# $\operatorname{HarvardX}\mid\operatorname{PH}125.9x\mid\operatorname{CASDatasets}$ Project - Claims Frequency

# Reema Sajnani

## 2024-05-22

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### 1 EXECUTIVE SUMMARY

It is important for insurers to understand what portion of their policy holders will file claims and, how often. This project puts us in the shoes of insurers and analyzes third party motor insurance claims made in France. The goal is to predict how frequently insurance claims are made on policies, with as much accuracy as possible. In order to test accuracy we will aim to have a Mean Absolute Error closer to 0.

The particular data sets selected from CASdatasets (hosted by Christophe Dutang) and are referred to as FreMTPL2freq (frequency data set) and FreMTPL2sev (severity data set). The former comprises data on insurance policy and claim frequency, while the latter includes information on the associated claim severity amounts.

This project uses Generalized Linear Model and a Decision Tree model. These models obtain Mean Absolute Errors of 7.29% and 11.09% respectively. The GLM is our model of choice due to it's low error value, making it a good fit.

### 2 PACKAGE INSTALLATION AND DATA SETUP

```
if(!require(knitr)) install.packages("knitr", repos = "http://cran.us.r-project.org")
## Loading required package: knitr
## Warning: package 'knitr' was built under R version 4.3.3
if(!require(tidyverse)) install.packages("tidyverse", repos = "http://cran.us.r-project.org")
## Loading required package: tidyverse
## Warning: package 'tidyverse' was built under R version 4.3.3
## Warning: package 'ggplot2' was built under R version 4.3.3
## Warning: package 'dplyr' was built under R version 4.3.3
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.4 v readr
                                   2.1.4
## v forcats 1.0.0 v stringr 1.5.0
## v ggplot2 3.5.1
                      v tibble
                                   3.2.1
## v lubridate 1.9.2
                        v tidyr
                                    1.3.0
## v purrr
              1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
if(!require(dplyr)) install.packages("dplyr", repos = "http://cran.us.r-project.org")
if(!require(lattice)) install.packages("lattice", repos = "http://cran.us.r-project.org")
## Loading required package: lattice
## Warning: package 'lattice' was built under R version 4.3.3
if(!require(caret)) install.packages("caret", repos = "http://cran.us.r-project.org")
## Loading required package: caret
## Warning: package 'caret' was built under R version 4.3.3
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
      lift
##
```

```
if(!require(rpart)) install.packages("rpart", repos = "https://cran.r-project.org/package=rpart")
## Loading required package: rpart
## Warning: package 'rpart' was built under R version 4.3.3
if(!require(rpart.plot)) install.packages("rpart.plot", repos = "https://CRAN.R-project.org")
## Loading required package: rpart.plot
## Warning: package 'rpart.plot' was built under R version 4.3.3
if(!require(repr)) install.packages("repr", repos = "http://cran.us.r-project.org")
## Loading required package: repr
## Warning: package 'repr' was built under R version 4.3.3
if(!require(xts)) install.packages("xts", repos = "http://cran.us.r-project.org")
## Loading required package: xts
## Warning: package 'xts' was built under R version 4.3.3
## Loading required package: zoo
## Warning: package 'zoo' was built under R version 4.3.3
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
      as.Date, as.Date.numeric
##
##
## # The dplyr lag() function breaks how base R's lag() function is supposed to
## # work, which breaks lag(my_xts). Calls to lag(my_xts) that you type or
## # source() into this session won't work correctly.
## #
## # Use stats::lag() to make sure you're not using dplyr::lag(), or you can add #
## # conflictRules('dplyr', exclude = 'lag') to your .Rprofile to stop
## # dplyr from breaking base R's lag() function.
## #
## # Code in packages is not affected. It's protected by R's namespace mechanism #
## # Set `options(xts.warn_dplyr_breaks_lag = FALSE)` to suppress this warning.
## #
```

```
##
## Attaching package: 'xts'
##
## The following objects are masked from 'package:dplyr':
##
##
      first, last
if(!require(sp)) install.packages("sp", repos = "http://cran.us.r-project.org")
## Loading required package: sp
## Warning: package 'sp' was built under R version 4.3.3
if(!require(zoo)) install.packages("zoo", repos = "http://cran.us.r-project.org")
if(!require(modelr)) install.packages("modelr", repos = "http://cran.us.r-project.org")
## Loading required package: modelr
## Warning: package 'modelr' was built under R version 4.3.3
install.packages("CASdatasets", repos = "http://cas.uqam.ca/pub/", type="source")
## Installing package into 'C:/Users/Reema/AppData/Local/R/win-library/4.3'
## (as 'lib' is unspecified)
if(!require(AER)) install.packages("AER", repos = "http://cran.us.r-project.org")
## Loading required package: AER
## Warning: package 'AER' was built under R version 4.3.3
## Loading required package: car
## Warning: package 'car' was built under R version 4.3.3
## Loading required package: carData
## Warning: package 'carData' was built under R version 4.3.3
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
      recode
## The following object is masked from 'package:purrr':
##
##
      SOME
##
## Loading required package: lmtest
```

```
## Warning: package 'lmtest' was built under R version 4.3.3
## Loading required package: sandwich
## Warning: package 'sandwich' was built under R version 4.3.3
## Loading required package: survival
##
## Attaching package: 'survival'
## The following object is masked from 'package:caret':
##
       cluster
library("knitr")
library("tidyverse")
library("dplyr")
library("lattice")
library("caret")
library("rpart")
library("rpart.plot")
library("repr")
library("modelr")
library("CASdatasets")
library("AER")
```

### 3 LOAD DATA SETS

```
#load the two data sets and convert into tibbles
data(freMTPL2freq)
data <- as_tibble(freMTPL2freq)
data(freMTPL2sev)
sev<- as_tibble(freMTPL2sev)</pre>
```

### 4 DATA EXPLORATION

#### 4.1 Data Class and Details

We first explore the data sets.

freMTPL2freq (frequency data set) - this has 12 vectors and 678,013 rows of observations. Below we explore their class and description.

## Dimensions 678013 12

### CLASS:

- IDpol <numeric> unique Policy ID
- ClaimNb Number of claims during the exposed time period
- Exposure <numeric> time period (years)
- VehPower <integer> Power of the insured car
- VehAge <integer> Vehicle age (in years)
- DrivAge <integer> Driver age (in years)
- Bonus Malus <<br/>integer> Bonus/malus, between 50 and 230  $\,$
- VehBrand <factor> Car Brand
- VehGas <character> Car Fuel Type
- Area <factor> "A" for rural to "F" for urban centre
- Density <integer> Population density in the area where driver resides
- Region <factor> Policy region in France

freMTPL2sev (severity data set) - this has 2 vectors and 26,639 rows of observations. Below we explore their class and description.

## Dimensions 26639 2

#### CLASS:

- IDpol <numeric> unique Policy ID
- ClaimAmount Amount per claim made

### 4.2 Data Clean-up and Modifications

We start by making sure all columns are in a format that can be filtered and used ahead for visualization and model calculation.

## This is what the frequency data set looks like after changing the class of VehGas vector and double

## # A tibble: 6 x 12 IDpol ClaimNb Exposure VehPower VehAge DrivAge BonusMalus VehBrand VehGas ## ## <dbl> <dbl><dbl> <int> <int> <int> <int> <fct> <fct> ## 1 1 0.1 5 0 55 50 B12 Regular 1 ## 2 3 1 0.77 5 0 55 50 B12 Regular ## 3 2 Diesel 5 1 0.75 6 52 50 B12 ## 4 10 1 0.09 7 0 46 50 B12 Diesel ## 5 11 1 0.84 7 Λ 46 50 B12 Diesel 13 0.52 2 38 50 B12 Regular ## # i 3 more variables: Area <fct>, Density <int>, Region <fct>

We will add claim numbers to severity data set and join these into the frequency data set. This is because there are many rows in the frequency dataset which show a claim was made, however, their corresponding claim amounts are not mentioned in the severity data set. Vice-Versa also applies.

## Updated severity data set with claim frequencies:

```
##
     IDpol ClaimNb
## 1
        139
## 2
        190
                    1
## 3
        414
                    1
                    2
## 4
        424
## 5
        463
                    1
## 6
        606
                    1
```

Joining the frequency and severity data sets ensures we work only with those policy IDs that have valid corresponding claim entries in both sets.

## Sample View of the Joint data set after taking claim frequencies from the severity data set:

```
## # A tibble: 6 x 12
##
     IDpol Exposure VehPower VehAge DrivAge BonusMalus VehBrand VehGas
                                                                              Area
                         <int>
##
     <dbl>
               <dbl>
                                <int>
                                         <int>
                                                     <int> <fct>
                                                                      <fct>
                                                                              <fct>
## 1
         1
                0.1
                             5
                                     0
                                            55
                                                        50 B12
                                                                     Regular D
## 2
         3
                0.77
                             5
                                     0
                                            55
                                                        50 B12
                                                                     Regular D
## 3
         5
                0.75
                             6
                                     2
                                            52
                                                        50 B12
                                                                     Diesel
                                                                              В
                             7
                                     0
## 4
        10
                0.09
                                            46
                                                        50 B12
                                                                     Diesel
                                                                              В
## 5
        11
                0.84
                             7
                                     0
                                            46
                                                        50 B12
                                                                     Diesel
                                                                              В
        13
## 6
                0.52
                             6
                                     2
                                            38
                                                        50 B12
                                                                     Regular E
## # i 3 more variables: Density <int>, Region <fct>, ClaimNb <dbl>
```

### 4.3 Data Insights

#### 4.3.1 Number of Claims

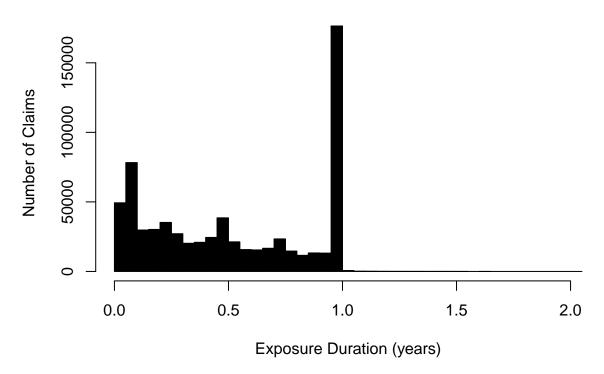
Only about 3.67% of policies seem to have made claims, with one claim being the most commonly occurring (3.48% policies).

```
##
  # A tibble: 11 x 3
##
      ClaimNb
                count
                         percent
##
        <dbl>
                <int>
                            <dbl>
##
    1
             0 653069 96.3
##
    2
                23571
                        3.48
             1
##
    3
             2
                 1298
                        0.191
    4
             3
                    62
                        0.00914
##
##
    5
             4
                     5
                        0.000737
##
    6
             5
                     2
                        0.000295
    7
             6
                        0.000147
##
                     1
##
    8
             8
                     1
                        0.000147
    9
             9
##
                     1
                        0.000147
## 10
            11
                     2
                        0.000295
                        0.000147
## 11
            16
                     1
```

### 4.3.2 Policy Exposures

In this histogram, we notice that very few cases have exposures durrations greater than one year.

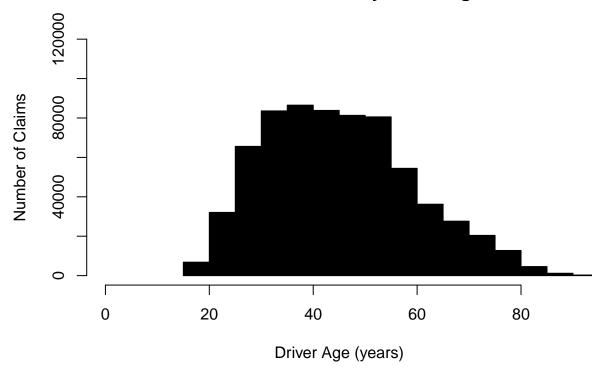
# **Number of Claims by Exposure Duration**



### 4.3.3 Drivers' Age

We notice that there are very few instances of drivers above the age of 90, making claims.

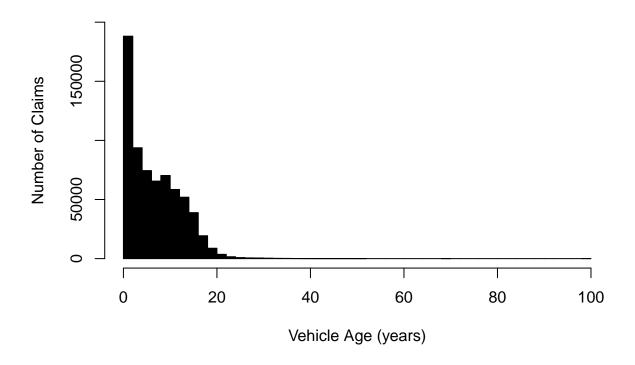
# **Number of Claims by Driver Age**



## 4.3.4 Vehicle Age

In this case it is visible that very few claims are made on cars that are more than 20 years old.

# **Number of Claims by Vehicle Age**



### 4.4 Data Pre-Processing

Based on our visualization above, we make some corrections to the data in order to make our analysis more effective. Next steps will include:

- a. Correcting number of claims above 4 to equal to 4. We believe greater than 4 claims are highly unlikely and are caused from data entry errors
- b. Correcting exposures over 1 year, to 1 year. Since this is yearly claim data set, exposure greater than 1 year could be from data entry errors
- c. Correcting all Driver Ages above 90 years, to 90. It is unlikely for someone at that age to be driving
- d. Correcting Vehicle Ages over 40 years, to 40 year. It is unlikely cars last that long and we assume these entries are from data entry errors

## After making the above changes, the data set looks something like this:

##	# A tibble	: 678,013	x 12						
##	VehBrand	d ClaimNb	DrivAge	Exposure	Area	${\tt BonusMalus}$	IDpol	Region	VehGas
##	<fct></fct>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<fct></fct>	<int></int>	<dbl></dbl>	<fct></fct>	<fct></fct>
##	1 B12	0	55	0.1	D	50	1	Rhone-Alpes	Regul~
##	2 B12	0	55	0.77	D	50	3	Rhone-Alpes	Regul~
##	3 B12	0	52	0.75	В	50	5	Picardie	Diesel
##	4 B12	0	46	0.09	В	50	10	Aquitaine	Diesel

```
5 B12
                      0
                             46
                                     0.84 B
                                                         50
                                                                11 Aquitaine
##
    6 B12
                             38
                                     0.52 E
                      0
                                                         50
                                                                13 Nord-Pas-de-~ Regul~
                                                                15 Nord-Pas-de-~ Regul~
##
   7 B12
                      0
                             38
                                     0.45 E
                                                         50
                      0
                             33
##
   8 B12
                                     0.27 C
                                                         68
                                                                17 Languedoc-Ro~ Diesel
                                                                18 Languedoc-Ro~ Diesel
## 9 B12
                      0
                             33
                                     0.71 C
                                                         68
## 10 B12
                      0
                                     0.15 B
                                                                21 Pays-de-la-L~ Diesel
                             41
                                                         50
## # i 678,003 more rows
```

## # i 3 more variables: Density <int>, VehAge <dbl>, VehPower <int>

### 4.5 Impact on Claim Rate

So far we saw the number of claims made by sub groups in each vector. Now we will analyze how frequently these groups make claims.

We start by adding a column for the claim frequency of every entry.

## the New Joint data set looks something like this:

```
## # A tibble: 678,013 x 13
##
       Freq VehBrand ClaimNb VehPower BonusMalus Region
                                                              VehGas IDpol Area VehAge
##
      <dbl> <fct>
                        <dbl>
                                  <int>
                                              <int> <fct>
                                                              <fct>
                                                                     <dbl> <fct>
    1
          0 B12
                            0
                                      5
                                                 50 Rhone-A~ Regul~
                                                                         1 D
                                                                                       0
##
##
    2
          0 B12
                            0
                                      5
                                                 50 Rhone-A~ Regul~
                                                                         3 D
                                                                                       0
                                                                                       2
##
    3
          0 B12
                            0
                                      6
                                                 50 Picardie Diesel
                                                                         5 B
##
    4
          0 B12
                            0
                                      7
                                                 50 Aquitai~ Diesel
                                                                        10 B
                                                                                       0
                                      7
##
    5
          0 B12
                            0
                                                 50 Aquitai~ Diesel
                                                                        11 B
                                                                                       0
##
    6
          0 B12
                            0
                                      6
                                                                        13 E
                                                                                       2
                                                 50 Nord-Pa~ Regul~
   7
                                                                                       2
##
          0 B12
                            0
                                      6
                                                 50 Nord-Pa~ Regul~
                                                                        15 E
##
   8
          0 B12
                            0
                                      7
                                                 68 Langued~ Diesel
                                                                        17 C
                                                                                       0
## 9
          0 B12
                            0
                                      7
                                                 68 Langued~ Diesel
                                                                        18 C
                                                                                       0
## 10
          0 B12
                            0
                                      7
                                                 50 Pays-de~ Diesel
                                                                        21 B
                                                                                       0
## # i 678,003 more rows
## # i 3 more variables: Density <int>, DrivAge <dbl>, Exposure <dbl>
```

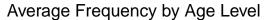
### 4.5.1 Driver Age

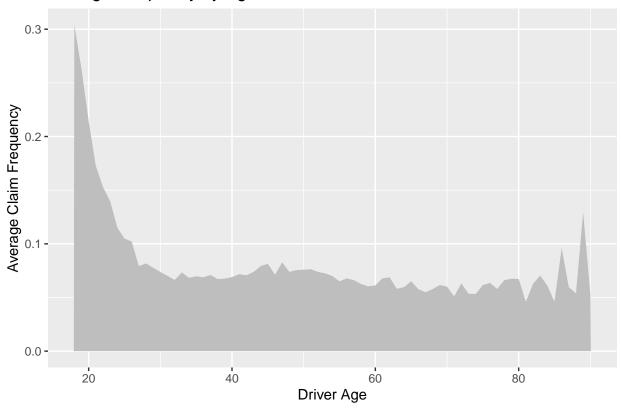
First we analyze driver age impact on claim frequency.

From the below plot, it is clear that the highest claim frequency is coming from the age group under 25, with 18 year-olds being the most frequent claimants.

## These are the top 5 age groups with highest average claim rates:

```
## # A tibble: 5 x 2
##
     DrivAge claim_frequency
##
       <dbl>
                         <dbl>
## 1
           18
                         0.304
## 2
           19
                         0.263
## 3
           20
                         0.214
## 4
                         0.173
           21
## 5
                         0.153
           22
```



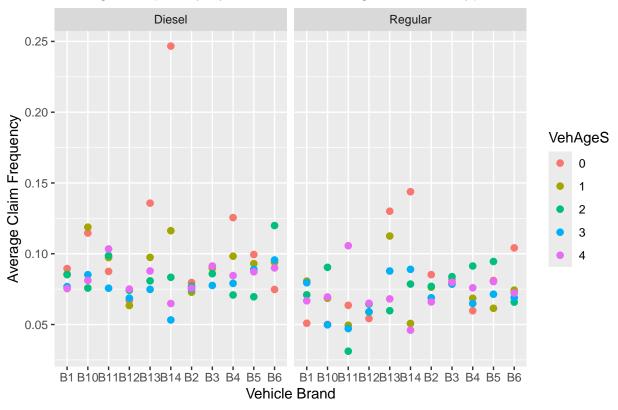


### 4.5.2 Fuel Type, Vehicle Brand and Vehicle Age

When assessing Fuel Type and Car Brand groups, we notice overall lower frequencies for regular fuel cars compared to diesel powered ones. We also see that vehicles that are newer (orange plot dot in the graph), seem to be the ones claiming more often.

```
## `summarise()` has grouped output by 'VehBrand', 'VehAgeS'. You can override
## using the `.groups` argument.
```





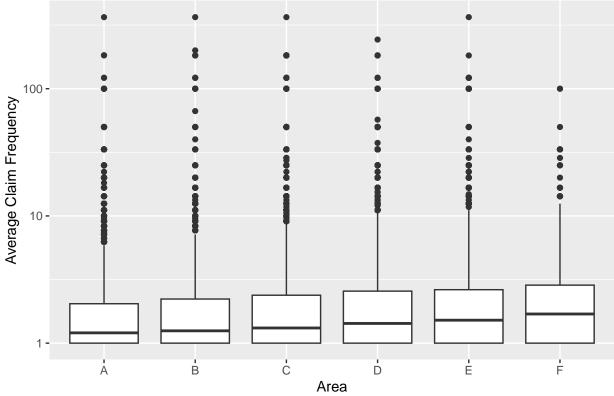
#### 4.5.3 Area

Looking at the below chart, it is clear that claims flow in more often from urban areas (Area F). This Area also has an overall higher median claim frequency.

## Warning in scale\_y\_log10(): log-10 transformation introduced infinite values.

## Warning: Removed 653069 rows containing non-finite outside the scale range
## (`stat\_boxplot()`).

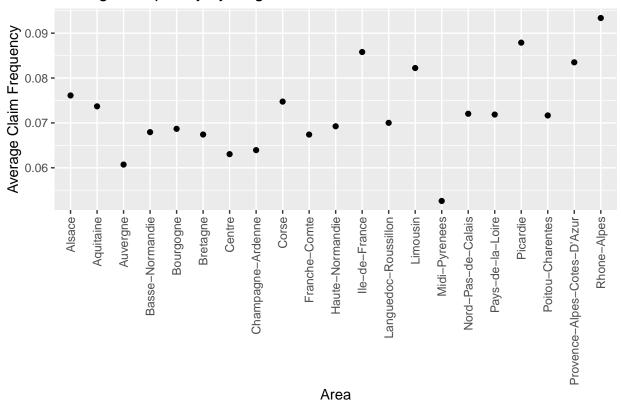




## 4.5.4 Region

Rhone-Alps, Ile-de-France and Picardie regions have the highest claims frequency. One of these is a major city, which could be a reason for the higher claim rate.

# Average Frequency by Region

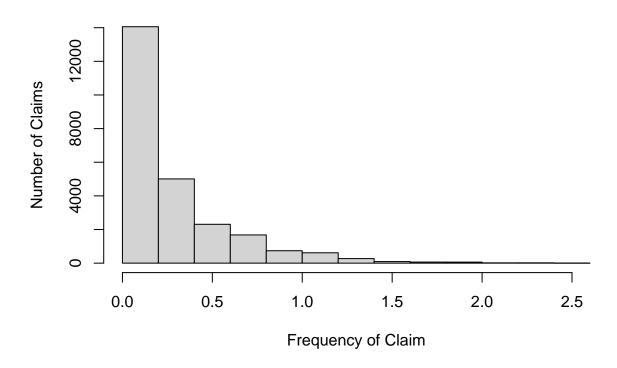


### 5 DATA MODELLING

### 5.1 Distribution Type

From the below histogram we conclude that our data is based on a Poisson Distribution (rate related data). This will play an important role in the model we choose later in this project and the arguments to be included in the code. This also means that Poisson GLM will be a natural first modelling approach.

# **Frequency Distribution**



### 5.2 Train and Test Sets

We split our data into a 70:30 split to ensure there is enough representation of variability in the test set.

NOTE: We also tried 80:20 and 90:10 splits but got very poor results. Hence we conclude that 70:30 is a good representation.

The train set has 203404 observations.

### 5.3 Generalized Linear Model

They key assumptions for this model are:

- a. the relationship between number of claims and log(claim frequency) is linear
- b. each claim outcome are independent of one another
- c. mean is equal to the variance

Formula applicable to Poisson Distribution

$$log(y) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_p x_p$$

Where:

y: Is the rate variable or 'Lambda'. In our case this is the claim frequency rate

Beta: numeric coefficients, Beta0 being the intercept

x: predictor variables

Since this is rate based data, we need an offset of the logarithmic denominator. So, customizing the above equation for our model, we use this formula, where log(Exposure) is the offset.

$$log(ClaimNb) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p + log(Exposure)$$

After fitting the Generalized Linear Model (GLM), we are able to see the most significant objects.

```
##
## Call:
## glm(formula = ClaimNb ~ VehPower + VehAge + DrivAge + BonusMalus +
       VehBrand + VehGas + Area + Density + Region + offset(log(Exposure)),
##
       family = "poisson", data = train_set)
##
##
## Coefficients:
##
                                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                     -4.735e+00 1.369e-01 -34.576 < 2e-16 ***
                                                                     < 2e-16 ***
## VehPower
                                      3.734e-02 3.932e-03
                                                              9.497
## VehAge
                                     -1.720e-02
                                                  1.541e-03 -11.159
                                                                     < 2e-16 ***
## DrivAge
                                      5.116e-03
                                                 5.517e-04
                                                              9.273
                                                                     < 2e-16 ***
## BonusMalus
                                      2.632e-02
                                                 3.941e-04
                                                             66.773
                                                                     < 2e-16 ***
## VehBrandB10
                                     -9.041e-03
                                                 4.704e-02
                                                             -0.192
                                                                     0.84758
## VehBrandB11
                                      1.219e-01
                                                                     0.01556 *
                                                 5.041e-02
                                                              2.419
## VehBrandB12
                                     -3.062e-01
                                                 2.640e-02 -11.602
                                                                     < 2e-16 ***
## VehBrandB13
                                      1.372e-02
                                                 5.436e-02
                                                                     0.80081
                                                              0.252
## VehBrandB14
                                     -1.757e-01
                                                  1.060e-01
                                                             -1.658
                                                                     0.09730 .
## VehBrandB2
                                      8.324e-03
                                                  2.043e-02
                                                              0.407
                                                                     0.68375
## VehBrandB3
                                      4.250e-02 2.855e-02
                                                                     0.13659
                                                              1.489
## VehBrandB4
                                     -6.084e-03 3.929e-02
                                                             -0.155
                                                                     0.87694
## VehBrandB5
                                      9.005e-02
                                                 3.260e-02
                                                              2.763
                                                                     0.00573
## VehBrandB6
                                      1.486e-02
                                                 3.734e-02
                                                              0.398
                                                                     0.69056
## VehGasRegular
                                     -1.913e-01
                                                 1.521e-02 -12.574
                                                                     < 2e-16 ***
## AreaB
                                      1.256e-01
                                                 3.147e-02
                                                              3.990 6.60e-05 ***
## AreaC
                                      1.737e-01
                                                  2.625e-02
                                                              6.620 3.60e-11 ***
## AreaD
                                      3.261e-01
                                                 2.777e-02 11.743
                                                                     < 2e-16 ***
## AreaE
                                      4.334e-01
                                                  3.600e-02
                                                             12.038
                                                                     < 2e-16 ***
## AreaF
                                                 1.238e-01
                                      5.187e-01
                                                              4.188 2.81e-05 ***
## Density
                                     -3.571e-06
                                                  5.112e-06
                                                             -0.699
                                                                     0.48475
## RegionAquitaine
                                      8.312e-02
                                                 1.295e-01
                                                              0.642
                                                                     0.52110
## RegionAuvergne
                                     -3.908e-02
                                                 1.603e-01
                                                             -0.244
                                                                     0.80734
## RegionBasse-Normandie
                                     -2.397e-02
                                                 1.368e-01
                                                             -0.175
                                                                     0.86090
## RegionBourgogne
                                     -3.304e-03
                                                 1.406e-01
                                                             -0.023
                                                                     0.98126
## RegionBretagne
                                      5.341e-02 1.273e-01
                                                              0.420
                                                                     0.67481
## RegionCentre
                                      1.665e-02 1.255e-01
                                                              0.133
                                                                     0.89443
## RegionChampagne-Ardenne
                                      2.743e-02 1.854e-01
                                                                     0.88240
                                                              0.148
```

```
## RegionCorse
                                     1.801e-01 1.626e-01
                                                            1.108
                                                                   0.26796
                                     -6.481e-03 2.292e-01
                                                           -0.028
## RegionFranche-Comte
                                                                   0.97744
## RegionHaute-Normandie
                                     3.496e-02 1.474e-01
                                                            0.237
                                                                   0.81260
## RegionIle-de-France
                                                1.274e-01
                                                            0.274
                                                                   0.78442
                                     3.485e-02
## RegionLanguedoc-Roussillon
                                     2.518e-02
                                                1.298e-01
                                                            0.194
                                                                   0.84623
## RegionLimousin
                                     3.530e-01 1.519e-01
                                                            2.324
                                                                   0.02015 *
## RegionMidi-Pyrenees
                                     -2.169e-01
                                               1.389e-01
                                                           -1.562
                                                                   0.11837
## RegionNord-Pas-de-Calais
                                     -9.876e-03 1.283e-01
                                                           -0.077
                                                                   0.93864
## RegionPays-de-la-Loire
                                     6.266e-02 1.278e-01
                                                            0.490
                                                                   0.62393
## RegionPicardie
                                     1.087e-01
                                                1.418e-01
                                                            0.767
                                                                   0.44334
## RegionPoitou-Charentes
                                     8.339e-02
                                                1.314e-01
                                                            0.634
                                                                   0.52582
## RegionProvence-Alpes-Cotes-D'Azur 1.425e-01
                                                1.260e-01
                                                             1.131
                                                                   0.25816
## RegionRhone-Alpes
                                      2.536e-01
                                                1.255e-01
                                                            2.021
                                                                   0.04327 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 119900 on 474608 degrees of freedom
##
## Residual deviance: 114732 on 474567 degrees of freedom
## AIC: 150357
##
## Number of Fisher Scoring iterations: 6
```

From the table above we can infer that the most significant predictors are Vehicle Power, Vehicle Age, Driver Age, Bonus Malus, a couple of Car Brands and all areas (except A). We also noticed the difference between the residual deviance and degrees of freedom, leading us to a dispersion test.

```
##
## Overdispersion test
##
## data: train_glm_offset
## z = 6.1563, p-value = 3.723e-10
## alternative hypothesis: true alpha is greater than 0
## sample estimates:
## alpha
## 0.1059802
```

Since alpha is quite close to 0 we don't have to worry about dispersion here and it is already a good sign of model fitting our data well.

As a next step, we must take exponential of the GLM fit summary table to ensure the formula mentioned at the start of the model is adhered.

##	(Intercept)	VehPower
##	0.009	1.038
##	VehAge	DrivAge
##	0.983	1.005
##	BonusMalus	VehBrandB10
##	1.027	0.991
##	VehBrandB11	VehBrandB12
##	1.130	0.736
##	VehBrandB13	VehBrandB14
##	1.014	0.839

##	VehBrandB2	VehBrandB3
##	1.008	1.043
##	VehBrandB4	VehBrandB5
##	0.994	1.094
##	VehBrandB6	VehGasRegular
##	1.015	0.826
##	AreaB	AreaC
##	1.134	1.190
##	AreaD	AreaE
##	1.386	1.543
##	AreaF	Density
##	1.680	1.000
##	${ t Region Aquitaine}$	RegionAuvergne
##	1.087	0.962
##	RegionBasse-Normandie	RegionBourgogne
##	0.976	0.997
##	RegionBretagne	RegionCentre
##	1.055	1.017
##	RegionChampagne-Ardenne	RegionCorse
##	1.028	1.197
##	RegionFranche-Comte	RegionHaute-Normandie
##	0.994	1.036
##	RegionIle-de-France	RegionLanguedoc-Roussillon
##	1.035	1.025
##	RegionLimousin	RegionMidi-Pyrenees
##	1.423	0.805
##	RegionNord-Pas-de-Calais	RegionPays-de-la-Loire
##	0.990	1.065
##	RegionPicardie	RegionPoitou-Charentes
##	1.115	1.087
##	RegionProvence-Alpes-Cotes-D'Azur	RegionRhone-Alpes
##	1.153	1.289

We provide couple of examples below of interpreting the coefficients:

- If Vehicle Age increases by 1, the claim frequency goes up by a factor of 0.983
- If Vehicle Power goes up by 1, the claim frequency goes up by a factor of 1.038
- If a driver resides in Rhone-Alpes, the claim frequency goes up by a factor of 1.289

The next step was to calculate predictions and analyze the model's capability to predict on the test set using the below code.

A sample of predictions generated are seen here:

```
## 103230 85624 89437 108287 196069 106591
## 0.028 0.042 0.061 0.003 0.019 0.005
```

We will use Mean Absolute Error to evaluate accuracy of the model.

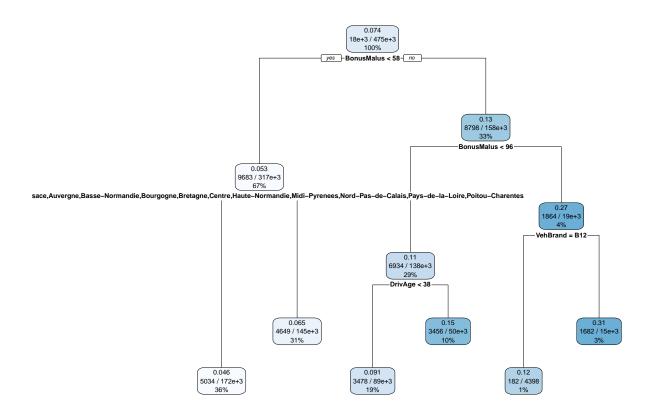
$$MAE = (\Sigma |yi-xi|)/n$$

## [1] 0.07293719

Our model achieves an MAE of 7.29% which is not too far from 0, meaning the model is quite good at predicting the rate of claims.

#### 5.4 Decision Tree Model

Our second model in this project is a decision tree model. The first node of the the below decision tree shows that overall claim frequency is about 7.4%. The highest claim frequency is of the group that has a Bonus Malus above 96 and car brand is not B12 (31%).



The next step was to calculate predictions and analyze the model's capability to predict on the test set using the below code.

A sample of predictions generated are seen here:

```
## 67294 197989 146557 36874 23059 152205
## 0.046 0.046 0.065 0.091 0.046 0.123
```

We will use Mean Absolute Error to evaluate accuracy of the model.

$$MAE = (\Sigma |yi-xi|)/n$$

## [1] 0.1108888

Our model achieves an MAE of 11.09% which is a bit high, meaning the model is not too great at predicting the rate of claims

## 6 RESULTS

The objective was to forecast the frequency of insurance claims on policies with utmost precision. To assess accuracy, we used Mean Absolute Error on the predictions from GLM and Decision Tree models. The models resulted in an error of 7.29% and 11.09% respectively. The GLM is our model of choice as the error is not too far from 0, indicating a strong fit.

### 7 Limitations

Due to limited computing power, and this data set being quite large, we couldn't try other models such as KNN.

### 8 References

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