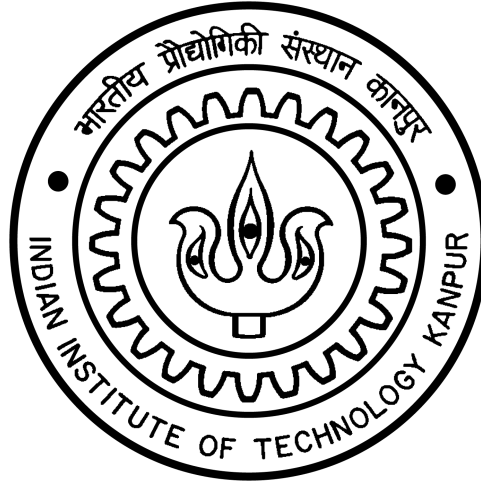


MPC BASED AUTONOMOUS LANDING OF MAV ON A MOVING PLATFORM



Instructor :- Dr. Indranil Saha

Course :- **CS637** (Fall 2022-23)

Contributor :- Rahul Rustagi, B.Anshuman, Shubham Kumar
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Related Links:

[LINK OF REFERRED LITERATURE](#)

[LINK OF IMPLEMENTATION](#)

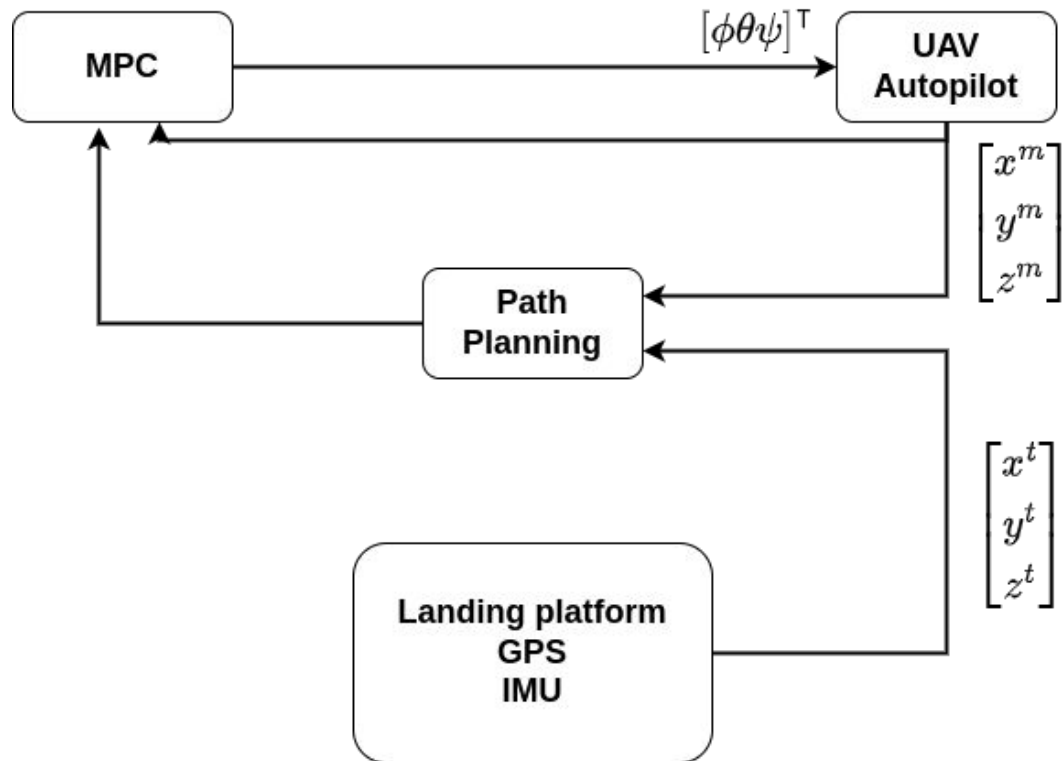
INTRODUCTION

- Autonomous landing of unmanned aerial vehicles (UAVs) on moving targets has the potential to resolve many limitations.
- Here we present an MPC-based guidance and control system for a MAV to land autonomously on a moving landing platform under dynamic uncertainties

RELATED WORK

- An extended back-stepping [nonlinear control for landing rotary wing UAVs](#) that are attached to their mobile platforms via tethers has been implemented
- Learning based and intelligent control methods such as [fuzzy logic based controllers](#) and adaptive neural networks have also been employed to achieve optimal control policies under uncertainties and disturbances
- However, a control loop for model predictive controller (MPC) would be a better choice for this application

APPROACH



MODEL DYNAMICS

- The UAV dynamics are governed by Newton-Euler equations.

$$ma = \begin{bmatrix} 0 \\ 0 \\ mg \end{bmatrix} + R_B^W \begin{bmatrix} 0 \\ 0 \\ -T \end{bmatrix} + F_D$$

- Using the roll pitch and altitude parametrization.

$$m \begin{bmatrix} \ddot{p}^n \\ \ddot{p}^e \\ \ddot{p}^d \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ mg \end{bmatrix} - \begin{bmatrix} C_\phi S_\theta C_\psi + S_\phi S_\psi \\ C_\phi S_\theta S_\psi + S_\phi C_\psi \\ C_\phi C_\theta \end{bmatrix} T - k_d \begin{bmatrix} \dot{p}^n \|\dot{p}^n\| \\ \dot{p}^e \|\dot{p}^e\| \\ \dot{p}^d \|\dot{p}^d\| \end{bmatrix}$$

- For constant flight altitude we have $\ddot{p}^d = 0$ and $\dot{p}^d = 0$. Further assuming $\psi = 0$ and $T = mg/C_\phi C_\theta$.

$$m \begin{bmatrix} \ddot{p}^n \\ \ddot{p}^e \end{bmatrix} = mg \begin{bmatrix} -\tan\theta \\ \tan\phi/\cos\theta \end{bmatrix} - k_d \begin{bmatrix} \dot{p}^n \|\dot{p}^n\| \\ \dot{p}^e \|\dot{p}^e\| \end{bmatrix}$$

- Under the assumption of non aggressive maneuvers, the state of the UAV remain near equilibrium point($\theta = 0$, $\phi = 0$).Linearizing the dynamics about this point.

$$\begin{bmatrix} \ddot{p}^n \\ \ddot{p}^e \end{bmatrix} = -k_d/m \begin{bmatrix} \dot{p}^n \|\dot{p}^n\| \\ \dot{p}^e \|\dot{p}^e\| \end{bmatrix} + g \begin{bmatrix} -\theta \\ \phi \end{bmatrix}$$

- Finally the state representation of the linearized dynamics of the UAV can be written as :

$$\dot{x}^m = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & -k_d/m0 & \\ 0 & 0 & 0 & -k_d/m \end{bmatrix} x^m + \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ -g & 0 \\ 0 & g \end{bmatrix} u$$

- Where $u = [\theta \ \phi]^T$ is the input to the system and $x_k = [p_k^{m,n} \ p_k^{m,e} \ \ddot{p}_k^{m,n} \ \ddot{p}_k^{m,e}]^T$ represents the state vector of the UAV dynamics.

MODEL PREDICTIVE CONTROL

- We have used a linear MPC control for controlling the motion of the drone
- The predicted state with m calculated future control inputs are given by

$$x_{k+p} = A^p x_k + A^{p-1} B u_k + \dots + B u_{k+m-1} = A^p x_k + A^{p-m} \sum_{i=1}^m A^{i-1} B u_{k+m-i}$$

Where $x_k = \begin{bmatrix} p_k^{m,n} & p_k^{m,e} & \dot{p}_k^{m,n} & \dot{p}_k^{m,e} \end{bmatrix}^T$

Where x_{k+p} is the P -step prediction of the state at time k with $p > m$.
Hence, the augmented state predictions are

$$X = S^x x_k + S^u u_m$$

- The quadratic cost function used in this work is formulated as :

$$j_k = q\tilde{x}^T Q \tilde{x} + (1 - q)u_m^T R u_m$$

$$\tilde{x} = r_p - X$$

Here Q and R are state and input weights matrices.

IMPLEMENTATION

File Panels Help

Interact Move Camera Select Focus Camera Measure 2D Pose Estimate 2D Nav Goal Publish Point

Displays

Links	
Link Tree Style	Links in Alphabetic Order
Expand Link Details	<input type="checkbox"/>
All Links Enabled	<input checked="" type="checkbox"/>
base_footprint	<input checked="" type="checkbox"/>
base_link	<input checked="" type="checkbox"/>
front_bumper_link	<input checked="" type="checkbox"/>
front_left_wheel_link	<input checked="" type="checkbox"/>
front_right_wheel_link	<input checked="" type="checkbox"/>
imu_link	<input checked="" type="checkbox"/>
inertial_link	<input checked="" type="checkbox"/>
rear_bumper_link	<input checked="" type="checkbox"/>
rear_left_wheel_link	<input checked="" type="checkbox"/>
rear_right_wheel_link	<input checked="" type="checkbox"/>
top_chassis_link	<input checked="" type="checkbox"/>
top_plate_front_link	<input checked="" type="checkbox"/>
top_plate_link	<input checked="" type="checkbox"/>
Alpha	1
Show Trail	<input type="checkbox"/>
Show Axes	<input type="checkbox"/>
Position	0.0812; 0; 0.245
Orientation	0; 0; 1
top_plate_rear_link	<input checked="" type="checkbox"/>
user_rail_link	<input checked="" type="checkbox"/>
TF	
Status: Ok	<input checked="" type="checkbox"/>
Show Names	<input checked="" type="checkbox"/>
Show Axes	<input checked="" type="checkbox"/>
Show Arrows	<input type="checkbox"/>
Marker Scale	0.5
Update Interval	0
Frame Timeout	15
Frames	
Tree	

user_rail_link

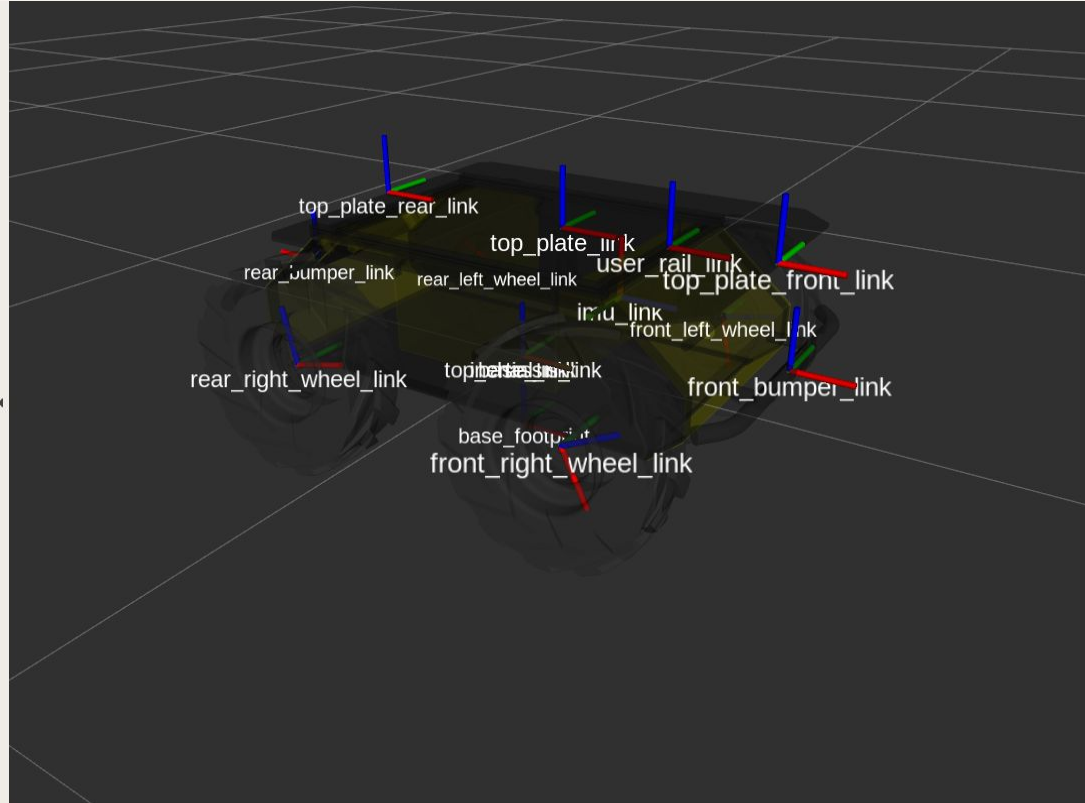
Link **user_rail_link** with parent joint **user_rail** has no children. Check/uncheck to show/hide this link in the display. This link has visible geometry but no collision geometry.

Add

Duplicate

Remove

Rename



Views

Type: Orbit (rviz) Zero

Current View: Orbit (rviz)	
Near Clipping	0.01
Invert Near	<input type="checkbox"/>
Target Frame	<Fixed Frame>
Distance	1.76684
Focal Length	0.05
Focal Point	<input checked="" type="checkbox"/>
Yaw	5.27176
Pitch	0.470396
Focal Point	0.039862; 0.043104...

Save

Remove

Rename

Time

ROS Time: 1666813152.39 ROS Elapsed: 201.42 Wall Time: 1666813152.42 Wall Elapsed: 201.36

Reset Left-Click: Rotate. Middle-Click: Move X/Y. Right-Click/Mouse Wheel: Zoom. Shift: More options.

☐ Experimental

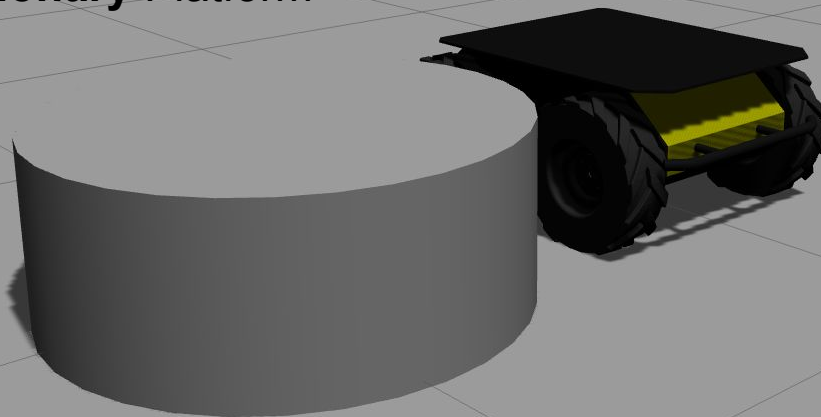
31 fps

World Insert Layers

- ▼ ground_plane
 - LINKS
 - link
 - ▶ firefly
 - ▼ husky
 - LINKS
 - base_link
 - front_left_wheel_link
 - front_right_wheel_link
 - rear_left_wheel_link
 - rear_right_wheel_link
 - JOINTS
 - front_left_wheel

Property	Value
name	ground_plane
is_static	<input checked="" type="checkbox"/> True
self_collide	<input type="checkbox"/> False
enable_wind	<input type="checkbox"/> False
▶ pose	
▶ link	ground_plane::link

Testing Landing on
Stationary Platform

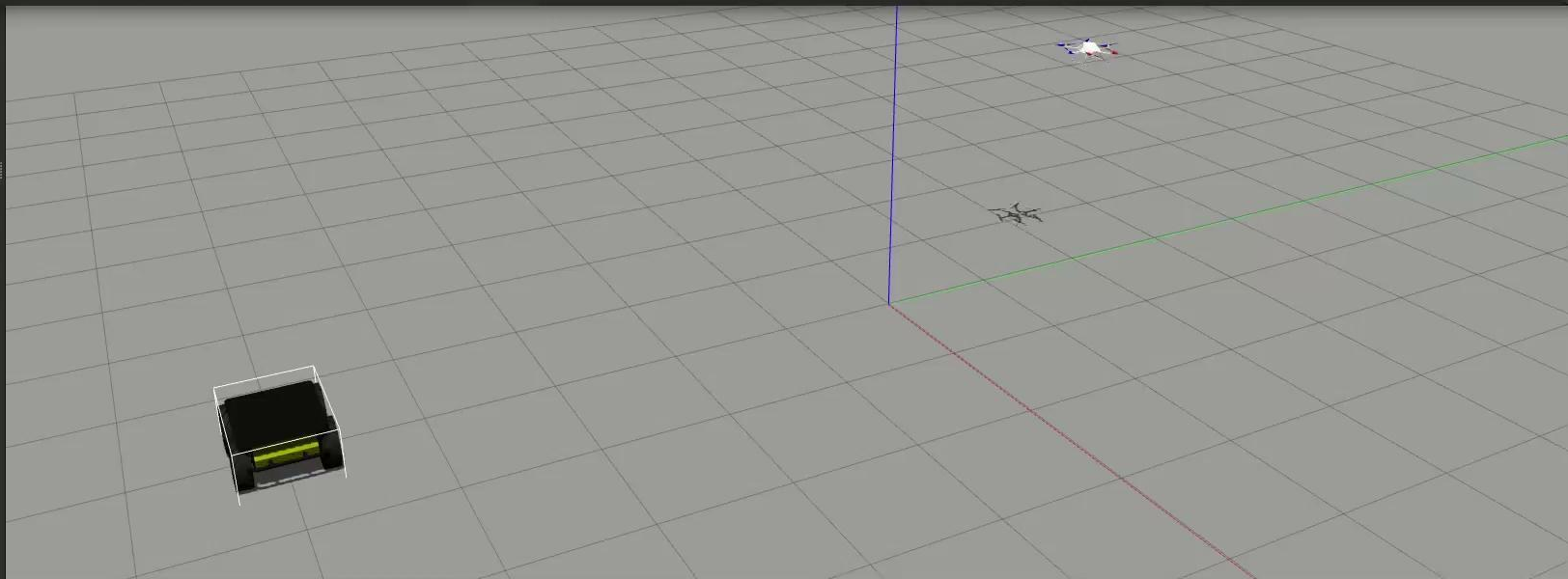


```
→ workspace git:(main) X rosservice call /gazebo/reset_world
```

UAV_Launch MPC_Launch UGV_Launch publish_reset_ control **reset**

LINKS

Property	Value
name	husky
is_static	<input type="checkbox"/> False
self_coll...	<input type="checkbox"/> False
enable_...	<input type="checkbox"/> False
▶ pose	
▶ link	husky::base ...
▶ link	husky::front_l...
▶ link	husky::front_...
▶ link	husky::rear_l...
▶ link	husky::rear_r...

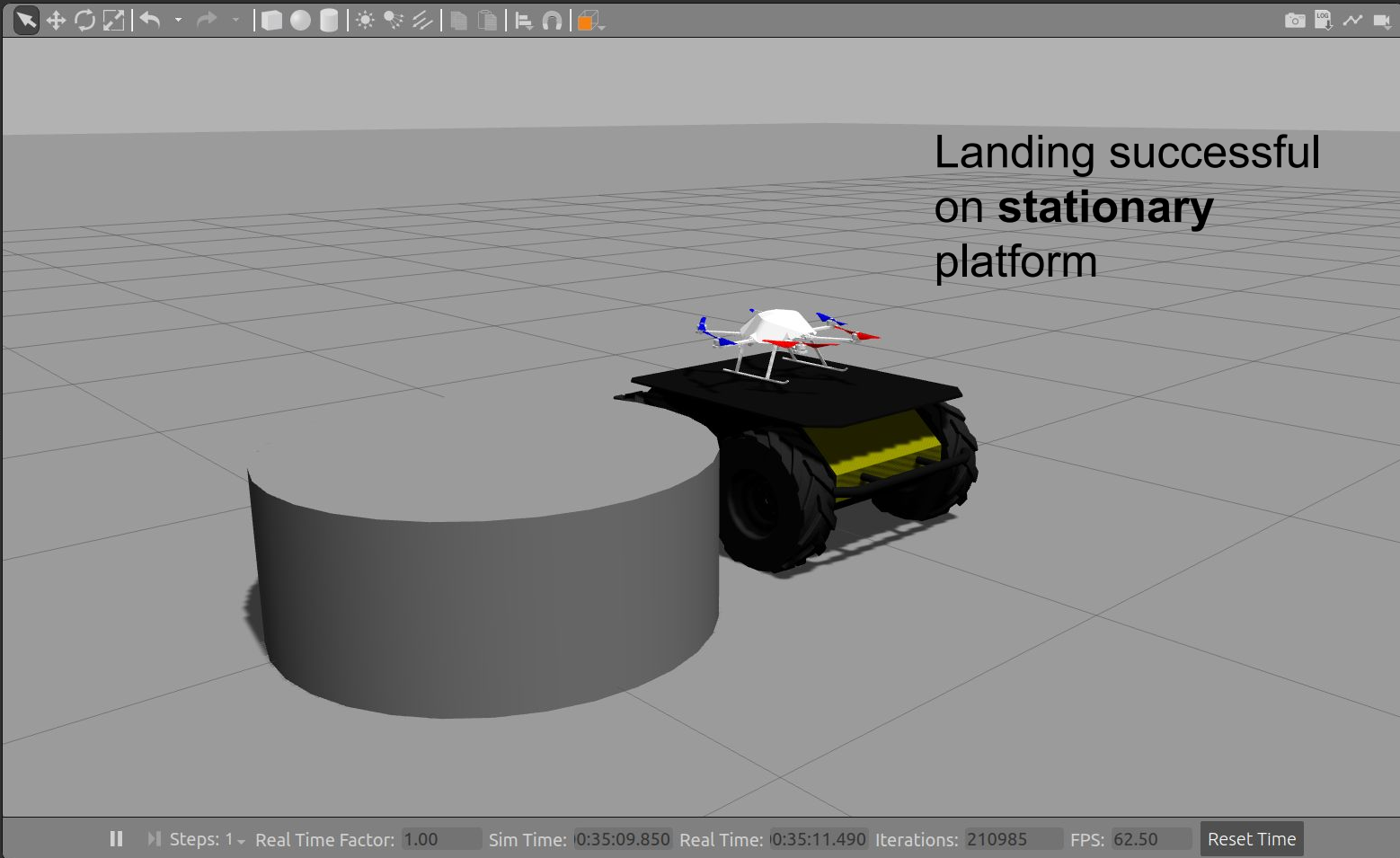


|| ▶ Steps: 1 ▾ Real Time Factor: 1.00 Sim Time: 0:59:16.740 Real Time: 0:59:19.063 Iterations: 355674 FPS: 62.54 Reset Time

World Insert Layers

- ground_plane
 - LINKS
 - link
 - firefly
 - husky
 - LINKS
 - base_link
 - front_left_wheel_link
 - front_right_wheel_link
 - rear_left_wheel_link
 - rear_right_wheel_link
 - JOINTS
 - front_left_wheel

Property	Value
name	ground_plane
is_static	<input checked="" type="checkbox"/> True
self_collide	<input type="checkbox"/> False
enable_wind	<input type="checkbox"/> False
pose	
link	ground_plane::link




```
[ INFO] [1666846426.157115332, 3898.130000000]: UGV: 3.436565 8.459305 0.490000
[ INFO] [1666846426.157175328, 3898.130000000]: UAV: 4.092339 8.214300 0.749085
[ INFO] [1666846426.157205360, 3898.130000000]: To go to: 3.108678 8.581807 0.360458
[ INFO] [1666846426.206219158, 3898.180000000]: UGV: 3.397203 8.469800 0.490000
[ INFO] [1666846426.206269655, 3898.180000000]: UAV: 4.041045 8.234704 0.743613
[ INFO] [1666846426.206288792, 3898.180000000]: To go to: 3.075282 8.587348 0.363193
[ INFO] [1666846426.259540991, 3898.230000000]: UGV: 3.364462 8.477951 0.490000
[ INFO] [1666846426.259587228, 3898.230000000]: UAV: 4.006863 8.248296 0.740763
[ INFO] [1666846426.259604479, 3898.230000000]: To go to: 3.043262 8.592779 0.364619
```

Models

ground_plane

LINKS

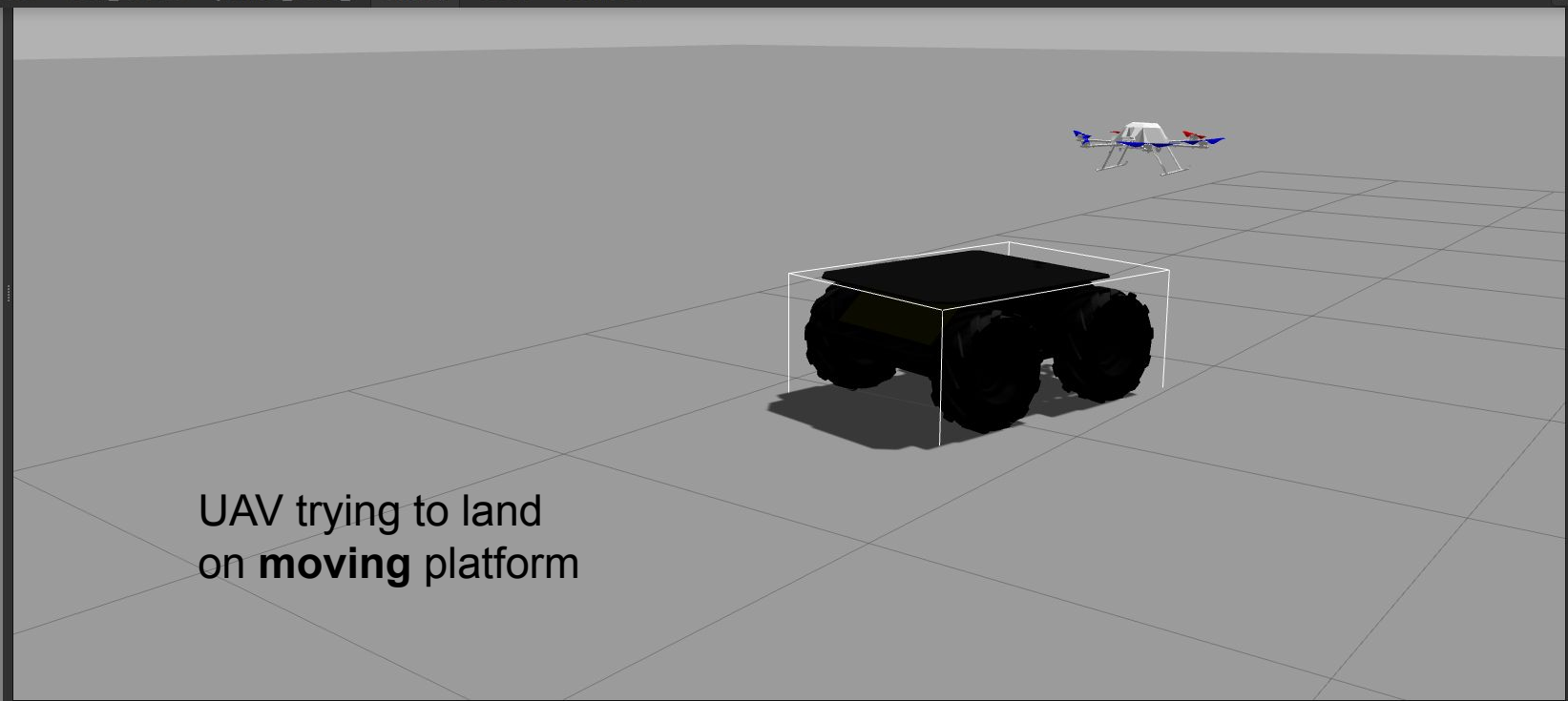
link

firefly

husky

LINKS

Property	Value
name	husky
is_static	<input type="checkbox"/> False
self_coll...	<input type="checkbox"/> False
enable_...	<input type="checkbox"/> False
pose	
link	husky::base_...
link	husky::front_l...
link	husky::front_...
link	husky::rear_l...
link	husky::rear_r...



UAV trying to land
on **moving** platform


```
→ workspace git:(main) X rosservice call /gazebo/reset_world
```

```
→ workspace git:(main) X rosservice call /gazebo/reset_world
```

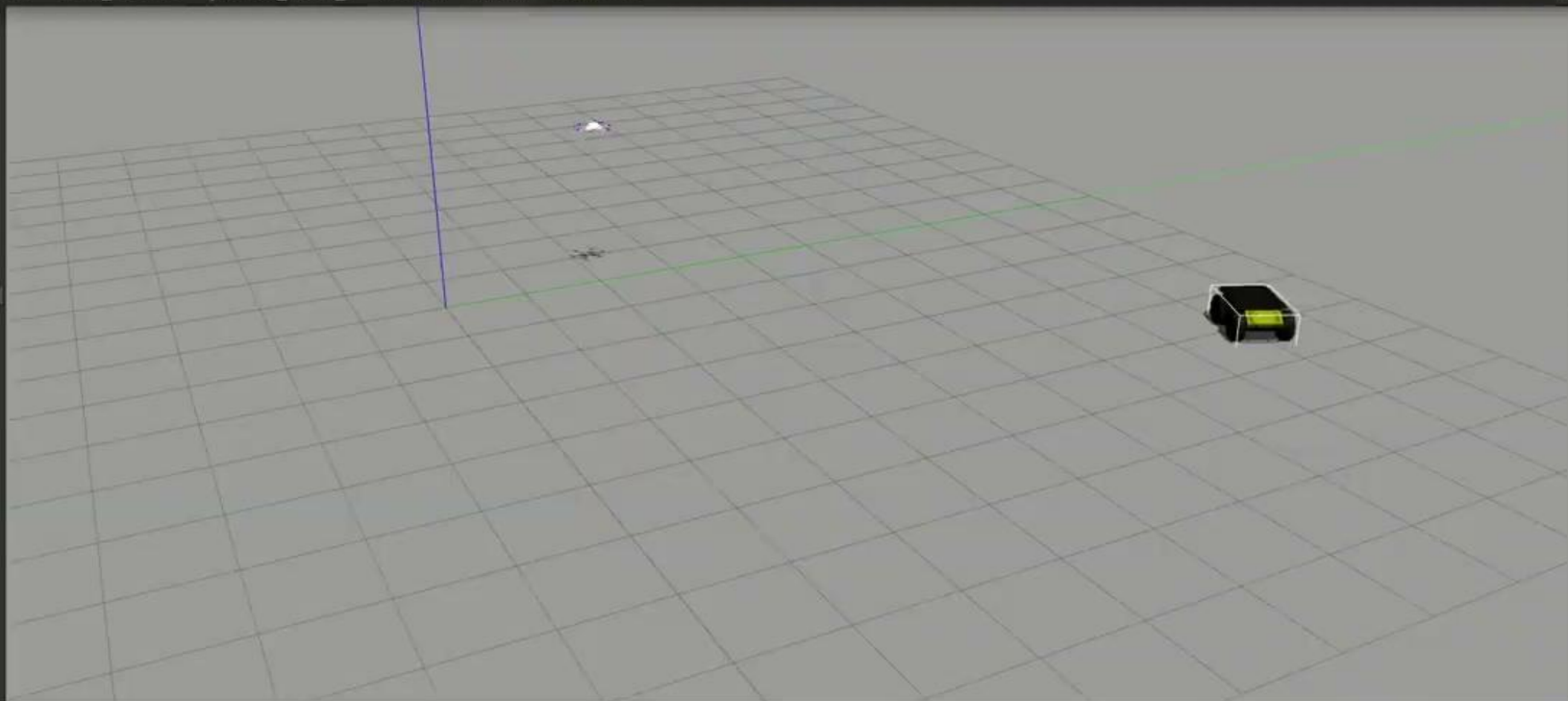
```
→ workspace git:(main) X
```

UAV_Launch MPC_Launch UGV_Launch publish_reset_ control **reset** Terminal

Models

- ground_plane
 - LINKS
 - link
- firefly
- husky
 - LINKS

Property	Value
name	husky
is_static	<input type="checkbox"/> False
self_coll...	<input type="checkbox"/> False
enable_...	<input type="checkbox"/> False
pose	
link	husky::base ...
link	husky::front_l ...
link	husky::front ...
link	husky::rear_l ...
link	husky::rear_f ...



Steps: 1 - Real Time Factor: 1.00

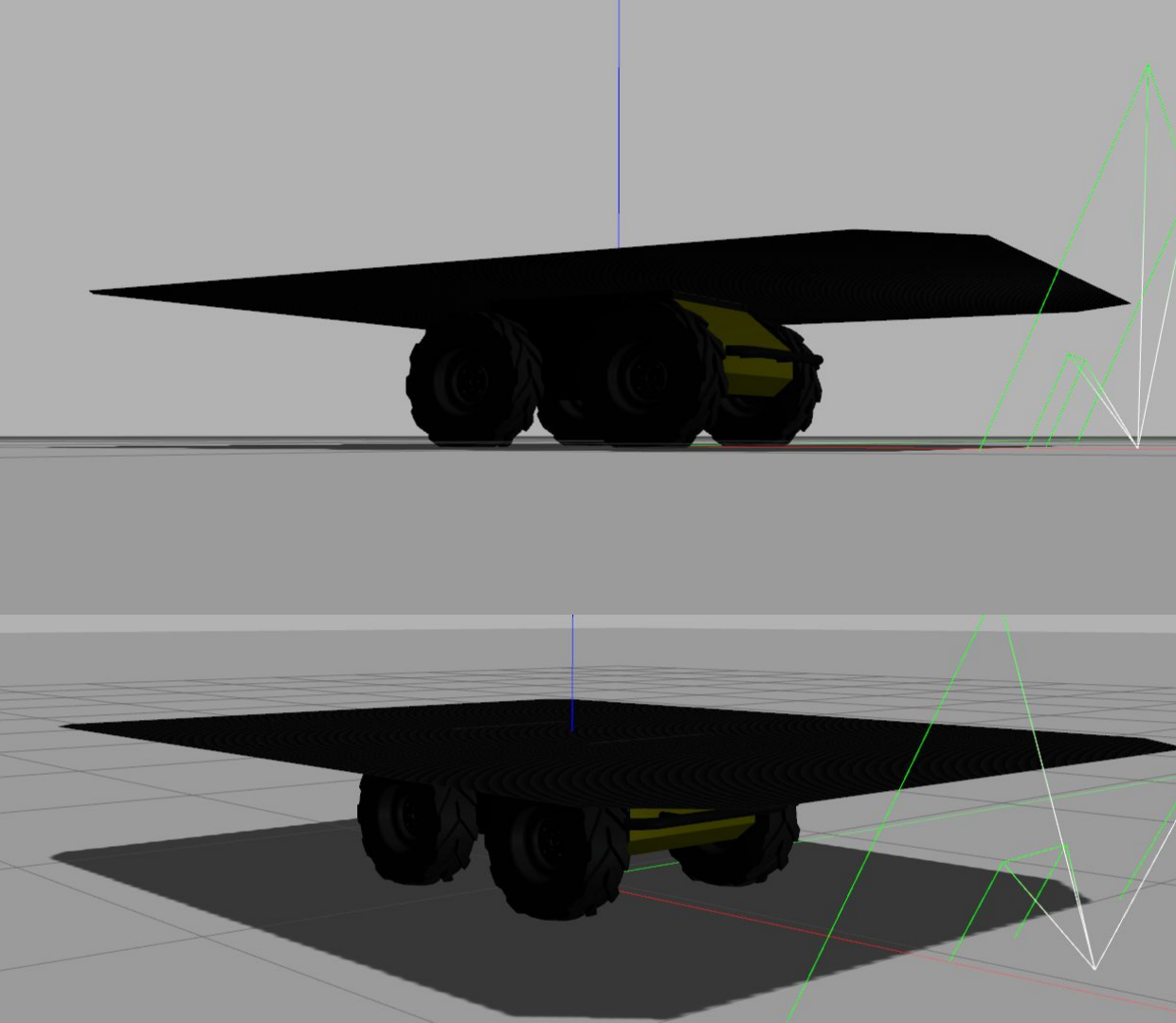
Sim Time: 11:04:07.880

Real Time: 11:04:10.389

Iterations: 384788

FPS: 62.51

Reset Time



Integrated a large plate on top of moving platform

ToDo:
Implementing a robust path planning problem to achieve landing on the **moving** platform

Summary

- Literature review of Model Predictive Control
- Used MPC for position control of UAV
- Integrated path planning with MPC for autonomous landing
- Implemented stationary and moving platform with coded trajectory
- Integrated and Simulated the modules in gazebo

Further Work

- Used an extended platform for giving more margin for the UAV to land on.
- Included platform path predictive aspect for avoiding steady state chasing of platform.
- Tried using Velocity control through MPC for the above problem.
- Implemented 3 trajectory planning algorithms:
 - XY-approach then changing altitude once XY-radius is within a threshold.
 - Half waypoint approach that directs the next position be the midpoint of UAV and platform pose.
 - 1/k waypoint approach that extends the above idea.

Contribution

- Shubham Kumar - Read Literature on MPC, prepared presentation and integrated modules
- Rahul Rustagi - Implemented stationary/moving platform and coded platform trajectory
- B.Anshuman - Created pipeline for using MPC, and implemented UAV trajectory