

NPTEL Week 7 Live Session

on Deep Learning (noc24_ee04)

A course offered by: Prof. Prabir Kumar Biswas, IIT Kharagpur

- Week 6 quiz solution (Autoencoder, PCA)
- Week 7 practice questions (Variety of AE, Convolution, Cross-correlation)



By

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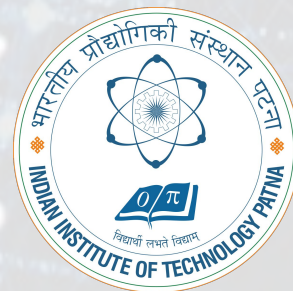
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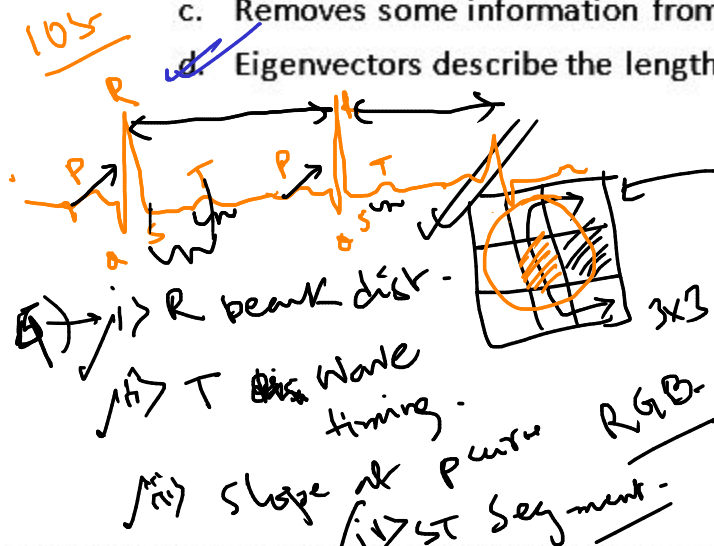
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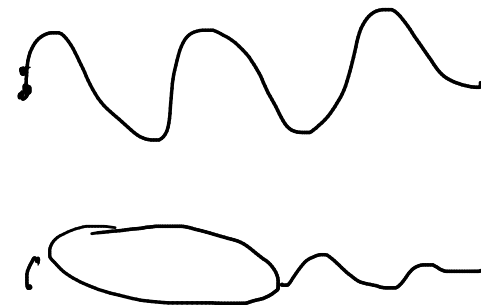
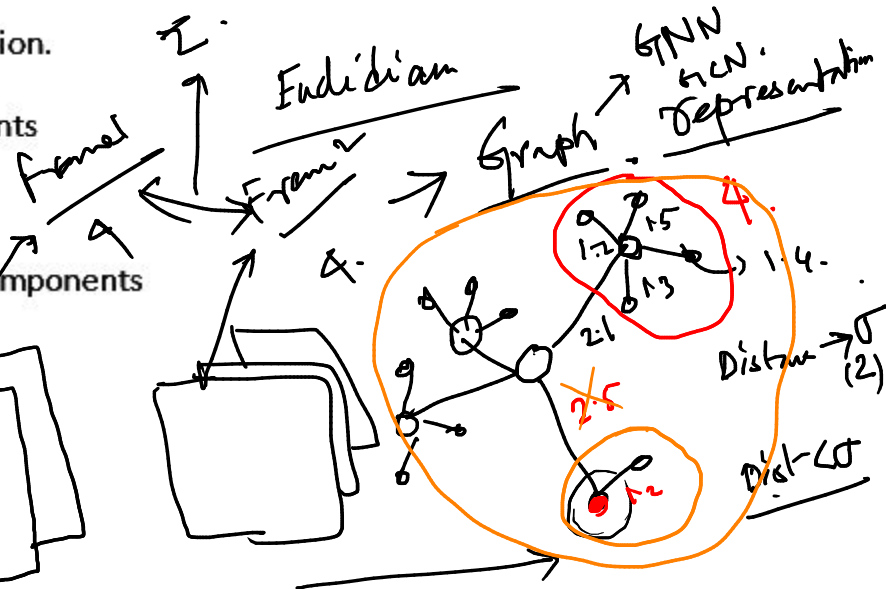
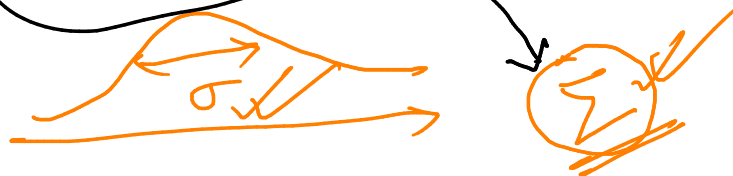
Which of the following is not true for PCA? Choose the correct option.

- a. Rotates the axes to lie along the principal components
 - b. Is calculated from the covariance matrix
 - c. Removes some information from the data
 - d. Eigenvectors describe the length of the principal components
- Handwritten notes:* "Frame" with arrows pointing to the axes, and a blue checkmark next to option d.



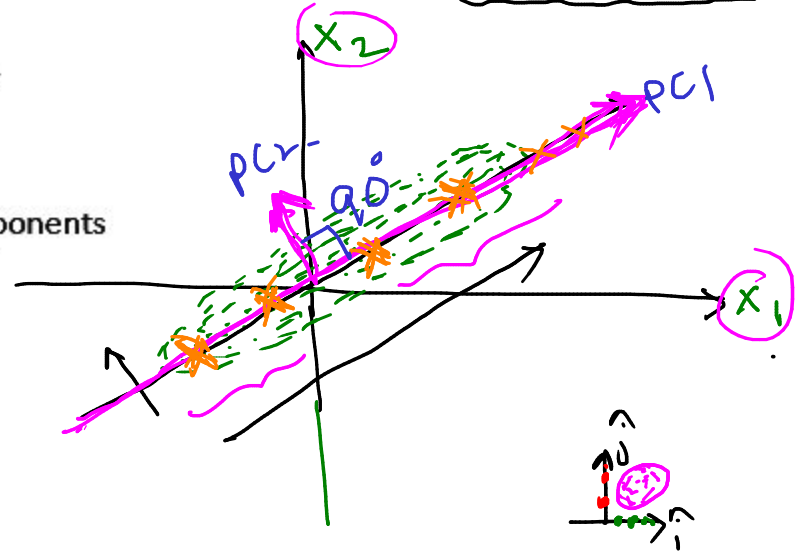
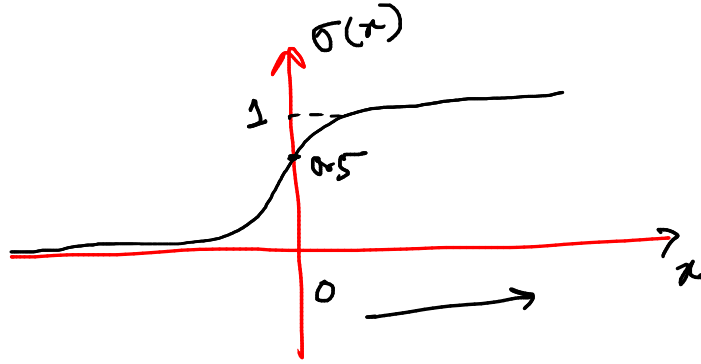
What is the output of sigmoid function for an input with dynamic range $[0, \infty]$?

- $[0, 1]$
- $[-1, 1]$
- $[0.5, 1]$
- $[0.25, 1]$



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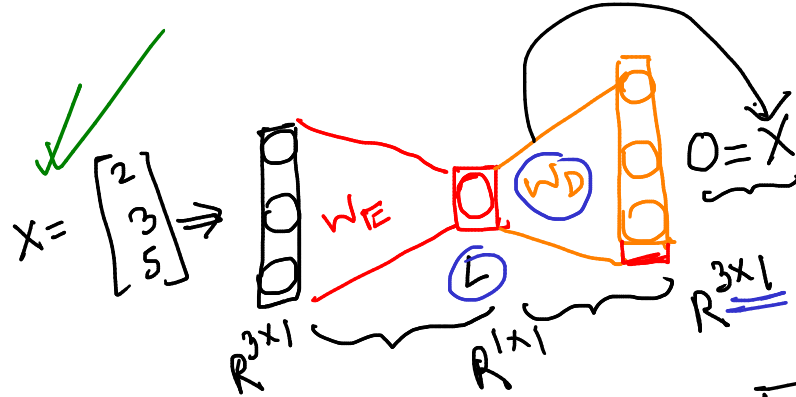


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- a. $[0, 1]$
- b. $[-1, 1]$
- c. $[0.5, 1]$
- d. $[0.25, 1]$

A zero-bias autoencoder has 3 input neurons, 1 hidden neuron and 3 output neurons. If the network is perfectly trained using an input $\begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}$. What would be the values of the weights in the autoencoder?

- a. $[1 \ 1 \ 1], \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}$
- ~~b. $[1 \ 1 \ 1], \begin{bmatrix} 0.2 \\ 0.3 \\ 0.5 \end{bmatrix}$~~
- c. $[0.2 \ 0.3 \ 0.5], \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$
- d. $[2 \ 3 \ 5], \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$



$$L = \frac{||0 - X||^2}{\text{MSE}(O, X)} = \frac{0}{\text{very low}} = 0$$

$$L (R^{1 \times 1}) = [W_E]_{1 \times 3} \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}_{3 \times 1}$$

$$L = W_E^T X$$

option (a), $L = [1 \ 1 \ 1] \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix} = 2 + 3 + 5 = 10$
 $O = \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix} \cdot 10 = \begin{bmatrix} 20 \\ 30 \\ 50 \end{bmatrix}$

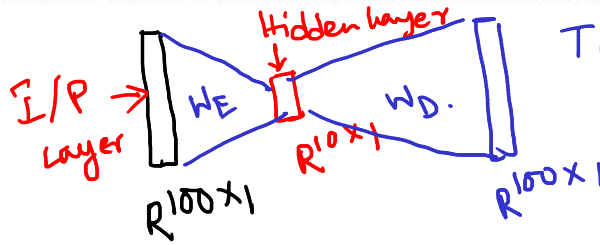
$$O = W_D \cdot L$$

$$(3 \times 1) \quad 3 \times 5 \quad 1 \times 1$$

⑥ $L = [1 \ 1 \ 1] \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix} = 10$
 $O = \begin{bmatrix} 0.2 \\ 0.3 \\ 0.5 \end{bmatrix} \times 10 = \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}$

A single hidden and no-bias autoencoder has 100 input neurons and 10 hidden neurons. What will be the number of parameters associated with this autoencoder?

- 1000
- 2000
- 2110
- 1010



Total Parameter
 $W_E: 100 \times 10 = 1000$

$W_D: 10 \times 100 = 1000$

2000

$y = \min(a, b)$ and $a > b$. What is the value of $\frac{dy}{da}$ and $\frac{dy}{db}$?

- 1, 0
- 0, 1
- 0, 0
- 1, 1

$y = \min(a, b); a > b$

$y = b$

$\frac{dy}{da} = 0$

$\frac{dy}{db} = 1$

$\Sigma \rightarrow$ Covariance
 \rightarrow Symmetric matrix.

\downarrow Eigen vector values.

Orthogonal to each other.

Let's say vectors $\vec{a} = \{2; 4\}$ and $\vec{b} = \{n; 1\}$ forms the first two principle components, after applying PCA. Under such circumstances, which among the following can be a possible value of n ?

- 2
- 2
- 0
- 1

PC are orthogonal to each other $\Rightarrow \vec{a} \cdot \vec{b} = 0$

$\Rightarrow 2n + 4 = 0$

$\Rightarrow n = -2$

$A = \begin{bmatrix} a_1 \\ a_2 \end{bmatrix} \quad \Sigma = \begin{bmatrix} a_1 a_1 & a_1 a_2 \\ a_2 a_1 & a_2 a_2 \end{bmatrix}$
 $2 \times 1 \quad \quad \quad 2 \times 2$
 $a_1 = \text{gender}$
 $a_2 = \text{profession}$

A single hidden and no-bias autoencoder has 100 input neurons and 10 hidden neurons. What will be the number of parameters associated with this autoencoder?

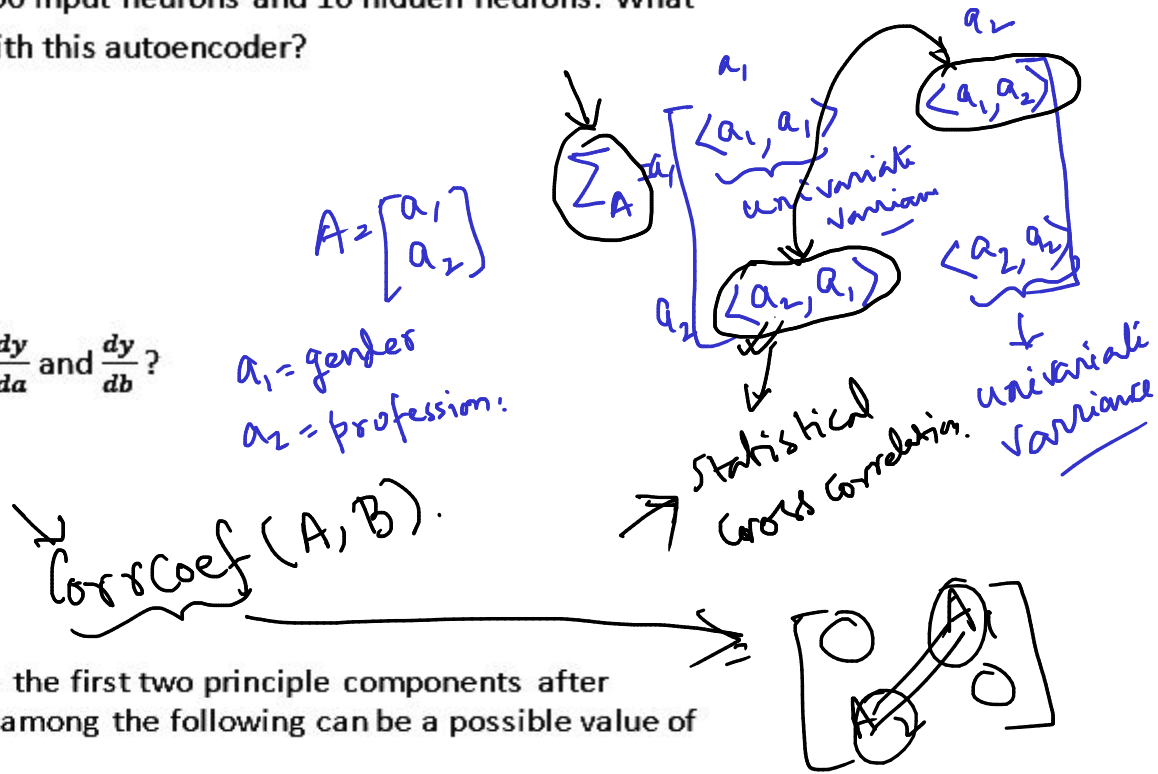
- a. 1000
- b. 2000
- c. 2110
- d. 1010

$y = \min(a, b)$ and $a > b$. What is the value of $\frac{dy}{da}$ and $\frac{dy}{db}$?

- a. 1, 0
- b. 0, 1
- c. 0, 0
- d. 1, 1

Let's say vectors $\vec{a} = \{2; 4\}$ and $\vec{b} = \{n; 1\}$ forms the first two principle components after applying PCA. Under such circumstances, which among the following can be a possible value of n ?

- a. 2
- b. -2
- c. 0
- d. 1



Consider the 2-layer neural network shown below. The weights are represented as follows:
 (w_{mn}^k) = weight between n^{th} node of k^{th} layer and m^{th} node $(k-1)^{\text{th}}$ layer. 0^{th} node is the bias node = 1 as depicted in the diagram.

$$A = \begin{bmatrix} a_1 \\ a_2 \end{bmatrix} \quad 2 \times 1$$

$$X = \begin{bmatrix} 1 \\ 1 \\ 0 \\ 1 \end{bmatrix} \quad 4 \times 1$$

e.g. w_{32}^1 = weight between 2^{nd} node of hidden layer and 3^{rd} node of input layer. Refer to the diagram. All weights have not been shown to maintain clarity.

Sigmoid activation function is applied to both the hidden layer and the output layer. The loss function is defined as $J(\cdot) = 0.5(y - t)^2$ where t is the true label.

The initial weights are given as:

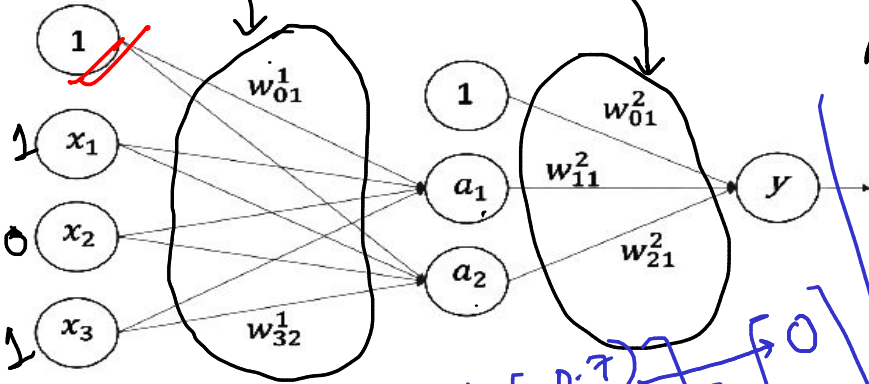
$$w^1 = \begin{bmatrix} -0.4 & 0.2 & 0.4 & -0.5 \\ 0.2 & -0.3 & 0.1 & 0.2 \end{bmatrix} \quad w^2 = \begin{bmatrix} 0.1 & -0.3 & -0.2 \end{bmatrix}$$

Find the output at node a_1 and a_2 for given input $\{x_1 = 1, x_2 = 0, x_3 = 1\}$?

$$A = \sigma(w^1 \cdot X) \quad (2 \times 4) \quad (4 \times 1)$$

$$A = \sigma \left(\begin{bmatrix} -0.4 & 0.2 & 0.4 & -0.5 \\ 0.2 & -0.3 & 0.1 & 0.2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 0 \\ 1 \end{bmatrix} \right)$$

$$= \sigma \left(\begin{bmatrix} -0.7 \\ 0.1 \end{bmatrix} \right) = \begin{bmatrix} \sigma(-0.7) \\ \sigma(0.1) \end{bmatrix} = \begin{bmatrix} 0.33 \\ 0.52 \end{bmatrix}$$



- a. 0.13, 0.54
- ~~b. 0.33, 0.52~~
- c. 0.23, 0.51
- d. 0.13, 0.51

$$\begin{bmatrix} \text{Relu}(-0.7) \\ \text{Relu}(0.1) \end{bmatrix} = \begin{bmatrix} 0 \\ 0.1 \end{bmatrix}$$

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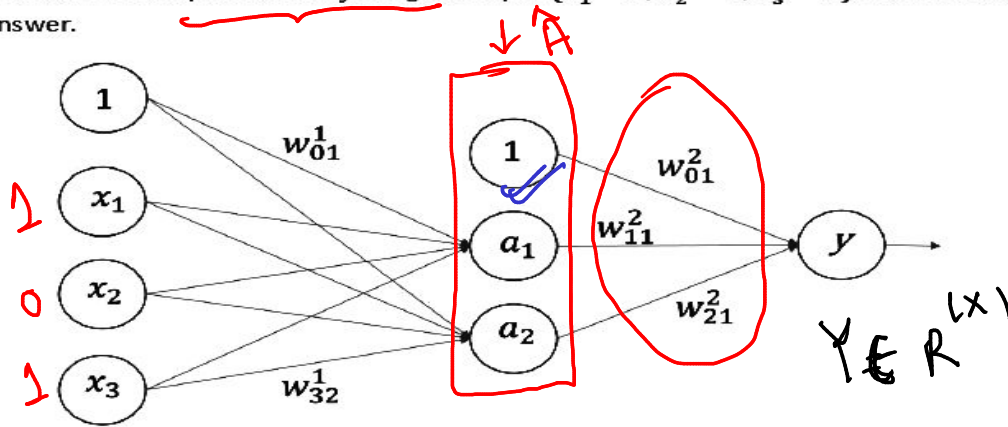
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Find the final output at node y for given input $\{x_1 = 1, x_2 = 0, x_3 = 1\}$? Choose the closest answer.



- a. 0.13
- b. 0.33
- ☒ c. 0.48
- d. 0.51

$$\hat{A} = \begin{bmatrix} 1 \\ 0.33 \\ 0.52 \end{bmatrix}_{3 \times 1} \quad W^2 = \begin{bmatrix} 0.1 & -0.3 & -0.2 \end{bmatrix}_{1 \times 3}$$

$$Y = \sigma(W^2 \cdot \hat{A})$$

$$= \sigma \left(\begin{bmatrix} 0.1 & -0.3 & -0.2 \end{bmatrix} \begin{bmatrix} 1 \\ 0.33 \\ 0.52 \end{bmatrix} \right)$$

$$= \sigma(-0.103) = \underline{\underline{0.48}}$$

Consider the 2-layer neural network shown below. The weights are represented as follows: w_{mn}^k = weight between n^{th} node of k^{th} layer and m^{th} node $(k-1)^{\text{th}}$ layer. 0^{th} node is the bias node = 1 as depicted in the diagram.

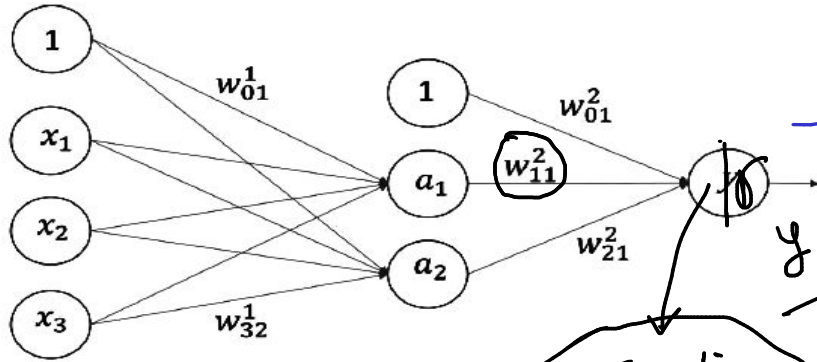
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Find the gradient component $\frac{\partial J}{\partial w_{11}^2}$ for $t = 1$ and given input $\{x_1 = 1, x_2 = 0, x_3 = 1\}$. Choose the closest answer.



- 0.09
- 0.11
- 0.13
- 0.04

$$\frac{\partial J}{\partial w_{11}^2} \quad f(x) = x^2 + u^2$$

$$J(y) = \frac{1}{2} (y - t)^2$$

$$y = \sigma(p)$$

$$p = w_{01}^2 + w_{11}^2 \cdot a_1 + w_{21}^2 \cdot a_2$$

$$\frac{\partial y}{\partial p} = \text{derivative of sigmoid function} = \sigma(p) \cdot (1 - \sigma(p)) = y \cdot (1 - y)$$

$$\frac{\partial J}{\partial w_{11}^2} = \frac{\partial J}{\partial y} \cdot \frac{\partial y}{\partial p} \cdot \frac{\partial p}{\partial w_{11}^2}$$

$$\begin{aligned} \frac{\partial J}{\partial w_{11}^2} &= (y - t) \cdot y \cdot (1 - y) \cdot a_1 \\ &= (0.48 - 1) \cdot 0.48 \cdot (1 - 0.48) \cdot 0.33 \\ &= -0.04 \end{aligned}$$

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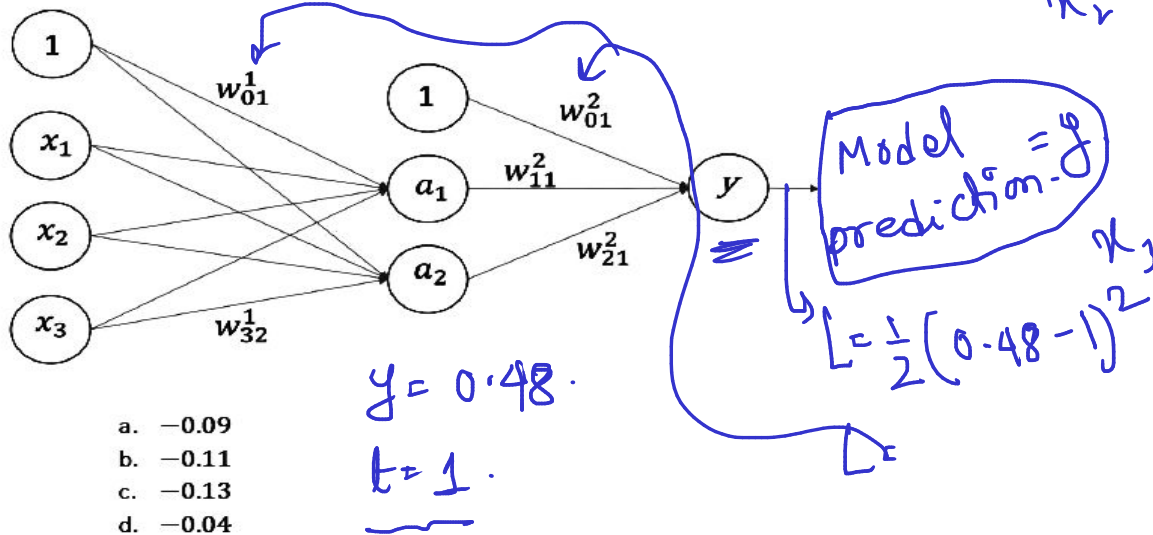
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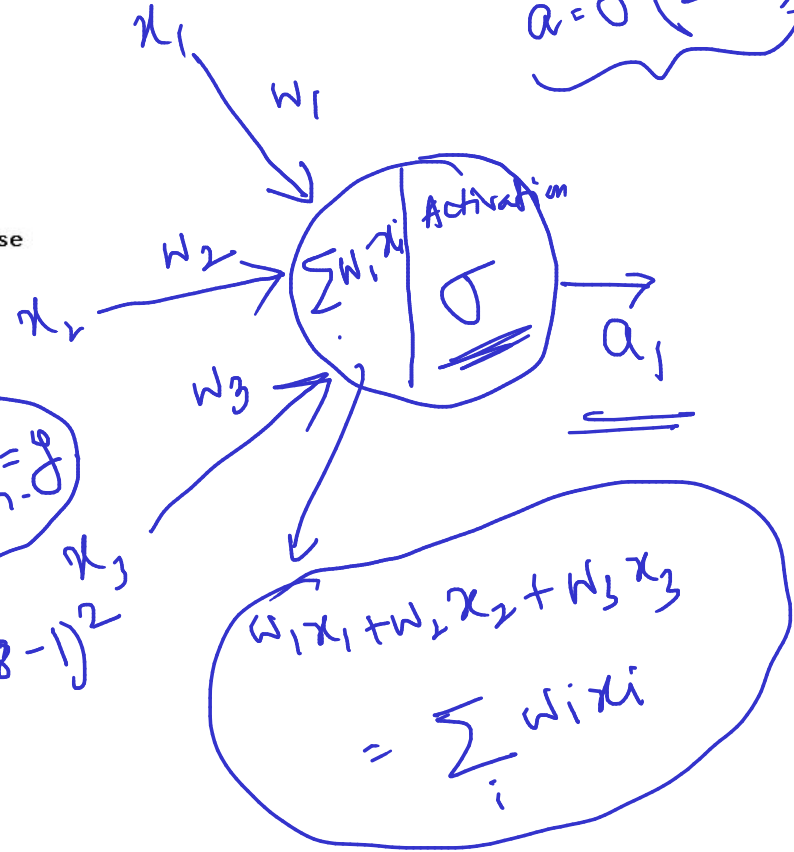
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- a. -0.09
- b. -0.11
- c. -0.13
- d. -0.04

$$f = \max(0, x)$$

$$a = \sigma(\sum w_i x_i)$$



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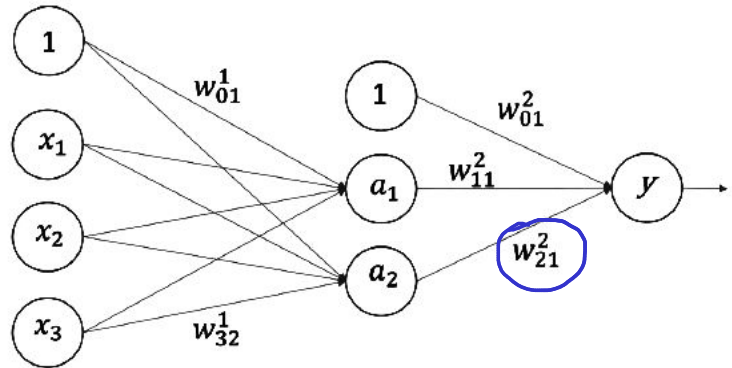
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Find the updated value of w_{21}^2 after 1 iteration for $t = 1$, the learning rate $\eta = 0.9$ and given input $\{x_1 = 1, x_2 = 0, x_3 = 1\}$? Choose the closest answer.



- a. -0.29
- b. -0.1
- ☒ c. -0.14
- d. -0.04

w_{21}^2 after 1st iteration \Rightarrow

$w_{21}^{2(1)} \leftarrow w_{21}^{2(0)} - \eta \cdot \frac{\partial J}{\partial w_{21}^2}$
 1st iteration

$$\frac{\partial J}{\partial w_{21}^2} = \frac{\partial J}{\partial y} \cdot \frac{\partial y}{\partial p} \cdot \frac{\partial p}{\partial w_{21}^2}$$

$$= (y - t) \cdot \gamma(1 - \gamma) \cdot a_2$$

$$\frac{\partial J}{\partial w_{21}^2} = -0.067$$

$w_{21}^{2(1)} \leftarrow (-0.2) - [0.9 \times -0.067]$

$= -0.139$

≈ -0.14

Select the correct option.

Initializers \rightarrow He, Glorot, Uniform.

$$W(n) \leftarrow W(n-1) - \eta \frac{dE}{dW}$$

$$\frac{n=1}{N(1)} \leftarrow \frac{10/1m}{W(0)} - \eta \frac{dE}{dW}$$

Randomly.



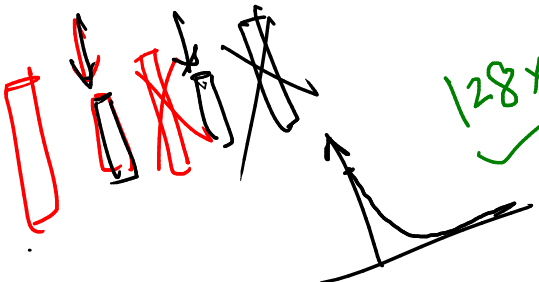
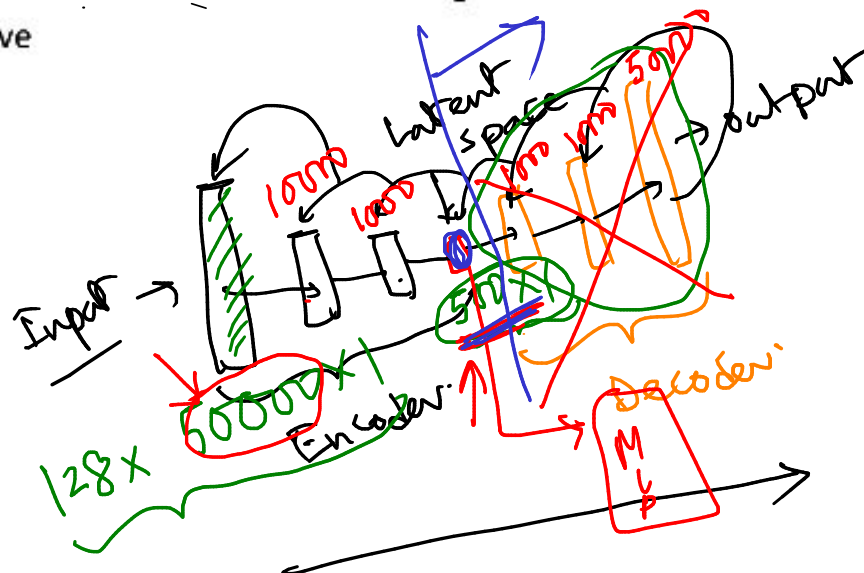
2% - 3%

If requires high RAM
 \uparrow GPU mem

Training of SAE from scratch then
 too many parameter
 has to be optimized

- a. Layer-by-layer autoencoder pretraining reduces GPU/CPU RAM requirements
- b. Layer-by-layer autoencoder pretraining alleviates slow convergence
- c. Layer-by-layer autoencoder pretraining followed by finetuning converges to more optimal parameters than End-to-End training of autoencoders
- d. All of the above

Stacked AE



Regularization of Contractive Autoencoder is imposed on

- a. Jacobian matrix of encoder activations with respect to the input
- b. Weights
- c. Inputs
- d. Does not use regularization

$$\left(\begin{array}{c} \downarrow \\ \frac{\partial A(x)}{\partial x_1} \end{array} \quad \frac{\partial A(x)}{\partial x_2} \quad \dots \right)$$

Select true statements about KL Divergence

a. Measures ~~distance~~ between two probability distribution

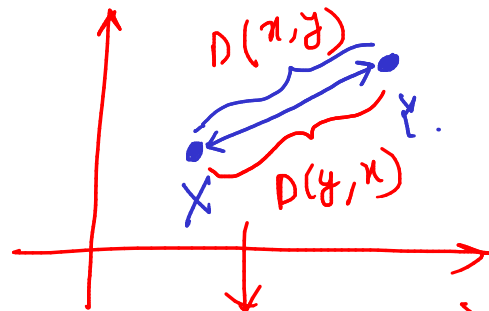
b. Has range from 0 to 1

c. Is symmetric, i.e. $KL(P|Q) = KL(Q|P)$

d. None of above

(incorrect)

(incorrect)



Distance is symmetric in nature

$$KL \text{ divergen } (P|Q) = P \log \frac{P}{Q} = P \log P - P \log Q$$

$$KL \text{ div } (Q|P) = Q \log \frac{Q}{P} = Q \log Q - Q \log P$$

$$KL(P|Q) \neq KL(Q|P)$$

$$P, Q = 0$$

$$P \cdot \log \frac{P}{0}$$

$$P \log(\infty)$$

$$P \times \infty = \infty$$

$$P=0, \left(P \log \frac{P}{Q} \right) = 0 \cdot \left(\log \frac{0}{Q} \right)$$

$$P=0, Q=0$$

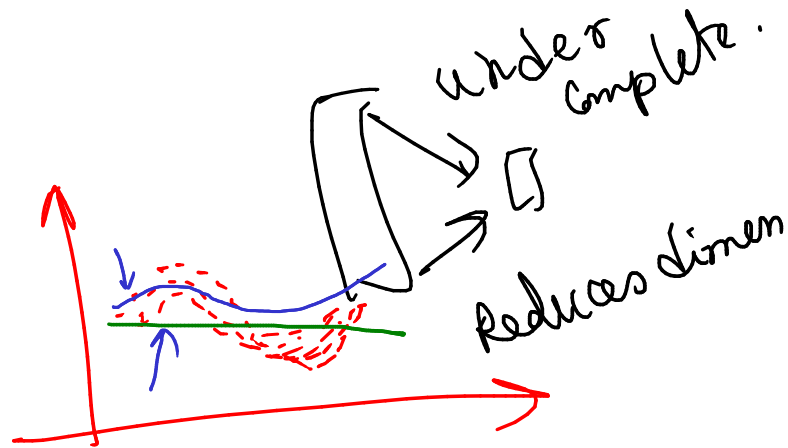
$$0 \cdot \log \left(\frac{0}{0} \right)$$

Range $0 \rightarrow \infty$

In which conditions, autoencoder has more powerful generalization than Principal Components Analysis (PCA) while performing dimensionality reduction?

- a. Undercomplete Linear Autoencoder
- ~~b. Overcomplete Linear Autoencoder~~
- ~~c. Undercomplete~~ Non-linear Autoencoder
- ~~d. Overcomplete Non-Linear Autoencoder~~

→ linear
→ transform.



overcomplete

either same dimension or increased dimension to that of input size

An autoencoder consists of 128 input neurons, 32 hidden neurons. If the network weights are represented using single precision floating point numbers (size= 4 bytes) then what will be size of weight matrix?

- a. 33408 Bytes
- b. 16704 Bytes
- c. 8352 Bytes
- d. 32768 Bytes

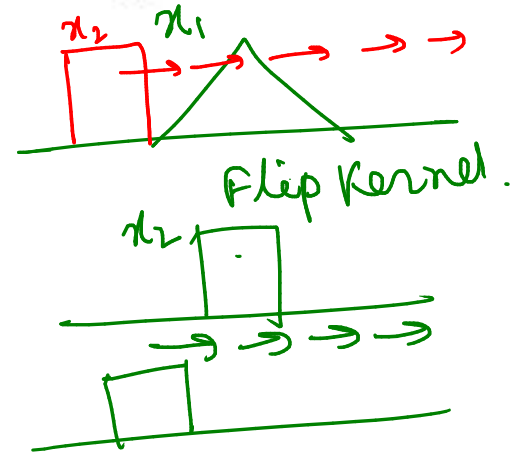
Which of the following is used to match template pattern in a signal

a. Cross Correlation

b. Convolution

c. Normalized cross correlation

d. None of the above



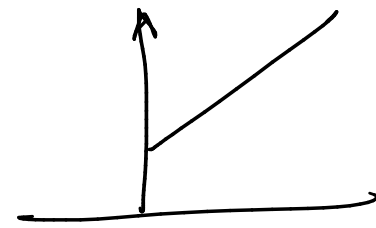
Lecture 35
at 28:49

Which of the following is an LTI/LSI system? y and x are output and input respectively.

Non linear

- a. $y = m \times x + n \times x$
- b. $y = m \times x + c$
- c. $y = m \times x - c$
- d. $y = m \times x^2$

Super position theorem



(a) $y = (m+n)x$. Super position theorem obeys

$x_1 \rightarrow y_1 = (m+n)x_1 = mx_1 + nx_1$

$x_2 \rightarrow y_2 = (m+n)x_2 = mx_2 + nx_2$

Now, $y_F = (m+n)(x_1 + x_2)$

$= mx_1 + mx_2 + nx_1 + nx_2$

$= mx_1 + nx_1 + mx_2 + nx_2$

$y_F = y_1 + y_2$

(b) $y = mx + c$

x_1, x_2

$y_1 = mx_1 + c$

$y_2 = mx_2 + c$

$y_1 + y_2 = mx_1 + mx_2 + 2c$

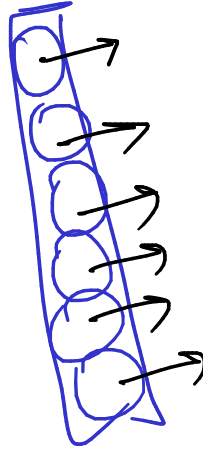
you apply $(x_1 + x_2)$

$y_3 = m(x_1 + x_2) + c$

$y_3 \neq y_1 + y_2 \rightarrow$ Super position theorem is not valid

What is the role of sparsity constraint in a sparse autoencoder?

- ☒ a. Control the number of active nodes in a hidden layer
- ☒ b. Control the noise level in a hidden layer
- ☒ c. Control the hidden layer length
- ☒ d. Not related to sparse autoencoder

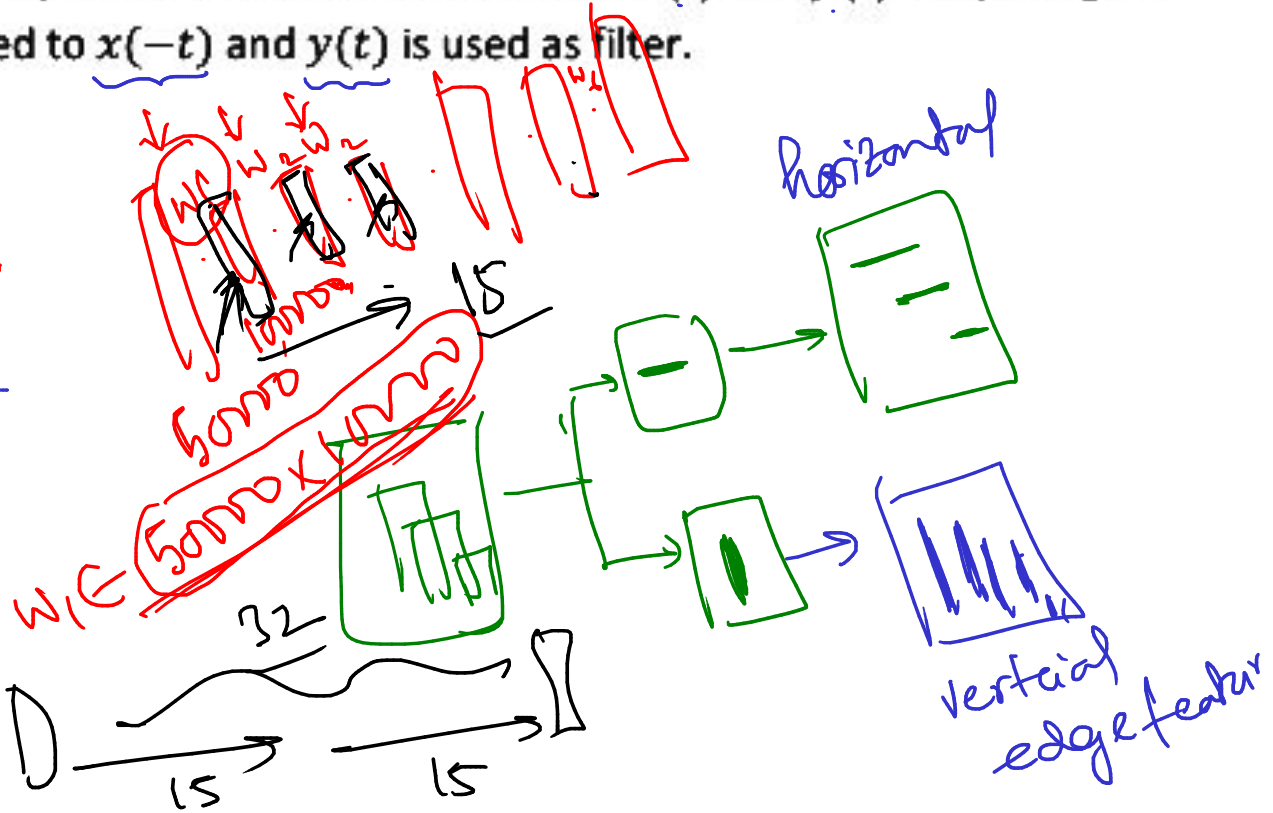
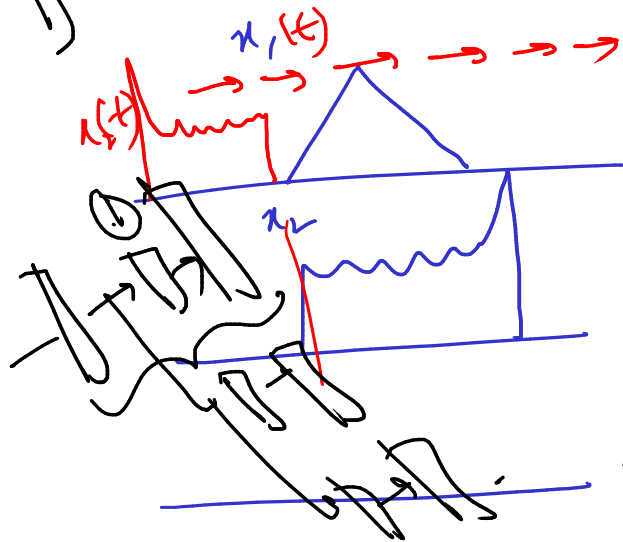


Aim to
control the
activation of
the neurons
in the hidden
layer

Which of the following is true about convolution?

- ☒ a. Convolution is used to compute features from signal
- ☐ b. Can be used to compute cross correlation between $x(t)$ and $y(t)$ if input signal $x(t)$ is transformed to $x(-t)$ and $y(t)$ is used as filter.
- ☐ c. Both a and b
- ☐ d. None of above

shallow network



Thank you