Pustaka GPU-Cuda Untuk Poisson Solver 3D Dalam Koordinat Silinder



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PoissonSolver3DCylindricalGPU

PoissonSolver3D adalah pustaka yang dikembangkan untuk menyelesaikan persamaan Poisson 3 dimensi dalam sistem koordinat silinder. Persamaan Poisson secara umum berbentuk $\nabla^2(r,\phi,z)=\rho(r,\phi,z)$ dengan diketahui nilai tepi pada potensial ${\bf V}$ dan distribusi buatan ρ .

Untuk menyelesaikan persamaan tersebut digunakan metode multigrid yang diimplementasikan pada akselerator GPU.

Pengembang

Pustaka ini dikembangkan oleh Kelompok Penelitian Komputasi Kinerja Tinggi, Pusat Penelitian Informatika, Lembaga Ilmu Pengetahuan Indonesia. Tim pengembang terdiri dari:

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Dokumentasi

Petunjuk penggunaan dapat dilihat pada berkas PETUNJUKPENGGUNAAN.md

Petunjuk Penggunaan

```
pembuat : Rifki Sadikin (rifki.sadikin@lipi.go.id)
tanggal : 6 November 2018
```

Petunjuk penggunaan ini berisi:

- Cara **membuat** dan **menginstal** Pustaka Pemercepat Komputasi berbasis GPU CUDA untuk Penyelesaian Persamaan *Poisson* dalam Koordinat Silindrikal.
- Cara memakai Pustaka Pemercepat Komputasi berbasis GPU CUDA untuk Penyelesaian Persamaan Poisson dalam Koordinat Silindrikal dalam C++.

Struktur Berkas

Struktur berkas pustaka Pemercepat Komputasi berbasis GPU CUDA untuk Penyelesaian Persamaan *Poisson* dalam Koordinat Silindrikal adalah sebagai berikut:

```
|-- CMakeLists.txt
|-- docs
| '-- Doxyfile.in
|-- example
| |-- CMakeLists.txt
| |-- PoissonSolver3DGPUTest.cpp
| '-- PoissonSolver3DGPUTest.h
|-- interface
| |-- PoissonSolver3DCylindricalGPU.cxx
| '-- PoissonSolver3DCylindricalGPU.h
|-- kernel
| |-- PoissonSolver3DGPU.cu
| '-- PoissonSolver3DGPU.h
|-- PETUNJUKPENGGUNAAN.md
'-- README.md
```

Modul Program yang Dibutuhkan

Untuk menginstall pustaka dibutuhkan program pengembang di lingkungan sistem operasi Linux (saat ini masih di Linux) yaitu:

- 1. CMAKE versi minimal 3.10.3
- 2. GCC versi minimal 6.2.0
- 3. CUDA versi minimal 8.0
- 4. GIT versi minimal 1.8.3.1

Jika disediakan module program pada lingkungan sistem HPC maka dapat menjalankan perintah berikut ini:

```
module load cmake/3.10.3
module load gcc/6.2.0
module load cuda
```

4 Petunjuk Penggunaan

Instalasi

Untuk menginstall pustaka PoissonSolver3D lakukan langkah-langkah berikut:

 Jalankan git clone untuk menyalin kode sumber ke direktori local. Perintah ini akan menyalin kode sumber ke direktori PoissonSolver3D

```
$ git clone http://github.com/rsadikin/PoissonSolver3D.git
```

2. Pindah ke direktori PoissonSolver3D, dan lihat daftar direktori

3. Buatlah folder buildpoissonsolver di luar direktori kode sumber

```
$ mkdir $HOME/buildpoissonsolver
```

4. Pindah ke folder buildpoissonsolver

```
$ cd $HOME/buildpoissonsolver
```

1. Jalankan **cmake** di folder **buildpoissonsolver** dengan menyatakan di mana pustaka akan diinstal dengan perintah sebagai berikut

```
$ export PSLIB=/home/usertest/trypoissonsolver/PoissonSolver3D
$ export PSLIB_INSTALL=/home/usertest/buildpoissonsolver
$ cmake $PSLIB/ -DCMAKE_INSTALL_PREFIX=$PSLIB_INSTALL
-- The C compiler identification is GNU 6.2.0
-- The CXX compiler identification is GNU 6.2.0
-- Check for working C compiler: /apps/tools/gcc-6.2.0/bin/gcc
-- Check for working C compiler: /apps/tools/gcc-6.2.0/bin/gcc -- works
-- Detecting C compiler ABI info
-- Detecting C compiler ABI info - done
-- Detecting C compile features
-- Detecting C compile features - done
-- Check for working CXX compiler: /apps/tools/gcc-6.2.0/bin/c++
-- Check for working CXX compiler: /apps/tools/gcc-6.2.0/bin/c++ -- works
-- Detecting CXX compiler ABI info
-- Detecting CXX compiler ABI info - done
-- Detecting CXX compile features
-- Detecting CXX compile features - done
-- Looking for pthread.h -- Looking for pthread.h - found
-- Looking for pthread_create
-- Looking for pthread_create - not found
-- Looking for pthread_create in pthreads
-- Looking for pthread_create in pthreads - not found
-- Looking for pthread_create in pthread
-- Looking for pthread_create in pthread - found
-- Found Threads: TRUE
-- Found CUDA: /apps/tools/cuda-9.1 (found version "9.1")
-- Building SpaceCharge distortion framework with CUDA support
-- Found Doxygen: /usr/bin/doxygen (found version "1.8.5") found components: doxygen dot
Doxygen build started
-- Configuring done
-- Generating done
-- Build files have been written to: /home/usertest/buildpoissonsolver
```

Kompail kode sumbernya

```
$ make
```

3. Install modul PoissonSolver3D di folder buildpoissonsolver

```
$ make install
..
-- Install configuration: ""
-- Installing: /home/usertest/trypoissonsolver/buildpoissonsolver/lib/libPoissonSolver3DCylindricalGPU.so
-- Installing: /home/usertest/trypoissonsolver/buildpoissonsolver/include/PoissonSolver3DCylindricalGPU.h
-- Installing: /home/usertest/trypoissonsolver/buildpoissonsolver/include/PoissonSolver3DGPU.h
```

Hasil instalasi adalah sebuah pustaka yang dapat digunakan (**shared library**) yaitu libPoissonSolver3DCylindrical ← GPU.so pada direktori **lib** dan 2 berkas header yang mengandung definisi kelas /fungsi sehingga pengguna pustaka dapat menggunakannya.

Penggunaan Pustaka

Penggunaan Dalam CMAKE

Dalam folder **example** di struktur direktori sumber terdapat contoh penggunaan pustaka libpoissonsolvergpu.so dengan menggunakan **cmake**. Berikut ini langkah-langkahnya:

```
cmake_minimum_required (VERSION 2.8.11)
project (3DPoissonSolverGPUTest)
  find_package(CUDA)
 if (NOT CUDA FOUND)
                       message(FATAL_ERROR "NVIDIA CUDA package not found")
  else()
                         find_library(LIBCUDA_SO_PATH libcuda.so)
                         string(FIND ${LIBCUDA_SO_PATH} "-NOTFOUND" LIBCUDA_SO_PATH_NOTFOUND )
  endif(NOT CUDA_FOUND)
 message( STATUS "Building Poisson Solver % \left( 1\right) =\left( 1\right) +\left( 1\right) +\left
  if (LIBCUDA_SO_PATH_NOTFOUND GREATER -1)
          message (FATAL_ERROR "NVIDIA CUDA libcuda.so not found" )
  endif(LIBCUDA_SO_PATH_NOTFOUND GREATER -1)
  #set (CMAKE_MODULE_PATH "${CMAKE_SOURCE_DIR}/CMake/cuda" ${CMAKE_MODULE_PATH})
  #find_package(CUDA QUIET REQUIRED)
  set (PSLIBNAME libPoissonSolver3DCylindricalGPU.so)
find_library(PSLIB ${PSLIBNAME})
string(FIND ${PSLIB} "-NOTFOUND" PSLIB_NOTFOUND )
  if (PSLIB NOTFOUND GREATER -1)
           message(FATAL_ERROR "Poisson Solver Cuda Library libPoissonSolver3DCylindricalGPU.o not found")
  endif(PSLIB_NOTFOUND GREATER -1)
```

Setelah itu, baru tambahkan perintah pada CMakeLists.txt (dilanjutkan) untuk mengikut sertakan kode sumber user yaitu:

```
# tambah disini kode sumber user
set(CPP_SOURCE PoissonSolver3DGPUTest.cpp)
set(HEADERS PoissonSolver3DGPUTest.h)

set(TARGET_NAME poissonsolvergputest)

add_executable(${TARGET_NAME}
   PoissonSolver3DGPUTest.cpp
)

# ikut sertakan shared library cuda dan poisson solver
target_link_libraries(${TARGET_NAME} ${PSLIB} ${LIBCUDA_SO_PATH})
```

6 Petunjuk Penggunaan

Pada kode sumber include header file sehingga definisi fungsi dan kelas dapat dipanggil di badan kode.

```
{c++}
#include "PoissonSolver3DCylindricalGPU.h"

...
// create poissonSolver
PoissonSolver3DCylindricalGPU *poissonSolver = new PoissonSolver3DCylindricalGPU();
PoissonSolver3DCylindricalGPU::fgConvergenceError = 1e-8;
poissonSolver->SetExactSolution(VPotentialExact, kRows, kColumns, kPhiSlices);
poissonSolver->SetStrategy(PoissonSolver3DCylindricalGPU::kMultiGrid);
poissonSolver->SetCycleType(PoissonSolver3DCylindricalGPU::kFCycle);
poissonSolver->PoissonSolver3D(VPotential, RhoCharge, kRows, kColumns, kPhiSlices, kIterations, kSymmetry);
```

 Buat folder terpisah untuk mebangun proyek yang menggunakan pustaka misal buildexamplepoissonsolver lalu jalankan cmake dengan flag spesial yaitu **-DCMAKE_PREFIX_PATH** yang ditetapkan dengan absolute path tempat direktori PoissonSolver3DCylindricalGPU dibangun.

```
$ mkdir buildexamplepoissonsolver
$ cd buildexamplepoissonsolver
$ cmake ../PoissonSolver3D/example/ -DCMAKE_PREFIX_PATH=/home/usertest/trypoissonsolver/buildpoissonsolver
...
-- Found CUDA: /apps/tools/cuda-9.1 (found version "9.1")
-- Building Poisson Solver with CUDA support
-- Configuring done
-- Generating done
-- Build files have been written to: /home/usertest/trypoissonsolver/buildexamplepoissonsolver
```

1. Jalankan make untuk membuat executable file

```
$ make
-- Building Poisson Solver with CUDA support
-- Configuring done
-- Generating done
-- Build files have been written to: /home/usertest/trypoissonsolver/buildexamplepoissonsolver
[ 50%] Linking CXX executable poissonsolvergputest
[ 100%] Built target poissonsolvergputest
```

1. Hasil dari make adalah program yang dapat dieksekusi yang berjalan di GPU card

```
$ ./poissonsolverqputest
Poisson Solver 3D Cylindrical GPU test
Ukuran grid (r,phi,z) = (17,17,18)
Waktu komputasi:
                             0.55 s
Jumlah iterasi siklus multigrid:
Iterasi Error Convergen Error Ab: [0]: 8.362587e-01 2.430797e-03
                             Error Absolut
        5.126660e-02
                        4.434380e-04
[1]:
        9.490424e-03
                       1.892288e-04
[2]:
                        1.314385e-04
        2.084086e-03
                        1.217592e-04
[4]:
        1.141812e-03
Poisson Solver 3D Cylindrical GPU test
Ukuran grid (r, phi, z) = (33, 33, 36)
                             1.000000e-02 s
Waktu komputasi:
Jumlah iterasi siklus multigrid:
Iterasi Error Convergen
                             Error Absolut
                       1.315177e-04
1.266415e-04
[0]:
        1.724319e-03
        8.652242e-05
[1]:
        5.450314e-05
                        1.256187e-04
[2]:
        5.081671e-05
                        1.249848e-04
[3]:
        4.951065e-05
                         1.244460e-04
[5]:
        4.904093e-05
                         1.241379e-04
[6]:
        4.890266e-05
                         1.239894e-04
        4.885175e-05
                         1.239208e-04
[71:
        4.883604e-05
                        1.238959e-04
[8]:
        4.883501e-05
                         1.238844e-04
[9]:
Poisson Solver 3D Cylindrical GPU test
Ukuran grid (r,phi,z) = (65,65,72)
                             5.000000e-02 s
Waktu komputasi:
Jumlah iterasi siklus multigrid:
Iterasi Error Convergen
                             Error Absolut
[0]:
        1.084726e-04
                        1.291784e-04
```

```
[1]: 5.680057e-06 1.283386e-04
[2]: 1.501479e-06 1.278558e-04

Poisson Solver 3D Cylindrical GPU test
Ukuran grid (r,phi,z) = (129,129,144)
Waktu komputasi: 1.200000e-01 s
Jumlah iterasi siklus multigrid: 3
Iterasi Error Convergen Error Absolut
[0]: 1.373293e-05 1.302576e-04
[1]: 2.154564e-06 1.299626e-04
[2]: 1.048384e-06 1.297261e-04

Poisson Solver 3D Cylindrical GPU test
Ukuran grid (r,phi,z) = (257,257,288)
Waktu komputasi: 6.900000e-01 s
Jumlah iterasi siklus multigrid: 5
Iterasi Error Convergen Error Absolut
[0]: 5.469890e-06 1.388922e-04
[1]: 1.783695e-06 1.384964e-04
[2]: 1.345343e-06 1.381199e-04
[3]: 1.156555e-06 1.377524e-04
[4]: 1.050234e-06 1.373983e-04
```

		ınaan

Indeks Kelas

3.1 Daftar Kelas

Berikut ini daftar kelas, struct, union, dan interface, dengan penjelasan singkat:

PoissonSolver3DCylindricalGPU::MGParameters	13
PoissonSolver3DCylindricalGPU	
Kelas ini merupakan interface PoissonSolver 3D dalam koordinat silindrikal yang diterapkan pada	
NVDIA Cuda	14

10 Indeks Kelas

Indeks File

4.1 Daftar File

Berikut ini daftar seluruh file yang didokumentasikan, dengan penjelasan singkat:

??
21
??
24
24
49

12 Indeks File

Dokumentasi Kelas

5.1 Referensi Struct PoissonSolver3DCylindricalGPU::MGParameters

Atribut Publik

bool isFull3D

TRUE: full coarsening, FALSE: semi coarsening.

CycleType cycleType

cycleType follow CycleType

GridTransferType gtType

gtType grid transfer type follow GridTransferType

RelaxType relaxType

relaxType follow RelaxType

• int gamma

number of iteration at coarsest level

• int nPre

number of iteration for pre smoothing

• int nPost

number of iteration for post smoothing

int nMGCycle

number of multi grid cycle (V type)

int maxLoop

the number of tree-deep of multi grid

5.1.1 Keterangan Lengkap

Definisi pada baris 51 dalam file PoissonSolver3DCylindricalGPU.h.

Dokumentasi untuk struct ini dibangkitkan dari file berikut:

/home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3D/interface/PoissonSolver3DCylindrical
 GPU.h

14 Dokumentasi Kelas

5.2 Referensi Kelas PoissonSolver3DCylindricalGPU

Kelas ini merupakan interface PoissonSolver 3D dalam koordinat silindrikal yang diterapkan pada NVDIA Cuda.

```
#include <PoissonSolver3DCylindricalGPU.h>
```

Kelas

struct MGParameters

Tipe Publik

```
    enum StrategyType { kRelaxation = 0, kMultiGrid = 1, kFastRelaxation = 2 }
        < Enumeration of Poisson Solver Strategy Type</li>
    enum CycleType { kVCycle = 0, kWCycle = 1, kFCycle = 2 }
    enum GridTransferType { kHalf = 0, kFull = 1 }
    enum RelaxType { kJacobi = 0, kWeightedJacobi = 1, kGaussSeidel = 2 }
    enum InterpType { kHalfInterp = 0, kFullInterp = 1 }
```

Fungsi Anggota Publik

- void SetExactSolution (float *exactSolution, const int fPhiSlices)
- void **SetCycleType** (PoissonSolver3DCylindricalGPU::CycleType cycleType)
- PoissonSolver3DCylindricalGPU ()
- PoissonSolver3DCylindricalGPU (int nRRow, int nZColumn, int nPhiSlice)
- PoissonSolver3DCylindricalGPU (const char *name, const char *title)
- virtual \sim PoissonSolver3DCylindricalGPU ()

destructor

- void PoissonSolver3D (float *matricesV, float *matricesChargeDensities, int nRRow, int nZColumn, int phi
 Slice, int maxIterations, int symmetry)
- void SetStrategy (StrategyType strategy)
- StrategyType GetStrategy ()
- void SetExactSolution (float *exactSolution, int nRRow, int nZColumn, int phiSlice)
- float GetErrorConv (int iteration)
- float GetErrorExact (int iteration)

Atribut Publik

· int flterations

number of maximum iteration

MGParameters fMgParameters

parameters multi grid

StrategyType fStrategy

strategy used default multiGrid

• float * fExactSolutionF

Atribut Publik Statis

static const float fgkZ0 = 249.7

nominal gating grid position

• static const float fgkIFCRadius = 83.5

Mean Radius of the Inner Field Cage (82.43 min, 83.70 max) (cm)

• static const float fgkOFCRadius = 254.5

Mean Radius of the Outer Field Cage (252.55 min, 256.45 max) (cm)

• static float fgExactErr = 1e-4

Error tolerated.

• static float fgConvergenceError = 1e-3

Error tolerated.

5.2.1 Keterangan Lengkap

Kelas ini merupakan interface PoissonSolver 3D dalam koordinat silindrikal yang diterapkan pada NVDIA Cuda.

Penulis

```
Rifki Sadikin rifki.sadikin@lipi.go.id, Indonesian Institute of Sciences
```

Tanggal

Nov 8, 2018

Penulis

Rifki Sadikin rifki.sadikin@lipi.go.id, Indonesian Institute of Sciences

Tanggal

Nov 20, 2017

Definisi pada baris 15 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.2 Dokumentasi Anggota: Enumerasi

5.2.2.1 CycleType

enum PoissonSolver3DCylindricalGPU::CycleType

Nilai enumerasi

kVCycle	V Cycle.
kWCycle	W Cycle (TODO)
kFCycle	Full Cycle.

16 Dokumentasi Kelas

Definisi pada baris 25 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.2.2 GridTransferType

enum PoissonSolver3DCylindricalGPU::GridTransferType

Nilai enumerasi

kHalf	Half weighting.
kFull	Full weighting.

Definisi pada baris 32 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.2.3 InterpType

enum PoissonSolver3DCylindricalGPU::InterpType

Nilai enumerasi

kHalfInterp	Half bi linear interpolation.
kFullInterp	Full bi linear interpolation.

Definisi pada baris 45 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.2.4 RelaxType

enum PoissonSolver3DCylindricalGPU::RelaxType

Nilai enumerasi

kJacobi Jacobi (5 Stencil 2D, 7 Stencil 3D	
kWeightedJacobi	(TODO)
kGaussSeidel	Gauss Seidel 2D (2 Color, 5 Stencil), 3D (7 Stencil)

Definisi pada baris 38 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.2.5 StrategyType

```
enum PoissonSolver3DCylindricalGPU::StrategyType
```

< Enumeration of Poisson Solver Strategy Type

Nilai enumerasi

kRelaxation	S.O.R Cascaded MultiGrid.
kMultiGrid	Geometric MG.
kFastRelaxation	Spectral (TODO)

Definisi pada baris 18 dalam file PoissonSolver3DCylindricalGPU.h.

5.2.3 Dokumentasi Konstruktor & Destruktor

5.2.3.1 PoissonSolver3DCylindricalGPU()

```
{\tt PoissonSolver3DCylindricalGPU::} {\tt PoissonSolver3DCylindricalGPU} \ \ (\ \ )
```

constructor

Definisi pada baris 42 dalam file PoissonSolver3DCylindricalGPU.cxx.

```
42
43
44 fErrorConvF = new float [fMgParameters.nMGCycle];
45 fErrorExactF = new float [fMgParameters.nMGCycle];
46
47 }
```

18 Dokumentasi Kelas

5.2.4 Dokumentasi Anggota: Fungsi

5.2.4.1 PoissonSolver3D()

Menyediakan solusi iteratif terhadap poisson solver pada koordinat silindrikal 3D

Disediakan algoritma iteratif

· Geometric MultiGrid

- Cycles: V, W, Full

- Relaxation: Gauss-Seidel

- Grid transfer operators: Full, Half

Parameter

matricesV	float * potential dalam array 1D berukuran nRRow*nZColumn *phiSlice
matricesCharge	float * charge dalam array 1D berukuran nRRow*nZColumn *phiSlice
nRRow	int jumlah titik grid pada arah radial
nZColumn	int jumlah titik grid pada arah z
phiSlice	int jumlah titik grid pada arah sudut (phi)
maxIteration	int jumlah iterasi maksimum pada multigrud
symmetry	int nilai simetri (tidak dipakai)

Definisi pada baris 79 dalam file PoissonSolver3DCylindricalGPU.cxx.

```
81
82
83 fNRRow = nRRow;
84 fNZColumn = nZColumn;
85 fPhiSlice = phiSlice;
86
87 PoissonMultiGrid3D2D(matricesV, matricesCharge, nRRow, nZColumn, phiSlice, symmetry);
88
89
90 }
```

5.2.4.2 SetExactSolution()

Helper untuk menset nilai V dari fungsi analitik (diperlukan untuk memastikan implementasi benar

Parameter

exactSolution	float * array 1D sebesar nRRow * nZColumn * phiSlice
nRRow	int jumlah titik grid pada arah radial
nZColumn	int jumlah titik grid pada arah z
phiSlice	int jumlah titik grid pada arah sudut (phi)

Definisi pada baris 171 dalam file PoissonSolver3DCylindricalGPU.cxx.

```
171
        fNRRow = nRRow;
        fNZColumn = nZColumn;
fPhiSlice = phiSlice;
173
174
175
        fExactSolutionF = new float[fNRRow * fPhiSlice * fNZColumn];
        fExactPresent = true;
176
177
        fMaxExact = 0.0;;
178
179
        for (int i=0;i<nRRow*nZColumn*phiSlice;i++) {</pre>
             fExactSolutionF[i] = exactSolution[i];
             if (abs(fExactSolutionF[i]) > fMaxExact) fMaxExact = abs(fExactSolutionF[i]);
180
182 }
```

5.2.5 Dokumentasi Anggota: Data

5.2.5.1 fgklFCRadius

```
const float PoissonSolver3DCylindricalGPU::fgkIFCRadius = 83.5 [static]
```

Mean Radius of the Inner Field Cage (82.43 min, 83.70 max) (cm)

radius which renders the "18 rod manifold" best -> compare calc. of Jim Thomas

Definisi pada baris 80 dalam file PoissonSolver3DCylindricalGPU.h.

Dokumentasi untuk kelas ini dibangkitkan dari file-file berikut:

- /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3D/interface/PoissonSolver3DCylindrical
 GPU.h
- /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3D/interface/PoissonSolver3DCylindrical
 GPU.cxx

20 Dokumentasi Kelas

Dokumentasi File

6.1 Referensi File /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3

D/example/PoissonSolver3DGPUTest.h

Berkas ini berisi definisi fungs untuk memakai pustaka libPoissonSolver3DCylindrialGPU.so.

```
#include <iostream>
#include "PoissonSolver3DCylindricalGPU.h"
```

Fungsi

void DoPoissonSolverExperiment (const int kRows, const int kColumns, const int kPhiSlices, const int k
 Iterations, const int kSymmetry)

Lakukan eksperimen poisson solver.

 void InitVoltandCharge3D (float *VPotentialExact, float *VPotential, float *RhoCharge, const int kRows, const int kColumns, const int kPhiSlices, float gridSizeR, float gridSizeZ, float gridSizePhi)

Inisisasi nilai volt dan charge.

- float TestFunction1PotentialEval (double a, double b, double c, float radius0, float phi0, float z0) analytic function untuk potensial
- float TestFunction1ChargeEval (double a, double b, double c, float radius0, float phi0, float z0) analytic function untuk charge

Variabel

```
    const double fgkTPCZ0 = 249.7
```

nominal gating grid position

• const double fgkIFCRadius = 83.5

radius which renders the "18 rod manifold" best -> compare calc. of Jim Thomas

• const double fgkOFCRadius = 254.5

Mean Radius of the Outer Field Cage (252.55 min, 256.45 max) (cm)

• const double fgConvergenceError = 1e-6

vacuum permittivity [A·s/(V·m)]

6.1.1 Keterangan Lengkap

Berkas ini berisi definisi fungs untuk memakai pustaka libPoissonSolver3DCylindrialGPU.so.

Penulis

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Tanggal

November 8, 2018

6.1.2 Dokumentasi Fungsi

6.1.2.1 DoPoissonSolverExperiment()

Lakukan eksperimen poisson solver.

```
const float ratioPhi = gridSizeR*gridSizeR / (gridSizePhi*gridSizePhi); // ratio_\text{phi}, gridsize_\text{r}, const float ratioZ = gridSizeR*gridSizeR / (gridSizeZ*gridSizeZ); // ratio_\text{Z} = gridsize_\text{r} / gridsize_\text{r};
= fgConvergenceError;
const float convErr = fgConvergen
const float IFCRadius = fgkIFCRadius;
const int fparamsize = 8;
float * fparam = new float[fparamsize];
fparam[0] = gridSizeR;
fparam[1] = gridSizePhi;
fparam[2] = gridSizeZ;
fparam[3] = ratioPhi;
fparam[4] = ratioZ;
fparam[5] = convErr;
fparam[6] = IFCRadius;
int iparamsize = 4;
      * iparam = new int[iparamsize];
iparam[0] = 2;//nPre
iparam[1] = 2;//nPost;
iparam[2] = 6;//maxLoop;
iparam[3] = 200; //nMGCycle;
for (int k=0; k<kPhiSlices; k++) {
for (int i=0;i<kRows;i++) {
           for (int j=0; j < kColumns; j++) \ printf("\$.3f\t", RhoCharge[k * (kRows * kColumns) + i * kColumns + j]); \\
          printf("\n");
}
printf("\n");
}
```

VCycle PoissonMultigrid3DSemiCoarseningGPUError(VPotential, RhoCharge, kRows, kColumns ,kPhiSlices, 0 , fparam, iparam, true, errorConv,errorExact, VPotentialExact); Call poisson solver

for (int k=0;k<1;k++) { for (int i=0;i<kRows;i++) { for (int j=0;j< kColumns;j++) printf("%.3f\t",VPotential[k* (kRows * kColumns) + i * kColumns + j]); printf("\n"); } printf("\n"); }

Definisi pada baris 15 dalam file PoissonSolver3DGPUTest.cpp.

```
15
                                            {
16
        int kPhiSlicesPerSector = kPhiSlices/18;
18
19
        \begin{array}{lll} \mbox{const float gridSizeR} & = & (\mbox{fgkOFCRadius} - \mbox{fgkIFCRadius}) \ / \ (\mbox{kRows-1}) \ ; \\ \mbox{const float gridSizeZ} & = & \mbox{fgkTPC20} \ / \ (\mbox{kColumns-1}) \ ; \\ \end{array}
21
2.2
23
        const float gridSizePhi = (M_PI * 2)/ ( 18.0 * kPhiSlicesPerSector);
24
        int size = kRows * kColumns * kPhiSlices;
2.5
26
        float * VPotential = new float[size];
2.7
28
        float * VPotentialExact = new float[size];
        float * RhoCharge = new float[size];
float * errorConv = new float[200];
29
30
        float * errorExact = new float[200];
31
        InitVoltandCharge3D(VPotentialExact, VPotential, RhoCharge, kRows, kColumns, kPhiSlices,
33
       gridSizeR, gridSizeZ, gridSizePhi);
34
3.5
82
        // create poissonSolver
        PoissonSolver3DCylindricalGPU *poissonSolver = new
83
       PoissonSolver3DCylindricalGPU();
84
85
        PoissonSolver3DCylindricalGPU::fgConvergenceError = 1e
       -6;
        // zeroring array of error
86
        poissonSolver->SetExactSolution(VPotentialExact, kRows, kColumns, kPhiSlices);
88
89
90
        // Case 1. Set the strategy as multigrid, fullmultigrid, and full 3d
91
92
        poissonSolver->SetStrategy(PoissonSolver3DCylindricalGPU::kMultiGrid
93
        poissonSolver->SetCycleType(PoissonSolver3DCylindricalGPU::kFCycle
94
95
        // TStopwatch w;
        std::clock_t start,stop;
96
        double duration;
98
99
             start = std::clock();
100
101
        //w.Start();
         poissonSolver->PoissonSolver3D(VPotential, RhoCharge, kRows, kColumns, kPhiSlices,
102
       kIterations, kSymmetry) ;
103
         //w.Stop();
104
         stop = std::clock();
114
              duration = ( stop - start ) / (double) CLOCKS_PER_SEC;
115
         std::cout<<"Poisson Solver 3D Cylindrical GPU test" << '\n';
116
        std::cout<<"UKuran grid (r,phi,z) = (" < kRows << "," << kColumns << "," << kPhiSlices <<") \n"; std::cout<<"Waktu komputasi: \t\t\t"<< duration <<" s \n";
117
118
         std::cout<<"Jumlah iterasi siklus multigrid: \t"<< poissonSolver->
119
       fIterations << '\n';
         std::cout<<"Iterasi\tError Convergen\t\tError Absolut \n";
120
         std::cout<< std::scientific;</pre>
121
       for (int i=0;i<poissonSolver->fIterations;i++) {
    std::cout<<"[" << i << "]:\t" << poissonSolver->GetErrorConv(i) << "\t" << poissonSolver->
GetErrorExact(i) << '\n' << std::scientific;</pre>
122
123
124
125
         delete poissonSolver;
126
         delete VPotential;
127
         delete VPotentialExact;
128
         delete RhoCharge;
129 }
```

6.2 Referensi File /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3 D/interface/PoissonSolver3DCylindricalGPU.h

```
#include "PoissonSolver3DGPU.h"
```

Kelas

- class PoissonSolver3DCylindricalGPU
 - Kelas ini merupakan interface PoissonSolver 3D dalam koordinat silindrikal yang diterapkan pada NVDIA Cuda.
- struct PoissonSolver3DCylindricalGPU::MGParameters

6.3 Referensi File /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3 D/kernel/PoissonSolver3DGPU.cu

Berkas ini berisi implementasi kernel dalam cuda untuk PoissonSolver Cylindrical berbasis Multigrid.

```
#include "PoissonSolver3DGPU.h"
#include <cuda.h>
#include <math.h>
```

Fungsi

- __global__ void relaxationGaussSeidelRed (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, float *coef1, float *coef2, float *coef3, float *coef4)
- __global__ void relaxationGaussSeidelBlack (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, float *coef1, float *coef2, float *coef3, float *coef4)
- __global__ void residueCalculation (float *VPotential, float *RhoChargeDensity, float *DeltaResidue, const int RRow, const int ZColumn, const int PhiSlice, float *coef1, float *coef2, float *coef3, float *icoef4)
- __global__ void restriction2DFull (float *RhoChargeDensity, float *DeltaResidue, const int RRow, const int ZColumn, const int PhiSlice)
- __global__ void zeroingVPotential (float *VPotential, const int RRow, const int ZColumn, const int PhiSlice)
- __global__ void zeroingBoundaryTopBottom (float *VPotential, int RRow, int ZColumn, int PhiSlice)
- __global__ void zeroingBoundaryLeftRight (float *VPotential, int RRow, int ZColumn, int PhiSlice)
- __global__ void prolongation2DHalf (float *VPotential, const int RRow, const int ZColumn, const int Phi
 — Slice)
- __global__ void **prolongation2DHalfNoAdd** (float *VPotential, const int RRow, const int ZColumn, const int PhiSlice)
- __global__ void **errorCalculation** (float *VPotentialPrev, float *VPotential, float *EpsilonError, const int R← Row, const int ZColumn, const int PhiSlice)
- float GetErrorNorm2 (float *VPotential, float *VPotentialPrev, const int rows, const int cols, float weight)
- float **GetAbsMax** (float *VPotentialExact, int size)
- void Restrict_Boundary (float *VPotential, const int RRow, const int ZColumn, const int PhiSlice, const int Offset)
- void PrintMatrix (float *Mat, const int Row, const int Column)
- void **VCycleSemiCoarseningGPU** (float *d_VPotential, float *d_RhoChargeDensity, float *d_DeltaResidue, float *d_coef1, float *d_coef2, float *d_coef3, float *d_coef4, float *d_icoef4, float gridSizeR, float ratioZ, float ratioPhi, int RRow, int ZColumn, int PhiSlice, int gridFrom, int gridTo, int nPre, int nPost)

- void PoissonMultigrid3DSemiCoarseningGPUError (float *VPotential, float *RhoChargeDensity, const int R

 Row, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, bool isExact

 Present, float *errorConv, float *errorExact, float *VPotentialExact)
- void PoissonMultigrid3DSemiCoarseningGPUErrorWCycle (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, float *errorConv, float *errorExact, float *VPotentialExact)
- void PoissonMultigrid3DSemiCoarseningGPUErrorFCycle (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, bool is← ExactPresent, float *errorConv, float *errorExact, float *VPotentialExact)

Variabel

```
    __device____constant__ int d_coef_StartPos
    __device___constant__ int d_grid_StartPos
    __device__constant__ float d_h2
    __device__constant__ float d_ih2
    __device__constant__ float d_tempRatioZ
```

6.3.1 Keterangan Lengkap

Berkas ini berisi implementasi kernel dalam cuda untuk PoissonSolver Cylindrical berbasis Multigrid.

Penulis

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Tanggal

November 8, 2018

6.3.2 Dokumentasi Fungsi

6.3.2.1 PoissonMultigrid3DSemiCoarseningGPUError()

Fungsi ini menghitung solusi terhadap Persamaan Poisson

$$\nabla^2(r,\phi,z) = \rho(r,\phi,z)$$

dengan diketahui nilai tepi (Boundary Value) pada V (potensial) dan distribusi buatan ρ

Parameter

in,out	VPotential	float[nrows*ncols*nphi] distribusi potensial. Input: hanya nilai tepi. Output: hasil perhitungan penyelesaian persamaan Poisson
in	RhoChangeDensity	float[nrows*ncols*nphi] distributsi muatan listrik.

Mengembalikan

A fixed number that has nothing to do with what the function does

Definisi pada baris 893 dalam file PoissonSolver3DGPU.cu.

```
907 {
908
        // variables for CPU memory
909
        float *temp_VPotential;
910
        float *VPotentialPrev;
911
        float *EpsilonError;
912
913
        // variables for GPU memory
914
        float *d_VPotential;
915
        float *d_RhoChargeDensity;
916
        float *d_DeltaResidue;
917
        float *d_VPotentialPrev;
918
        float *d_EpsilonError;
919
920
        float *d_coef1;
921
        float *d_coef2;
922
        float *d_coef3;
923
        float *d_coef4;
924
        float *d_icoef4;
925
926
        // variables for coefficent calculations
927
        float *coef1;
928
        float *coef2;
929
        float *coef3;
930
        float *coef4;
931
        float *icoef4;
float tempRatioZ;
932
933
        float tempRatioPhi;
934
        float radius;
935
936
        int gridFrom;
937
        int gridTo;
938
        int loops;
939
940
941
        // variables passed from ALIROOT
942
        float gridSizeR
                             = fparam[0];
        float gridSizePhi
943
                             = fparam[1];
        float gridSizeZ
                             = fparam[2];
944
945
        float ratioPhi
                             = fparam[3];
946
        float ratioZ
                             = fparam[4];
                             = fparam[5];
= fparam[6];
947
        float convErr
948
        float IFCRadius
                    = iparam[0];
949
        int nPre
                        = iparam[1];
950
        int nPost
951
        int maxLoop
                        = iparam[2];
952
                         = iparam[3];
        int nCycle
953
954
        \ensuremath{//} variables for calculating GPU memory allocation
955
        int grid_RRow;
956
        int grid_ZColumn;
957
        int grid_PhiSlice = PhiSlice;
        int grid_Size = 0;
958
959
        int grid_StartPos;
960
        int coef_Size = 0;
961
        int coef_StartPos;
        int iOne, jOne;
float h, h2, ih2;
962
963
964
965
        // variables for calculating multigrid maximum depth
966
        int depth_RRow = 0;
967
        int depth_ZColumn = 0;
968
        int temp_RRow = RRow;
        int temp_ZColumn = ZColumn;
969
970
971
        // calculate depth for multigrid
```

```
while (temp_RRow >>= 1) depth_RRow++;
973
         while (temp_ZColumn >>= 1) depth_ZColumn++;
974
975
         loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
         loops = (loops > maxLoop) ? maxLoop : loops;
976
977
978
         gridFrom = 1;
979
         gridTo = loops;
980
981
         // calculate GPU memory allocation for multigrid
982
         for (int step = gridFrom; step <= gridTo; step++)</pre>
983
984
              grid_RRow = ((RRow - 1) / (1 << (step - 1))) + 1;
985
              grid_ZColumn = ((ZColumn - 1) / (1 << (step - 1))) + 1;
986
              grid_Size += grid_RRow * grid_ZColumn * grid_PhiSlice;
coef_Size += grid_RRow;
987
988
989
990
991
         // allocate memory for temporary output
         temp_VPotential = (float *) malloc(grid_Size * sizeof(float));
VPotentialPrev = (float *) malloc(RRow * ZColumn * PhiSlice * sizeof(float));
992
993
         EpsilonError = (float *) malloc(1 * sizeof(float));
994
995
996
997
         // allocate memory for relaxation coefficient
998
         coef1 = (float *) malloc(coef_Size * sizeof(float));
         coef2 = (float *) malloc(coef_Size * sizeof(float));
999
          coef3 = (float *) malloc(coef_Size * sizeof(float));
coef4 = (float *) malloc(coef_Size * sizeof(float));
1000
1001
          icoef4 = (float *) malloc(coef_Size * sizeof(float));
1002
1003
1004
          // pre-compute relaxation coefficient
1005
          coef_StartPos = 0;
          iOne = 1 << (gridFrom - 1);
jOne = 1 << (gridFrom - 1);</pre>
1006
1007
1008
1009
          for (int step = gridFrom; step <= gridTo; step++)</pre>
1010
1011
               grid_RRow = ((RRow - 1) / iOne) + 1;
1012
1013
               h = gridSizeR * iOne;
               h2 = h * h;
1014
               ih2 = 1.0 / h2;
1015
1016
1017
               tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1018
               tempRatioPhi = ratioPhi * iOne * iOne;
1019
1020
               for (int i = 1; i < grid RRow - 1; i++)
1021
1022
                    radius = IFCRadius + i * h;
                    coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1023
1024
1025
1026
1027
1029
               coef_StartPos += grid_RRow;
               iOne = 2 * iOne;
jOne = 2 * jOne;
1030
1031
1032
         1
1033
1034
          // device memory allocation
1035
          cudaMalloc( &d_VPotential, grid_Size * sizeof(float) );
1036
          cudaMalloc( &d_VPotentialPrev, RRow * ZColumn * PhiSlice * sizeof(float) );
          cudaMalloc( &d_EpsilonError, 1 \star sizeof(float) );
1037
1038
          cudaMalloc( &d_DeltaResidue, grid_Size * sizeof(float) );
          cudaMalloc( &d_RhoChargeDensity, grid_Size * sizeof(float) );
cudaMalloc( &d_coef1, coef_Size * sizeof(float) );
1039
1040
          cudaMalloc( &d_coef2, coef_Size * sizeof(float) );
1041
          cudaMalloc( &d_coef3, coef_Size * sizeof(float) );
cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
1042
1043
1044
          cudaMalloc( &d_icoef4, coef_Size * sizeof(float) );
1045
1046
          // set memory to zero
          cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
1047
1048
1049
          cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
          cudaMemset( d_VPotentialPrev, 0, RRow * ZColumn * PhiSlice * sizeof(float) );
cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1050
1051
1052
1053
1054
          // copy data from host to device
1055
          cudaMemcpy( d_VPotential, VPotential, RRow * ZColumn * PhiSlice * sizeof(float), cudaMemcpyHostToDevice
        ); //check
1056
          cudaMemcpvHostToDevice ); //check
```

```
cudaMemcpy( d_coef1, coef1, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
                     cudaMemcpy( d_coef2, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1058
                     cudaMemcpy( d_coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1059
                     cudaMemcpy( d_coef4, coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1060
                     cudaMemcpy( d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
cudaMemcpy( d_VPotentialPrev, VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1061
1062
              cudaMemcpyHostToDevice );
1063
1064
                      // max exact
1065
                      // float maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
1066
1067
                     float maxAbsExact = 1.0;
1068
1069
                     if (isExactPresent == true)
1070
                              maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
1071
                     dim3 error_BlockPerGrid((RRow < 16) ? 1 : (RRow / 16), (ZColumn < 16) ? 1 : (ZColumn / 16), PhiSlice);
1072
                     dim3 error_ThreadPerBlock(16, 16);
1073
1074
1075
                      for (int cycle = 0; cycle < nCycle; cycle++)</pre>
1076
1077
                               cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
              cudaMemcpyDeviceToHost );
                              if (isExactPresent == true) errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact,
1078
              RRow * PhiSlice, ZColumn, maxAbsExact);
1079
1080
1081
                              \label{thm:control} VCycleSemiCoarseningGPU(d\_VPotential, d\_RhoChargeDensity, d\_DeltaResidue, d\_coef1, d\_coef2, d\_coef3, d\_coef3, d\_coef2, d\_coef3, d\_coef
              , d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, gridFrom, gridTo, nPre, nPost);
1082
1083
1084
                               errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev, d_VPotential,
             d_EpsilonError, RRow, ZColumn, PhiSlice);
1085
1086
                               \verb|cudaMemcpy| ( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost ); \\
1087
1088
1089
                              errorConv[cycle] = *EpsilonError / (RRow * ZColumn * PhiSlice);
1090
1091
                               if (errorConv[cycle] < convErr)</pre>
1092
1093
                                        //errorConv
1094
                                        nCycle = cycle;
1095
                                        break;
1096
1097
1098
                              cudaMemcpy( d_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
             cudaMemcpyDeviceToDevice );
1099
                              cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1100
1101
1102
                     iparam[3] = nCycle;
1103
1104 // for (int cycle = 0; cycle < nCycle; cycle++)
1105 //
1106 //
                              cudaMemcpy( temp VPotentialPrev, d VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
                cudaMemcpyDeviceToHost );
1107
1108
1109 //
                              \label{lem:coarseningGPU} VCycleSemiCoarseningGPU(d\_VPotential, d\_RhoChargeDensity, d\_DeltaResidue, d\_coef1, d\_coef2, 
                d_coef3, d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, gridFrom, gridTo, nPre, nPost);
1110
1111 //
                              cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
                cudaMemcpyDeviceToHost );
1112 //
                              errorConv[cycle] = GetErrorNorm2(temp_VPotential, temp_VPotentialPrev, RRow * PhiSlice, ZColumn,
                1.0);
1113 //
                              //errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact, RRow * PhiSlice, ZColumn,
                1.0);
1114 // }
1115
1116
1117
                      // copy result from device to host
1118
                     cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
             cudaMemcpyDeviceToHost );
1119
                     memcpy(VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
1120
1121
1122
                     // free device memory
1123
                     cudaFree( d_VPotential );
1124
                     cudaFree( d DeltaResidue );
                     cudaFree ( d RhoChargeDensity );
1125
                     cudaFree( d_VPotentialPrev );
1126
1127
                     cudaFree( d_EpsilonError );
1128
                     cudaFree( d_coef1 );
1129
                     cudaFree( d_coef2 );
1130
                     cudaFree ( d coef3 );
1131
                    cudaFree( d coef4 );
```

```
cudaFree( d_icoef4 );
        // free host memory
1134
1135
        free( coef1 );
1136
        free ( coef2 );
1137
        free ( coef3 );
       free( coef4 );
1138
1139
        free( icoef4 );
1140
       free( temp_VPotential );
1141
        free ( VPotentialPrev );
1142 }
```

6.3.2.2 PoissonMultigrid3DSemiCoarseningGPUErrorFCycle()

```
void PoissonMultigrid3DSemiCoarseningGPUErrorFCycle (
    float * VPotential,
    float * RhoChargeDensity,
    const int RRow,
    const int ZColumn,
    const int PhiSlice,
    const int Symmetry,
    float * fparam,
    int * iparam,
    bool isExactPresent,
    float * errorConv,
    float * errorExact,
    float * VPotentialExact )
```

 $\label{lem:condition} \verb|cudaMemcpy| temp_VPotential|, d_RhoChargeDensity + grid_StartPos|, grid_RRow * grid_ZColumn * PhiSlice * sizeof(float)|, cudaMemcpyDeviceToHost|);$

Definisi pada baris 1837 dalam file PoissonSolver3DGPU.cu.

```
1851 {
1852
           // variables for CPU memory
         float *temp_VPotential;
float *VPotentialPrev;
1853
1854
1855
         float *EpsilonError;
1856
          // variables for GPU memory
         float *d_VPotential;
float *d_RhoChargeDensity;
1858
1859
1860
          float *d_DeltaResidue;
float *d_coef1;
1861
1862
          float *d_coef2;
1863
          float *d_coef3;
         float *d_coef4;
float *d_icoef4;
1864
1865
1866
          float *d_VPotentialPrev;
1867
          float *d_EpsilonError;
1868
1869
1870
         // variables for coefficent calculations
1871
          float *coef1;
1872
          float *coef2;
          float *coef3;
1873
          float *coef4;
float *icoef4;
1874
1875
1876
          float tempRatioZ;
1877
           float tempRatioPhi;
          float radius;
1878
1879
1880
          int gridFrom;
         int gridTo;
int loops;
1881
1882
1883
        // variables passed from ALIROOT
float gridSizeR = fparam[0];
//float gridSizePhi = fparam[1];
//float gridSizeZ = fparam
float ratioPhi = fparam[3];
1884
1885
1886
1887
                                          = fparam[2];
```

```
float ratioZ
                                 = fparam[4];
                                 = fparam[5];
= fparam[6];
1890
          float convErr
1891
          float IFCRadius
          int nPre = iparam[0];
int nPost = iparam[1];
1892
1893
          int maxLoop = iparam[2];
int nCycle = iparam[3];
1894
1895
1896
1897
           // variables for calculating GPU memory allocation
1898
          int grid_RRow;
          int grid_ZColumn;
1899
          int grid_PhiSlice = PhiSlice;
1900
1901
          int grid_Size = 0;
1902
          int grid_StartPos;
1903
          int coef_Size = 0;
1904
          int coef_StartPos;
          int iOne, jOne;
float h, h2, ih2;
1905
1906
1907
1908
          // variables for calculating multigrid maximum depth
1909
          int depth_RRow = 0;
1910
          int depth_ZColumn = 0;
          int temp_RRow = RRow;
1911
1912
          int temp_ZColumn = ZColumn;
1913
1914
          // calculate depth for multigrid
1915
          while (temp_RRow >>= 1) depth_RRow++;
1916
          while (temp_ZColumn >>= 1) depth_ZColumn++;
1917
          loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
1918
1919
          loops = (loops > maxLoop) ? maxLoop : loops;
1920
1921
          gridFrom = 1;
1922
          gridTo = loops;
1923
          // calculate GPU memory allocation for multigrid
1924
1925
          for (int step = gridFrom; step <= gridTo; step++)</pre>
1926
               grid_RRow = ((RRow - 1) / (1 << (step - 1))) + 1;
grid_ZColumn = ((ZColumn - 1) / (1 << (step - 1))) + 1;
1927
1928
1929
               grid_Size += grid_RRow * grid_ZColumn * grid_PhiSlice;
coef_Size += grid_RRow;
1930
1931
1932
1933
          \ensuremath{//} allocate memory for temporary output
1934
          1935
1936
          EpsilonError = (float *) malloc(1 * sizeof(float));
1937
1938
1939
1940
1941
          for (int i=0;i<grid_Size;i++) temp_VPotential[i] = 0.0;</pre>
1942
1943
1944
          // allocate memory for relaxation coefficient
1945
          coef1 = (float *) malloc(coef_Size * sizeof(float));
1946
          coef2 = (float *) malloc(coef_Size * sizeof(float));
          coef3 = (float *) malloc(coef_Size * sizeof(float));
coef4 = (float *) malloc(coef_Size * sizeof(float));
icoef4 = (float *) malloc(coef_Size * sizeof(float));
1947
1948
1949
1950
1951
          // pre-compute relaxation coefficient
1952
          // restrict boundary
1953
          coef_StartPos = 0;
1954
          grid_StartPos = 0;
1955
          iOne = 1 << (gridFrom - 1);
jOne = 1 << (gridFrom - 1);</pre>
1956
1957
1958
1959
          for (int step = gridFrom; step <= gridTo; step++)</pre>
1960
               grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / iOne) + 1;
1961
1962
1963
               h = gridSizeR * iOne;
1964
1965
               h2 = h * h;
1966
               ih2 = 1.0 / h2;
1967
               tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1968
               tempRatioPhi = ratioPhi * iOne * iOne;
1969
1970
               for (int i = 1; i < grid_RRow - 1; i++)</pre>
1971
1972
1973
                    radius = IFCRadius + i * h;
                    coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
1974
1975
```

```
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
                    coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1977
1978
1979
1980
               // call restrict boundary
1981
1982
               if (step == gridFrom) {
1983
                    // Copy original VPotential to tempPotential
1984
                    memcpy(temp_VPotential,
                                                   VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
1985
1986
                // else
1987
1988
1989
                    Restrict_Boundary(temp_VPotential, grid_RRow, grid_ZColumn, PhiSlice, grid_StartPos);
1990
1991
1992
1993
               coef_StartPos += grid_RRow;
               grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1994
1995
1996
1997
               iOne = 2 * iOne;
               jOne = 2 * jOne;
1998
1999
2000
2001
          // device memory allocation
2002
          cudaMalloc( &d_VPotential, grid_Size * sizeof(float) );
2003
          cudaMalloc( &d_DeltaResidue, grid_Size * sizeof(float) );
2004
          cudaMalloc( &d_RhoChargeDensity, grid_Size * sizeof(float) );
          cudaMalloc( &d_coef1, coef_Size * sizeof(float) );
cudaMalloc( &d_coef2, coef_Size * sizeof(float) );
cudaMalloc( &d_coef3, coef_Size * sizeof(float) );
2005
2006
2007
2008
          cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
2009
          cudaMalloc( &d_icoef4, coef_Size * sizeof(float) );
          cudaMalloc( &d_VPotentialPrev, grid_Size * sizeof(float) );
cudaMalloc( &d_EpsilonError, 1 * sizeof(float) );
2010
2011
2012
2013
2014
           // set memory to zero
          cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
cudaMemset( d_VPotentialPrev, 0, grid_Size * sizeof(float) );
cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
2015
2016
2017
2018
2019
2020
2021
           // set memory to zero
          cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
2022
2023
2024
2025
2026
           // copy data from host to devicei
2027
           // case of FCycle you need to copy all boundary for all
2028
           2029 // cudaMemcpy( d_VPotential, VPotential, grid_Size * isizeof(float), cudaMemcpyHostToDevice ); //check
2030
2031
          cudaMemcpy( d RhoChargeDensity, RhoChargeDensity, RRow * ZColumn * PhiSlice * sizeof(float),
       cudaMemcpyHostToDevice ); //check
2032 // cudaMemcpy( d_RhoChargeDensity, temp_VPotentialPrev, grid_Size * sizeof(float), cudaMemcpyHostToDevice
        ); //check
2033
          cudaMemcpy( d_coef1, coef1, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
          cudaMemcpy( d_coef2, coef2, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
2034
          cudaMemcpy(d_coef3, coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
2035
          cudaMemcpy( d_coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
cudaMemcpy( d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
2036
2037
2038 // cudaMemcpy( d_VPotentialPrev, temp_VPotential, grid_Size * sizeof(float), cudaMemcpyHostToDevice);
2039
2041
2042
          // max exact
2043
2044
          float maxAbsExact = 1.0;
2045
          if (isExactPresent == true)
2046
2047
               maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
2048
2049
2050
           // init iOne,grid_RRow, grid_ZColumn, grid_StartPos, coef_StartPos
2051
          iOne = 1 << (gridFrom - 1);
jOne = 1 << (gridFrom - 1);</pre>
2052
2053
2054
          grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
2055
2056
2057
2058
          grid StartPos = 0;
2059
          coef StartPos = 0:
```

```
2060
2061
2063
          for (int step = gridFrom + 1; step <= gridTo; step++)</pre>
2064
2065
              iOne = 1 << (step - 1);
2066
              jOne = 1 << (step - 1);
2067
2068
              grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
coef_StartPos += grid_RRow;
2069
2070
2071
2072
                               = ((RRow - 1) / iOne) + 1;
              arid RRow
2073
              grid_ZColumn
                               = ((ZColumn - 1) / jOne) + 1;
2074
2075
              // pre-compute constant memory
              h = gridSizeR * iOne;
h2 = h * h;
2076
2077
2078
              ih2 = 1.0 / h2;
2079
2080
              tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
2081
              tempRatioPhi = ratioPhi * iOne * iOne;
2082
2083
              // copy constant to device memory
              cudaMemcpyToSymbol( d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
2084
2085
              cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
2086
2087
              \verb| cudaMemcpyToSymbol( d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
2088
              cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
2089
2090
              // set kernel grid size and block size
              dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
2091
      grid_ZColumn / 16), PhiSlice);
2092
              dim3 grid_ThreadPerBlock(16, 16);
2093
2094
              // restriction
              restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
2095
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice );
2096
2097
                 restrict boundary (already done in cpu)
2099 //
              PrintMatrix(temp_VPotential,grid_RRow * PhiSlice,grid_ZColumn);
2100
              restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, d_VPotential,
      grid_RRow, grid_ZColumn, grid_PhiSlice );
2101
2102
2103
2104
2105
         dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (grid_ZColumn
        / 16), PhiSlice);
2106
         dim3 grid ThreadPerBlock(16, 16);
2107
2108
2109
          // relax on the coarsest
2110
          // red-black gauss seidel relaxation (nPre times)
2111 // printf("rho\n");
2112 // cudaMemcpy( temp
         cudaMemcpy( temp_VPotential, d_RhoChargeDensity + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice *
       sizeof(float), cudaMemcpyDeviceToHost );
2113 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
2114
2115 // printf("v\n");
2116 //
         cudaMemcpy( temp_VPotential, d_VPotential + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice *
       sizeof(float), cudaMemcpyDeviceToHost );
2117 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
2118
          for (int i = 0; i < nPre; i++)</pre>
2120
              relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
2121
              cudaDeviceSynchronize();
              relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
2122
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
2123
              cudaDeviceSynchronize();
2124
2125
2126 // printf("v after relax\n");
2127 // cudaMemcpy( temp_VPotentia
       / cudaMemcpy( temp_VPotential, d_VPotential + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToHost );
2128 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
2129
          // V-Cycle => from coarser to finer grid
2130
2131
          for (int step = gridTo -1; step >= gridFrom; step--)
2132
              iOne = iOne / 2;
2133
2134
              jOne = jOne / 2;
2135
              grid_RRow
2136
                               = ((RRow - 1) / iOne) + 1;
              grid_ZColumn
2137
                               = ((ZColumn - 1) / jOne) + 1;
2138
2139
              grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
```

```
coef_StartPos -= grid_RRow;
2141
2142
                       h = gridSizeR * iOne;
                       h2 = h * h;
2143
                       ih2 = 1.0 / h2;
2144
2145
                       tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
2146
                       tempRatioPhi = ratioPhi * iOne * iOne;
2147
2148
2149
                       // copy constant to device memory
                       \verb|cudaMemcpyToSymbol(d_grid_StartPos, \&grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice)|;\\
2150
                       cudaMemopyToSymbol(d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemopyHostToDevice);
2151
                       cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
cudaMemcpyToSymbol( d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
2152
2153
2154
                       cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
2155
2156
2157
2158
                       // set kernel grid size and block size
2159
                       dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
          grid_ZColumn / 16), PhiSlice);
2160
                      dim3 grid_ThreadPerBlock(16, 16);
2161
2162
2163
                       prolongation2DHalfNoAdd<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential, grid_RRow,
          grid_ZColumn, grid_PhiSlice );
2164
2165
2166
2167
                      // just
2168
2169
2170
                       \verb|cudaMemcpy| ( d_VPotentialPrev + grid_StartPos, d_VPotential + grid_StartPos, grid_RRow * to the following that the description of the descrip
2171
          grid_ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToDevice );
2172
2173
                       float maxAbsExact = 1.0;
2174
2175
                       if (isExactPresent == true)
                      maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
dim3 error_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (</pre>
2176
2177
          grid_ZColumn / 16), PhiSlice);
    dim3 error_ThreadPerBlock(16, 16);
2178
2179
2180
2181
2182
                       for (int cycle = 0; cycle < nCycle; cycle++)</pre>
2183
2184
2185
2186
                              if (step == gridFrom) {
                                     cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
2187
           cudaMemcpyDeviceToHost );
2188
                                     if (isExactPresent == true )errorExact[cycle] = GetErrorNorm2(temp_VPotential,
          VPotentialExact, RRow * PhiSlice, ZColumn, maxAbsExact);
2189
2190
2191
2192
2193
                              //cudaDeviceSynchronize();
                              VCycleSemiCoarseningGPU(d_VPotential, d_RhoChargeDensity, d_DeltaResidue, d_coef1, d_coef2,
2194
          d_coef3, d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, step, gridTo, nPre, nPost);
2195
2196
2197
2198
                                     //if (step == gridFrom) {
2199
                                      //cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
            cudaMemcpvDeviceToHost );
2200
2201
                                      //errorConv[cycle] = GetErrorNorm2(temp_VPotential, VPotentialPrev, RRow *
            PhiSlice, ZColumn, 1.0);
2202
2203
                                     errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev +
           grid_StartPos, d_VPotential + grid_StartPos, d_EpsilonError, grid_RRow, grid_ZColumn, PhiSlice);
2204
2205
                                     cudaMemcpy( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost );
2206
2207
                                     errorConv[cycle] = *EpsilonError / (grid_RRow * grid_ZColumn * PhiSlice);
2208
2209
                                     if (errorConv[cvcle] < convErr)</pre>
2210
2211
                                            nCycle = cycle;
2212
2213
2214
                                     \verb|cudaMemcpy| ( d_VPotentialPrev + grid_StartPos, d_VPotential + grid_StartPos, grid_RRow * \\
2215
           grid ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToDevice);
```

```
cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
2217
2218
2219
2220
2221
         }
2222
2223
         iparam[3] = nCycle;
2224
         // copy result from device to host cudaMemopy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
2225
2226
      cudaMemcpyDeviceToHost );
2227
2228
         memcpy(VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
2229
2230
         // free device memory
2231
         cudaFree( d_VPotential );
cudaFree( d_DeltaResidue );
2232
2233
         cudaFree( d_RhoChargeDensity );
2234
         cudaFree( d_coef1 );
2235
         cudaFree( d_coef2 );
2236
         cudaFree( d_coef3 );
2237
         cudaFree( d_coef4 );
2238
         cudaFree( d_icoef4 );
2239
2240
         // free host memory
2241
         free( coef1 );
2242
         free ( coef2 );
2243
         free( coef3 );
2244
         free ( coef4 );
         free ( icoef4 );
2245
2246
         free( temp_VPotential );
2247
         free ( VPotentialPrev );
2248 }
```

6.3.2.3 PoissonMultigrid3DSemiCoarseningGPUErrorWCycle()

innner w cycle up one down one

end up one down on

up two down two

up one down one

end up one down one

Definisi pada baris 1147 dalam file PoissonSolver3DGPU.cu.

```
float *d_VPotential;
          float *d_RhoChargeDensity;
1168
1169
          float *d_DeltaResidue;
1170
          float *d_coef1;
          float *d_coef2;
1171
1172
          float *d_coef3;
         float *d_coef4;
1173
1174
          float *d_icoef4;
1175
          float *d_VPotentialPrev;
1176
          float *d_EpsilonError;
1177
1178
        // variables for coefficent calculations
float *coef1;
1179
1180
1181
          float *coef2;
         float *coef3;
float *coef4;
1182
1183
         float *icoef4;
float tempRatioZ;
1184
1185
1186
          float tempRatioPhi;
1187
         float radius;
1188
1189
          int gridFrom;
         int gridTo;
int loops;
1190
1191
1192
1193
          // variables passed from ALIROOT
        float gridSizeR = fparam[0];
//float gridSizePhi = fparam[1];
1194
         //float gridSizeZ
float ratioPhi = fparam[3];
Cloat ratioZ = fparam[4];
Cloat ratioZ = fparam[5];
1195
                                       = fparam[2];
1196
1197
         float ratioZ
float convErr
1198
          float ratioZ = fparam[4];
float convErr = fparam[5];
float IFCRadius = fparam[6];
1199
1200
         int nPre = iparam[0];
int nPost = iparam[1];
1201
1202
         int maxLoop = iparam[2];
int nCycle = iparam[3];
1203
1204
1205
1206
          // variables for calculating GPU memory allocation
1207
         int grid_RRow;
          int grid_ZColumn;
1208
          int grid_PhiSlice = PhiSlice;
1209
1210
          int grid_Size = 0;
         int grid_StartPos;
int coef_Size = 0;
1211
1212
1213
         int coef_StartPos;
          int iOne, jOne; float h, h2, ih2;
1214
1215
1216
1217
          // variables for calculating multigrid maximum depth
1218
          int depth_RRow = 0;
1219
          int depth_ZColumn = 0;
1220
          int temp_RRow = RRow;
          int temp_ZColumn = ZColumn;
1221
1222
          // calculate depth for multigrid
1224
          while (temp_RRow >>= 1) depth_RRow++;
1225
          while (temp_ZColumn >>= 1) depth_ZColumn++;
1226
          loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
1227
          loops = (loops > maxLoop) ? maxLoop : loops;
1228
1229
1230
          gridFrom = 1;
1231
          gridTo = loops;
1232
1233
          // calculate GPU memory allocation for multigrid
1234
          for (int step = gridFrom; step <= gridTo; step++)</pre>
1235
               grid_RRow = ((RRow - 1) / (1 << (step - 1))) + 1;
grid_ZColumn = ((ZColumn - 1) / (1 << (step - 1))) + 1;
1236
1237
1238
               grid_Size += grid_RRow * grid_ZColumn * grid_PhiSlice;
coef_Size += grid_RRow;
1239
1240
1241
          }
1242
1243
          // allocate memory for temporary output
          temp_VPotential = (float *) malloc(grid_Size * sizeof(float));
VPotentialPrev = (float *) malloc(RRow * ZColumn * PhiSlice * sizeof(float));
1244
1245
          EpsilonError = (float *) malloc(1 * sizeof(float));
1246
1247
1248
          // allocate memory for relaxation coefficient
1249
1250
          coef1 = (float *) malloc(coef_Size * sizeof(float));
          coef2 = (float *) malloc(coef_Size * sizeof(float));
1251
          coef3 = (float *) malloc(coef_Size * sizeof(float));
coef4 = (float *) malloc(coef_Size * sizeof(float));
1252
1253
```

```
icoef4 = (float *) malloc(coef_Size * sizeof(float));
1255
1256
            // pre-compute relaxation coefficient
1257
            coef_StartPos = 0;
            iOne = 1 << (gridFrom - 1);
1258
            jOne = 1 << (gridFrom - 1);
1259
1260
1261
            for (int step = gridFrom; step <= gridTo; step++)</pre>
1262
                 grid_RRow = ((RRow - 1) / iOne) + 1;
1263
1264
                 h = gridSizeR * iOne;
1265
                 h2 = h * h;
1266
1267
                 ih2 = 1.0 / h2;
1268
1269
                  tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1270
                 tempRatioPhi = ratioPhi * iOne * iOne;
1271
1272
                  for (int i = 1; i < grid_RRow - 1; i++)</pre>
1273
                  {
1274
                       radius = IFCRadius + i * h;
                       coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
1275
1276
1277
                       coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1278
1279
1280
1281
                  coef_StartPos += grid_RRow;
                 iOne = 2 * iOne;
jOne = 2 * jOne;
1282
1283
1284
1285
1286
            // device memory allocation
1287
            cudaMalloc( &d_VPotential, grid_Size \star sizeof(float) );
            cudaMalloc( &d_DeltaResidue, grid_Size * sizeof(float) );
cudaMalloc( &d_VPotentialPrev, RRow * ZColumn * PhiSlice * sizeof(float) );
cudaMalloc( &d_EpsilonError, 1 * sizeof(float) );
1288
1289
1290
1291
1292
            cudaMalloc( &d_RhoChargeDensity, grid_Size * sizeof(float) );
            cudaMalloc( &d_coef1, coef_Size * sizeof(float) );
cudaMalloc( &d_coef2, coef_Size * sizeof(float) );
1293
1294
            cudaMalloc( &d_coef3, coef_Size * sizeof(float) );
cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
cudaMalloc( &d_icoef4, coef_Size * sizeof(float) );
1295
1296
1297
1298
1299
            // set memory to zero
1300
            cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
            cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
cudaMemset( d_VPotentialPrev, 0, RRow * ZColumn * PhiSlice * sizeof(float) );
1301
1302
1303
            cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1304
1305
1306
1307
            // copy data from host to device % \left( 1\right) =\left( 1\right) ^{2}
            cudaMemcpy( d_VPotential, VPotential, RRow * ZColumn * PhiSlice * sizeof(float), cudaMemcpyHostToDevice
1308
         ); //check
1309
            cudaMemcpy( d_RhoChargeDensity, RhoChargeDensity, RRow * ZColumn * PhiSlice * sizeof(float),
        cudaMemcpyHostToDevice ); //check
1310
            cudaMemcpy( d_coef1, coef1, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1311
            cudaMemcpy( d_coef2, coef2, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
            cudaMemcpy(d_coef3, coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
cudaMemcpy(d_coef4, coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
cudaMemcpy(d_icoef4, coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
cudaMemcpy(d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
cudaMemcpy(d_VPotentialPrev, VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1312
1313
1314
1315
        cudaMemcpyHostToDevice );
1316
                                 float maxAbsExact = GetAbsMax(VPotentialExact,RRow * PhiSlice * ZColumn);
1317
            float maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
1318
            dim3 error_BlockPerGrid((RRow < 16) ? 1 : (RRow / 16), (ZColumn < 16) ? 1 : (ZColumn / 16), PhiSlice);
1319
1320
            dim3 error_ThreadPerBlock(16, 16);
1321
1322
1323
            for (int cycle = 0; cycle < nCycle; cycle++)</pre>
1324
1325
            /*V-Cycle starts*/
1326
1327
                    error conv
1328
                  // cudaMemcpy( temp_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
         cudaMemcpyDeviceToHost );
1329
                 cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1330
        cudaMemcpyDeviceToHost );
                  errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact, RRow * PhiSlice, ZColumn,
        maxAbsExact);
1332
1333
1334
                 // V-Cvcle => Finest Grid
```

```
iOne = 1 \ll (gridFrom - 1);
             jOne = 1 << (gridFrom - 1);</pre>
1336
1337
                             = ((RRow - 1) / iOne) + 1;
= ((ZColumn - 1) / jOne) + 1;
1338
             grid RRow
1339
             grid ZColumn
1340
1341
             grid_StartPos = 0;
             coef_StartPos = 0;
1342
1343
1344
             // pre-compute constant memory
             h = gridSizeR * iOne;
h2 = h * h;
1345
1346
1347
             ih2 = 1.0 / h2;
1348
1349
             tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1350
             tempRatioPhi = ratioPhi * iOne * iOne;
1351
1352
             // copy constant to device memory
1353
             cudaMemcpyToSymbol( d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
             cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice);
1354
             cudaMemcpyToSymbol(d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice); cudaMemcpyToSymbol(d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
1355
1356
1357
             \verb|cudaMemcpyToSymbol(d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice)|; \\
1358
               set kernel grid size and block size
1359
             dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1360
     grid_ZColumn / 16), PhiSlice);
1361
             dim3 grid_ThreadPerBlock(16, 16);
1362
1363
             // red-black gauss seidel relaxation (nPre times)
             for (int i = 0; i < nPre; i++)</pre>
1364
1365
             {
                 relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1366
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1367
                 //cudaDeviceSynchronize();
                 relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1368
     1369
1370
1371
1372
             // residue calculation
             residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, d_RhoChargeDensity,
1373
       d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1374
             //cudaDeviceSynchronize();
1375
1376
             // V-Cycle => from finer to coarsest grid
1377
             for (int step = gridFrom + 1; step <= gridTo; step++)</pre>
1378
             {
1379
                 iOne = 1 << (step - 1);
jOne = 1 << (step - 1);
1380
1381
1382
                 grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1383
                 coef_StartPos += grid_RRow;
1384
                 grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1385
1386
1387
1388
                 // pre-compute constant memory
                 h = gridSizeR * iOne;
h2 = h * h;
1389
1390
                 ih2 = 1.0 / h2;
1391
1392
1393
                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1394
                 tempRatioPhi = ratioPhi * iOne * iOne;
1395
                 // copy constant to device memory
1396
                 1397
       );
1398
                 cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
       );
1399
                 \verb|cudaMemcpyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice |);|\\
1400
                 \verb|cudaMemcpyToSymbol(d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);|\\
1401
                 \verb| cudaMemcpyToSymbol( d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
1402
                 // set kernel grid size and block size
1403
                 dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
      grid_ZColumn / 16), PhiSlice);
1405
                 dim3 grid_ThreadPerBlock(16, 16);
1406
1407
                 // restriction
                 restriction2DFull<<< grid BlockPerGrid, grid ThreadPerBlock >>>( d RhoChargeDensity,
1408
     d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1409
                 //cudaDeviceSynchronize();
1410
1411
                 // zeroing V
                 zeroingVPotential<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1412
      grid_ZColumn, grid_PhiSlice );
```

```
1413
                 //cudaDeviceSynchronize();
1414
1415
                  // red-black gauss seidel relaxation (nPre times)
1416
                  for (int i = 0; i < nPre; i++)</pre>
1417
                      relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1418
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1419
                      //cudaDeviceSynchronize();
1420
                      relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1421
                      //cudaDeviceSynchronize();
1422
1423
1424
                  // residue calculation
1425
                  if (step < gridTo)</pre>
1426
                      residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1427
      \verb|d_RhoChargeDensity|, | \verb|d_DeltaResidue|, | grid_RRow|, | grid_ZColumn|, | grid_PhiSlice|, | \verb|d_coef1|, | d_coef2|, | d_coef3|, | d_icoef4|); \\
1428
                     //cudaDeviceSynchronize();
1429
1430
1431
             }
1434
             // up one
1435
1436
1437
1438
1439
                  int step = (gridTo - 1);
                 iOne = iOne / 2;
jOne = jOne / 2;
1440
1441
1442
1443
                  grid_RRow
                                  = ((RRow - 1) / iOne) + 1;
1444
                  grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1445
                  grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
coef_StartPos -= grid_RRow;
1446
1447
1448
                 h = gridSizeR * iOne;
h2 = h * h;
1449
1450
1451
                  ih2 = 1.0 / h2;
1452
1453
                  tempRatioPhi = ratioPhi * iOne * iOne;
1454
                  // copy constant to device memory
1455
1456
                  );
1457
                  cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
       );
1458
                  cudaMemcpyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
                 cudaMemcpyToSymbol(d_in2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
cudaMemcpyToSymbol(d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
1459
1460
1461
1462
                  // set kernel grid size and block size
1463
                 dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
      grid_ZColumn / 16), PhiSlice);
1464
                 dim3 grid_ThreadPerBlock(16, 16);
1465
1466
             // prolongation
                 prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
      grid_ZColumn, grid_PhiSlice );
1468 //
                 cudaDeviceSynchronize();
1469
1470
                  // red-black gauss seidel relaxation (nPost times)
1471
                  for (int i = 0; i < nPost; i++)</pre>
1472
1473
                      relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1474 //
                      cudaDeviceSvnchronize();
                      relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1475
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1476 //
                     cudaDeviceSynchronize();
1477
                 }
1478
             }
1479
              // down one
1480
1481
                  residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1482
      d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1483
                  iOne = iOne * 2:
1484
                  jOne = jOne * 2;
1485
1486
                  grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1487
1488
                  coef_StartPos += grid_RRow;
1489
                 grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1490
1491
```

```
1493
                            // pre-compute constant memory
                           h = gridSizeR * iOne;
h2 = h * h;
1494
1495
1496
                           ih2 = 1.0 / h2;
1497
                            tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1498
1499
                            tempRatioPhi = ratioPhi * iOne * iOne;
1500
1501
1502
                            // copy constant to device memory
                            1503
           );
1504
                            cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
           );
                           1505
1506
1507
                            cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1508
                            // set kernel grid size and block size
                            \label{eq:dim3} \ \mbox{grid\_BlockPerGrid((grid\_RRow < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_RRow / 16) ? 1 : (grid\_RRow / 16), (grid\_RRow / 16) ? 1 : (
         grid_ZColumn / 16), PhiSlice);
1511
                           dim3 grid_ThreadPerBlock(16, 16);
1512
1513
                            // restriction
                            restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
1514
         d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1515
                           //cudaDeviceSynchronize();
1516
1517
                            // zeroing V
                           zeroingVPotential<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1518
         grid_ZColumn, grid_PhiSlice );
1519
                           //cudaDeviceSynchronize();
1520
                           // red-black gauss seidel relaxation (nPre times) for (int i = 0; i < nPre; i++)
1521
1522
1523
                            {
1524
                                  relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1525
                               //cudaDeviceSynchronize();
1526
                                  relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1527
                                 //cudaDeviceSynchronize();
1528
1529
1530
                     }
1532
                     // up two from gridTo - 1, to gridTo -3
for (int step = (gridTo - 1); step >= gridTo - 3; step--)
1534
1535
1536
1537
                            iOne = iOne / 2;
1538
                            jOne = jOne / 2;
1539
                                                  = ((RRow - 1) / iOne) + 1;
= ((ZColumn - 1) / jOne) + 1;
1540
                            grid RRow
1541
                           grid_ZColumn
1542
1543
                            grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
                           coef_StartPos -= grid_RRow;
1544
1545
                           h = gridSizeR * iOne;
h2 = h * h;
1546
1547
                           ih2 = 1.0 / h2;
1548
1549
1550
                            tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1551
                            tempRatioPhi = ratioPhi * iOne * iOne;
1552
1553
                            // copy constant to device memory
                            \verb|cudaMemcpyToSymbol(d_grid_StartPos, \&grid_StartPos, 1 * size of (int), 0, cudaMemcpyHostToDevice| \\
1554
           );
1555
                            );
1556
                            \verb|cudaMemcpyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice |);|
1557
                            \verb|cudaMemcpyToSymbol(d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice |);|\\
                            cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1558
1559
1560
                             // set kernel grid size and block size
                            dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1561
         grid_ZColumn / 16), PhiSlice);
1562
                           dim3 grid_ThreadPerBlock(16, 16);
1563
                            // prolongation
1564
                           prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1565
          grid_ZColumn, grid_PhiSlice );
1566 //
                           cudaDeviceSynchronize();
1567
                           // red-black gauss seidel relaxation (nPost times) for (int i = 0; i < nPost; i++)
1568
1569
```

```
{
                                     relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1571
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1572 //
                                    cudaDeviceSynchronize();
1573
                                    relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1574 //
                                   cudaDeviceSynchronize();
1575
1576
                       }
1577
                      // down to from gridTo - 1, to gridTo -3
for (int step = gridTo - 3; step <= gridTo - 1; step++)</pre>
1578
1579
1580
                             iOne = iOne * 2;
1581
1582
                             jOne = jOne * 2;
1583
                             grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1584
                             coef_StartPos += grid_RRow;
1585
1586
1587
                             grid_RRow
                                                        = ((RRow - 1) / iOne) + 1;
1588
                                                        = ((ZColumn - 1) / jOne) + 1;
                             grid ZColumn
1589
1590
                              // pre-compute constant memory
                             h = gridSizeR * iOne;
h2 = h * h;
1591
1592
                             ih2 = 1.0 / h2;
1593
1594
1595
                             tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1596
                             tempRatioPhi = ratioPhi * iOne * iOne;
1597
1598
                              // copy constant to device memory
1599
                             cudaMemcpyToSymbol(d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
            );
1600
                             );
1601
                             \verb| cudaMemcpyToSymbol( d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
                             cudaMemcpyToSymbol(d_ih2,&ih2,1 * sizeof(float),0, cudaMemcpyHostToDevice);
cudaMemcpyToSymbol(d_tempRatioZ, &tempRatioZ,1 * sizeof(float),0, cudaMemcpyHostToDevice);
1602
1603
1604
1605
                              // set kernel grid size and block size
1606
                             \label{eq:dim3} \mbox{grid\_BlockPerGrid((grid\_RRow < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_Rrow 
          grid_ZColumn / 16), PhiSlice);
1607
                             dim3 grid ThreadPerBlock (16, 16);
1608
1609
                              // restriction
1610
                             restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_RhoChargeDensity,
          d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1611
                             //cudaDeviceSynchronize();
1612
1613
                             // zeroing V
1614
                             zeroingVPotential <<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential, grid_RRow,
          grid_ZColumn, grid_PhiSlice );
1615
                             //cudaDeviceSynchronize();
1616
                             // red-black gauss seidel relaxation (nPre times)
1617
                             for (int i = 0; i < nPre; i++)
1618
1619
                                     relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1620
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1621
                                    //cudaDeviceSynchronize();
1622
                                     relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1623
                                    //cudaDeviceSynchronize();
1624
1625
1626
                             // residue calculation
1627
                             if (step < gridTo)</pre>
1628
                                     residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1629
          d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1630
                                   //cudaDeviceSynchronize();
1631
1632
                       }
1633
1634
1635
1636
1638
1639
                             int step = (gridTo - 1);
                             iOne = iOne / 2;
jOne = jOne / 2;
1640
1641
1642
                             grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1643
1644
1645
                             grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
1646
                             coef_StartPos -= grid_RRow;
1647
```

```
h = gridSizeR * iOne;
h2 = h * h;
1649
1650
                                                ih2 = 1.0 / h2;
1651
1652
                                                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1653
1654
                                                 tempRatioPhi = ratioPhi * iOne * iOne;
1655
1656
                                                  // copy constant to device memory
1657
                                                 \verb|cudaMemcpyToSymbol(d_grid_StartPos, \&grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice| | (int), (int)
                    );
1658
                                                 cudaMemcpvToSymbol ( d coef StartPos, &coef StartPos, 1 * sizeof(int), 0, cudaMemcpvHostToDevice
                    );
1659
                                                 cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1660
                                                 \verb| cudaMemcpyToSymbol(d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice); \\
1661
                                                 \verb|cudaMemcpyToSymbol(d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);| \\
1662
1663
                                                 // set kernel grid size and block size
                                                 dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1664
                grid_ZColumn / 16), PhiSlice);
1665
                                                dim3 grid_ThreadPerBlock(16, 16);
1666
1667
                                     // prolongation
                                                prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1668
                 grid_ZColumn, grid_PhiSlice );
1669 //
                                              cudaDeviceSynchronize();
1670
                                                // red-black gauss seidel relaxation (nPost times) for (int i = 0; i < nPost; i++)  
1671
1672
1673
                                                             relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1674
                 d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1675 //
                                                           cudaDeviceSynchronize();
                                                             relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1676
                 d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1677 //
                                                           cudaDeviceSynchronize();
1678
1679
                                     }
1680
1681
                                      // down one
1682
                                                \verb|residueCalculation| <<< \verb|grid_BlockPerGrid|, grid_ThreadPerBlock| >>> ( | d_VPotential|, | d_VPotential
1683
                d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1684
1685
                                                 iOne = iOne * 2;
1686
                                                 jOne = jOne * 2;
1687
1688
                                                 grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
                                                 coef_StartPos += grid_RRow;
1689
1690
1691
                                                 grid_RRow
                                                                                             = ((RRow - 1) / iOne) + 1;
1692
                                                                                         = ((ZColumn - 1) / jOne) + 1;
                                                 grid_ZColumn
1693
1694
                                                 // pre-compute constant memory
                                                h = gridSizeR * iOne;
h2 = h * h;
1695
1696
1697
                                                 ih2 = 1.0 / h2;
1698
1699
                                                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1700
                                                 tempRatioPhi = ratioPhi * iOne * iOne;
1701
1702
1703
                                                 // copy constant to device memory
1704
                                                 );
1705
                                                 );
                                                1706
1707
1709
1710
                                                 // set kernel grid size and block size
1711
                                                 dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (</pre>
                 grid_ZColumn / 16), PhiSlice);
                                                dim3 grid_ThreadPerBlock(16, 16);
1712
1713
1714
1715
                                                 restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
                 d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1716
                                                //cudaDeviceSynchronize();
1717
1718
                                                 // zeroing V
                                                 {\tt zeroing VPotential} <<< {\tt grid\_BlockPerGrid}, {\tt grid\_ThreadPerBlock} >>>  ( {\tt d\_VPotential}, {\tt grid\_RRow}, {\tt grid\_Rr
1719
                 grid_ZColumn, grid_PhiSlice );
1720
                                                //cudaDeviceSynchronize();
1721
1722
                                                 // red-black gauss seidel relaxation (nPre times)
```

```
1723
                for (int i = 0; i < nPre; i++)</pre>
1724
1725
                    relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
     d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1726
                    //cudaDeviceSynchronize();
                    relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential,
1727
     d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1728
                    //cudaDeviceSynchronize();
1729
1730
            }
1731
1733
1735
1736
            // V-Cycle => from coarser to finer grid
1737
            for (int step = (gridTo - 1); step >= gridFrom; step--)
1738
                iOne = iOne / 2;
1739
                jOne = jOne / 2;
1740
1741
1742
                grid_RRow
                               = ((RRow - 1) / iOne) + 1;
1743
                              = ((ZColumn - 1) / jOne) + 1;
                grid ZColumn
1744
                grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
coef_StartPos -= grid_RRow;
1745
1746
1747
1748
                h = gridSizeR * iOne;
h2 = h * h;
1749
1750
                ih2 = 1.0 / h2;
1751
1752
                tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1753
                tempRatioPhi = ratioPhi * iOne * iOne;
1754
1755
                 // copy constant to device memory
1756
                );
1757
                cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
      );
1758
                cudaMemcpyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
1759
                cudaMemcpyToSymbol( d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1760
                cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1761
1762
                // set kernel grid size and block size
                dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1763
     grid_ZColumn / 16), PhiSlice);
1764
                dim3 grid_ThreadPerBlock(16, 16);
1765
1766
                // prolongation
1767
                grid_ZColumn, grid_PhiSlice );
1768 //
                cudaDeviceSvnchronize();
1769
1770
                 // red-black gauss seidel relaxation (nPost times)
1771
                for (int i = 0; i < nPost; i++)</pre>
1772
                    relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1773
     d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4 );
1774 //
                   cudaDeviceSynchronize();
                    relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1775
     d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1776 //
                    cudaDeviceSynchronize();
1777
1778
            }
1779
1780
        /*V-Cvcle ends*/
1781
1782
            errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev, d_VPotential,
     d_EpsilonError, RRow, ZColumn, PhiSlice);
1783
1784
            cudaMemcpy( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost );
1785
1786
1787
            errorConv[cycle] = *EpsilonError / (RRow * ZColumn * PhiSlice);
1788
1789
            if (errorConv[cycle] < convErr)</pre>
1790
1791
                 //errorConv
1792
                nCycle = cycle;
1793
                iparam[3] = nCycle;
1794
                break;
1795
1796
1797
            cudaMemcpy( d_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
     cudaMemcpyDeviceToDevice );
1798
            cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1799
1800
1801
```

```
1804
          cudaDeviceSynchronize();
1805
          \ensuremath{//} copy result from device to host
1806
          cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyDeviceToHost );
1807
1808
          \verb|memcpy| (VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float)); \\
1809
1810
         // free device memory
         cudaFree( d_VPotential );
cudaFree( d_VPotentialPrev );
1811
1812
1813
         cudaFree( d_EpsilonError );
1814
1815
1816
       cudaFree( d_DeltaResidue );
1817
         cudaFree( d_RhoChargeDensity );
         cudaFree( d_coef1 );
1818
         cudaFree( d_coef2 );
1819
        cudaFree( d_coef3 );
cudaFree( d_coef4 );
1820
1821
1822
         cudaFree( d_icoef4 );
1823
       // free host memory
free( coef1 );
free( coef2 );
1824
1825
1826
1827
         free( coef3 );
1828
         free( coef4 );
1829
         free( icoef4 );
         free( temp_VPotential );
1830
1831
         //free( temp_VPotentialPrev );
1832 }
```

6.3.2.4 PrintMatrix()

```
void PrintMatrix (
            float * Mat,
             const int Row,
             const int Column )
```

Print matrix

Definisi pada baris 675 dalam file PoissonSolver3DGPU.cu.

```
680 {
        printf("Matrix (%d,%d)\n",Row,Column);
681
        for (int i=0; i<Row; i++)
682
684
            for (int j=0; j<Column; j++)</pre>
685
                 printf("%11.4g ",Mat[i*Column + j]);
686
687
688
            printf("\n");
689
690
691 }
```

6.3.2.5 relaxationGaussSeidelBlack()

```
__global__ void relaxationGaussSeidelBlack (
            float * VPotential,
            float * RhoChargeDensity,
            const int RRow,
            const int ZColumn,
            const int PhiSlice,
            float * coef1,
            float * coef2,
            float * coef3,
            float * coef4 )
```

Relaksasi menggunakan penyelesaian iteratif Red-Black Gauss-Seidel (bagian Black)

Parameter

VPotential	float* Array potensial	
RhoChargeDensity	float* Array rapat arus	
RRow	int Jumlah baris di arah sumbu \boldsymbol{r}	
ZColumn	int Jumlah kolom di arah sumbu \boldsymbol{z}	
PhiSlice	int Jumlah irisan di arah sumbu ϕ	
coef1	float st Array untuk koefisien $V_{x+1,y,z}$	
coef2	float st Array untuk koefisien $V_{x-1,y,z}$	
coef3	float st Array untuk koefisien z	
coef4	float $*$ Array untuk koefisien $f(r,\phi,z)$	

Definisi pada baris 104 dalam file PoissonSolver3DGPU.cu.

```
115 {
116
        int index_x, index_y, index, index_left, index_right, index_up, index_down, index_front, index_back,
      index_coef;
117
118
        index_x = blockIdx.x * blockDim.x + threadIdx.x;
119
       index_y = blockIdx.y * blockDim.y + threadIdx.y;
120
121
                    = d_qrid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + index_x;
       index_left = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x - 1);
122
123
        index_right = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x + 1);
       index_up = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y - 1) * ZColumn + index_x; index_down = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y + 1) * ZColumn + index_x;
124
125
       index_front = d_grid_StartPos + ((blockIdx.z - 1 + PhiSlice) % PhiSlice) * RRow * ZColumn + index_y *
126
      ZColumn + index_x;
127
        index_back = d_grid_StartPos + ((blockIdx.z + 1) % PhiSlice) * RRow * ZColumn + index_y * ZColumn +
       index_coef = d_coef_StartPos + index_y;
128
129
        if (index_x != 0 && index_x < (ZColumn - 1) && index_y != 0 && index_y < (RRow - 1))
130
131
       {
132
            //calculate black
133
            if ((blockIdx.z % 2 == 0 && (index_x + index_y) % 2 != 0) || (blockIdx.z % 2 != 0 && (index_x +
      index_y) % 2 == 0))
134
               135
136
137
                                     d_tempRatioZ * (VPotential[index_left] + VPotential[index_right]) +
                                     coef3[index_coef] * (VPotential[index_front] + VPotential[index_back]) +
138
                                     d_h2 * RhoChargeDensity[index]) * coef4[index_coef];
140
141
       }
142 }
```

6.3.2.6 relaxationGaussSeidelRed()

```
__global__ void relaxationGaussSeidelRed (
    float * VPotential,
    float * RhoChargeDensity,
    const int RRow,
    const int ZColumn,
    const int PhiSlice,
    float * coef1,
    float * coef2,
    float * coef3,
    float * coef4 )
```

Relaksasi menggunakan penyelesaian iteratif Red-Black Gauss-Seidel (bagian Red)

Parameter

VPotential	float* Array potensial
RhoChargeDensity	float* Array rapat arus
RRow	int Jumlah baris di arah sumbu \boldsymbol{r}
ZColumn	int Jumlah kolom di arah sumbu \boldsymbol{z}
PhiSlice	int Jumlah irisan di arah sumbu ϕ
coef1	float st Array untuk koefisien $V_{x+1,y,z}$
coef2	float st Array untuk koefisien $V_{x-1,y,z}$
coef3	float st Array untuk koefisien z
coef4	float $*$ Array untuk koefisien $f(r,\phi,z)$

Definisi pada baris 52 dalam file PoissonSolver3DGPU.cu.

```
int index_x, index_y, index, index_left, index_right, index_up, index_down, index_front, index_back,
      index_coef;
65
       index_x = blockIdx.x * blockDim.x + threadIdx.x;
66
       index_y = blockIdx.y * blockDim.y + threadIdx.y;
69
                     = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + index_x;
       index_left = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x - 1);
index_right = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x + 1);
index_up = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y - 1) * ZColumn + index_x;
index_down = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y + 1) * ZColumn + index_x;
70
71
72
73
74
        index_front = d_grid_StartPos + ((blockIdx.z - 1 + PhiSlice) % PhiSlice) * RRow * ZColumn + index_y *
       ZColumn + index_x;
7.5
        index_back = d_grid_StartPos + ((blockIdx.z + 1) % PhiSlice) * RRow * ZColumn + index_y * ZColumn +
      index_x;
76
       index coef = d coef StartPos + index v;
78
        if (index_x != 0 && index_x < (ZColumn - 1) && index_y != 0 && index_y < (RRow - 1))
79
80
             //calculate red
            if ((blockIdx.z % 2 == 0 && (index_x + index_y) % 2 == 0) || (blockIdx.z % 2 != 0 && (index_x +
81
      index_y) % 2 != 0))
83
                 VPotential[index] = (coef2[index_coef] * VPotential[index_up] +
                                         coef1[index_coef] * VPotential[index_down] +
85
                                         d_tempRatioZ * (VPotential[index_left] + VPotential[index_right]) +
86
                                         87
                                         d_h2 * RhoChargeDensity[index]) * coef4[index_coef];
88
            }
89
        }
90 }
```

6.3.2.7 residueCalculation()

Menghitung residu dari hasil proses relaksasi

Rumus:

Parameter

<i>VPotential</i>	float* Array potensial
RhoChargeDensity	float* Array rapat arus
DeltaResidue	float* Array residu
RRow	int Jumlah baris di arah sumbu \boldsymbol{r}
ZColumn	int Jumlah kolom di arah sumbu \boldsymbol{z}
PhiSlice	int Jumlah irisan di arah sumbu ϕ
coef1	float st Array untuk koefisien $V_{x+1,y,z}$
coef2	float st Array untuk koefisien $V_{x-1,y,z}$
coef3	float $*$ Array untuk koefisien z
icoef4	float* Array untuk koefisien invers dari $f(r,\phi,z)$

Definisi pada baris 160 dalam file PoissonSolver3DGPU.cu.

```
172 {
173
         int index_x, index_y, index, index_left, index_right, index_up, index_down, index_front, index_back,
      index_coef;
174
175
         index_x = blockIdx.x * blockDim.x + threadIdx.x;
176
         index_y = blockIdx.y * blockDim.y + threadIdx.y;
177
178
                      = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + index_x;
179
         index_left = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x - 1);
180
         index_right = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + (index_x + 1);
         index_up = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y - 1) * ZColumn + index_x;
index_down = d_grid_StartPos + blockIdx.z * RRow * ZColumn + (index_y + 1) * ZColumn + index_x;
index_front = d_grid_StartPos + ((blockIdx.z * RRow * ZColumn + index_y * RRow * ZColumn + index_y *
181
182
183
      ZColumn + index_x;
184
         index_back = d_grid_StartPos + ((blockIdx.z + 1) % PhiSlice) * RRow * ZColumn + index_y * ZColumn +
      index_x;
185
         index_coef = d_coef_StartPos + index_y;
186
187
         if (index_x != 0 && index_x < (ZColumn - 1) && index_y != 0 && index_y < (RRow - 1))
188
             DeltaResidue[index] = d_ih2 * (coef2[index_coef] * VPotential[index_up] +
189
190
                                coef1[index_coef] * VPotential[index_down] +
191
                                d_tempRatioZ * (VPotential[index_left] + VPotential[index_right]) +
192
                                coef3[index_coef] * (VPotential[index_front] + VPotential[index_back]) -
193
                                icoef4[index_coef] * VPotential[index]) + RhoChargeDensity[index];
194
         }
195 }
```

6.3.2.8 Restrict_Boundary()

top left (0,0)

boundary in top and down for (j = 1, jj = 2; j < ZColumn-1; j++,jj+=2) { VPotential[Offset + sliceStart + (0 * ZColumn) + j] = 0.5 * VPotential[finer_Offset + finer_SliceStart + (0 * finer_ZColumn) + j] + 0.25 * VPotential[finer_Offset + finer_SliceStart + (0 * finer_ZColumn) + j] + 0.25 * VPotential[finer_Offset + finer_SliceStart + (0 * finer_ZColumn) + j] + 1];

 $\begin{tabular}{ll} $$V$Potential[Offset + sliceStart + ((RRow - 1) * ZColumn) + j] = 0.5 * VPotential[finer_Offset + finer_SliceStart + ((finer_RRow - 1) * finer_ZColumn) + jj] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((finer_RRow - 1) * finer_ZColumn) + jj - 1] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((finer_RRow - 1) * finer_ZColumn) + jj + 1]; \\ \end{tabular}$

```
boundary in left and right for (i = 1, ii =2; i < RRow - 1; i++,ii+=2) { VPotential[Offset + sliceStart + (i * ZColumn)]
= 0.5 * VPotential[finer_Offset + finer_SliceStart + (ii * finer_ZColumn)] + 0.25 * VPotential[finer_Offset + finer_←
SliceStart + ((ii-1) * finer ZColumn)] + 0.25 * VPotential[finer Offset + finer SliceStart + ((ii + 1) * finer ZColumn)];
VPotential[Offset + sliceStart + (i * ZColumn) + (ZColumn - 1)] = 0.5 * VPotential[finer_Offset + finer_SliceStart +
(ii * finer_ZColumn) + jj + (finer_ZColumn - 1)] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((ii -1) * finer←
_ZColumn) + (finer_ZColumn - 1)] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((ii +1) * finer_ZColumn) +
(finer_ZColumn - 1)];
top left (0,0)
     VPotential[Offset + sliceStart + (0 * ZColumn) + 0] =
          0.5 * VPotential[finer_Offset + finer_SliceStart] +
          0.25 * VPotential[finer_Offset + finer_SliceStart + (0 * finer_ZColumn) + 1] +
          0.25 * VPotential[finer_Offset + finer_SliceStart + (1 * finer_ZColumn)];
top right VPotential[Offset + sliceStart + (0 * ZColumn) + (ZColumn - 1)] = 0.5 * VPotential[finer_Offset + finer←
_SliceStart + (0 * finer_ZColumn) + (finer_ZColumn -1) ] + 0.25 * VPotential[finer_Offset + finer_SliceStart + (0 *
finer_ZColumn) + (finer_ZColumn - 2)] + 0.25 * VPotential[finer_Offset + finer_SliceStart + (1 * finer_ZColumn) +
(finer ZColumn - 1)];
bottom left VPotential[Offset + sliceStart + ((RRow - 1) * ZColumn) + 0] = 0.5 * VPotential[finer Offset + finer ←
SliceStart + ((finer_RRow - 1) * finer_ZColumn) + 0] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((finer_←
RRow - 1) * finer_ZColumn) + 1] + 0.25 * VPotential[finer_Offset + finer_SliceStart + ((finer_RRow - 2) * finer_Z ←
Column) + 0];
bottom right VPotential[Offset + sliceStart + ((RRow - 1) * ZColumn) + (ZColumn - 1)] = 0.5 * VPotential[finer_Offset
+ finer_SliceStart + ((finer_RRow - 1) * finer_ZColumn) + (finer_ZColumn - 1)] + 0.25 * VPotential[finer_Offset +
finer_SliceStart + ((finer_RRow - 1) * finer_ZColumn) + (finer_ZColumn - 2)] + 0.25 * VPotential[finer_Offset +
finer_SliceStart + ((finer_RRow - 2) * finer_ZColumn) + (finer_ZColumn - 1)];
}
Definisi pada baris 566 dalam file PoissonSolver3DGPU.cu.
573 {
        int i,ii,j,jj;
574
575
        int finer_RRow = 2 * RRow - 1;
        int finer_ZColumn = 2 * ZColumn - 1;
576
577
578
        int finer_Offset = Offset - (finer_RRow * finer_ZColumn * PhiSlice);
        int sliceStart;
580
        int finer_SliceStart;
581
582
        \label{eq:continuous} $$//\text{printf}("(%d,%d,%d) -> (%d,%d,%d) n",RRow,ZColumn,Offset,finer_RRow,finer_ZColumn,finer_Offset); $$
583
        // do for each slice
584
        for ( int m = 0;m < PhiSlice;m++)</pre>
585
             sliceStart = m * (RRow * ZColumn);
586
587
             finer_SliceStart = m * (finer_RRow * finer_ZColumn);
             // copy boundary
588
             for (j = 0, jj = 0; j < ZColumn; j++, jj+=2)
589
590
                 VPotential[Offset + sliceStart + (0 * ZColumn) + j] =
592
                     VPotential[finer_Offset + finer_SliceStart + (0 * finer_ZColumn) + jj];
593
```

 $\begin{tabular}{ll} VP otential [Offset + sliceStart + ((RRow - 1) * ZColumn) + j] = \\ \end{tabular}$

VPotential[Offset + sliceStart + (i * ZColumn) + (ZColumn - 1)] =

VPotential[finer_Offset + finer_SliceStart + (ii * finer_ZColumn)];

for (i = 0, ii =0; i < RRow ; i++,ii+=2) +</pre>

VPotential[Offset + sliceStart + (i * ZColumn)] =

 $\label{lem:potential} $$ VPotential[finer_Offset + finer_SliceStart + ((finer_RRow -1) * finer_ZColumn) + jj]; $$ The substitution of the substi$

VPotential[finer_Offset + finer_SliceStart + (ii * finer_ZColumn) + (finer_ZColumn - 1)];

}

594

595 596 597

599

600

601

602 603

604 605 606

668 }

6.3.2.9 restriction2DFull()

```
__global__ void restriction2DFull (
    float * RhoChargeDensity,
    float * DeltaResidue,
    const int RRow,
    const int ZColumn,
    const int PhiSlice )
```

Restriksi dari finer grid ke coarser grid dengan operator Half Weighting

```
\begin{array}{l} I_h^{2h} = \frac{1}{8}[ccc]010 \\ 141 \end{array}
```

Parameter

RhoChargeDensity	float* Array rapat arus
DeltaResidue	float* Array residu hasil relaksasi
RRow	const int Jumlah baris di arah sumbu \boldsymbol{r}
ZColumn	const int Jumlah kolom di arah sumbu \boldsymbol{z}
PhiSlice	const int Jumlah irisan di arah sumbu ϕ

Definisi pada baris 253 dalam file PoissonSolver3DGPU.cu.

```
260 {
261
       int index_x, index_y, index;
       int finer_RRow, finer_ZColumn, finer_grid_StartPos;
262
263
       int finer_index_x, finer_index_y, finer_index, finer_index_left, finer_index_right, finer_index_up,
264
       int finer_index_up_left, finer_index_up_right, finer_index_down_left, finer_index_down_right;
265
       index_x = blockIdx.x * blockDim.x + threadIdx.x;
266
       index_y = blockIdx.y * blockDim.y + threadIdx.y;
267
              = d_grid_StartPos + blockIdx.z * RRow * ZColumn + index_y * ZColumn + index_x;
268
269
       finer_RRow = 2 * RRow - 1;
270
       finer_ZColumn = 2 * ZColumn - 1;
271
272
273
       finer_grid_StartPos = d_grid_StartPos - (finer_RRow * finer_ZColumn * PhiSlice);
274
275
       finer_index_x = index_x \star 2;
276
       finer_index_y = index_y * 2;
277
278
       finer index
                         = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + finer_index_y *
     finer_ZColumn + finer_index_x;
                         = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + finer_index_y *
279
       finer index left
     finer_ZColumn + (finer_index_x - 1);
280
                         = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + finer_index_y *
       finer_index_right
     finer_ZColumn + (finer_index_x + 1);
281
       finer_index_up
                          = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + (finer_index_y -
     1) * finer_ZColumn + finer_index_x;
                          = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + (finer_index_y +
282
       finer index down
     283
       finer_index_up_right
284
                             = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + (
     finer_index_y - 1) * finer_ZColumn + (finer_index_x + 1);
       finer_index_down_left
285
                            = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + (
     finer_index_y + 1) * finer_ZColumn + (finer_index_x -
       finer_index_down_right = finer_grid_StartPos + blockIdx.z * finer_RRow * finer_ZColumn + (
     finer_index_y + 1) * finer_ZColumn + (finer_index_x + 1);
287
288
       289
           RhoChargeDensity[index] = 0.25 * DeltaResidue[finer_index] +
290
291
                                 0.125 * (DeltaResidue[finer_index_left] + DeltaResidue[finer_index_right] +
```

6.4 Referensi File /home/nfs/aswardiana/Workspace/mp-headnode/lipi/PoissonSolver3 D/kernel/PoissonSolver3DGPU.h

Berkas ini berisi definisi fungsi extern yang dimiliki implementasi CUDA yang didapat dipanggil CPU.

```
#include <ctime>
#include <iomanip>
#include <iostream>
#include <stdio.h>
#include <stdlib.h>
```

Fungsi

- void PoissonMultigrid3DSemiCoarseningGPUError (float *VPotential, float *RhoChargeDensity, const int R← Row, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, bool isExact← Present, float *errorConv, float *errorExact, float *VPotentialExact)
- void PoissonMultigrid3DSemiCoarseningGPUErrorWCycle (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, float *errorConv, float *errorExact, float *VPotentialExact)
- void PoissonMultigrid3DSemiCoarseningGPUErrorFCycle (float *VPotential, float *RhoChargeDensity, const int RRow, const int ZColumn, const int PhiSlice, const int Symmetry, float *fparam, int *iparam, bool is← ExactPresent, float *errorConv, float *errorExact, float *VPotentialExact)

6.4.1 Keterangan Lengkap

Berkas ini berisi definisi fungsi extern yang dimiliki implementasi CUDA yang didapat dipanggil CPU.

Penulis

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Tanggal

November 8, 2018

6.4.2 Dokumentasi Fungsi

6.4.2.1 PoissonMultigrid3DSemiCoarseningGPUError()

Fungsi ini menghitung solusi terhadap Persamaan Poisson

$$\nabla^2(r,\phi,z) = \rho(r,\phi,z)$$

dengan diketahui nilai tepi (Boundary Value) pada V (potensial) dan distribusi buatan ρ

Parameter

in,out	VPotential	float[nrows*ncols*nphi] distribusi potensial. Input: hanya nilai tepi. Output:
		hasil perhitungan penyelesaian persamaan Poisson
in	RhoChangeDensity	float[nrows*ncols*nphi] distributsi muatan listrik.

Mengembalikan

A fixed number that has nothing to do with what the function does

Definisi pada baris 893 dalam file PoissonSolver3DGPU.cu.

```
907 {
           // variables for CPU memory
float *temp_VPotential;
float *VPotentialPrev;
908
909
910
            float *EpsilonError;
912
            // variables for GPU memory
913
            float *d_VPotential;
float *d_RhoChargeDensity;
914
915
            float *d_DeltaResidue;
float *d_VPotentialPrev;
float *d_EpsilonError;
916
917
918
919
920
            float *d_coef1;
           float *d_coef2;
float *d_coef3;
float *d_coef4;
921
922
923
924
            float *d_icoef4;
925
            \ensuremath{//} variables for coefficent calculations
926
           float *coef1;
float *coef2;
927
928
929
           float *coef3;
            float *coef4;
```

```
float *icoef4;
932
         float tempRatioZ;
933
         float tempRatioPhi;
934
        float radius;
935
936
        int gridFrom;
937
        int gridTo;
938
        int loops;
939
940
        // variables passed from ALIROOT
941
        float gridSizeR = fparam[0];
float gridSizePhi = fparam[1];
942
943
        float gridSizerii = [param[1];
float gridSizeZ = fparam[2];
float ratioPhi = fparam[3];
float ratioZ = fparam[4];
float convErr = fparam[5];
float IFCRadius = fparam[6];
944
945
946
947
948
        949
950
951
952
953
        // variables for calculating GPU memory allocation
954
955
         int grid_RRow;
         int grid_ZColumn;
957
         int grid_PhiSlice = PhiSlice;
958
         int grid_Size = 0;
959
         int grid_StartPos;
960
         int coef_Size = 0;
961
         int coef_StartPos;
        int iOne, jOne;
float h, h2, ih2;
962
963
964
        // variables for calculating multigrid maximum depth int depth_RRow = 0;
965
966
         int depth_ZColumn = 0;
967
         int temp_RRow = RRow;
968
969
         int temp_ZColumn = ZColumn;
970
971
         \ensuremath{//} calculate depth for multigrid
         while (temp_RRow >>= 1) depth_RRow++;
while (temp_ZColumn >>= 1) depth_ZColumn++;
972
973
974
975
         loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
976
         loops = (loops > maxLoop) ? maxLoop : loops;
977
978
         gridFrom = 1;
979
         gridTo = loops;
980
981
         // calculate GPU memory allocation for multigrid
982
         for (int step = gridFrom; step <= gridTo; step++)</pre>
983
             984
985
986
             grid_Size += grid_RRow * grid_ZColumn * grid_PhiSlice;
988
             coef_Size += grid_RRow;
989
990
         \ensuremath{//} allocate memory for temporary output
991
                                 = (float *) malloc(grid_Size * sizeof(float));
992
         temp VPotential
993
         VPotentialPrev = (float *) malloc(RRow * ZColumn * PhiSlice * sizeof(float));
994
         EpsilonError = (float *) malloc(1 * sizeof(float));
995
996
997
         \ensuremath{//} allocate memory for relaxation coefficient
         coef1 = (float *) malloc(coef_Size * sizeof(float));
coef2 = (float *) malloc(coef_Size * sizeof(float));
998
999
         coef3 = (float *) malloc(coef_Size * sizeof(float));
coef4 = (float *) malloc(coef_Size * sizeof(float));
1000
1001
1002
          icoef4 = (float *) malloc(coef_Size * sizeof(float));
1003
1004
         // pre-compute relaxation coefficient
1005
         coef_StartPos = 0;
1006
         iOne = 1 << (gridFrom - 1);
1007
          jOne = 1 << (gridFrom - 1);
1008
1009
          for (int step = gridFrom; step <= gridTo; step++)</pre>
1010
               grid_RRow = ((RRow - 1) / iOne) + 1;
1011
1012
               h = gridSizeR * iOne;
1013
1014
              h2 = h * h;
1015
              ih2 = 1.0 / h2;
1016
1017
               tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
```

```
tempRatioPhi = ratioPhi * iOne * iOne;
1019
1020
              for (int i = 1; i < grid_RRow - 1; i++)</pre>
1021
                   radius = IFCRadius + i * h;
1022
                  coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
1023
1024
1025
                  coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1026
1027
1028
              coef StartPos += grid RRow;
1029
1030
              iOne = 2 * iOne;
jOne = 2 * jOne;
1031
1032
1033
          // device memory allocation
1034
         cudaMalloc( &d_VPotential, grid_Size * sizeof(float) );
cudaMalloc( &d_VPotentialPrev, RRow * ZColumn * PhiSlice * sizeof(float) );
1035
1036
          cudaMalloc( &d_EpsilonError, 1 * sizeof(float) );
1037
1038
          cudaMalloc(&d_DeltaResidue, grid_Size * sizeof(float));
1039
          cudaMalloc( &d_RhoChargeDensity, grid_Size * sizeof(float) );
1040
          cudaMalloc( &d_coef1, coef_Size * sizeof(float) );
         cudaMalloc(&d_coef2, coef_Size * sizeof(float));
cudaMalloc(&d_coef3, coef_Size * sizeof(float));
1041
1042
          cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
1043
1044
          cudaMalloc( &d_icoef4, coef_Size * sizeof(float) );
1045
1046
          // set memory to zero
          cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
1047
         cudaMemset( d_PoltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
cudaMemset( d_VPotentialPrev, 0, RRow * ZColumn * PhiSlice * sizeof(float) );
1048
1049
1050
1051
          cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1052
1053
1054
          // copy data from host to device
1055
          cudaMemcpy( d_VPotential, VPotential, RRow * ZColumn * PhiSlice * sizeof(float), cudaMemcpyHostToDevice
       ); //check
1056
          cudaMemcpyHostToDevice ); //check
1057
          \verb|cudaMemcpy(d_coef1, coef_Size * sizeof(float), cudaMemcpyHostToDevice );|\\
          cudaMemcpy( d_coef2, coef2, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1058
1059
          cudaMemcpy( d_coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
          cudaMemcpy( d_coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1060
1061
          cudaMemopy( d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemopyHostToDevice );
1062
          cudaMemcpy( d_VPotentialPrev, VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyHostToDevice );
1063
1064
          // max exact
1065
          // float maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
1066
1067
          float maxAbsExact = 1.0;
1068
1069
          if (isExactPresent == true)
1070
              maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
          dim3 error_BlockPerGrid((RRow < 16) ? 1 : (RRow / 16), (ZColumn < 16) ? 1 : (ZColumn / 16), PhiSlice);
1071
1072
          dim3 error_ThreadPerBlock(16, 16);
1073
1074
1075
          for (int cycle = 0; cycle < nCycle; cycle++)</pre>
1076
1077
              cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyDeviceToHost );
1078
                 (isExactPresent == true) errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact,
      RRow * PhiSlice, ZColumn, maxAbsExact);
1079
1080
              VCycleSemiCoarseningGPU(d_VPotential, d_RhoChargeDensity, d_DeltaResidue, d_coef1, d_coef2, d_coef3
1081
      , d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, gridFrom, gridTo, nPre, nPost);
1082
1083
1084
              errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev, d_VPotential,
      d_EpsilonError, RRow, ZColumn, PhiSlice);
1085
1086
              cudaMemcpy( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost );
1087
1088
1089
              errorConv[cycle] = *EpsilonError / (RRow * ZColumn * PhiSlice);
1090
1091
              if (errorConv[cycle] < convErr)</pre>
1092
1093
                   //errorConv
1094
                   nCycle = cycle;
1095
                  break;
1096
1097
```

```
cudaMemcpy( d_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
     cudaMemcpyDeviceToDevice );
1099
            cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1100
1101
1102
        iparam[3] = nCvcle;
1103
1104 // for (int cycle = 0; cycle < nCycle; cycle++)
1105 // {
1106 //
            cudaMemcpy( temp_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyDeviceToHost );
1107
1108
           VCycleSemiCoarseningGPU(d_VPotential, d_RhoChargeDensity, d_DeltaResidue, d_coef1, d_coef2,
      d_coef3, d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, gridFrom, gridTo, nPre, nPost);
1110
            cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1111 //
      cudaMemcpyDeviceToHost );
1112 //
           errorConv[cycle] = GetErrorNorm2(temp_VPotential, temp_VPotentialPrev, RRow * PhiSlice, ZColumn,
            //errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact, RRow * PhiSlice, ZColumn,
      1.0);
1114 // }
1115
1116
1117
        // copy result from device to host
        1118
     cudaMemcpyDeviceToHost );
1119
1120
        memcpy(VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
1121
1122
        // free device memory
1123
       cudaFree( d_VPotential );
1124
        cudaFree( d_DeltaResidue );
1125
       cudaFree( d_RhoChargeDensity );
1126
       cudaFree( d_VPotentialPrev );
       cudaFree( d_EpsilonError );
1127
1128
       cudaFree( d_coef1 );
1129
       cudaFree( d_coef2 );
1130
       cudaFree( d_coef3 );
1131
        cudaFree( d_coef4 );
1132
       cudaFree( d_icoef4 );
1133
1134
        // free host memory
       free( coef1 );
1135
1136
        free( coef2 );
1137
       free ( coef3 );
1138
        free ( coef4 );
1139
        free ( icoef4 );
1140
        free( temp_VPotential );
1141
        free ( VPotentialPrev );
1142 }
```

6.4.2.2 PoissonMultigrid3DSemiCoarseningGPUErrorFCycle()

cudaMemcpy(temp_VPotential, d_RhoChargeDensity + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToHost);

Definisi pada baris 1837 dalam file PoissonSolver3DGPU.cu.

```
1851 {
1852
           // variables for CPU memory
1853
           float *temp_VPotential;
           float *VPotentialPrev;
1854
1855
          float *EpsilonError;
1856
1857
           // variables for GPU memory
1858
           float *d_VPotential;
1859
           float *d_RhoChargeDensity;
1860
           float *d_DeltaResidue;
          float *d_coef1;
float *d_coef2;
1861
1862
1863
           float *d_coef3;
1864
           float *d_coef4;
1865
           float *d_icoef4;
1866
           float *d_VPotentialPrev;
1867
          float *d_EpsilonError;
1868
1869
1870
           // variables for coefficent calculations
1871
           float *coef1;
1872
           float *coef2;
1873
           float *coef3;
1874
           float *coef4;
1875
           float *icoef4;
1876
           float tempRatioZ;
1877
           float tempRatioPhi;
1878
          float radius;
1879
          int gridFrom;
1880
1881
          int gridTo:
1882
          int loops;
1883
1884
           \ensuremath{//} variables passed from ALIROOT
          float gridSizeR = fparam[0];
//float gridSizePhi = fparam[1];
//float gridSizeZ = fparam
float ratioPhi = fparam[3];
1885
1886
1887
                                        = fparam[2];
1888
1889
           float ratioZ
                                   = fparam[4];
                                = fparam[5];
= fparam[6];
1890
           float convErr
1891
           float IFCRadius
          int nPre = iparam[0];
int nPost = iparam[1];
1892
1893
          int maxLoop = iparam[2];
int nCycle = iparam[3];
1894
1895
1896
1897
           // variables for calculating GPU memory allocation
1898
          int grid_RRow;
           int grid_ZColumn;
1899
          int grid_PhiSlice = PhiSlice;
1900
           int grid_Size = 0;
1901
1902
           int grid_StartPos;
1903
           int coef_Size = 0;
1904
          int coef_StartPos;
1905
          int iOne, jOne; float h, h2, ih2;
1906
1907
1908
           // variables for calculating multigrid maximum depth
1909
           int depth_RRow = 0;
1910
           int depth_ZColumn = 0;
           int temp_RRow = RRow;
1911
          int temp_ZColumn = ZColumn;
1912
1913
1914
           // calculate depth for multigrid
1915
           while (temp_RRow >>= 1) depth_RRow++;
1916
          while (temp_ZColumn >>= 1) depth_ZColumn++;
1917
          loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
loops = (loops > maxLoop) ? maxLoop : loops;
1918
1919
1920
1921
           gridFrom = 1;
1922
           gridTo = loops;
1923
           // calculate GPU memory allocation for multigrid
1924
1925
           for (int step = gridFrom; step <= gridTo; step++)</pre>
1926
               grid_RRow = ((RRow - 1) / (1 << (step - 1))) + 1;
grid_ZColumn = ((ZColumn - 1) / (1 << (step - 1))) + 1;
1927
1928
1929
1930
                grid Size += grid RRow * grid ZColumn * grid PhiSlice;
                coef_Size += grid_RRow;
1931
1932
1933
1934
           // allocate memory for temporary output
          temp_VPotential = (float *) malloc(grid_Size * sizeof(float));
VPotentialPrev = (float *) malloc(grid_Size * sizeof(float));
EpsilonError = (float *) malloc(1 * sizeof(float));
1935
1936
1937
```

```
1939
1940
1941
            for (int i=0;i<grid_Size;i++) temp_VPotential[i] = 0.0;</pre>
1942
1943
1944
            // allocate memory for relaxation coefficient
1945
            coef1 = (float *) malloc(coef_Size * sizeof(float));
1946
            coef2 = (float *) malloc(coef_Size * sizeof(float));
           coef3 = (float *) malloc(coef_Size * sizeof(float));
coef4 = (float *) malloc(coef_Size * sizeof(float));
icoef4 = (float *) malloc(coef_Size * sizeof(float));
1947
1948
1949
1950
1951
            // pre-compute relaxation coefficient
1952
            // restrict boundary
1953
           coef_StartPos = 0;
           grid_StartPos = 0;
1954
1955
1956
           iOne = 1 << (gridFrom - 1);
           jOne = 1 << (gridFrom - 1);
1957
1958
1959
            for (int step = gridFrom; step <= gridTo; step++)</pre>
1960
                 grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / iOne) + 1;
1961
1962
1963
1964
                 h = gridSizeR * iOne;
                h2 = h * h;

ih2 = 1.0 / h2;
1965
1966
1967
1968
                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1969
                 tempRatioPhi = ratioPhi * iOne * iOne;
1970
1971
                 for (int i = 1; i < grid_RRow - 1; i++)</pre>
1972
                       radius = IFCRadius + i * h;
1973
                      coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
1974
1975
1976
                      coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1977
1978
1979
                }
1980
1981
                 // call restrict boundary
                 if (step == gridFrom) {
1982
1983
                       // Copy original VPotential to tempPotential
1984
                       memcpy(temp_VPotential,
                                                         VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
1985
1986
1987
                 // else
1988
                 //{
1989
                      Restrict_Boundary(temp_VPotential, grid_RRow, grid_ZColumn, PhiSlice, grid_StartPos);
1990
1991
1992
1993
                 coef_StartPos += grid_RRow;
1994
                 grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1995
1996
                 iOne = 2 * iOne;
jOne = 2 * jOne;
1997
1998
1999
           }
2000
2001
           // device memory allocation
2002
            cudaMalloc( &d_VPotential, grid_Size * sizeof(float) );
2003
            cudaMalloc( &d_DeltaResidue, grid_Size * sizeof(float) );
2004
            \verb|cudaMalloc(&d_RhoChargeDensity, grid_Size * size of(float));|\\
           cudaMalloc(&d_coef1, coef_Size * sizeof(float));
cudaMalloc(&d_coef2, coef_Size * sizeof(float));
2005
2006
            cudaMalloc( &d_coef3, coef_Size * sizeof(float) );
2007
2008
            cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
            cudaMalloc(&d_icoef4, coef_Size * sizeof(float));
2009
           cudaMalloc( &d_VPotentialPrev, grid_Size * sizeof(float) );
cudaMalloc( &d_EpsilonError, 1 * sizeof(float) );
2010
2011
2012
2013
2014
            // set memory to zero
            cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
2015
2016
2017
           cudaMemset( d_VPotentialPrev, 0, grid_Size * sizeof(float) );
cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
2018
2019
2020
2021
            // set memory to zero
           cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
2022
2023
2024
```

```
2025
2026
          // copy data from host to devicei
2027
         // case of FCycle you need to copy all boundary for all
         cudaMemcpy( d_VPotential, temp_VPotential, grid_Size * sizeof(float), cudaMemcpyHostToDevice ); //check
cudaMemcpy( d_VPotential, VPotential, grid_Size * isizeof(float), cudaMemcpyHostToDevice ); //check
2028
2029 //
2030
2031
          cudaMemcpy( d_RhoChargeDensity, RhoChargeDensity, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyHostToDevice ); //check
2032 // cudaMemcpy( d_RhoChargeDensity, temp_VPotentialPrev, grid_Size * sizeof(float), cudaMemcpyHostToDevice
       ); //check
2033
         cudaMemcpy( d_coef1, coef1, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
2034
         \verb|cudaMemcpy(d_coef2, coef2| size * size of(float), cudaMemcpyHostToDevice );\\
         cudaMemcpy( d_coef3, coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
2035
2036
         cudaMemcpy( d_coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
2037
         cudaMemcpy( d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
2038 //
         cudaMemcpy( d_VPotentialPrev, temp_VPotential, grid_Size * sizeof(float), cudaMemcpyHostToDevice );
2039
2040 // cudaMemcpy( d VPotentialPrev, VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
       cudaMemcpyHostToDevice );
2041
2042
         // max exact
2043
2044
         float maxAbsExact = 1.0;
2045
2046
         if (isExactPresent == true)
2047
             maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
2048
2049
2050
2051
         // init iOne,grid_RRow, grid_ZColumn, grid_StartPos, coef_StartPos
2052
         iOne = 1 << (gridFrom - 1);
2053
         jOne = 1 << (gridFrom - 1);</pre>
2054
         grid_RRow
2055
                          = ((RRow - 1) / iOne) + 1;
2056
         grid_ZColumn
                          = ((ZColumn - 1) / jOne) + 1;
2057
2058
         grid StartPos = 0;
         coef_StartPos = 0;
2059
2060
2061
2063
         for (int step = gridFrom + 1; step <= gridTo; step++)</pre>
2064
2065
2066
              iOne = 1 << (step - 1);
              jOne = 1 << (step - 1);
2067
2068
2069
              grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
2070
              coef_StartPos += grid_RRow;
2071
                              = ((RRow - 1) / iOne) + 1;
2072
              grid RRow
              grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
2073
2074
2075
              // pre-compute constant memory
              h = gridSizeR * iOne;
h2 = h * h;
2076
2077
2078
              ih2 = 1.0 / h2;
2079
2080
              tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
2081
              tempRatioPhi = ratioPhi * iOne * iOne;
2082
2083
              // copy constant to device memory
              cudaMemcpyToSymbol(d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice); cudaMemcpyToSymbol(d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice);
2084
2085
              cudaMemopyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemopyHostToDevice);
2086
2087
              \verb| cudaMemcpyToSymbol( d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
2088
              \verb|cudaMemcpyToSymbol(d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice)|;\\
2089
2090
              // set kernel grid size and block size
              dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
2091
      grid_ZColumn / 16), PhiSlice);
2092
              dim3 grid_ThreadPerBlock(16, 16);
2093
2094
              // restriction
              restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
2095
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice );
2096
2097
               // restrict boundary (already done in cpu)
2099 //
              PrintMatrix(temp_VPotential,grid_RRow * PhiSlice,grid_ZColumn);
              restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, d_VPotential,
2100
      grid_RRow, grid_ZColumn, grid_PhiSlice );
2101
2102
2103
2104
2105
         dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (grid_ZColumn
        / 16), PhiSlice);
2106
         dim3 grid_ThreadPerBlock(16, 16);
```

```
2108
2109
                      // relax on the coarsest
                     // red-black gauss seidel relaxation (nPre times)
2110
2111 // printf("rho\n");
2112 //
                     cudaMemcpy(temp_VPotential, d_RhoChargeDensity + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice *
                sizeof(float), cudaMemcpyDeviceToHost );
2113 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
2114
2115 // printf("v\n");
2116 // cudaMemcpy( temp_VPotential, d_VPotential + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice *
                sizeof(float), cudaMemcpyDeviceToHost );
2117 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
                    for (int i = 0; i < nPre; i++)
2118
2119
                               relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
2120
             d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
2121
                              cudaDeviceSynchronize();
2122
                               relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
             d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
2123
                          cudaDeviceSynchronize();
2124
2125
2126 // printf("v after relax\n");
2127 //
                     cudaMemcpy( temp_VPotential, d_VPotential + grid_StartPos , grid_RRow * grid_ZColumn * PhiSlice *
                sizeof(float), cudaMemcpyDeviceToHost );
2128 // PrintMatrix(temp_VPotential,grid_RRow,grid_ZColumn);
2129
2130
                      // V-Cycle => from coarser to finer grid
2131
                     for (int step = gridTo -1; step >= gridFrom; step--)
2132
                     {
2133
                                iOne = iOne / 2;
2134
                               jOne = jOne / 2;
2135
                             grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
2136
2137
2138
2139
                          grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
2140
                              coef_StartPos -= grid_RRow;
2141
                             h = gridSizeR * iOne;
h2 = h * h;
ih2 = 1.0 / h2;
2142
2143
2144
2145
                               tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
2146
2147
                               tempRatioPhi = ratioPhi * iOne * iOne;
2148
2149
                               // copy constant to device memory
                               cudaMemcpyToSymbol( d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
2150
                               cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
2151
                               cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
cudaMemcpyToSymbol( d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
2152
2153
2154
                               \verb|cudaMemcpyToSymbol(d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);| \\
2155
2156
2157
                               // set kernel grid size and block size
                               \label{eq:dim3}  \texttt{grid\_Bloc} \\ \texttt{PerGrid((grid\_RRow < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_RRow / 16), (grid\_RRow / 16) ? 1 : (grid\_RRow / 16), (gri
2159
              grid_ZColumn / 16), PhiSlice);
2160
                              dim3 grid_ThreadPerBlock(16, 16);
2161
2162
2163
                               prolongation2DHalfNoAdd<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
             grid_ZColumn, grid_PhiSlice );
2164
2165
2166
2167
2168
                              // just
2169
2170
2171
                               \verb|cudaMemcpy| ( d_VPotentialPrev + grid_StartPos, d_VPotential + grid_StartPos, grid_RRow * to the following that the description of the descrip
              grid_ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToDevice );
2172
2173
                               float maxAbsExact = 1.0;
2174
2175
                               if (isExactPresent == true)
                               maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
dim3 error_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (</pre>
2176
2177
             grid_ZColumn / 16), PhiSlice);
   dim3 error_ThreadPerBlock(16, 16);
2178
2179
2180
2181
2182
                               for (int cycle = 0; cycle < nCycle; cycle++)</pre>
2183
2184
```

```
2185
                 if (step == gridFrom) {
2186
2187
                     cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
      cudaMemcpyDeviceToHost );
2188
                     if (isExactPresent == true )errorExact[cycle] = GetErrorNorm2(temp_VPotential,
      VPotentialExact, RRow * PhiSlice, ZColumn, maxAbsExact);
2189
2190
2191
2192
2193
                 //cudaDeviceSynchronize();
                 VCycleSemiCoarseningGPU(d_VPotential, d_RhoCharqeDensity, d_DeltaResidue, d_coef1, d_coef2,
2194
      d_coef3, d_coef4, d_icoef4, gridSizeR, ratioZ, ratioPhi, RRow, ZColumn, PhiSlice, step, gridTo, nPre, nPost);
2195
2196
2197
                     //if (step == gridFrom) {
2198
                      //cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
2199
       cudaMemcpyDeviceToHost );
2200
                      //errorConv[cycle] = GetErrorNorm2(temp_VPotential, VPotentialPrev, RRow *
2201
       PhiSlice, ZColumn, 1.0);
2202
      errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev + grid_StartPos, d_VPotential + grid_StartPos, d_EpsilonError, grid_RRow, grid_ZColumn, PhiSlice);
2203
2204
2205
                     cudaMemcpy( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost );
2206
                     errorConv[cycle] = *EpsilonError / (grid_RRow * grid_ZColumn * PhiSlice);
2207
2208
2209
                      if (errorConv[cvcle] < convErr)
2210
2211
                          nCycle = cycle;
2212
2213
2214
                     cudaMemcpy( d_VPotentialPrev + grid_StartPos, d_VPotential + grid_StartPos, grid_RRow *
2215
      grid_ZColumn * PhiSlice * sizeof(float), cudaMemcpyDeviceToDevice );
2216
                     cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
2217
2218
             }
2219
2220
2221
         }
2222
2223
         iparam[3] = nCycle;
2224
2225
         // copy result from device to host
         2226
      cudaMemcpvDeviceToHost );
2227
2228
         memcpy(VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
2229
2230
         // free device memory
         cudaFree ( d_VPotential );
2231
2232
         cudaFree ( d DeltaResidue );
2233
         cudaFree( d_RhoChargeDensity );
2234
         cudaFree( d_coef1 );
2235
         cudaFree( d_coef2 );
2236
         cudaFree( d_coef3 );
2237
         cudaFree ( d_coef4 );
2238
         cudaFree ( d icoef4 );
2239
2240
         // free host memory
2241
         free( coef1 );
2242
         free( coef2 );
2243
         free ( coef3 );
2244
         free ( coef4 );
2245
         free ( icoef4 );
2246
         free( temp_VPotential );
2247
         free( VPotentialPrev );
2248 }
```

6.4.2.3 PoissonMultigrid3DSemiCoarseningGPUErrorWCycle()

```
const int PhiSlice,
const int Symmetry,
float * fparam,
int * iparam,
float * errorConv,
float * errorExact,
float * VPotentialExact )
```

innner w cycle up one down one

end up one down on

up two down two

up one down one

end up one down one

Definisi pada baris 1147 dalam file PoissonSolver3DGPU.cu.

```
1160 {
1161
              // variables for CPU memory
             float *temp_VPotential;
float *VPotentialPrev;
1162
1163
             float *EpsilonError;
1164
1165
1166
             // variables for GPU memory
           float *d_VPotential;
float *d_RhoChargeDensity;
1167
1168
            float *d_DeltaResidue;
float *d_coef1;
float *d_coef2;
1169
1170
1171
1172
            float *d_coef3;
            float *d_coef4;
float *d_icoef4;
1173
1174
1175
             float *d_VPotentialPrev;
1176
             float *d_EpsilonError;
1177
1178
           // variables for coefficent calculations
1179
1180
             float *coef1;
            float *coef2;
float *coef3;
1181
1182
            float *coef4;
float *icoef4;
float tempRatioZ;
1183
1184
1185
1186
             float tempRatioPhi;
            float radius;
1187
1188
           int gridFrom;
int gridTo;
1189
1190
1191
           int loops;
1192
1193
             // variables passed from ALIROOT
           // variables passed from ALIROOT
float gridSizeR = fparam[0];
//float gridSizePi = fparam[1];
//float gridSizeZ = fparam[2];
float ratioPhi = fparam[3];
float ratioZ = fparam[4];
float convErr = fparam[5];
float IFCRadius = fparam[6];
int nPre = iparam[0];
int nPost = iparam[1];
int maxLoop = iparam[2];
int nCycle = iparam[3];
1194
1195
1196
1197
1198
1199
1200
1201
1202
1203
1204
1205
            // variables for calculating GPU memory allocation
1206
1207
           int grid_RRow;
int grid_ZColumn;
1208
             int grid_PhiSlice = PhiSlice;
1209
1210
            int grid_Size = 0;
           int grid_StartPos;
int coef_Size = 0;
int coef_Size = 0;
int coef_StartPos;
int iOne, jOne;
float h, h2, ih2;
1211
1212
1213
1214
1215
```

```
// variables for calculating multigrid maximum depth
            int depth_RRow = 0;
1218
1219
            int depth_ZColumn = 0;
           int temp_RRow = RRow;
1220
1221
           int temp_ZColumn = ZColumn;
1222
1223
            // calculate depth for multigrid
1224
           while (temp_RRow >>= 1) depth_RRow++;
1225
           while (temp_ZColumn >>= 1) depth_ZColumn++;
1226
1227
           loops = (depth_RRow > depth_ZColumn) ? depth_ZColumn : depth_RRow;
1228
           loops = (loops > maxLoop) ? maxLoop : loops;
1229
1230
           gridFrom = 1;
1231
           gridTo = loops;
1232
            // calculate GPU memory allocation for multigrid
1233
1234
           for (int step = gridFrom; step <= gridTo; step++)</pre>
1235
                 grid_RRow = ((RRow - 1) / (1 << (step - 1))) + 1;
grid_ZColumn = ((ZColumn - 1) / (1 << (step - 1))) + 1;
1236
1237
1238
                 grid_Size += grid_RRow * grid_ZColumn * grid_PhiSlice;
coef_Size += grid_RRow;
1239
1240
1241
1242
1243
            // allocate memory for temporary output
           temp_VPotential = (float *) malloc(grid_Size * sizeof(float));
VPotentialPrev = (float *) malloc(RRow * ZColumn * PhiSlice * sizeof(float));
1244
1245
           EpsilonError = (float *) malloc(1 * sizeof(float));
1246
1247
1248
1249
            // allocate memory for relaxation coefficient
1250
           coef1 = (float *) malloc(coef_Size * sizeof(float));
           coef2 = (float *) malloc(coef_Size * sizeof(float));
1251
           coef3 = (float *) malloc(coef_Size * sizeof(float));
1252
           coef4 = (float *) malloc(coef_Size * sizeof(float));
1253
           icoef4 = (float *) malloc(coef_Size * sizeof(float));
1254
1255
1256
            // pre-compute relaxation coefficient
1257
           coef_StartPos = 0;
           iOne = 1 << (gridFrom - 1);
jOne = 1 << (gridFrom - 1);
1258
1259
1260
1261
            for (int step = gridFrom; step <= gridTo; step++)</pre>
1262
1263
                 grid_RRow = ((RRow - 1) / iOne) + 1;
1264
1265
                 h = gridSizeR * iOne;
1266
                 h2 = h * h;
                 ih2 = 1.0 / h2;
1267
1268
1269
                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1270
                 tempRatioPhi = ratioPhi * iOne * iOne;
1271
                 for (int i = 1; i < grid_RRow - 1; i++)</pre>
1272
1273
1274
                      radius = IFCRadius + i * h;
                      coef1[coef_StartPos + i] = 1.0 + h / (2 * radius);
coef2[coef_StartPos + i] = 1.0 - h / (2 * radius);
1275
1276
                      coef2[coef_StartPos + i] = 1.0 - ii / (2 * ladius);
coef3[coef_StartPos + i] = tempRatioPhi / (radius * radius);
coef4[coef_StartPos + i] = 0.5 / (1.0 + tempRatioZ + coef3[coef_StartPos + i]);
icoef4[coef_StartPos + i] = 1.0 / coef4[coef_StartPos + i];
1277
1278
1279
1280
1281
                 coef_StartPos += grid_RRow;
                 iOne = 2 * iOne;
jOne = 2 * jOne;
1282
1283
1284
           }
1285
1286
           // device memory allocation
1287
           cudaMalloc( &d_VPotential, grid_Size * sizeof(float) );
1288
           cudaMalloc( &d_DeltaResidue, grid_Size \star sizeof(float) );
           cudaMalloc( &d_VPotentialPrev, RRow * ZColumn * PhiSlice * sizeof(float) );
cudaMalloc( &d_EpsilonError, 1 * sizeof(float) );
1289
1290
1291
1292
           cudaMalloc( &d_RhoChargeDensity, grid_Size * sizeof(float) );
           cudaMalloc(&d_coef1, coef_Size * sizeof(float));
cudaMalloc(&d_coef2, coef_Size * sizeof(float));
1293
1294
           cudaMalloc( &d_coef3, coef_Size * sizeof(float) );
cudaMalloc( &d_coef4, coef_Size * sizeof(float) );
cudaMalloc( &d_icoef4, coef_Size * sizeof(float) );
1295
1296
1297
1298
1299
1300
           cudaMemset( d_VPotential, 0, grid_Size * sizeof(float) );
           cudaMemset( d_DeltaResidue, 0, grid_Size * sizeof(float) );
cudaMemset( d_RhoChargeDensity, 0, grid_Size * sizeof(float) );
cudaMemset( d_VPotentialPrev, 0, RRow * ZColumn * PhiSlice * sizeof(float) );
1301
1302
1303
```

```
cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1305
1306
1307
              // copy data from host to device
              1308
           ); //check
1309
              cudaMemcpyHostToDevice ); //check
1310
              cudaMemopy( d_coef1, coef1, coef_Size * sizeof(float), cudaMemopyHostToDevice );
1311
              \verb|cudaMemcpy(d_coef2, coef_Size * sizeof(float), cudaMemcpyHostToDevice );\\
              cudaMemcpy(d_coef3, coef3, coef_Size * sizeof(float), cudaMemcpyHostToDevice);
1312
              cudaMemcpy( d_coef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
cudaMemcpy( d_icoef4, icoef4, coef_Size * sizeof(float), cudaMemcpyHostToDevice );
1313
1314
              cudaMemcpy( d_VPotentialPrev, VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
         cudaMemcpyHostToDevice );
1316
                                      float maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
1317
              float maxAbsExact = GetAbsMax(VPotentialExact, RRow * PhiSlice * ZColumn);
dim3 error_BlockPerGrid((RRow < 16) ? 1 : (RRow / 16), (ZColumn < 16) ? 1 : (ZColumn / 16), PhiSlice);
1318
1319
1320
              dim3 error_ThreadPerBlock(16, 16);
1321
1322
              for (int cycle = 0; cycle < nCycle; cycle++)</pre>
1323
1324
1325
              /*V-Cycle starts*/
1326
1327
                     // cudaMemcpy( temp_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1328
           cudaMemcpyDeviceToHost );
1329
                    cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1330
         cudaMemcpyDeviceToHost );
1331
                    errorExact[cycle] = GetErrorNorm2(temp_VPotential, VPotentialExact, RRow * PhiSlice, ZColumn,
         maxAbsExact);
1332
1333
                    // V-Cycle => Finest Grid
iOne = 1 << (gridFrom - 1);</pre>
1334
1335
1336
                    jOne = 1 << (gridFrom - 1);</pre>
1337
                                             = ((RRow - 1) / iOne) + 1;
1338
                    grid_RRow
                    grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1339
1340
1341
                    grid_StartPos = 0;
1342
                    coef_StartPos = 0;
1343
1344
                    // pre-compute constant memory
                    h = gridSizeR * iOne;
h2 = h * h;
ih2 = 1.0 / h2;
1345
1346
1347
1348
1349
                     tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1350
                    tempRatioPhi = ratioPhi * iOne * iOne;
1351
1352
                    // copy constant to device memory
1353
                    cudaMemcpyToSymbol( d grid StartPos, &grid StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice );
                    cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice);
1354
                     cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1355
1356
                     cudaMemcpyToSymbol( d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1357
                     \verb| cudaMemcpyToSymbol( d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
1358
1359
                     // set kernel grid size and block size
1360
                    dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
         grid_ZColumn / 16), PhiSlice);
1361
                    dim3 grid_ThreadPerBlock(16, 16);
1362
1363
                    // red-black gauss seidel relaxation (nPre times) for (int i = 0; i < nPre; i++)
1364
1365
1366
                           relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1367
                           //cudaDeviceSynchronize();
         1368
1369
1370
1371
1372
                    // residue calculation
                    \verb|residueCalculation| << \verb|grid_BlockPerGrid|, grid_ThreadPerBlock| >>> ( \verb|d_VPotential|, d_RhoChargeDensity|, and the state of the 
1373
           d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1374
                    //cudaDeviceSynchronize();
1375
1376
                     // V-Cycle => from finer to coarsest grid
1377
                     for (int step = gridFrom + 1; step <= gridTo; step++)</pre>
1378
1379
                           iOne = 1 << (step - 1);
                           jOne = 1 << (step - 1);
1380
```

```
grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1382
1383
                              coef_StartPos += grid_RRow;
1384
                              grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1385
1386
1387
1388
                               // pre-compute constant memory
                              h = gridSizeR * iOne;
h2 = h * h;
1389
1390
                              ih2 = 1.0 / h2;
1391
1392
1393
                              tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1394
                              tempRatioPhi = ratioPhi * iOne * iOne;
1395
1396
                               // copy constant to device memory
                              \verb|cudaMemcpyToSymbol(d_grid_StartPos, \&grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice| \\
1397
            );
1398
                              cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
            );
                              1399
1400
1401
                              \verb| cudaMemcpyToSymbol( d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
1402
1403
                                   set kernel grid size and block size
                              dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1404
          grid_ZColumn / 16), PhiSlice);
1/105
                              dim3 grid_ThreadPerBlock(16, 16);
1406
1407
                              // restriction
                              restriction2DFull<<< grid BlockPerGrid, grid ThreadPerBlock >>> ( d RhoChargeDensity,
1408
          d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1409
                              //cudaDeviceSynchronize();
1410
                              // zeroing V
1411
                              {\tt zeroing VPotential} <<< {\tt grid\_BlockPerGrid}, {\tt grid\_ThreadPerBlock} >>>  ( {\tt d\_VPotential}, {\tt grid\_RRow}, {\tt grid\_Rr
1412
          grid_ZColumn, grid_PhiSlice );
1413
                              //cudaDeviceSynchronize();
1414
1415
                               // red-black gauss seidel relaxation (nPre times)
1416
                              for (int i = 0; i < nPre; i++)</pre>
1417
                                      relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1418
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
                                     //cudaDeviceSynchronize();
1419
1420
                                      relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
          d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1421
                                     //cudaDeviceSynchronize();
1422
1423
1424
                              // residue calculation
1425
                               if (step < gridTo)</pre>
1426
1427
                                     residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
          d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1428
                                     //cudaDeviceSynchronize();
1429
1430
                              }
1431
                       }
1434
                       // up one
1435
1436
1437
1438
1439
                              int step = (gridTo - 1);
                              iOne = iOne / 2;
jOne = jOne / 2;
1440
1441
1442
1443
                                                          = ((RRow - 1) / iOne) + 1;
                              arid RRow
                                                         = ((ZColumn - 1) / jOne) + 1;
1444
                              grid_ZColumn
1445
1446
                              grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
                              coef_StartPos -= grid_RRow;
1447
1448
1449
                                    = gridSizeR * iOne;
                              h2 = h * h;
1450
1451
                              ih2 = 1.0 / h2;
1452
                              tempRatioPhi = ratioPhi * iOne * iOne;
1453
1454
                              // copy constant to device memory
1455
1456
                              cudaMemcpyToSymbol( d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
            );
1457
                              cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
            );
                              1458
1459
```

```
cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1461
1462
                           // set kernel grid size and block size
1463
                          \label{lockperGrid} $$\dim 3$ \ grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (grid_RRow / 16), (grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16),
         grid_ZColumn / 16), PhiSlice);
1464
                          dim3 grid_ThreadPerBlock(16, 16);
1465
1466
                    // prolongation
                          prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1467
         grid_ZColumn, grid_PhiSlice );
1468 //
                          cudaDeviceSynchronize();
1469
1470
                           // red-black gauss seidel relaxation (nPost times)
1471
                           for (int i = 0; i < nPost; i++)
1472
1473
                                 relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1474 //
                                 cudaDeviceSynchronize();
1475
                                 relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1476 //
                                cudaDeviceSynchronize();
1477
                          }
1478
                    }
1479
1480
                     // down one
1481
                           residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1482
         d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1483
1484
                           iOne = iOne * 2:
1485
                          jOne = jOne * 2;
1486
1487
                          grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
1488
                          coef_StartPos += grid_RRow;
1489
                                                   = ((RRow - 1) / iOne) + 1;
1490
                           arid RRow
                          grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1491
1492
1493
                           // pre-compute constant memory
                          h = gridSizeR * iOne;
h2 = h * h;
1494
1495
                           ih2 = 1.0 / h2:
1496
1497
1498
                           tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1499
                           tempRatioPhi = ratioPhi * iOne * iOne;
1500
1501
1502
                           // copy constant to device memory
1503
                           );
1504
                           cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
           );
1505
                           \verb|cudaMemcpyToSymbol(d_h2, \&h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice |); \\
                           1506
1507
1508
                           // set kernel grid size and block size
                           dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1510
         grid_ZColumn / 16), PhiSlice);
1511
                          dim3 grid_ThreadPerBlock(16, 16);
1512
                           // restriction
1513
1514
                           restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
         d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1515
                           //cudaDeviceSynchronize();
1516
1517
                           // zeroing V
                          zeroingVPotential <<< grid BlockPerGrid, grid ThreadPerBlock >>> ( d VPotential, grid RRow,
1518
         grid ZColumn, grid PhiSlice );
1519
                          //cudaDeviceSynchronize();
1520
1521
                           // red-black gauss seidel relaxation (nPre times)
1522
                           for (int i = 0; i < nPre; i++)</pre>
1523
         relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential, d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4 );
1524
1525
                                 //cudaDeviceSynchronize();
1526
                                 relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1527
                                 //cudaDeviceSynchronize();
1528
1529
1530
1532
1534
                     // up two from gridTo - 1, to gridTo -3 \,
1535
                     for (int step = (gridTo - 1); step >= gridTo - 3; step--)
1536
```

```
iOne = iOne / 2;
                                       jOne = jOne / 2;
1538
1539
                                       grid_RRow = ((RRow - 1) / iOne) + 1;
grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1540
1541
1542
1543
                                       grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
                                       coef_StartPos -= grid_RRow;
1544
1545
1546
                                              = gridSizeR * iOne;
                                       h2 = h * h;
1547
                                       ih2 = 1.0 / h2;
1548
1549
1550
                                       tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1551
                                       tempRatioPhi = ratioPhi * iOne * iOne;
1552
1553
                                       // copy constant to device memory
                                       cudaMemcpyToSymbol(d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
1554
                );
1555
                                       cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
                );
1556
                                       \verb| cudaMemcpyToSymbol( d_h2, \&h2, 1 * size of (float), 0, cudaMemcpyHostToDevice ); \\
                                       \verb| cudaMemcpyToSymbol( d_ih2, \&ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice ); \\
1557
1558
                                       cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1559
1560
                                        // set kernel grid size and block size
                                       \label{eq:dim3} \ \mbox{grid\_BlockPerGrid((grid\_RRow < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16), (grid\_RRow / 16)
1561
             grid_ZColumn / 16), PhiSlice);
1562
                                       dim3 grid_ThreadPerBlock(16, 16);
1563
1564
                                       // prolongation
                                       prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
1565
              grid_ZColumn, grid_PhiSlice );
1566 //
                                       cudaDeviceSynchronize();
1567
1568
                                       // red-black gauss seidel relaxation (nPost times)
                                       for (int i = 0; i < nPost; i++)</pre>
1569
1570
1571
                                                 relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
             d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1572 //
                                                cudaDeviceSynchronize();
                                                relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1573
              d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1574 //
                                               cudaDeviceSynchronize();
1575
1576
1577
                              // down to from gridTo - 1, to gridTo -3 \,
1578
                              for (int step = gridTo - 3; step <= gridTo - 1; step++)
1579
1580
1581
                                       iOne = iOne * 2;
1582
                                       jOne = jOne * 2;
1583
                                       grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
coef_StartPos += grid_RRow;
1584
1585
1586
1587
                                       arid RRow
                                                                          = ((RRow - 1) / iOne) + 1;
                                                                           = ((ZColumn - 1) / jOne) + 1;
1588
                                       grid_ZColumn
1589
                                        // pre-compute constant memory
1590
                                       h = gridSizeR * iOne;
h2 = h * h;
1591
1592
1593
                                       ih2 = 1.0 / h2;
1594
1595
                                       tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1596
                                       tempRatioPhi = ratioPhi * iOne * iOne;
1597
1598
                                       // copy constant to device memory
                                       cudaMemcpyToSymbol(d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
1599
                );
1600
                                       cudaMemcpyToSymbol( d_coef_StartPos, &coef_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
                );
                                       1601
1602
1603
                                       cudaMemcpyToSymbol( d tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1604
1605
                                        // set kernel grid size and block size
1606
                                       \label{eq:dim3} \mbox{grid\_BlockPerGrid((grid\_RRow < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16) ? 1 : (grid\_RRow / 16), (grid\_ZColumn < 16), (grid\_
             grid_ZColumn / 16), PhiSlice);
1607
                                       dim3 grid_ThreadPerBlock(16, 16);
1608
1609
                                       // restriction
                                       restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
1610
             d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1611
                                       //cudaDeviceSynchronize();
1612
                                       // zeroing V
1613
```

```
1614
                 zeroingVPotential<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential, grid_RRow,
      grid_ZColumn, grid_PhiSlice );
1615
                 //cudaDeviceSynchronize();
1616
1617
                 // red-black gauss seidel relaxation (nPre times)
1618
                 for (int i = 0; i < nPre; i++)
1619
                     relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1620
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1621
                     //cudaDeviceSynchronize();
                     relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1622
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1623
                     //cudaDeviceSynchronize();
1624
1625
1626
                 // residue calculation
1627
                 if (step < gridTo)</pre>
1628
                 {
1629
                     residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
     d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1630
                     //cudaDeviceSynchronize();
1631
1632
                 }
             }
1633
1634
1635
1636
1638
                 int step = (gridTo - 1);
1639
                 iOne = iOne / 2;
jOne = jOne / 2;
1640
1641
1642
                                 = ((RRow - 1) / iOne) + 1;
1643
                 grid_RRow
                 grid_ZColumn = ((ZColumn - 1) / jOne) + 1;
1644
1645
                 grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
1646
                 coef_StartPos -= grid_RRow;
1647
1648
1649
                     = gridSizeR * iOne;
1650
                 h2 = h * h;
1651
                 ih2 = 1.0 / h2;
1652
                 tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1653
                 tempRatioPhi = ratioPhi * iOne * iOne;
1654
1655
1656
                 // copy constant to device memory
1657
                 cudaMemcpyToSymbol( d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
       );
1658
                 cudaMemcpvToSymbol ( d coef StartPos, &coef StartPos, 1 * sizeof(int), 0, cudaMemcpvHostToDevice
       );
1659
                 cudaMemcpyToSymbol( d_h2, &h2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
                 cudaMemcpyToSymbol(d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);
1660
1661
                 \verb|cudaMemcpyToSymbol(d_tempRatioZ, \& tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice);| \\
1662
                 // set kernel grid size and block size
1663
                 dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1664
     grid_ZColumn / 16), PhiSlice);
1665
                 dim3 grid_ThreadPerBlock(16, 16);
1666
1667
             // prolongation
1668
                 prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
      grid ZColumn, grid PhiSlice );
1669 //
                 cudaDeviceSynchronize();
1670
1671
                 // red-black gauss seidel relaxation (nPost times)
1672
                 for (int i = 0; i < nPost; i++)</pre>
1673
                     relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1674
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
                     cudaDeviceSynchronize();
                     relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1676
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1677 //
                     cudaDeviceSynchronize();
1678
1679
             }
1680
1681
1682
1683
                 residueCalculation<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
     d_RhoChargeDensity, d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_icoef4);
1684
1685
                 iOne = iOne * 2;
                 jOne = jOne * 2;
1686
1687
1688
                 grid_StartPos += grid_RRow * grid_ZColumn * PhiSlice;
                 coef_StartPos += grid_RRow;
1689
1690
```

```
1691
                          arid RRow
                                                  = ((RRow - 1) / iOne) + 1;
                                                  = ((ZColumn - 1) / jOne) + 1;
1692
                          grid ZColumn
1693
1694
                          // pre-compute constant memory
1695
                          h = gridSizeR * iOne;
h2 = h * h;
1696
                          ih2 = 1.0 / h2;
1697
1698
1699
                          tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1700
                          tempRatioPhi = ratioPhi * iOne * iOne;
1701
1702
1703
                          // copy constant to device memory
                          cudaMemcpyToSymbol(d_grid_StartPos, &grid_StartPos, 1 * sizeof(int), 0, cudaMemcpyHostToDevice
1704
           );
1705
                          );
                          1706
1707
1708
                          cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1709
1710
                           // set kernel grid size and block size
                          \label{lockPerGrid} $$\dim 3$ \ grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid_RRow / 16), (grid_RRow / 16) ? 1 : (grid
1711
         grid ZColumn / 16), PhiSlice);
1712
                          dim3 grid_ThreadPerBlock(16, 16);
1713
1714
1715
                          restriction2DFull<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_RhoChargeDensity,
         d_DeltaResidue, grid_RRow, grid_ZColumn, grid_PhiSlice );
1716
                          //cudaDeviceSynchronize();
1717
1718
                          // zeroing V
1719
                          zeroingVPotential<<< grid_BlockPerGrid, grid_ThreadPerBlock >>> ( d_VPotential, grid_RRow,
         grid_ZColumn, grid_PhiSlice );
1720
                          //cudaDeviceSynchronize();
1721
                          // red-black gauss seidel relaxation (nPre times) for (int i = 0; i < nPre; i++)  
1722
1723
1724
                                 relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1725
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1726
                                //cudaDeviceSynchronize();
                                 relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
1727
         d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1728
                               //cudaDeviceSynchronize();
1729
1730
1731
                    }
1733
1735
1736
                    // V-Cycle => from coarser to finer grid
1737
                    for (int step = (gridTo - 1); step >= gridFrom; step--)
1738
1739
                          iOne = iOne / 2;
                          jOne = jOne / 2;
1740
1741
1742
                                                  = ((RRow - 1) / iOne) + 1;
                          arid RRow
1743
                                                  = ((ZColumn - 1) / jOne) + 1;
                          grid_ZColumn
1744
1745
                          grid_StartPos -= grid_RRow * grid_ZColumn * PhiSlice;
                          coef_StartPos -= grid_RRow;
1746
1747
1748
                               = gridSizeR * iOne;
1749
                          h2 = \tilde{h} * h;
1750
                          ih2 = 1.0 / h2;
1751
                          tempRatioZ = ratioZ * iOne * iOne / (jOne * jOne);
1752
                          tempRatioPhi = ratioPhi * iOne * iOne;
1753
1754
                           // copy constant to device memory
1756
                          1757
                          );
1758
                          \verb"cudaMemcpyToSymbol" ( \verb"d_h2", \&h2", 1 * sizeof(float)", 0, \verb"cudaMemcpyHostToDevice")";
1759
                          cudaMemcpyToSymbol( d_ih2, &ih2, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1760
                          cudaMemcpyToSymbol( d_tempRatioZ, &tempRatioZ, 1 * sizeof(float), 0, cudaMemcpyHostToDevice );
1761
1762
                           // set kernel grid size and block size
                          dim3 grid_BlockPerGrid((grid_RRow < 16) ? 1 : (grid_RRow / 16), (grid_ZColumn < 16) ? 1 : (
1763
         grid_ZColumn / 16), PhiSlice);
1764
                          dim3 grid_ThreadPerBlock(16, 16);
1765
1766
1767
                          prolongation2DHalf<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential, grid_RRow,
         grid_ZColumn, grid_PhiSlice );
// cudaDeviceSynchronize();
1768 //
```

```
1770
                  // red-black gauss seidel relaxation (nPost times)
1771
                  for (int i = 0; i < nPost; i++)
1772
                 {
1773
                      relaxationGaussSeidelRed<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
// cudaDeviceSynchronize();
1774 //
1775
                      relaxationGaussSeidelBlack<<< grid_BlockPerGrid, grid_ThreadPerBlock >>>( d_VPotential,
      d_RhoChargeDensity, grid_RRow, grid_ZColumn, grid_PhiSlice, d_coef1, d_coef2, d_coef3, d_coef4);
1776 //
                     cudaDeviceSynchronize();
1777
1778
            }
1779
1780
        /*V-Cycle ends*/
1781
1782
             errorCalculation<<< error_BlockPerGrid, error_ThreadPerBlock >>> ( d_VPotentialPrev, d_VPotential,
     d EpsilonError, RRow, ZColumn, PhiSlice);
1783
1784
             cudaMemcpy( EpsilonError, d_EpsilonError, 1 * sizeof(float), cudaMemcpyDeviceToHost );
1785
1786
             errorConv[cycle] = *EpsilonError / (RRow * ZColumn * PhiSlice);
1787
1788
1789
             if (errorConv[cycle] < convErr)</pre>
1790
1791
                  //errorConv
1792
                  nCycle = cycle;
1793
                  iparam[3] = nCycle;
1794
                 break;
1795
             }
1796
1797
             cudaMemcpy( d_VPotentialPrev, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
     cudaMemcpyDeviceToDevice );
1798
             cudaMemset( d_EpsilonError, 0, 1 * sizeof(float) );
1799
1800
1801
1802
1803
1804
         cudaDeviceSynchronize();
1805
         // copy result from device to host
         cudaMemcpy( temp_VPotential, d_VPotential, RRow * ZColumn * PhiSlice * sizeof(float),
1806
      cudaMemcpyDeviceToHost );
1807
1808
         memcpy(VPotential, temp_VPotential, RRow * ZColumn * PhiSlice * sizeof(float));
1809
1810
         // free device memory
        cudaFree( d_VPotential );
cudaFree( d_VPotentialPrev );
cudaFree( d_EpsilonError );
1811
1812
1813
1814
1815
1816
         cudaFree( d_DeltaResidue );
1817
        cudaFree( d_RhoChargeDensity );
        cudaFree( d_coef1 );
1818
1819
        cudaFree( d coef2 );
1820
        cudaFree( d_coef3 );
1821
        cudaFree( d_coef4 );
1822
        cudaFree( d_icoef4 );
1823
        // free host memory
1824
1825
       free( coef1 );
1826
        free( coef2 );
1827
         free( coef3 );
1828
         free( coef4 );
1829
         free( icoef4 );
1830
         free( temp_VPotential );
         //free( temp_VPotentialPrev );
1831
1832 }
```

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