

The dataset creates a network of character interactions from Victor Hugo's "Les Miserables." It offers a unique way to visualize and analyze the relationships between characters, their prominence in the novel, and the narrative's structure. This analysis can provide insights into character development and plot dynamics.

III. Methods

The implementation of our PageRank algorithm starts by preprocessing the input data. For the NCAA Football dataset, this involves cleaning and reformatting the data before converting it to a data frame, ensuring consistency and accuracy for analysis. Next, a directed graph is constructed from the data frame, creating a network where nodes represent entities like football teams or novel characters or dolphins, and edges represent their interactions or connections.

The core of the implementation lies in the creation of the adjacency matrix from the graph, which is then used to form the transition matrix. This matrix is crucial for the PageRank calculation, as it reflects the probability of transitioning from one node to another in the network. The damping factor, a key component of the PageRank algorithm, is incorporated into the transition matrix to account for the likelihood of random jumps in the network. The damping factor is an optional argument, but the default is 0.85.

Finally, the PageRank values are computed iteratively using the transition matrix until convergence is achieved. The algorithm checks for convergence in each iteration to ensure the stability of PageRank values. The convergence value is set at 0.001. The final output is a ranked list of nodes based on their PageRank scores, providing insight into the importance or influence of each node within the network.

IV. Results

A. NCAA Football Dataset

In the PageRank analysis of the 2009 NCAA football season dataset, a damping factor of 0.85 and a convergence criterion of 0.001 was used.

Output 1: NCAA Football PageRank Results (Top 15)

Data File: NCAA_football.csv

Read Time: 0.02647 seconds
Processing Time: 0.00094 seconds
Number of Iterations: 4

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|----------------------|-----------|
| 1 | East Carolina | 0.002503 |
| 2 | North Carolina State | 0.002495 |
| 3 | Duke | 0.002490 |
| 4 | Louisiana-Lafayette | 0.002485 |
| 5 | Pittsburgh | 0.002476 |
| 6 | Vanderbilt | 0.002476 |
| 7 | West Virginia | 0.002468 |
| 8 | Rutgers | 0.002462 |
| 9 | Southern Miss | 0.002450 |
| 10 | Virginia | 0.002446 |
| 11 | Florida Atlantic | 0.002446 |
| 12 | Iowa | 0.002444 |
| 13 | Alabama | 0.002443 |
| 14 | Bowling Green | 0.002442 |
| 15 | Texas | 0.002441 |

The algorithm converged in just 4 iterations, indicating efficient processing. Interestingly, East Carolina, the 2009 Conference USA football champions, and North Carolina State, where Russell Wilson set a new Division I record for most passes attempted without an interception, ranked highly. This suggests PageRank's efficiency in identifying network centrality, though not necessarily on-field success. Teams like Alabama and Texas who were most dominant in terms of results were still in the top 15, indicating a reasonable alignment with their strong season performances. Other notable mentions include Pittsburgh players winning offensive and defensive player of the year in the Big East Conference, Virginia's firing of head coach Al Groh, Iowa's win in the FedEx Orange Bowl, and Bowling Green's Freddie Barnes breaking the single-season record for receptions in addition to their head coach Gregg Brandon being fired in the pre-season¹. This suggests that while PageRank is effective in identifying teams of key players in the network, it also reflects significant season highlights and team accomplishments.

B. Dolphins Dataset

For the dolphins dataset, the PageRank algorithm was applied with a damping factor of 0.85 and a convergence criterion of 0.001, converging in 8 iterations.

Output 2: Dolphins (Directed) PageRank Results (Top 15)

Data File: dolphinsDir.csv

Read Time: 0.00487 seconds

Processing Time: 0.00085 seconds

¹ https://en.wikipedia.org/wiki/2009_NCAA_Division_I_FBS_football_season

Number of Iterations: 8

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|-----------|-----------|
| 1 | TR88 | 0.001692 |
| 2 | TSN83 | 0.001602 |
| 3 | TR120 | 0.001602 |
| 4 | SMN5 | 0.001353 |
| 5 | Whitetip | 0.001345 |
| 6 | Zipfel | 0.001279 |
| 7 | Stripes | 0.001153 |
| 8 | TSN103 | 0.001095 |
| 9 | Thumper | 0.001020 |
| 10 | TR99 | 0.000991 |
| 11 | Zig | 0.000958 |
| 12 | Vau | 0.000950 |
| 13 | SN4 | 0.000949 |
| 14 | Patchback | 0.000946 |
| 15 | SN63 | 0.000942 |

The ranking generated by PageRank might not directly correspond to any known hierarchy or social structure within the dolphin group, as it primarily reflects the network centrality based on observed interactions. The ranking, therefore, could be indicative of the most connected or central dolphins in the social network, rather than a hierarchy or dominance order. This suggests that while PageRank effectively identifies central figures in a network, the results should be used cautiously. Given the lack of a ground truth or a well-defined social hierarchy for the dolphin group, it's challenging to verify the accuracy or relevance of the rankings. The PageRank algorithm excels at identifying central or highly connected nodes in a network, but interpreting these results in the context of dolphin social structures requires careful consideration and an understanding of the limitations and nature of the algorithm.

C. Les Miserables Dataset

For the Les Miserables dataset, the PageRank settings were set with a damping factor of 0.85 and a convergence criterion of 0.001, requiring 9 iterations for convergence.

Output 3: Les Miserables PageRank Results (Top 15)

Data File: lesmisDir.csv

Read Time: 0.00619 seconds
 Processing Time: 0.00096 seconds
 Number of Iterations: 9

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|----------------|-----------|
| 1 | MmeHucheloup | 0.003446 |
| 2 | Grantaire | 0.003383 |
| 3 | Joly | 0.003242 |
| 4 | Bahorel | 0.003132 |
| 5 | MotherPlutarch | 0.003123 |
| 6 | Courfeyrac | 0.003024 |
| 7 | Bossuet | 0.003022 |
| 8 | Feuilly | 0.002979 |
| 9 | Prouvaire | 0.002867 |
| 10 | Combeferre | 0.002774 |
| 11 | Brujon | 0.002710 |
| 12 | MmePontmercy | 0.002632 |
| 13 | Mabeuf | 0.002594 |
| 14 | Child2 | 0.002586 |
| 15 | Montparnasse | 0.002485 |

Interestingly, the top-ranked characters in the PageRank results, such as Madame Hucheloup, Grantaire, and Joly, are not the central characters in Victor Hugo's novel. The novel's main characters include Jean Valjean, Javert, Fantine, Cosette, and Eponine². This discrepancy indicates that either PageRank effectively identifies central figures in a network based on their connections, but it does not necessarily align with the narrative importance or prominence of characters in the literary context of *Les Misérables*. Or PageRank does not effectively identify the central figures in a network based on their connections. This reinforces the notion that the interpretation of PageRank results should be context-sensitive, particularly in literary analyses where character importance is not solely defined by their interactions but also by their narrative roles and development.

V. Performance Evaluation

In evaluating the performance of the PageRank implementation, the number of iterations and running times for each dataset were observed. For the NCAA Football dataset, the algorithm converged in 4 iterations with a processing time of 0.00094 seconds. For the Dolphins dataset, it took 8 iterations and 0.00085 seconds, while for the *Les Misérables* dataset, 9 iterations and 0.00096 seconds were needed. These results suggest efficient performance on small datasets. However, scaling up to larger graphs might present challenges, particularly in processing time and memory usage. The observed trend shows a correlation between the complexity of the network (in terms of nodes and edges) and the number of iterations and processing time required. This suggests that for larger graphs, optimizations may be needed to maintain efficiency.

² <https://bookanalysis.com/victor-hugo/les-miserables/character-list/>

VI. Conclusion

In conclusion, the PageRank implementation effectively identified central nodes in various datasets, but its efficacy varied. In the NCAA Football dataset, the algorithm didn't align well with actual season outcomes, suggesting it may be less suitable for sports ranking. For the Dolphins dataset, while it highlighted central individuals, the lack of ground truth in social hierarchies made the results speculative. In the Les Misérables dataset, PageRank identified central figures in the story network, but these did not always correspond to the main characters. Thus, PageRank works best with datasets where centrality is key, and less effectively where the importance is contextually or narratively defined.

VII. Appendix

A. README

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Professor Alexander Dekhtyar

CSC 466: Fall 2023

Lab 7

How to run: `python3 pageRank.py <datafile> <OPTIONAL: damping factor (default = 0.85)>`

Note: program only works with .csv files as the inputted datafile (undirected or directed)

Submitted files:

README.txt (this file)

pageRank.py

NCAA_football.csv

dolphins.csv

dolphinsDir.csv

lesmis.csv

lesmisDir.csv

B. NCAA Football Output

Data File: NCAA_football.csv

Read Time: 0.02647 seconds

Processing Time: 0.00094 seconds

Number of Iterations: 4

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|------------------------|-----------|
| 1 | East Carolina | 0.002503 |
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| 7 | West Virginia | 0.002468 |
| 8 | Rutgers | 0.002462 |
| 9 | Southern Miss | 0.002450 |
| 10 | Virginia | 0.002446 |
| 11 | Florida Atlantic | 0.002446 |
| 12 | Iowa | 0.002444 |
| 13 | Alabama | 0.002443 |
| 14 | Bowling Green | 0.002442 |
| 15 | Texas | 0.002441 |
| 16 | Tennessee | 0.002440 |
| 17 | Wake Forest | 0.002440 |
| 18 | Rice | 0.002438 |
| 19 | UTEP | 0.002434 |
| 20 | Connecticut | 0.002433 |
| 21 | Buffalo | 0.002429 |
| 22 | Michigan | 0.002425 |
| 23 | Michigan State | 0.002425 |
| 24 | Middle Tennessee State | 0.002420 |
| 25 | Texas A&M | 0.002419 |
| 26 | Boston College | 0.002417 |
| 27 | Northwestern | 0.002413 |
| 28 | Cincinnati | 0.002408 |
| 29 | San Diego State | 0.002408 |
| 30 | Miami (FL) | 0.002407 |
| 31 | South Florida | 0.002406 |
| 32 | LSU | 0.002405 |
| 33 | Nebraska | 0.002404 |
| 34 | Penn State | 0.002404 |
| 35 | Boise State | 0.002402 |
| 36 | South Carolina | 0.002402 |
| 37 | Utah | 0.002398 |
| 38 | Tulsa | 0.002395 |
| 39 | Florida International | 0.002393 |
| 40 | Utah State | 0.002392 |
| 41 | Colorado State | 0.002390 |
| 42 | Houston | 0.002384 |
| 43 | Virginia Tech | 0.002380 |
| 44 | Nevada | 0.002378 |
| 45 | North Carolina | 0.002377 |
| 46 | Ohio State | 0.002374 |
| 47 | Florida | 0.002369 |
| 48 | Kansas | 0.002367 |
| 49 | Wisconsin | 0.002367 |
| 50 | Fresno State | 0.002366 |
| 51 | Purdue | 0.002366 |
| 52 | New Mexico | 0.002365 |
| 53 | San Jose State | 0.002363 |
| 54 | Texas Tech | 0.002358 |
| 55 | Akron | 0.002356 |
| 56 | Minnesota | 0.002356 |
| 57 | Georgia | 0.002355 |
| 58 | Colorado | 0.002354 |

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|-----|-------------------|----------|
| 59 | Air Force | 0.002354 |
| 60 | Kentucky | 0.002351 |
| 61 | Navy | 0.002351 |
| 62 | Memphis | 0.002351 |
| 63 | Missouri | 0.002349 |
| 64 | Mississippi | 0.002348 |
| 65 | Kent State | 0.002342 |
| 66 | Kansas State | 0.002338 |
| 67 | Auburn | 0.002336 |
| 68 | Louisiana Tech | 0.002336 |
| 69 | Troy | 0.002335 |
| 70 | Illinois | 0.002333 |
| 71 | Georgia Tech | 0.002329 |
| 72 | UAB | 0.002324 |
| 73 | Louisville | 0.002318 |
| 74 | Ball State | 0.002317 |
| 75 | Army | 0.002313 |
| 76 | Maryland | 0.002312 |
| 77 | Clemson | 0.002309 |
| 78 | Mississippi State | 0.002309 |
| 79 | Wyoming | 0.002303 |
| 80 | Arkansas | 0.002302 |
| 81 | Syracuse | 0.002298 |
| 82 | UNLV | 0.002295 |
| 83 | Temple | 0.002292 |
| 84 | UCF | 0.002288 |
| 85 | Tulane | 0.002288 |
| 86 | TCU | 0.002287 |
| 87 | Louisiana-Monroe | 0.002287 |
| 88 | Arkansas State | 0.002280 |
| 89 | Toledo | 0.002279 |
| 90 | Marshall | 0.002270 |
| 91 | Central Michigan | 0.002270 |
| 92 | Western Michigan | 0.002238 |
| 93 | Oklahoma State | 0.002212 |
| 94 | Idaho | 0.002209 |
| 95 | Hawaii | 0.002203 |
| 96 | Ohio | 0.002193 |
| 97 | New Mexico State | 0.002184 |
| 98 | North Texas | 0.002174 |
| 99 | Villanova | 0.002171 |
| 100 | Florida State | 0.002162 |
| 101 | Indiana | 0.002157 |
| 102 | James Madison | 0.002156 |
| 103 | Brigham Young | 0.002153 |
| 104 | Oklahoma | 0.002141 |
| 105 | Hofstra | 0.002140 |
| 106 | Notre Dame | 0.002132 |
| 107 | Miami (OH) | 0.002111 |
| 108 | Iowa State | 0.002089 |
| 109 | William & Mary | 0.002048 |
| 110 | Northeastern | 0.002043 |
| 111 | Northern Illinois | 0.002039 |
| 112 | Massachusetts | 0.002027 |
| 113 | New Hampshire | 0.002017 |
| 114 | Richmond | 0.002010 |
| 115 | Maine | 0.002008 |
| 116 | Baylor | 0.001992 |
| 117 | Towson | 0.001977 |
| 118 | Northern Colorado | 0.001972 |
| 119 | USC | 0.001931 |
| 120 | Rhode Island | 0.001918 |

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|-----|------------------------|----------|
| 121 | Florida A&M | 0.001900 |
| 122 | Morgan State | 0.001890 |
| 123 | Colgate | 0.001887 |
| 124 | Oregon | 0.001880 |
| 125 | California | 0.001875 |
| 126 | Fayetteville State | 0.001874 |
| 127 | Western Kentucky | 0.001871 |
| 128 | Southern Methodist | 0.001864 |
| 129 | Winston-Salem | 0.001861 |
| 130 | Coastal Carolina | 0.001848 |
| 131 | Delaware State | 0.001846 |
| 132 | South Carolina State | 0.001838 |
| 133 | Oregon State | 0.001830 |
| 134 | Montana | 0.001826 |
| 135 | Lehigh | 0.001820 |
| 136 | Arizona | 0.001815 |
| 137 | Hampton | 0.001813 |
| 138 | Eastern Michigan | 0.001810 |
| 139 | Bethune-Cookman | 0.001801 |
| 140 | Holy Cross | 0.001781 |
| 141 | Idaho State | 0.001765 |
| 142 | Harvard | 0.001760 |
| 143 | Cal Poly | 0.001756 |
| 144 | Delaware | 0.001746 |
| 145 | Stony Brook | 0.001744 |
| 146 | Lafayette | 0.001741 |
| 147 | Tennessee State | 0.001725 |
| 148 | Nicholls State | 0.001721 |
| 149 | Fordham | 0.001720 |
| 150 | Eastern Washington | 0.001719 |
| 151 | Stanford | 0.001694 |
| 152 | Cornell | 0.001674 |
| 153 | Weber State | 0.001667 |
| 154 | Rhodes | 0.001662 |
| 155 | Tuskegee | 0.001658 |
| 156 | Portland State | 0.001653 |
| 157 | Eastern Kentucky | 0.001651 |
| 158 | Brown | 0.001641 |
| 159 | Bucknell | 0.001638 |
| 160 | Northern Arizona | 0.001631 |
| 161 | Jacksonville State | 0.001602 |
| 162 | UCLA | 0.001594 |
| 163 | Montana State | 0.001593 |
| 164 | Austin Peay | 0.001583 |
| 165 | Presbyterian | 0.001583 |
| 166 | Alabama State | 0.001574 |
| 167 | Appalachian State | 0.001567 |
| 168 | UC Davis | 0.001565 |
| 169 | Norfolk State | 0.001564 |
| 170 | Northern Iowa | 0.001560 |
| 171 | Yale | 0.001557 |
| 172 | Gardner-Webb | 0.001552 |
| 173 | North Carolina Central | 0.001552 |
| 174 | Texas State | 0.001552 |
| 175 | Princeton | 0.001536 |
| 176 | Central Arkansas | 0.001530 |
| 177 | Pennsylvania | 0.001527 |
| 178 | Albany | 0.001518 |
| 179 | Georgia Southern | 0.001501 |
| 180 | Arizona State | 0.001501 |
| 181 | Murray State | 0.001500 |
| 182 | Elon | 0.001498 |

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|-----|-----------------------------|----------|
| 183 | Wofford | 0.001497 |
| 184 | Sacramento State | 0.001493 |
| 185 | Washburn | 0.001483 |
| 186 | Charleston Southern | 0.001477 |
| 187 | Sam Houston State | 0.001469 |
| 188 | Liberty | 0.001465 |
| 189 | North Dakota State | 0.001464 |
| 190 | Southern Illinois | 0.001447 |
| 191 | Central Connecticut State | 0.001436 |
| 192 | Northwestern State | 0.001431 |
| 193 | Southern University | 0.001422 |
| 194 | Grambling State | 0.001418 |
| 195 | North Carolina Pembroke | 0.001411 |
| 196 | Tennessee-Martin | 0.001407 |
| 197 | Southeastern Louisiana | 0.001387 |
| 198 | Eastern Illinois | 0.001374 |
| 199 | South Dakota State | 0.001372 |
| 200 | Georgetown | 0.001359 |
| 201 | Stonehill | 0.001344 |
| 202 | Monmouth | 0.001343 |
| 203 | McNeese State | 0.001340 |
| 204 | Furman | 0.001328 |
| 205 | North Carolina A&T | 0.001322 |
| 206 | Tennessee Tech | 0.001289 |
| 207 | Jackson State | 0.001288 |
| 208 | Robert Morris | 0.001276 |
| 209 | Virginia Military Institute | 0.001270 |
| 210 | Dayton | 0.001267 |
| 211 | Prairie View A&M | 0.001262 |
| 212 | Alabama A&M | 0.001251 |
| 213 | Southeast Missouri State | 0.001232 |
| 214 | Columbia | 0.001227 |
| 215 | Missouri State | 0.001224 |
| 216 | Washington State | 0.001223 |
| 217 | Wesley College | 0.001222 |
| 218 | Illinois State | 0.001222 |
| 219 | Franklin | 0.001220 |
| 220 | Western Illinois | 0.001210 |
| 221 | Southern Utah | 0.001201 |
| 222 | Stephen F. Austin | 0.001200 |
| 223 | San Diego | 0.001196 |
| 224 | Arkansas-Monticello | 0.001172 |
| 225 | Henderson State | 0.001172 |
| 226 | Alcorn State | 0.001164 |
| 227 | Jacksonville | 0.001159 |
| 228 | Duquesne | 0.001156 |
| 229 | St. Francis (IL) | 0.001153 |
| 230 | Marian | 0.001153 |
| 231 | Howard | 0.001128 |
| 232 | Edward Waters | 0.001128 |
| 233 | Marist | 0.001095 |
| 234 | Citadel | 0.001082 |
| 235 | Sacred Heart | 0.001074 |
| 236 | Youngstown State | 0.001073 |
| 237 | Western Carolina | 0.001060 |
| 238 | Wagner | 0.001046 |
| 239 | Samford | 0.001033 |
| 240 | Bryant University | 0.001028 |
| 241 | Davidson | 0.000998 |
| 242 | Morehead State | 0.000978 |
| 243 | Arkansas-Pine Bluff | 0.000925 |
| 244 | Drake | 0.000925 |

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|-----|---------------------------|----------|
| 245 | Mississippi Valley State | 0.000916 |
| 246 | Butler | 0.000910 |
| 247 | Iona | 0.000891 |
| 248 | Valparaiso | 0.000864 |
| 249 | Savannah State | 0.000838 |
| 250 | North Dakota | 0.000825 |
| 251 | Birmingham Southern | 0.000760 |
| 252 | Methodist | 0.000760 |
| 253 | Texas Southern | 0.000751 |
| 254 | South Dakota | 0.000670 |
| 255 | Campbell | 0.000513 |
| 256 | Chattanooga | 0.000513 |
| 257 | Angelo State | 0.000259 |
| 258 | Cumberland University | 0.000259 |
| 259 | Johnson Smith | 0.000259 |
| 260 | Langston | 0.000259 |
| 261 | North Greenville | 0.000259 |
| 262 | Culver-Stockton | 0.000259 |
| 263 | Virginia State | 0.000259 |
| 264 | Shaw | 0.000259 |
| 265 | Missouri S&T | 0.000259 |
| 266 | Montana-Western | 0.000259 |
| 267 | Faulkner | 0.000259 |
| 268 | Albion | 0.000259 |
| 269 | Clark Atlanta | 0.000259 |
| 270 | Lenoir-Rhyne | 0.000259 |
| 271 | Delta State | 0.000259 |
| 272 | Assumption | 0.000259 |
| 273 | Carthage | 0.000259 |
| 274 | Southwest Baptist | 0.000259 |
| 275 | Humboldt State | 0.000259 |
| 276 | East Central Oklahoma | 0.000259 |
| 277 | Baker University | 0.000259 |
| 278 | Southern Oregon | 0.000259 |
| 279 | Western Washington | 0.000259 |
| 280 | Concordia University (WI) | 0.000259 |
| 281 | Central State | 0.000259 |
| 282 | Washington | 0.000259 |
| 283 | Central Washington | 0.000259 |
| 284 | West Chester | 0.000259 |
| 285 | Bentley College | 0.000259 |
| 286 | St. Ambrose | 0.000259 |
| 287 | Texas A&M-Kingsville | 0.000259 |
| 288 | Lambuth | 0.000259 |
| 289 | Wisconsin-La Crosse | 0.000259 |
| 290 | St. Francis (PA) | 0.000259 |
| 291 | Quincy | 0.000259 |
| 292 | Dartmouth | 0.000259 |
| 293 | Glenville State | 0.000259 |
| 294 | Azusa Pacific | 0.000259 |
| 295 | Tusculum | 0.000259 |
| 296 | Southeastern Oklahoma | 0.000259 |
| 297 | Kentucky Wesleyan | 0.000259 |
| 298 | Indiana State | 0.000259 |
| 299 | Southern Virginia | 0.000259 |
| 300 | Dixie State | 0.000259 |
| 301 | William Penn | 0.000259 |
| 302 | Pace | 0.000259 |
| 303 | Lincoln (MO) | 0.000259 |
| 304 | Texas College | 0.000259 |
| 305 | Shorter | 0.000259 |
| 306 | Stillman | 0.000259 |

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| 307 | Morehouse | 0.000259 |
| 308 | New Mexico Highlands | 0.000259 |
| 309 | Merrimack | 0.000259 |
| 310 | Delaware Valley | 0.000259 |
| 311 | Chowan | 0.000259 |
| 312 | Texas A&M-Commerce | 0.000259 |
| 313 | Upper Iowa | 0.000259 |
| 314 | Mars Hill | 0.000259 |
| 315 | Webber International | 0.000259 |
| 316 | Central Methodist | 0.000259 |
| 317 | Concordia College | 0.000259 |
| 318 | Western Oregon | 0.000259 |
| 319 | Benedict | 0.000259 |
| 320 | West Georgia | 0.000259 |
| 321 | Southern Connecticut State | 0.000259 |
| 322 | Adams State | 0.000259 |
| 323 | Livingstone | 0.000259 |
| 324 | St. Cloud State | 0.000259 |

C. Dolphins Output

Data File: dolphinsDir.csv

Read Time: 0.00487 seconds

Processing Time: 0.00085 seconds

Number of Iterations: 8

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|-----------|-----------|
| 1 | TR88 | 0.001692 |
| 2 | TSN83 | 0.001602 |
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| 6 | Zipfel | 0.001279 |
| 7 | Stripes | 0.001153 |
| 8 | TSN103 | 0.001095 |
| 9 | Thumper | 0.001020 |
| 10 | TR99 | 0.000991 |
| 11 | Zig | 0.000958 |
| 12 | Vau | 0.000950 |
| 13 | SN4 | 0.000949 |
| 14 | Patchback | 0.000946 |
| 15 | SN63 | 0.000942 |
| 16 | SN89 | 0.000927 |
| 17 | Topless | 0.000927 |
| 18 | Trigger | 0.000923 |
| 19 | MN105 | 0.000893 |
| 20 | Shmuddel | 0.000859 |
| 21 | TR77 | 0.000824 |
| 22 | Kringel | 0.000789 |
| 23 | Scabs | 0.000776 |
| 24 | Quasi | 0.000770 |
| 25 | Mus | 0.000770 |
| 26 | MN23 | 0.000770 |
| 27 | SN9 | 0.000752 |
| 28 | Zap | 0.000751 |
| 29 | Notch | 0.000736 |
| 30 | Number1 | 0.000733 |
| 31 | Oscar | 0.000693 |
| 32 | MN83 | 0.000686 |

| | | |
|----|-------------|----------|
| 33 | Web | 0.000670 |
| 34 | PL | 0.000651 |
| 35 | Ripplefluke | 0.000634 |
| 36 | SN100 | 0.000612 |
| 37 | Jonah | 0.000583 |
| 38 | Hook | 0.000583 |
| 39 | SN96 | 0.000560 |
| 40 | SN90 | 0.000537 |
| 41 | Upbang | 0.000521 |
| 42 | Jet | 0.000488 |
| 43 | Gallatin | 0.000422 |
| 44 | Double | 0.000341 |
| 45 | Knit | 0.000341 |
| 46 | Fish | 0.000341 |
| 47 | Haecksel | 0.000341 |
| 48 | Grin | 0.000341 |
| 49 | Wave | 0.000341 |
| 50 | Feather | 0.000341 |
| 51 | Beescratch | 0.000151 |
| 52 | CCL | 0.000151 |
| 53 | DN63 | 0.000151 |
| 54 | MN60 | 0.000151 |
| 55 | Five | 0.000151 |
| 56 | TR82 | 0.000151 |
| 57 | DN21 | 0.000151 |
| 58 | Bumper | 0.000151 |
| 59 | Cross | 0.000151 |
| 60 | Beak | 0.000151 |
| 61 | DN16 | 0.000151 |
| 62 | Fork | 0.000151 |

D. Les Miserables Output

Data File: lesmisDir.csv

Read Time: 0.00619 seconds

Processing Time: 0.00096 seconds

Number of Iterations: 9

Damping Factor: 0.85

| Rank | Node | Page Rank |
|------|----------------|-----------|
| 1 | MmeHucheloup | 0.003446 |
| 2 | Grantaire | 0.003383 |
| 3 | Joly | 0.003242 |
| 4 | Bahorel | 0.003132 |
| 5 | MotherPlutarch | 0.003123 |
| 6 | Courfeyrac | 0.003024 |
| 7 | Bossuet | 0.003022 |
| 8 | Feuilly | 0.002979 |
| 9 | Prouvaire | 0.002867 |
| 10 | Combeferre | 0.002774 |
| 11 | Brujon | 0.002710 |
| 12 | MmePontmercy | 0.002632 |
| 13 | Mabeuf | 0.002594 |
| 14 | Child2 | 0.002586 |
| 15 | Montparnasse | 0.002485 |
| 16 | BaronessT | 0.002482 |
| 17 | Claquesous | 0.002458 |
| 18 | Gribier | 0.002447 |
| 19 | MlleVaubois | 0.002429 |
| 20 | Enjolras | 0.002414 |

| | | |
|----|------------------|----------|
| 21 | Cochepaille | 0.002413 |
| 22 | Anzelma | 0.002412 |
| 23 | Child1 | 0.002329 |
| 24 | Boulatruelle | 0.002327 |
| 25 | Pontmercy | 0.002327 |
| 26 | Chenildieu | 0.002326 |
| 27 | Babet | 0.002318 |
| 28 | LtGillenormand | 0.002273 |
| 29 | Gueulemer | 0.002246 |
| 30 | Eponine | 0.002243 |
| 31 | Brevet | 0.002223 |
| 32 | Magnon | 0.002209 |
| 33 | Marius | 0.002200 |
| 34 | Champpathieu | 0.002097 |
| 35 | Simplice | 0.002071 |
| 36 | Toussaint | 0.002015 |
| 37 | Woman2 | 0.002015 |
| 38 | Javert | 0.001996 |
| 39 | Fauchelevant | 0.001957 |
| 40 | Woman1 | 0.001957 |
| 41 | Bamatabois | 0.001951 |
| 42 | MlleGillenormand | 0.001939 |
| 43 | Perpetue | 0.001938 |
| 44 | MotherInnocent | 0.001936 |
| 45 | Judge | 0.001933 |
| 46 | Gavroche | 0.001846 |
| 47 | Thenardier | 0.001841 |
| 48 | Gillenormand | 0.001779 |
| 49 | MmeThenardier | 0.001681 |
| 50 | Cosette | 0.001661 |
| 51 | Fantine | 0.001473 |
| 52 | Marguerite | 0.001425 |
| 53 | Isabeau | 0.001425 |
| 54 | Gervais | 0.001425 |
| 55 | MmeDeR | 0.001425 |
| 56 | Scaufflaire | 0.001425 |
| 57 | Zephine | 0.001355 |
| 58 | Dahlia | 0.001280 |
| 59 | Favourite | 0.001191 |
| 60 | Blacheville | 0.001081 |
| 61 | Valjean | 0.000994 |
| 62 | Fameuil | 0.000939 |
| 63 | MmeMagloire | 0.000939 |
| 64 | MmeBurgon | 0.000734 |
| 65 | Champtercier | 0.000734 |
| 66 | MlleBaptistine | 0.000734 |
| 67 | Count | 0.000734 |
| 68 | OldMan | 0.000734 |
| 69 | Cravatte | 0.000734 |
| 70 | Listolier | 0.000734 |
| 71 | Geborand | 0.000734 |
| 72 | CountessDeLo | 0.000734 |
| 73 | Napoleon | 0.000734 |
| 74 | Labarre | 0.000354 |
| 75 | Tholomyes | 0.000354 |
| 76 | Jondrette | 0.000354 |
| 77 | Myriel | 0.000354 |