

```

1 import numpy as np
2
3
4 def sigmoid(x):
5     return 1 / (1 + np.exp(-x))
6
7
8 def sigmoid_derivative(x):
9     return x * (1 - x)
10
11
12 def train_xor_nn(epochs=100_000, learning_rate=0.1):
13     # XOR input dataset
14     X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
15     # XOR output dataset
16     y = np.array([[0], [1], [1], [0]])
17
18     # Initialize weights and biases randomly
19     np.random.seed(0)
20     input_size, hidden_size, output_size = 2, 2, 1
21     W1 = np.random.uniform(-1, 1, (input_size, hidden_size))
22     b1 = np.random.uniform(-1, 1, (1, hidden_size))
23     W2 = np.random.uniform(-1, 1, (hidden_size, output_size))
24     b2 = np.random.uniform(-1, 1, (1, output_size))
25
26     for epoch in range(epochs):
27         # Forward pass
28         hidden_input = np.dot(X, W1) + b1
29         hidden_output = sigmoid(hidden_input)
30         final_input = np.dot(hidden_output, W2) + b2
31         final_output = sigmoid(final_input)
32
33         # Compute error
34         error = y - final_output
35
36         # Backpropagation
37         d_output = error * sigmoid_derivative(final_output)
38         d_hidden = np.dot(d_output, W2.T) * sigmoid_derivative(hidden_output)
39
40         # Update weights and biases
41         W2 += np.dot(hidden_output.T, d_output) * learning_rate
42         b2 += np.sum(d_output, axis=0, keepdims=True) * learning_rate
43         W1 += np.dot(X.T, d_hidden) * learning_rate
44         b1 += np.sum(d_hidden, axis=0, keepdims=True) * learning_rate
45
46         if epoch % 1000 == 0:
47             loss = np.mean(np.abs(error))
48             print(f"Epoch {epoch}, Loss: {loss}")
49
50     return W1, b1, W2, b2
51
52
53 def predict(X, W1, b1, W2, b2):
54     hidden_output = sigmoid(np.dot(X, W1) + b1)
55     final_output = sigmoid(np.dot(hidden_output, W2) + b2)
56     return np.round(final_output)
57
58
59 # Train the neural network
60 W1, b1, W2, b2 = train_xor_nn()

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61
62 # Test the trained model
63 X_test = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
64 y_pred = predict(X_test, W1, b1, W2, b2)
65 print("Predictions:", y_pred.flatten())
66 print("Exact Predictions:", y_pred)
67
```