

Robotic Vision

Assignment #3

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A1. ${}^c_c t = [4, -1, 3]^T$

${}^c_c R = R_y, -\pi/2$

$\therefore {}^{c'}_c t = [-4, 1, 3]^T$

${}^{c'}_c R = R_y, \pi/2$

f_screw ()

$$\begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix} = \begin{bmatrix} 0 & -t_z & t_y \\ t_z & 0 & t_x \\ -t_y & t_x & 0 \end{bmatrix}$$

$${}^c_c R = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

$$\therefore \begin{bmatrix} {}^c_c R \\ {}^c_c t \end{bmatrix}^T = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix} \quad \& \quad \begin{bmatrix} {}^c_c t \\ {}^c_c R \end{bmatrix}_x = \begin{bmatrix} 0 & 3 & 1 \\ -3 & 0 & 4 \\ -1 & -4 & 0 \end{bmatrix}$$

Given $K = \begin{bmatrix} 100 & 0 & 250 \\ 0 & 100 & 250 \\ 0 & 0 & 1 \end{bmatrix}$

Now we know $E = \begin{bmatrix} {}^c_c t \\ {}^c_c R \end{bmatrix}_x {}^c_c R$

$$\therefore E = \begin{bmatrix} 0 & 3 & 1 \\ -3 & 0 & 4 \\ -1 & 4 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix} = \begin{bmatrix} -1 & 3 & 0 \\ 4 & 0 & -3 \\ 0 & 4 & -1 \end{bmatrix}$$

2. To find co-ordinates in pixels for epipoles e & e' corresponding to $\{c\}$ & $\{c'\}$, the condition is

$$E \cdot p_e = 0 \quad \& \quad E^T \cdot p_{e'} = 0 \quad \& \quad e = K \cdot p_e \quad \& \quad e' = K \cdot p_{e'}$$

$$\therefore p_e = \text{null}(E),$$

$$p_e = p_e / p_e(3);$$

$$e = K * p_e;$$

\therefore using the above lines of code in matlab, we find

$$e = [125, 225]^T$$

$$\& \quad e' = [333.33, 216.67]^T;$$