

 $\label{eq:Figure 1: Multi-head Attention.}$

$$A^{[D],[\ell]} = [A_0^{[d],[\ell]} | A_1^{[d],[\ell]} | A_2^{[d],[\ell]}]$$
(1a)

$$A_0^{[d],[\ell]} = \text{scaled_dot_prod_att}(Q_0^{[d],[\ell]}, K_0^{[d],[\ell]}, V_0^{[d],[\ell]})$$
(1b)

$$A_1^{[d],[\ell]} = \text{scaled_dot_prod_att}(Q_1^{[d],[\ell]}, K_1^{[d],[\ell]}, V_1^{[d],[\ell]})$$
(1c)

$$A_2^{[d],[\ell]} = \text{scaled_dot_prod_att}(Q_2^{[d],[\ell]}, K_2^{[d],[\ell]}, V_2^{[d],[\ell]}) \tag{1d}$$

$$K^{[D],[\ell]} = W_k^{[D],[d]} e^{[d],[\ell]}$$
 (1e)

$$K_0^{[d],[\ell]} = \operatorname{linear}(K^{[D],[\ell]})$$
 (split, then project a component) (1f)

$$K_1^{[d],[\ell]} = \operatorname{linear}(K^{[D],[\ell]})$$
 (split, then project a component) (1g)

$$K_2^{[d],[\ell]} = \text{linear}(K^{[D],[\ell]})$$
 (split, then project a component) (1h)

$$O^{[D],[\ell]} = W_{\underline{o}}^{[D],[D]} A^{[D],[\ell]}$$
(1i)

$$Q^{[D],[\ell]} = W_q^{[D],[d]} e^{[d],[\ell]}$$
(1j)

$$Q_0^{[d],[\ell]} = \text{linear}(Q^{[D],[\ell]}) \text{ (split, then project a component)}$$
 (1k)

$$Q_1^{[d],[\ell]} = \operatorname{linear}(Q^{[D],[\ell]}) \text{ (split, then project a component)}$$
 (11)

$$Q_2^{[d],[\ell]} = \text{linear}(Q^{[D],[\ell]}) \text{ (split, then project a component)}$$
 (1m)

$$V^{[D],[\ell]} = W_v^{[D],[d]} e^{[d],[\ell]}$$
(1n)

$$V_0^{[d],[\ell]} = \text{linear}(V^{[D],[\ell]}) \text{ (split, then project a component)}$$
 (10)

$$V_1^{[d],[\ell]} = \operatorname{linear}(V^{[D],[\ell]}) \text{ (split, then project a component)} \tag{1p}$$

$$V_2^{[d],[\ell]} = \text{linear}(V^{[D],[\ell]})$$
 (split, then project a component) (1q)

$$e^{[d],[\ell]} = \text{prior}$$
 (1r)