

# Cosmotrips

In the year **3025**, *Intergalactic Miller Agency* maintains two gigantic networks of corridors:

- **Network A** – the ancient “**Gates of Silk**” discovered by humanity’s first pioneers.
- **Network B** – the brand-new “**Nebula Express**” built by the Cosmic Union.

Each network consists of exactly  $N - 1$  corridors and links all  $N$  planets, which are numbered from 1 to  $N$ . From every planet there is **exactly one** route to every other planet inside one network. Meaning that networks have structure of tree.

Both structures connect exactly the same  $N$  planets, but their corridors are *weighted*: the weight of a corridor is its **safety rating** – the lower the safer.

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For two planets  $u, v$  let

- $g(u, v)$  be the risk of fly from  $u$  to  $v$ . The risk of fly from  $u$  to  $v$  is defined as the **maximum weight** of all corridors on the unique route from  $u$  to  $v$  inside **Network A**
- $f(u, v)$  be the same quantity inside **Network B**

Thus  $g$  (respectively  $f$ ) is the worst corridor you must traverse inside Network A (respectively Network B). Remember that  $g(x, x) = f(x, x) = 0$  for any  $x$ .

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During a cargo mission commander **Nazarbek** needs to reach planet  $y$  from planet  $x$ . To finish his mission, he does the following:

1. He picks **any** planet  $z$ ;
2. Flies from  $x$  to  $z$  inside **Network A** (having  $g(x, z)$  risk);
3. Makes “*Hyper-jump*” to the **Network B** (instant, risk-free);
4. Continues trip from  $z$  to  $y$  inside **Network B** (having  $f(z, y)$  risk).

Total risk of trip using stopover  $z$  is  $\text{risk}(x, y, z) = \max(g(x, z), f(z, y))$

Nazarbek, being cautious, chooses the best stopover  $z$ :

$$\text{minrisk}(x, y) = \min_{1 \leq z \leq N} \text{risk}(x, y, z)$$

Given  $Q$  such missions, output every  $\text{minrisk}(x_i, y_i)$

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## Input

The first line contains an integer  $T$  — the number of test cases.

Each test case starts with a line containing two integers  $N$  and  $Q$  — the number of planets and the number of queries.

The next  $N - 1$  lines describe **Network A**. The  $i$ -th of these lines contains three integers  $u_i, v_i, w_i$  — the indices of two planets connected by a corridor and its safety rating.

The following  $N - 1$  lines describe **Network B** in the same format:  $a_i, b_i, c_i$ .

Finally,  $Q$  lines follow. The  $j$ -th line contains two integers  $x_j, y_j$  — the endpoint planets of the  $j$ -th mission query.

## Constraints

- $2 \leq N, Q \leq 2 \cdot 10^5$
- $0 \leq w_i, c_i \leq N$
- $1 \leq x_i, y_i \leq N$
- It is guaranteed that the two sets of  $N - 1$  edges each form trees on  $N$  vertices

## Subtasks

1. **(6 points)**  $N, Q \leq 500$  and each network forms a **path** (every planet has degree  $\leq 2$ )
  2. **(9 points)**  $N, Q \leq 5,000$  and each network forms a **path**
  3. **(21 points)** Each network forms a **path**
  4. **(8 points)**  $N, Q \leq 500$
  5. **(11 points)**  $N, Q \leq 5,000$
  6. **(45 points)** No additional constraints
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## Output

For each query print a single integer from a new line –  $\text{minrisk}(x_i, y_i)$ .

## Examples

### Example 1

#### Input

```
2
6 3
4 5 3
4 3 6
4 2 2
3 1 5
3 6 4
5 2 6
5 6 5
6 1 4
6 4 3
4 3 2
4 5
1 5
6 5
5 4
1 2 2
2 3 3
3 4 5
4 5 4
1 2 2
2 3 3
3 4 4
4 5 5
1 5
4 2
1 2
3 5
```

## Output

```
3
5
5
5
4
2
5
```