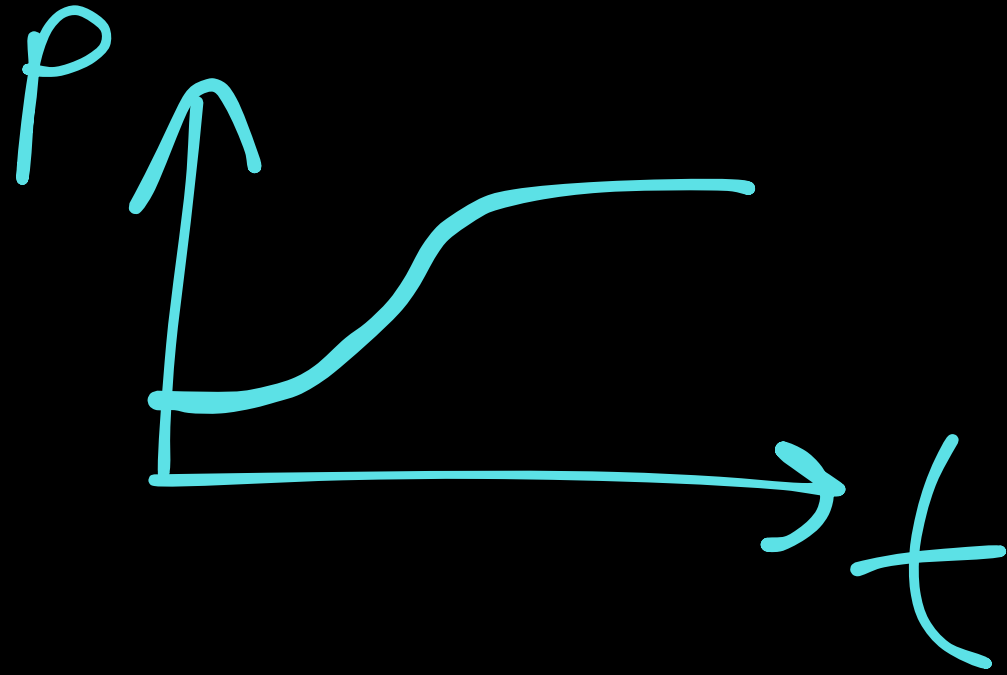


# Adaptive Dynamics

Raphaël Scherrer



**population  
genetics**



**quantitative  
genetics**

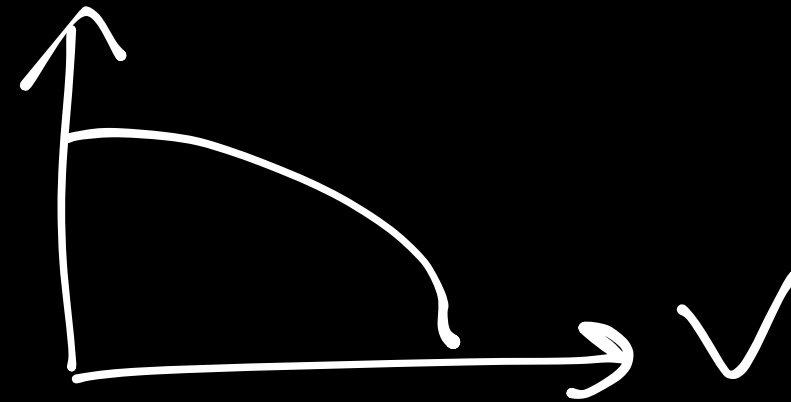
**adaptive  
dynamics**



**vigilance**

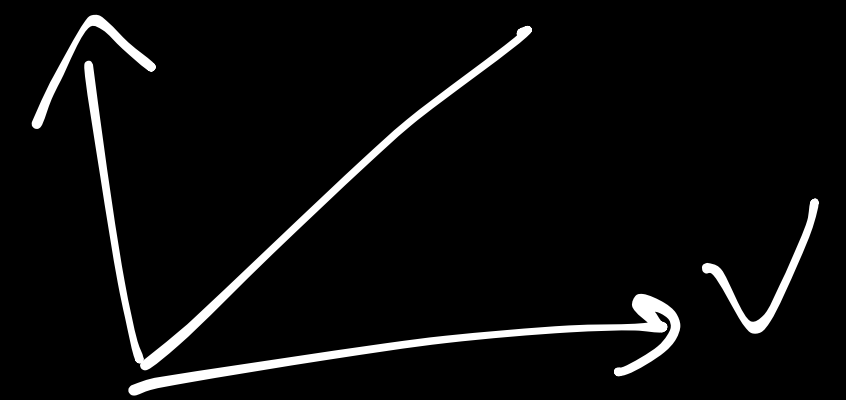
foraging

$$F(v) = 1 - v^2$$



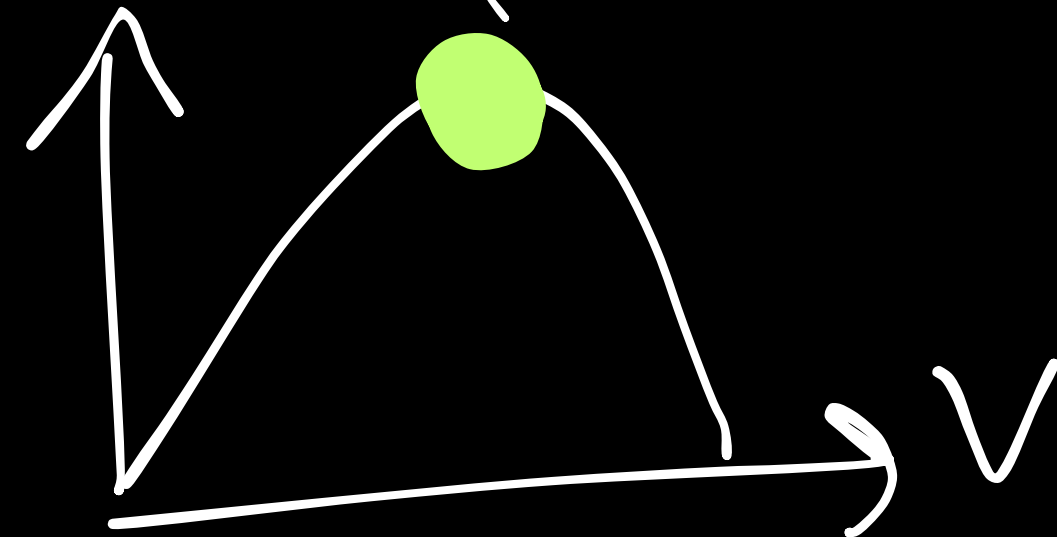
survival

$$S(v) = v$$



fitness

$$W(v)$$



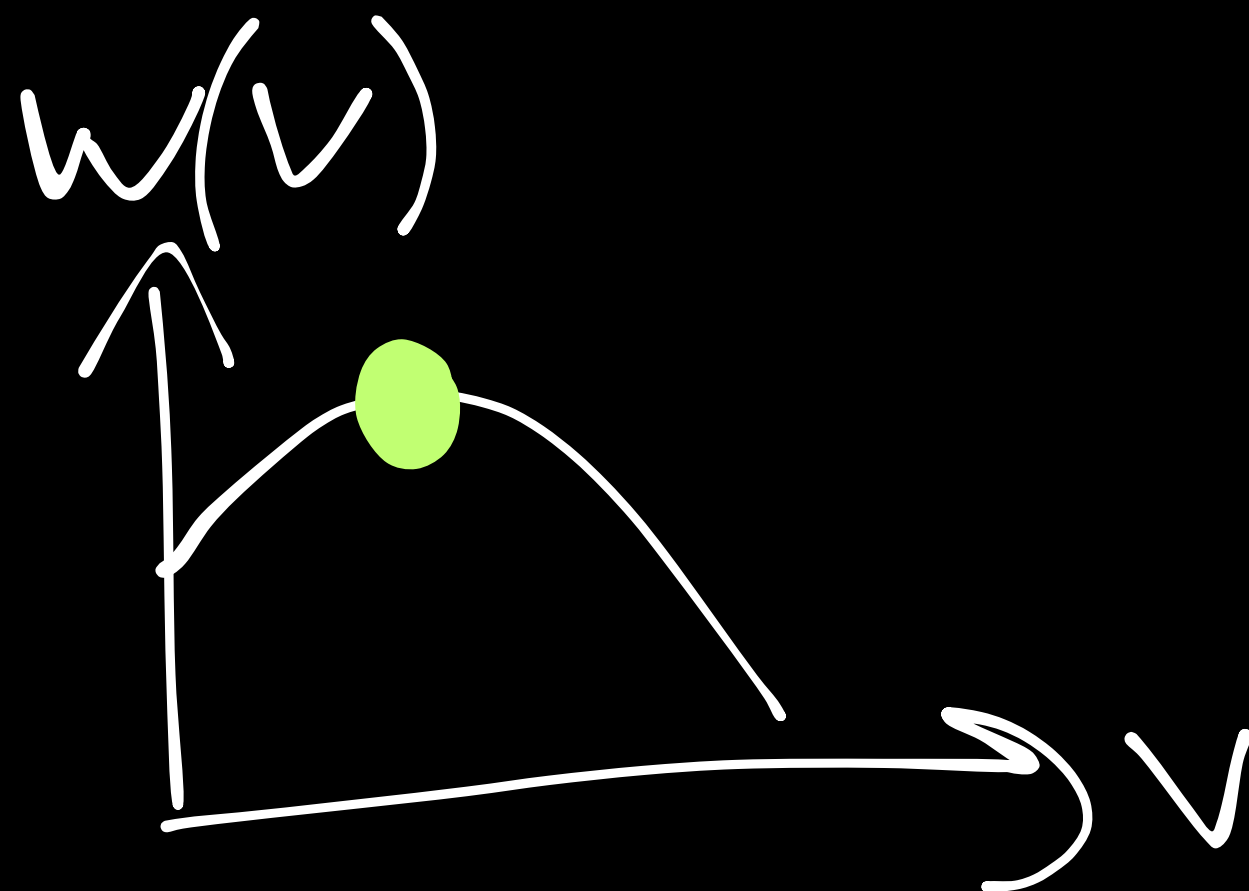
$$v^* = 0.5$$



$$S(v) = 1 - \frac{1}{n} (1-v)^n$$

probability of being  
the one caught

probability that  
no-one is watching



$$v^* = 0.33$$

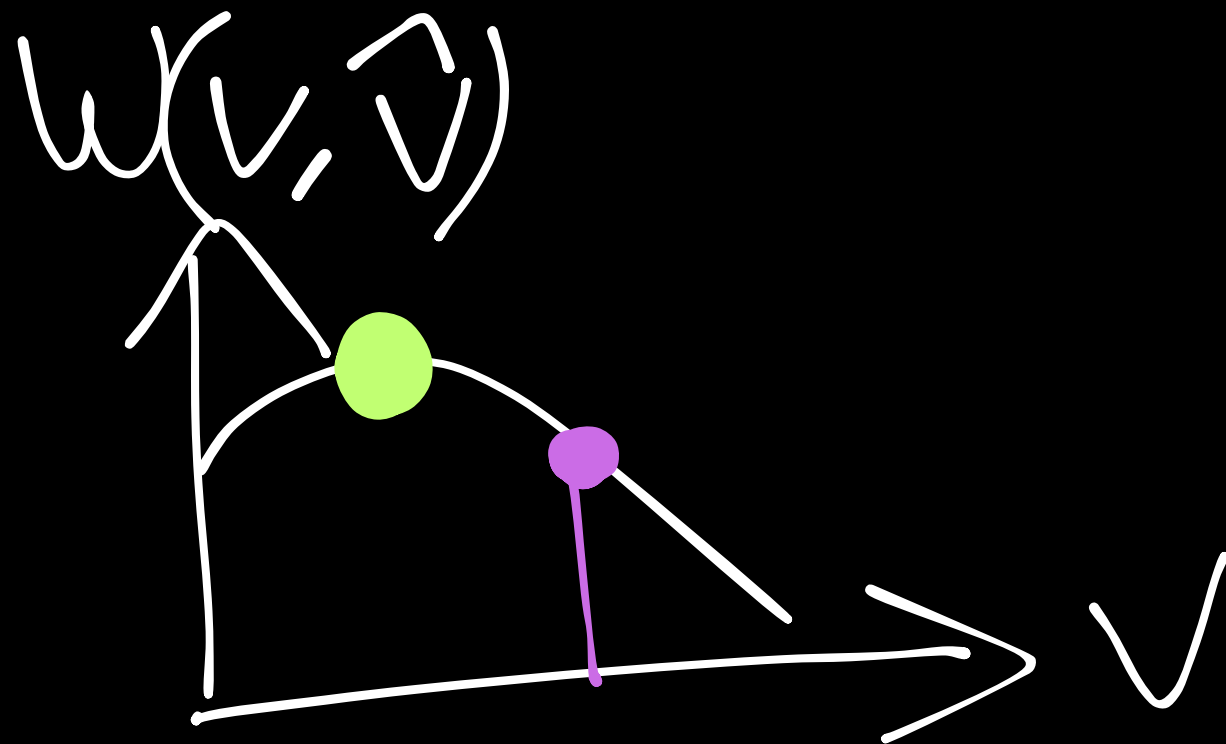


# frequency-dependent selection

$$S(v, \hat{v}) = 1 - \frac{1}{n} (1-v) (1-\hat{v})^{n-1}$$

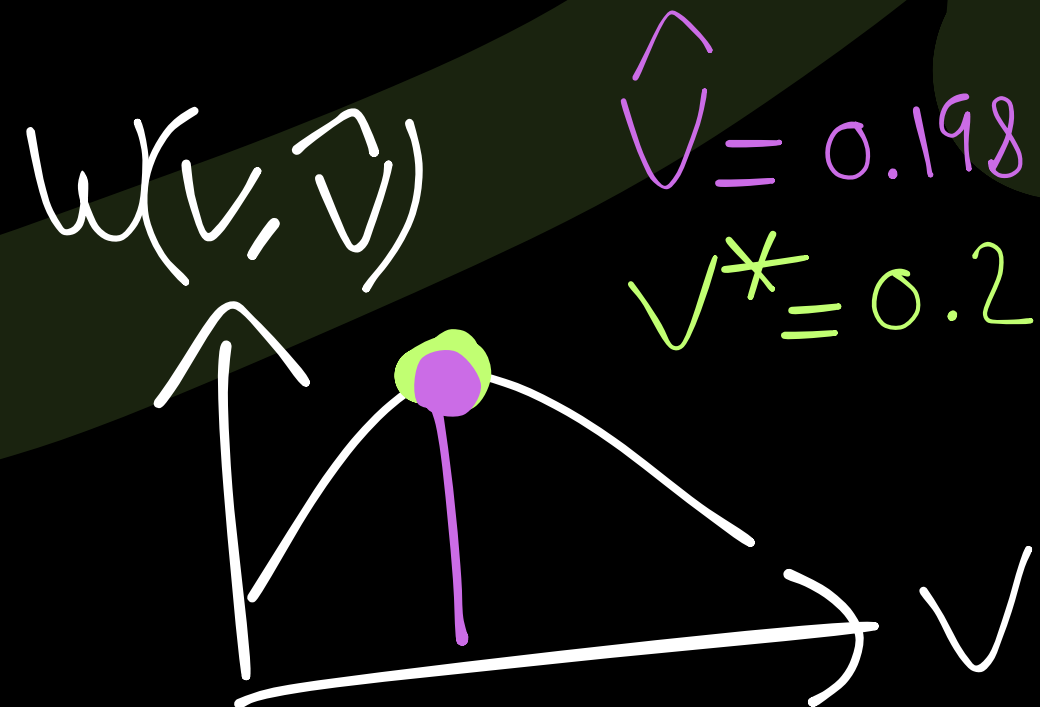
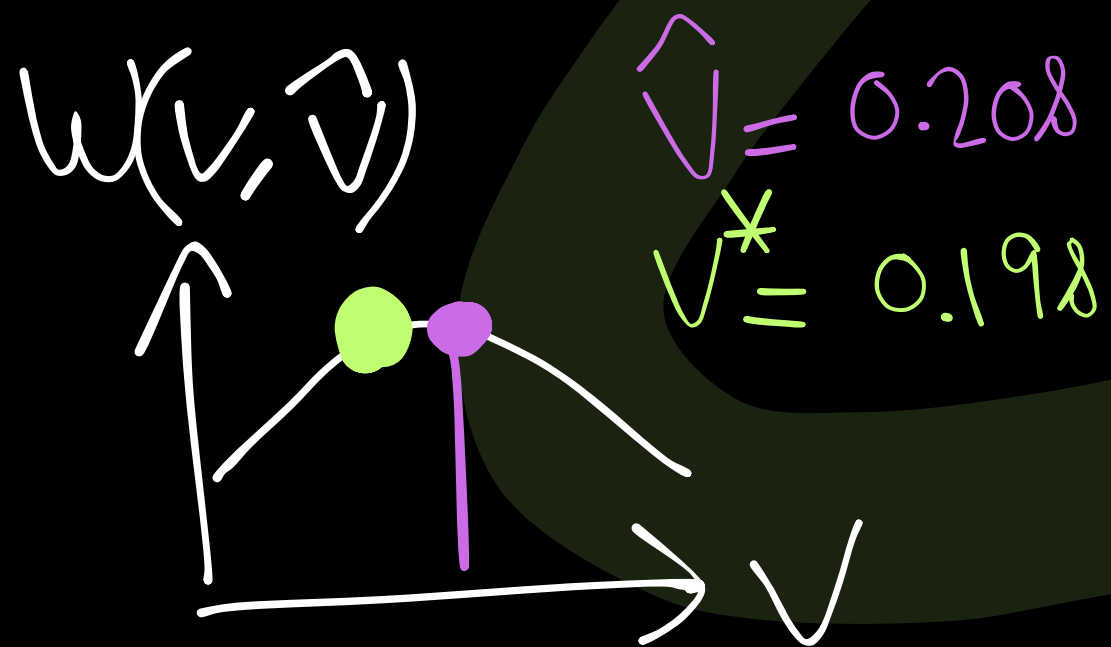
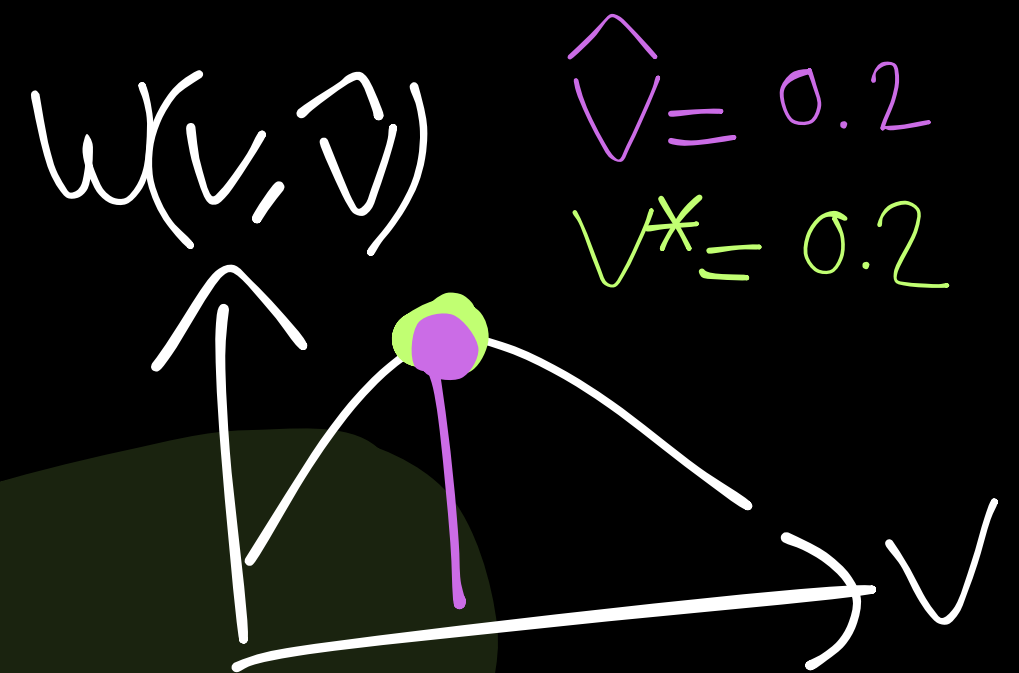
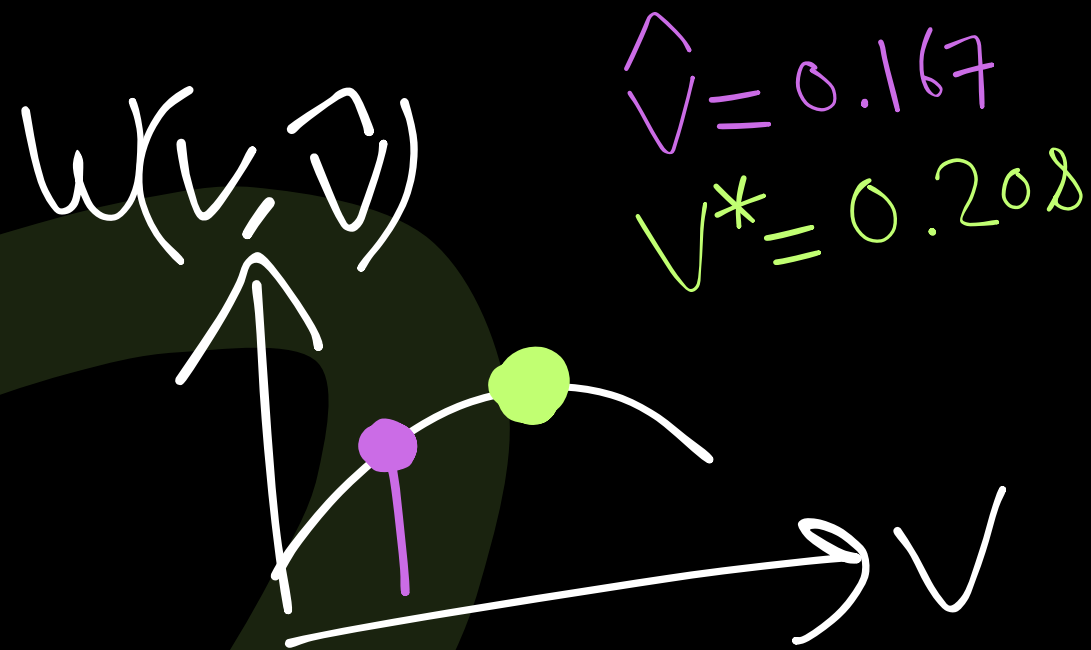
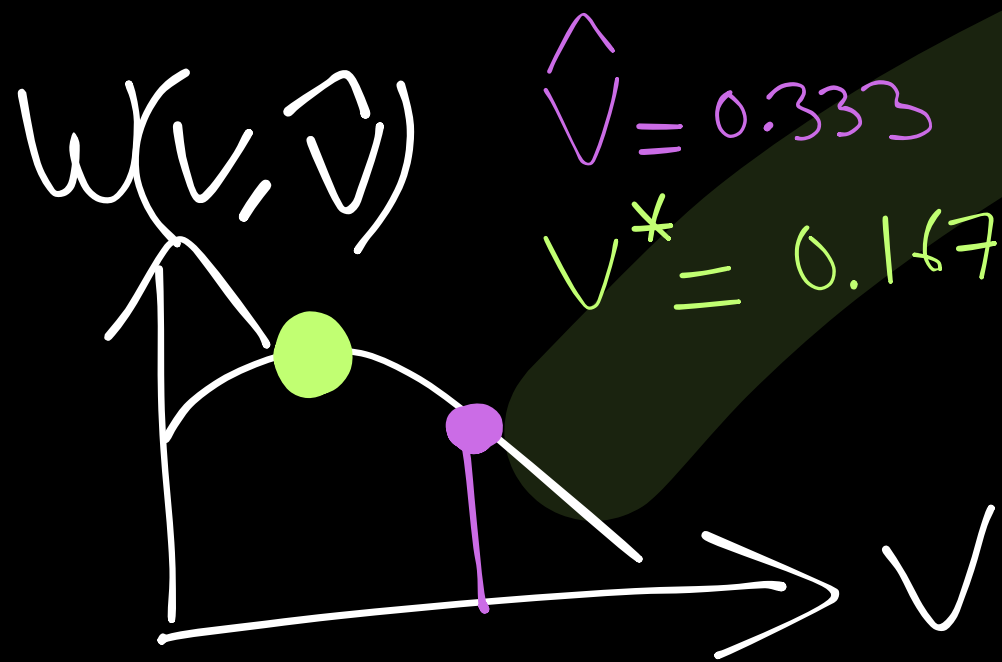
probability that the focal individual is not watching

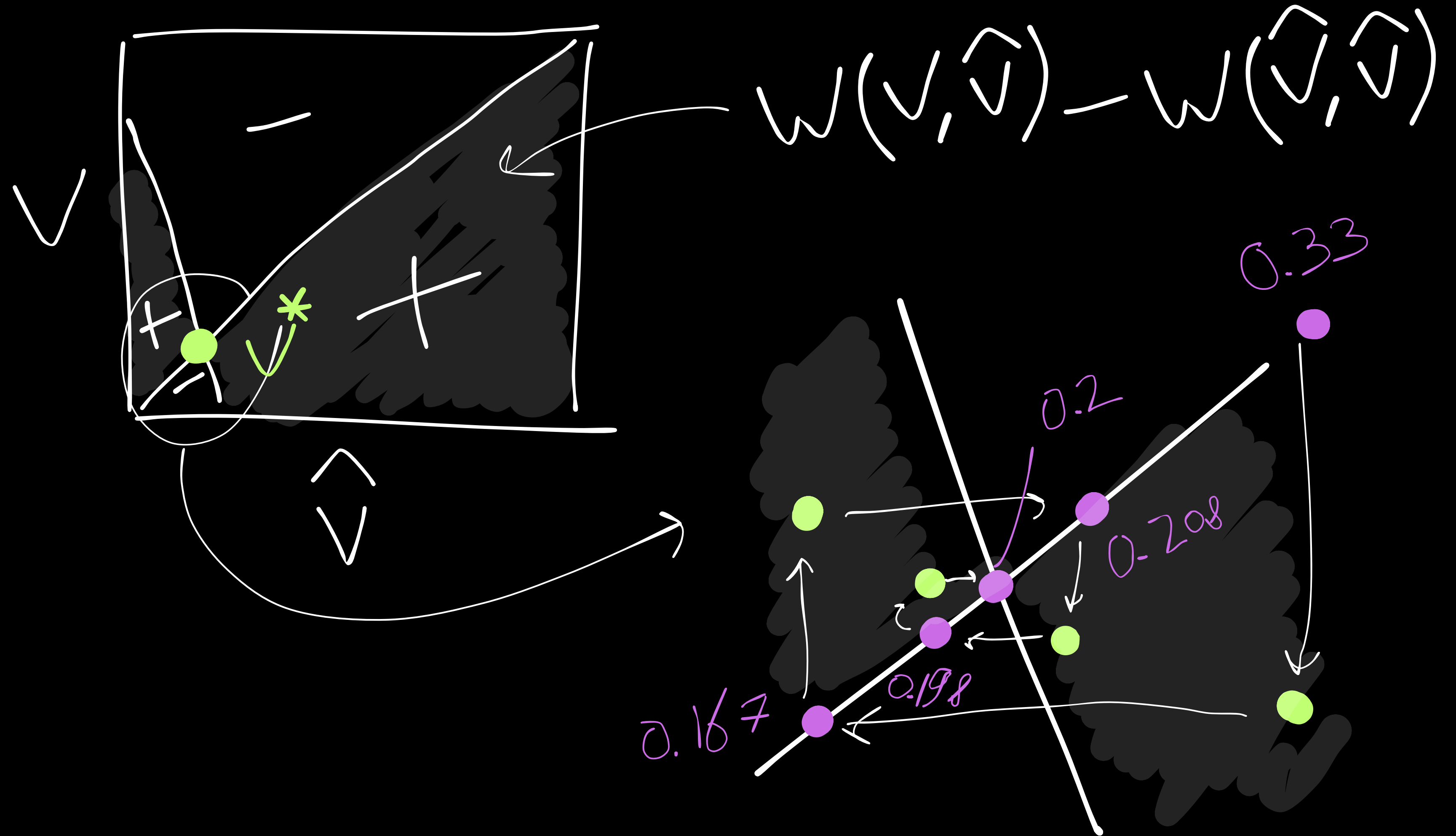
probability that none of the others is watching

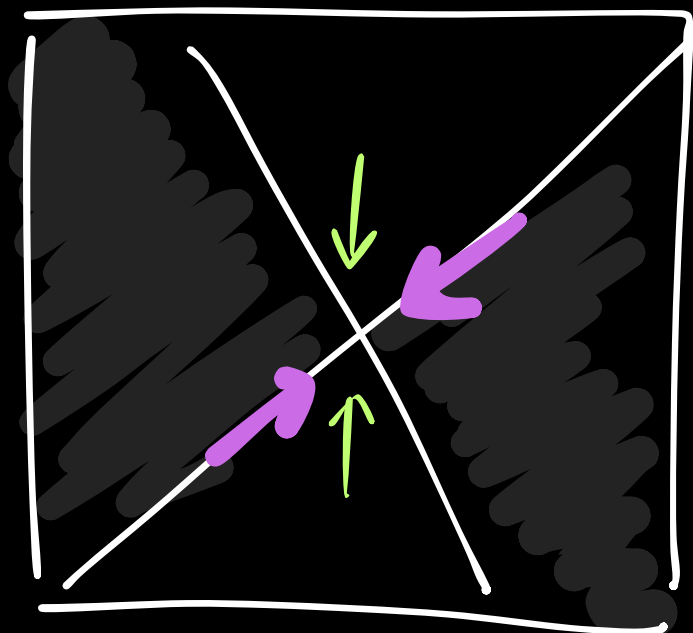


$$\hat{v} = 0.333$$

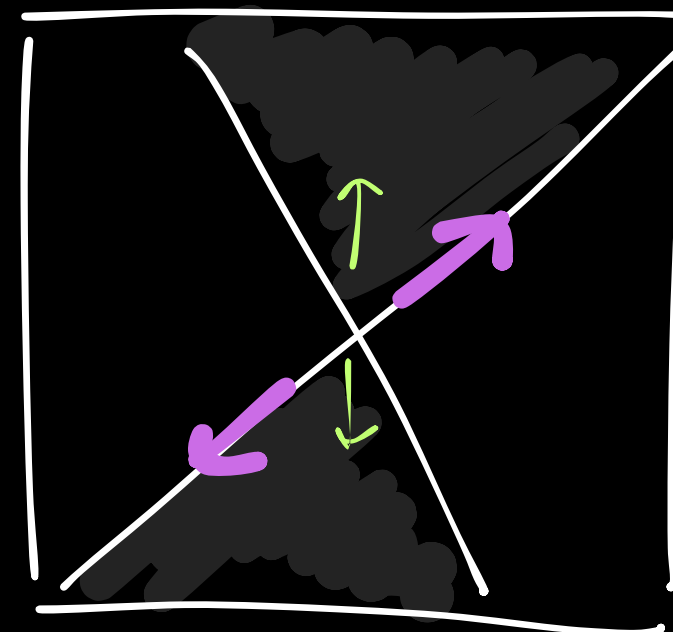
$$v^* = 0.167$$



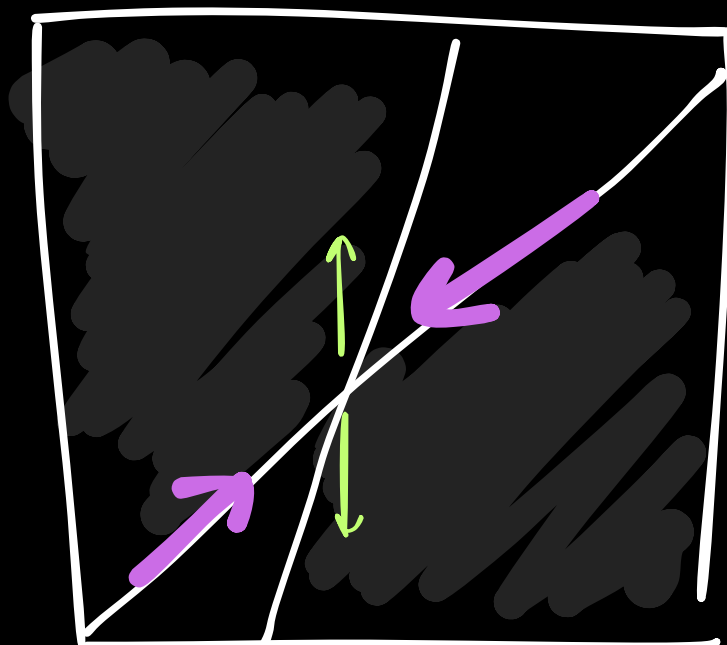




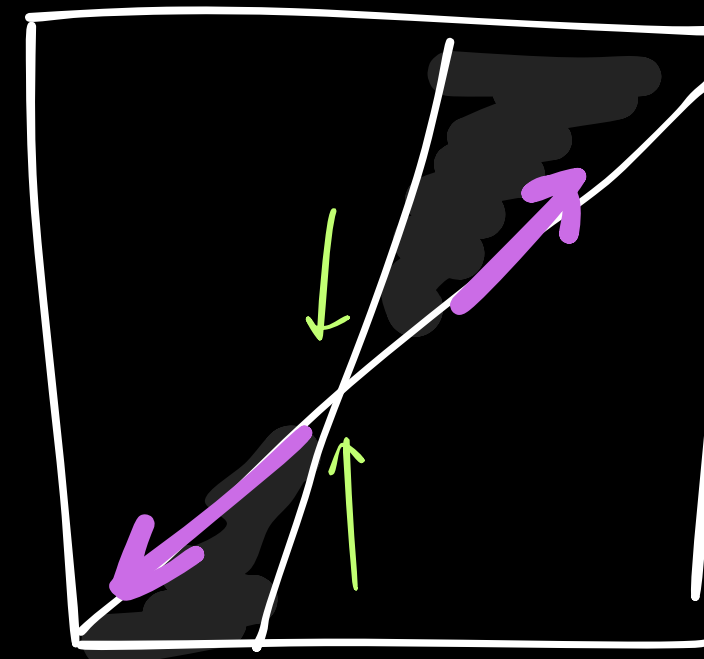
Evolutionarily  
Stable Strategy



Repeller



Branching point



Garden of Eden

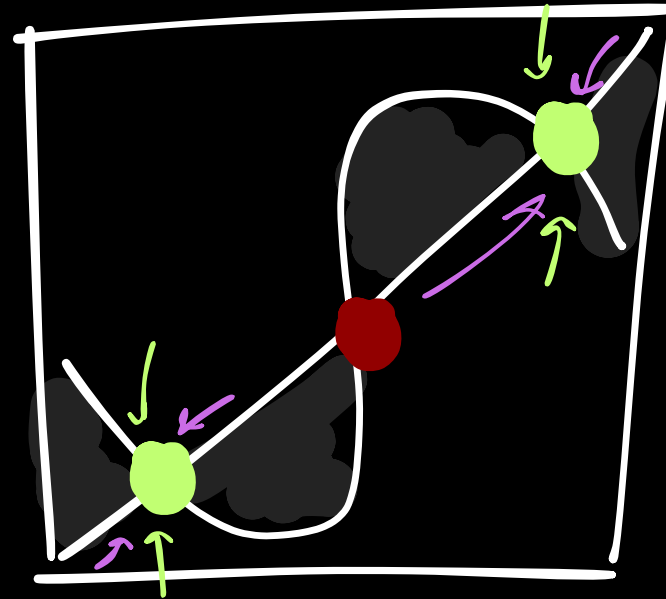
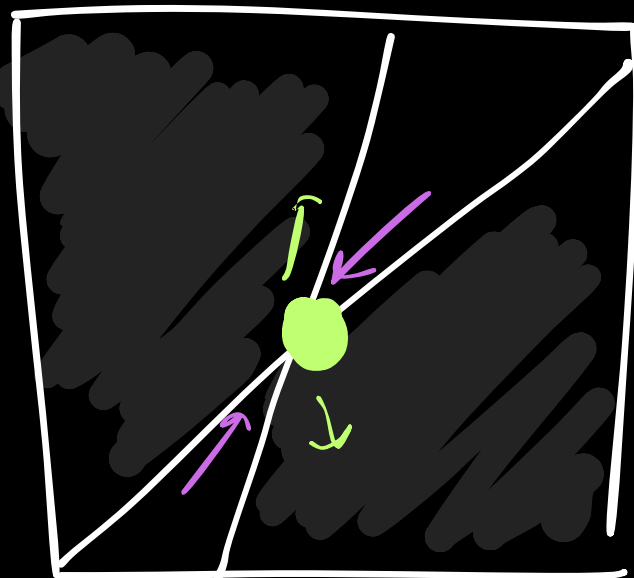
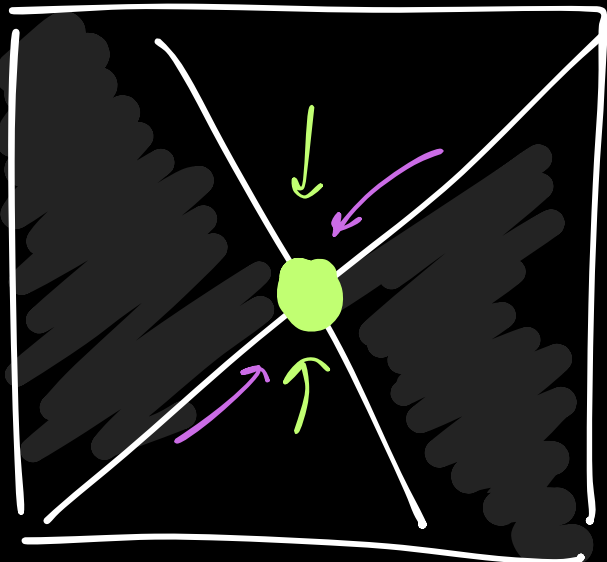
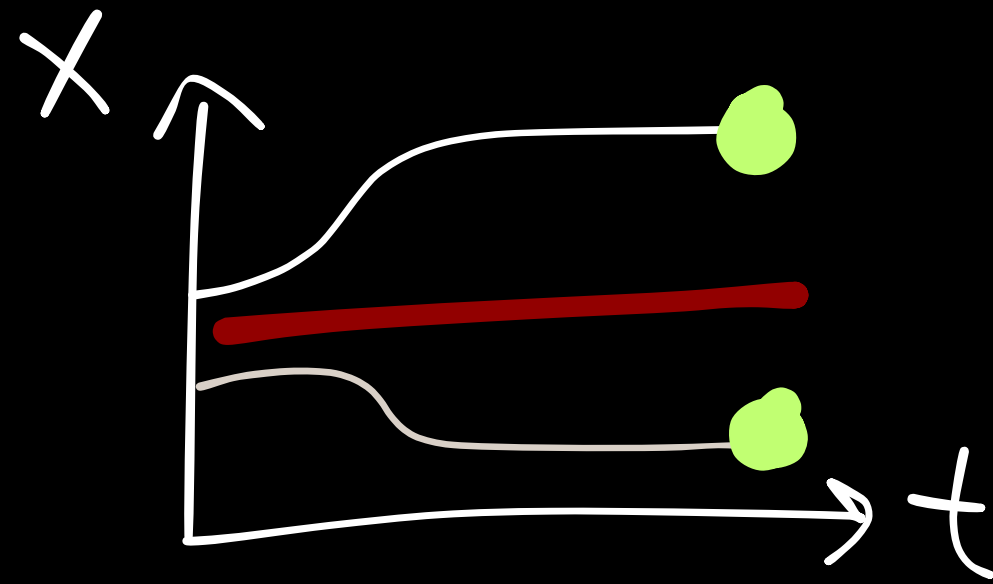
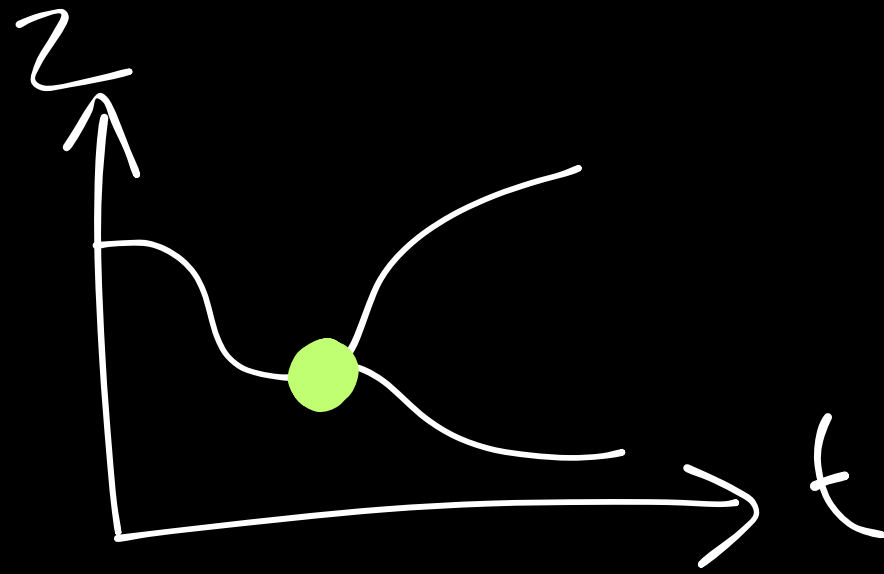
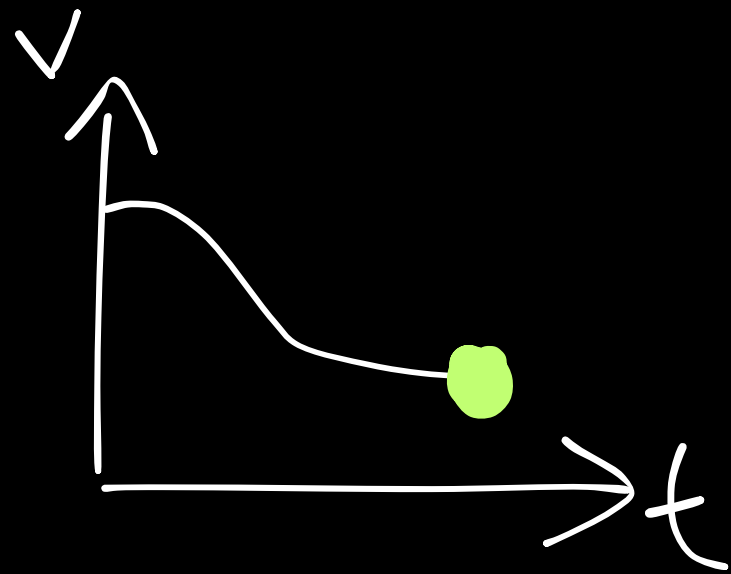


convergence stability



evolutionary stability



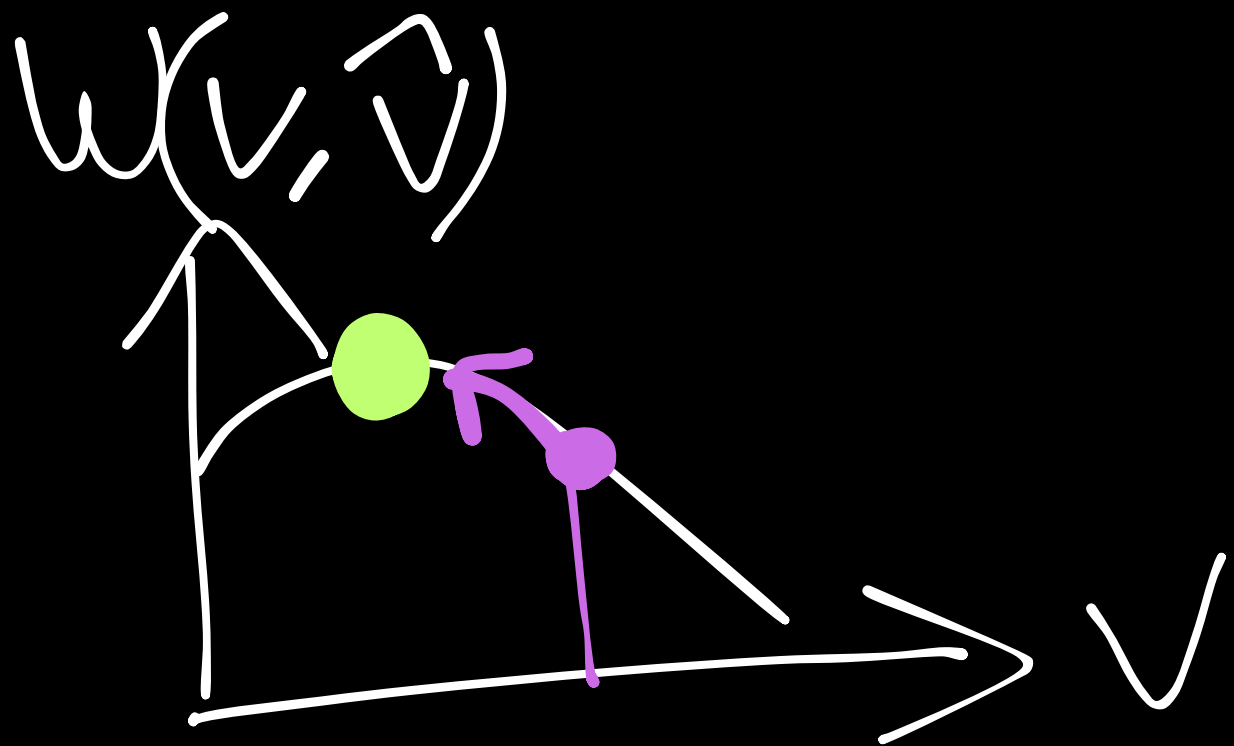




# game theory

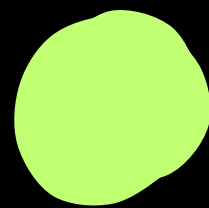
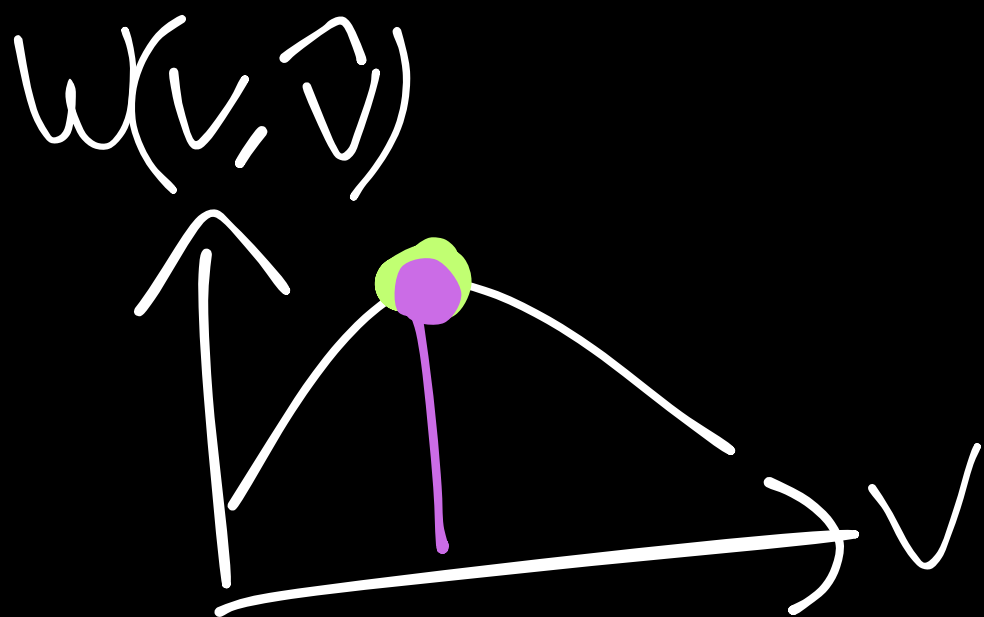


Prisoners' dilemma



$$\frac{\partial w}{\partial v} \Big|_{v=\hat{v}} = G(\hat{v})$$

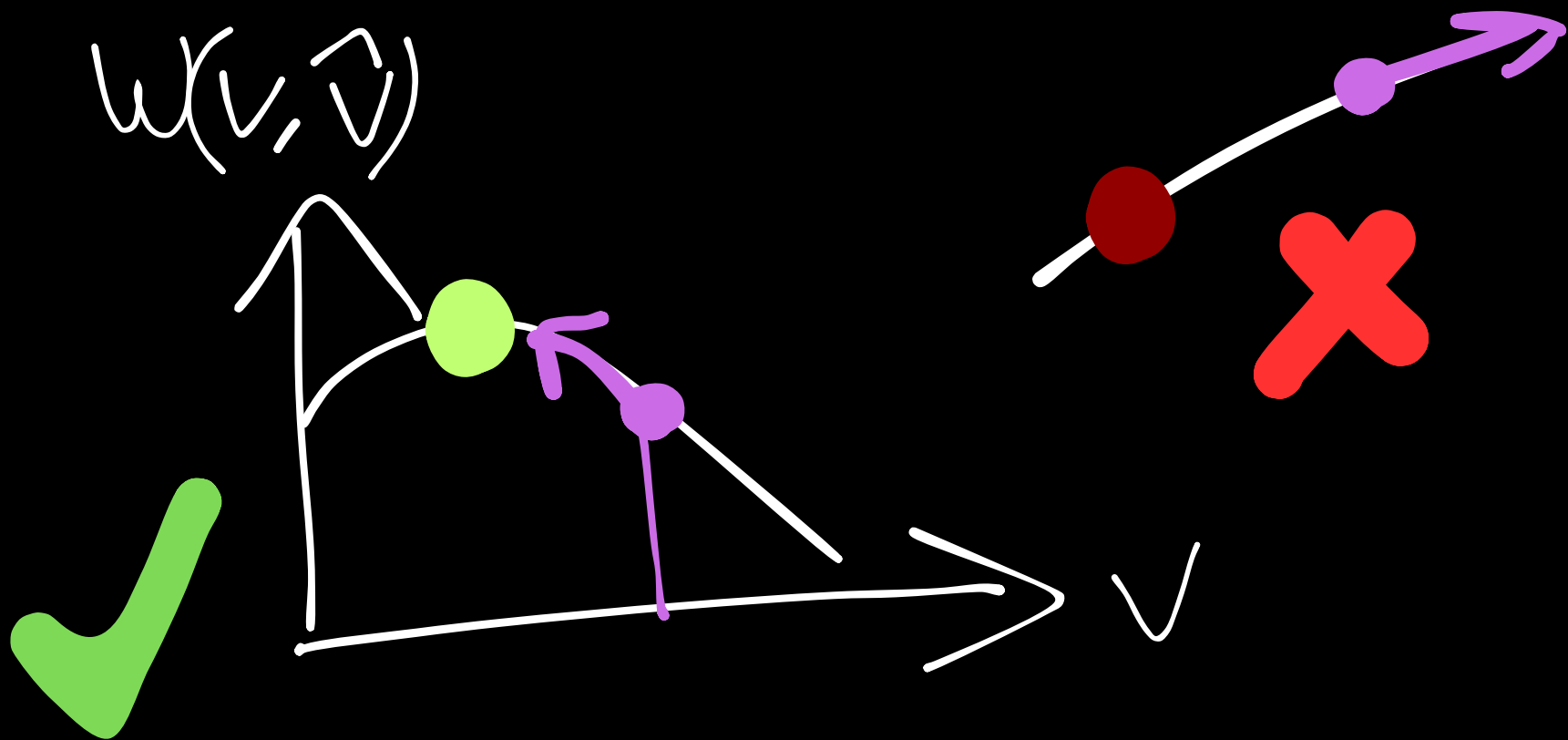
selection gradient



$$G(v^*) = 0$$

$$\left. \frac{\partial G}{\partial \hat{v}} \right|_{\hat{v} = v^*} < 0$$

convergence stability



$$\left. \frac{\partial^2 w}{\partial v^2} \right|_{v = \hat{v} = v^*} < 0$$

evolutionary stability

