Assignment 4

Rory Sarten 301005654

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Question 1

a)

```
food_prices <- readr::read_delim("food_prices_kg2019.csv", delim = ",", col_types = readr::cols())
theta_est <- IQR(food_prices$Data_value) %>% round(3)
theta_est
```

```
## [1] 6.675
```

b)

```
set.seed(1)
N <- 1e4
boot_IQR <- 1:N %>%
  lapply(function(i) sample(food_prices$Data_value, replace = TRUE)) %>%
  sapply(IQR) %>%
  round(3)

## standard error of estimator
sd(boot_IQR) %>% round(3)
```

```
## [1] 1.2
```

```
## standard 95% bootstrap confidence interval
(theta_est + 1.96*c(-1, 1)*sd(boot_IQR)) %>% round(3)
```

```
## [1] 4.322 9.028
```

c)

```
## Efron's interval
quantile(boot_IQR, probs = c(0.025, 0.975)) %>% round(3)
```

```
##    2.5%  97.5%
##   5.315 10.130
```

d)

```
## Hall's interval
hall <- (2 * theta_est - quantile(boot_IQR, probs = c(0.975, 0.025))) %>% round(3)
names(hall) <- c("2.5%", "97.5%")
hall
```

```
##  2.5% 97.5%
## 3.220 8.035
```

e)

```
## bias
bias <- (mean(boot_IQR) - theta_est) %>% round(3)
bias
```

```
## [1] 0.53
```

```
## size of bias in relation to the std error
bias_size <- (bias/sd(boot_IQR)) %>% round(3)
bias_size
```

```
## [1] 0.442
```

The bias is approximately 44% of the $s.e.(\hat{\theta})$. The size of this bias is considerable.

f)

```
## bias corrected Efron interval
(quantile(boot_IQR, probs = c(0.025, 0.975)) - bias) %>% round(3)
```

```
##  2.5% 97.5%
## 4.785 9.600
```

The lower bound of the confidence interval is above $4. We reject the hypothesis that the test IQR could be below 4NZD at the 5% confidenc interval.