

1. $x = \text{skull and bones}$ $y = \text{lullaby babies}$

| | | s | k | u | l | l | a | n | d | b | o | n | e | s |
|----------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| lcs[,] | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| l | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| u | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| l | 0 | 0 | 0 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
| l | 0 | 0 | 0 | 1 | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
| a | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| b | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| y | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| b | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| a | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| b | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| i | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 5 | 5 | 5 |
| e | 0 | 0 | 0 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 6 | 6 | 6 |
| s | 0 | 1 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 5 | 5 | 6 | 7 | 7 |

u l l a b e s

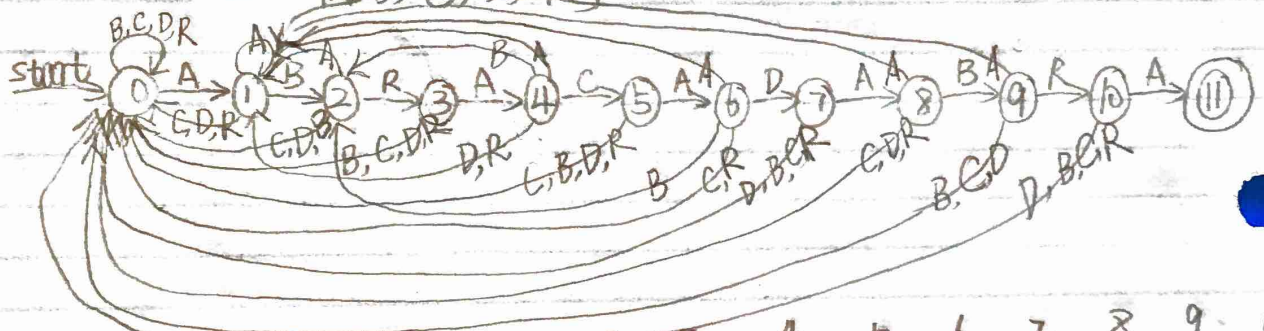
\therefore the longest common subsequence of the two strings is: u l l a b e s

- 2.
- ① Create a character array to store the lcs string lcs[]
 - ② Start from the right most bottom corner and one by one check and store character in lcs[]
 - ③ If current character in x[] and y[] are same, then current character is part of LCS
 - ④ If not same, then find the larger of $L[i-1][j]$ and $L[i][j-1]$ and go in the direction of larger value.
 - ④ print lcs[].

3. (a) ABRACADABRA = pattern
 $\Sigma = \{A, B, C, D, R\}$

| | | A | B | R | A | C | A | D | A | B | R | A | |
|---|----|---|---|---|---|---|---|---|---|---|---|----|-----------|
| C | | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | right [c] |
| A | -1 | 0 | | | 3 | | 5 | | 7 | | | 10 | 10 |
| B | -1 | | 1 | | | | | | | 8 | | | 8 |
| C | -1 | | | | | 4 | | | | | | | 4 |
| D | -1 | | | | | | | 6 | | | | | 6 |
| R | -1 | | | 2 | | | | | | | 9 | | 9 |

(b) pattern ABRACADABRA
 $\Sigma = \{A, B, C, D, R\}$



| dfa [] [] | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|-------------|---|---|---|---|---|---|---|---|---|----|----|
| A | 1 | 1 | 1 | 4 | 1 | 6 | 1 | 8 | 1 | 1 | 11 |
| B | 0 | 2 | 0 | 0 | 2 | 0 | 2 | 0 | 9 | 0 | 0 |
| C | 0 | 0 | 0 | 0 | 5 | 0 | 0 | 0 | 0 | 0 | 0 |
| D | 0 | 0 | 0 | 0 | 0 | 0 | 7 | 0 | 0 | 0 | 0 |
| R | 0 | 0 | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 10 | 0 |

4. import java.util.*;

class Blah {

public static void main(String args[]) {
String txt;

int M;

Scanner s = new Scanner(System.in);

System.out.println("enter string and value for M

txt = s.nextLine();

M = s.nextInt();

int length = txt.length();

int j = 0;

int i = 0;

while (i < length) {

if (txt.charAt(i) == ' ')

i = j;

while (j < length) {

if (txt.charAt(j) == ' ')

j = j + 1;

else {

break;

}

}

if (j - i >= M) {

System.out.println("string found
at " + i);

break;

}

i = j;

} else {

i = i + 1;

}

}

if (i == 1) {

System.out.println("string not found and
length = " + i);

}

Analysis Running time

charAt() \rightarrow constant time

of iteration $\rightarrow n$

\therefore it's $O(n)$

5. $T = \text{text}$
 $p = \text{Pattern}$
 $d = \text{domain of letters of characters}$
 $q = \text{prime number}$
 $k = k^{\text{th}} \text{ character of Pattern}$

Algorithm:

```

 $n = T.\text{length}$ 
 $m = p.\text{length}$ 
 $h = d^{m-1} \bmod q$ 
 $p = 0$ 
 $t_0 = 0$ 
for  $i = 1$  to  $M$ 
    if  $(i \neq k)$ 
         $p = (d \cdot p + p[i]) \% q$ 
         $t_0 = (d \cdot t_0 + T[i]) \% q$ 
for  $s = 0$  to  $n - m$ 
    if  $p = t_s$ 
        for  $j = 1$  to  $M$ 
            if  $j \neq k \ \&\& \ T[s+j] \neq p[j]$ 
                break;
        if  $j == M$ 
            print "Pattern occurs with s"
    if  $s < n - m$ 
         $t_{s+1} = (d(t_s - T[s+1] \cdot h) + T[s+m+1]) \bmod q$ 
         $t_{s+1} = [d(t_s - T[s+k+1] \cdot h) + T[s+k]] \bmod q$ 

```