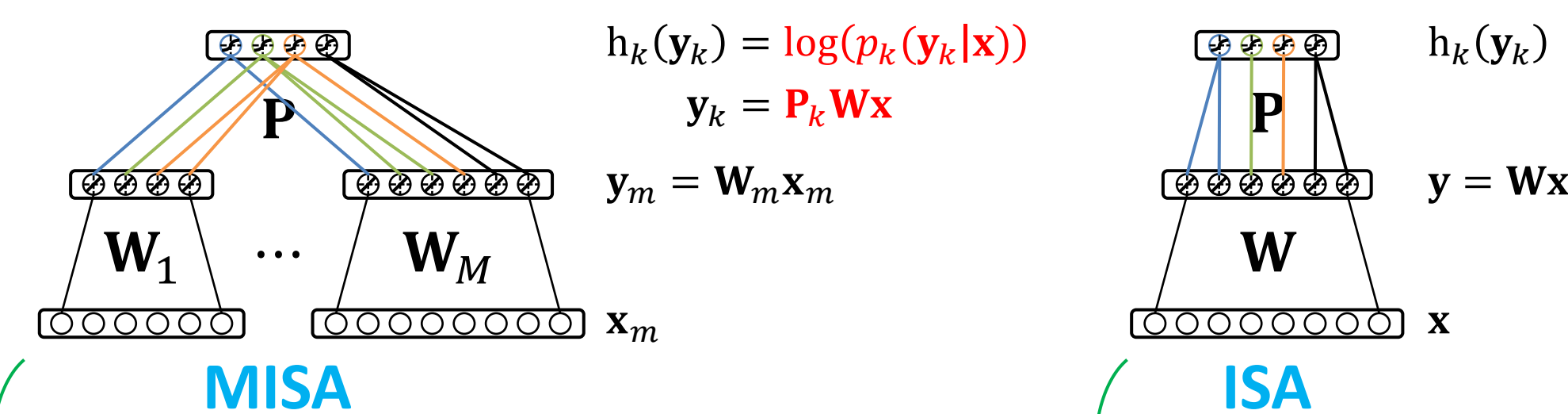


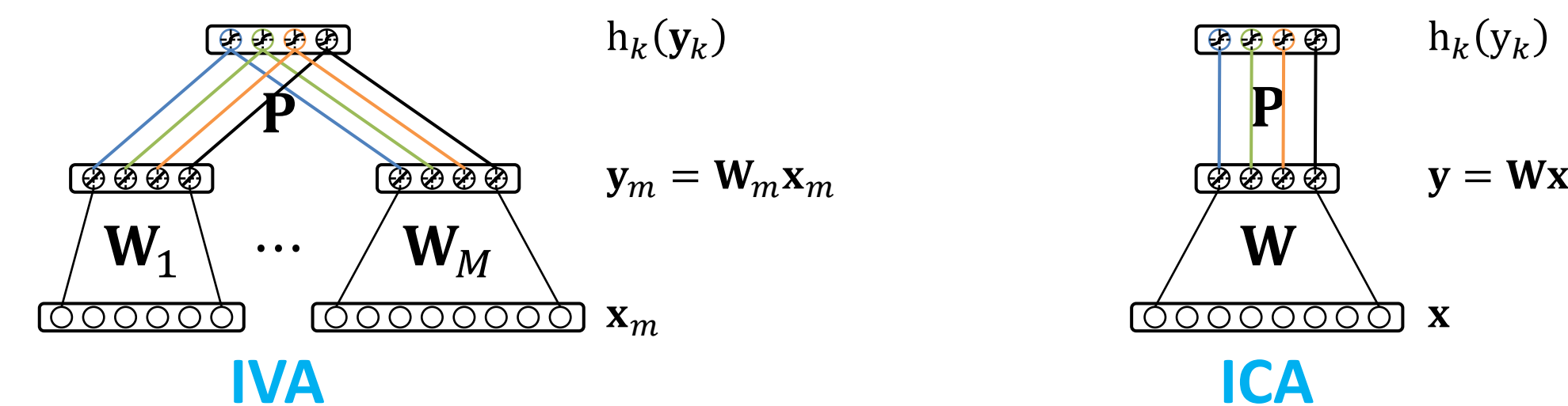
MISA: A Generalized Model for Independent Features

$$J(\mathbf{W}) = KL(p(\mathbf{y}), \prod_k^K p_k(\mathbf{y}_k|\mathbf{x})), \mathbf{W} = \text{blkdiag}(\mathbf{W}_m), \mathbf{x} = [\mathbf{x}_1^T \dots \mathbf{x}_M^T]^T$$

$$J(\mathbf{W}) = -\sum_m^M \sum_i^{C_m} \log|\sigma_{mi}| - \sum_k^K \mathbb{E}[h_k(\mathbf{y}_k)] \quad \rightarrow \quad J(\mathbf{W}) = -\sum_i^C \log|\sigma_i| - \sum_k^K \mathbb{E}[h_k(\mathbf{y}_k)]$$



$$J(\mathbf{W}) = -\sum_m^M \sum_i^{C_m=K} \log|\sigma_{mi}| - \sum_k^K \mathbb{E}[h_k(\mathbf{y}_k)]$$



ICA: Independent Component Analysis ISA: Indep. Subspace Analysis [2,3] IVA: Independent Vector Analysis [4]

Regularization: Modified Linear Autoencoder

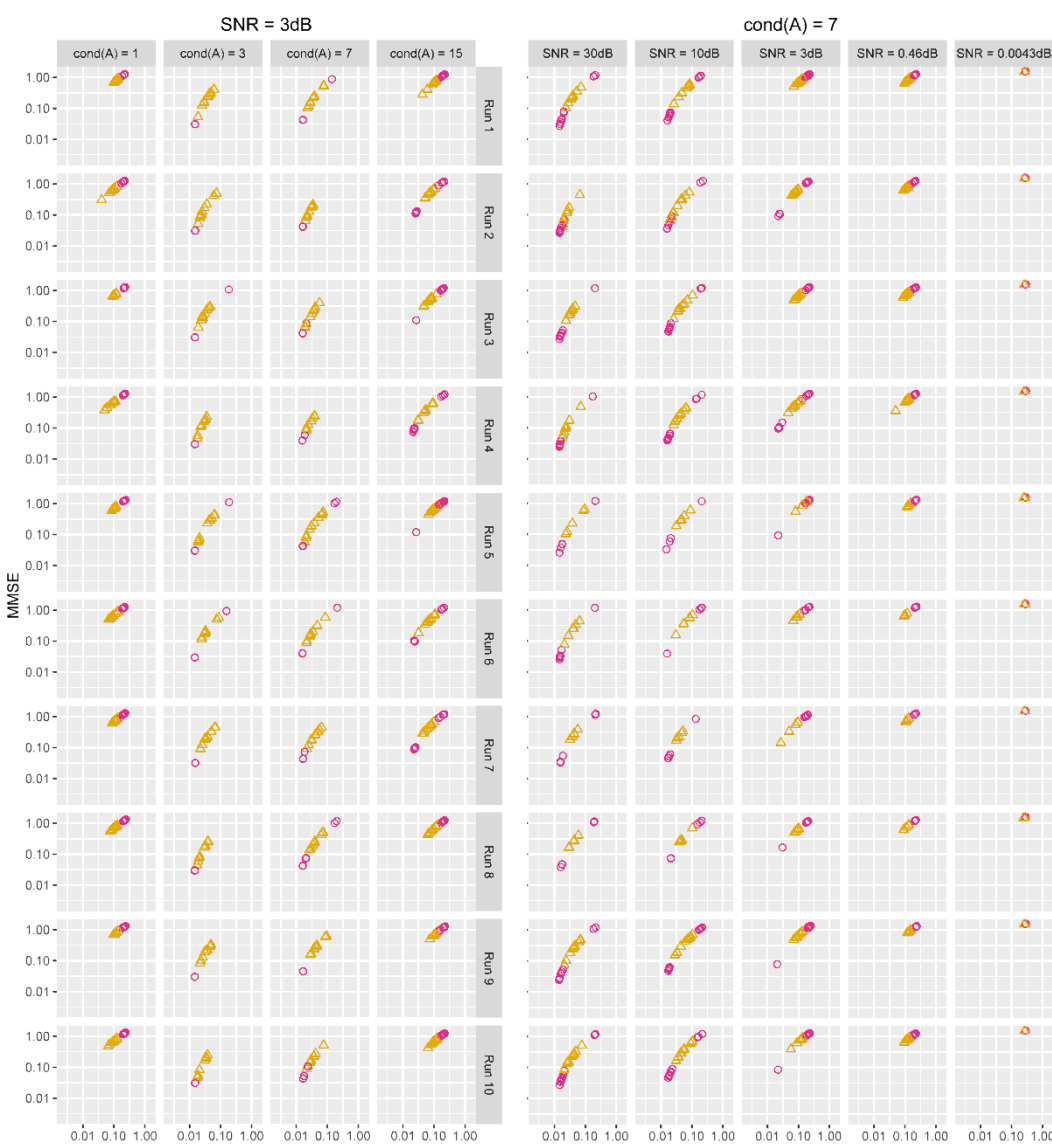
- Assuming white data \mathbf{z} , Le et al. [1] regularized ICA with a simple linear autoencoder $\hat{\mathbf{z}} = \mathbf{W}^T \mathbf{W} \mathbf{z}$.
- Simultaneously estimate the reduced space while learning statistically independent hidden units.
- Modified linear autoencoder for non-white data: $\hat{\mathbf{x}} = \mathbf{W}^+ \mathbf{W} \mathbf{x}$. Applied to all modalities as a **non-linear constraint**.

$$R(\mathbf{W}) = \|\mathbf{W}^+ \mathbf{W} \mathbf{x} - \mathbf{x}\|_2^2$$

Synthetic Data

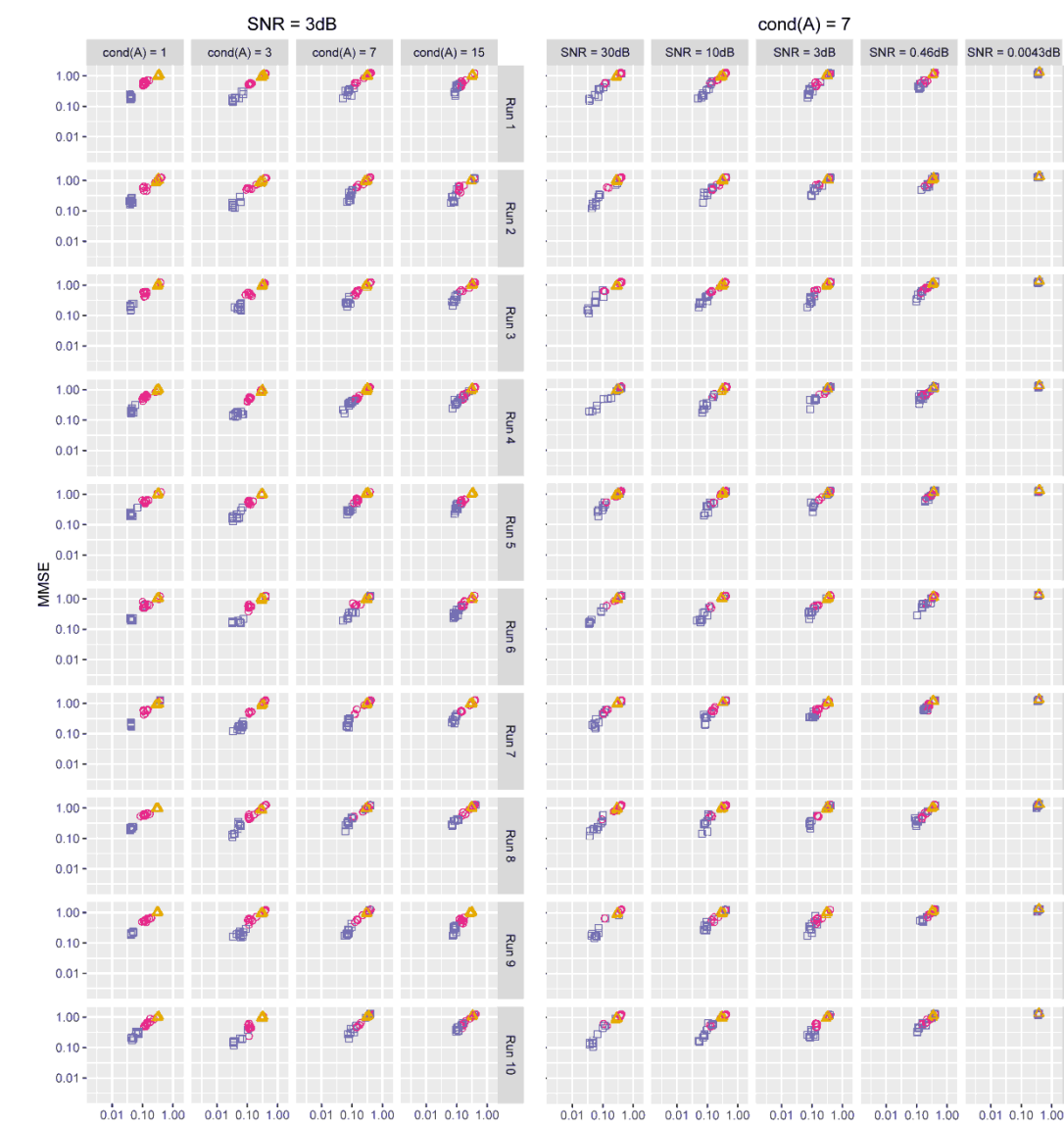
ICA

- M = 1 dataset
- C = 75 hidden units into K = 75 one-dimensional subspaces
- N = 3500 examples sampled from a Laplace distribution
- Each run a new, unique (V × C) rectangular mixing matrix A (V = 8000)
- Initialized with ten different random row-orthogonal W0



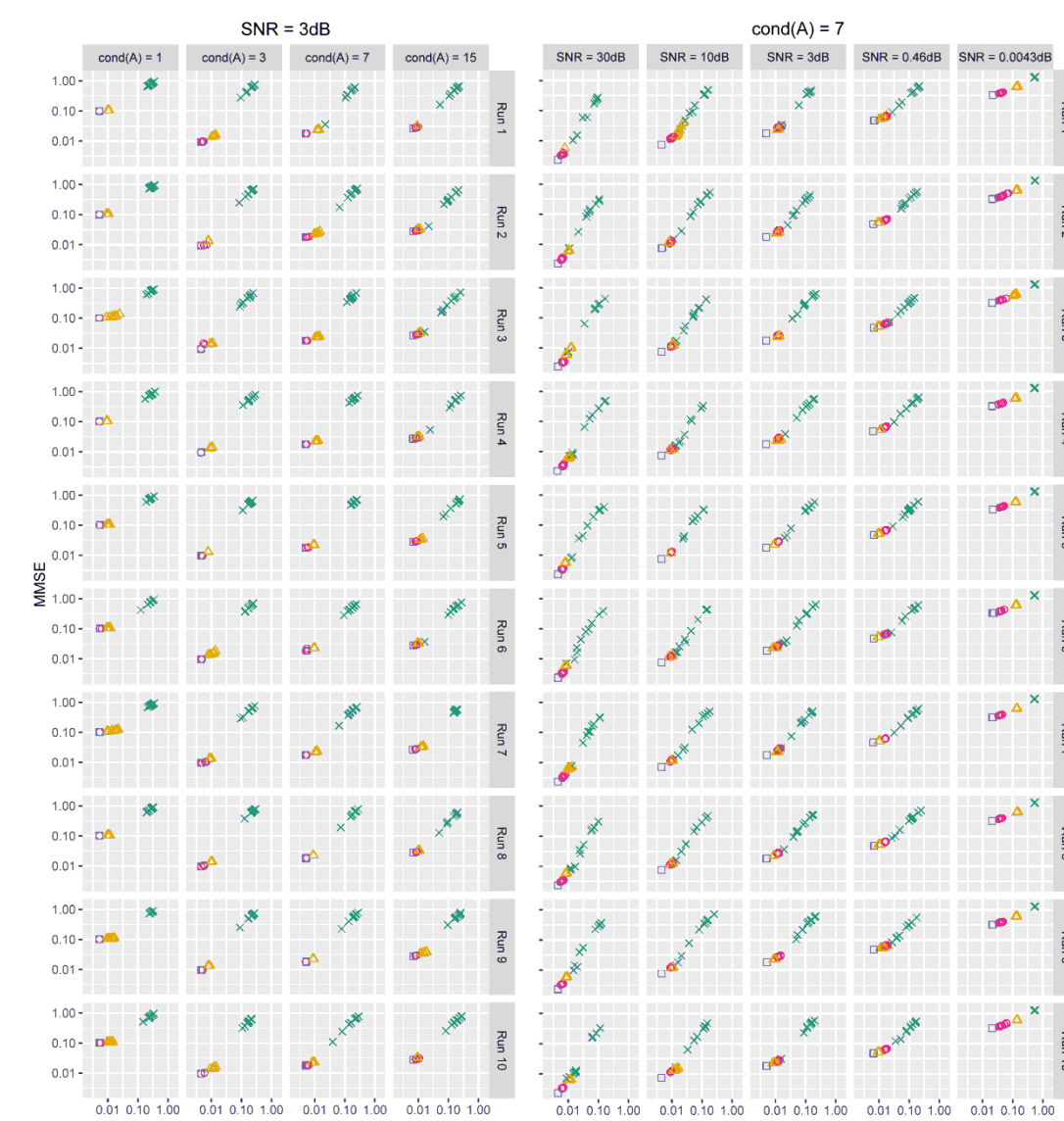
ISA

- M = 1 Dataset
- C = 51 hidden units
- K = 18 d_k -dimensional subspaces, $d_k = [1.5; 5.1; 1.5; 2; 2; 2]$
- N = 5250 examples sampled from a Multivariate Laplace Distribution
- Each run a new, unique (V × C) rectangular mixing matrix A (V = 8000)
- Initialized with ten different random row-orthogonal W0



IVA

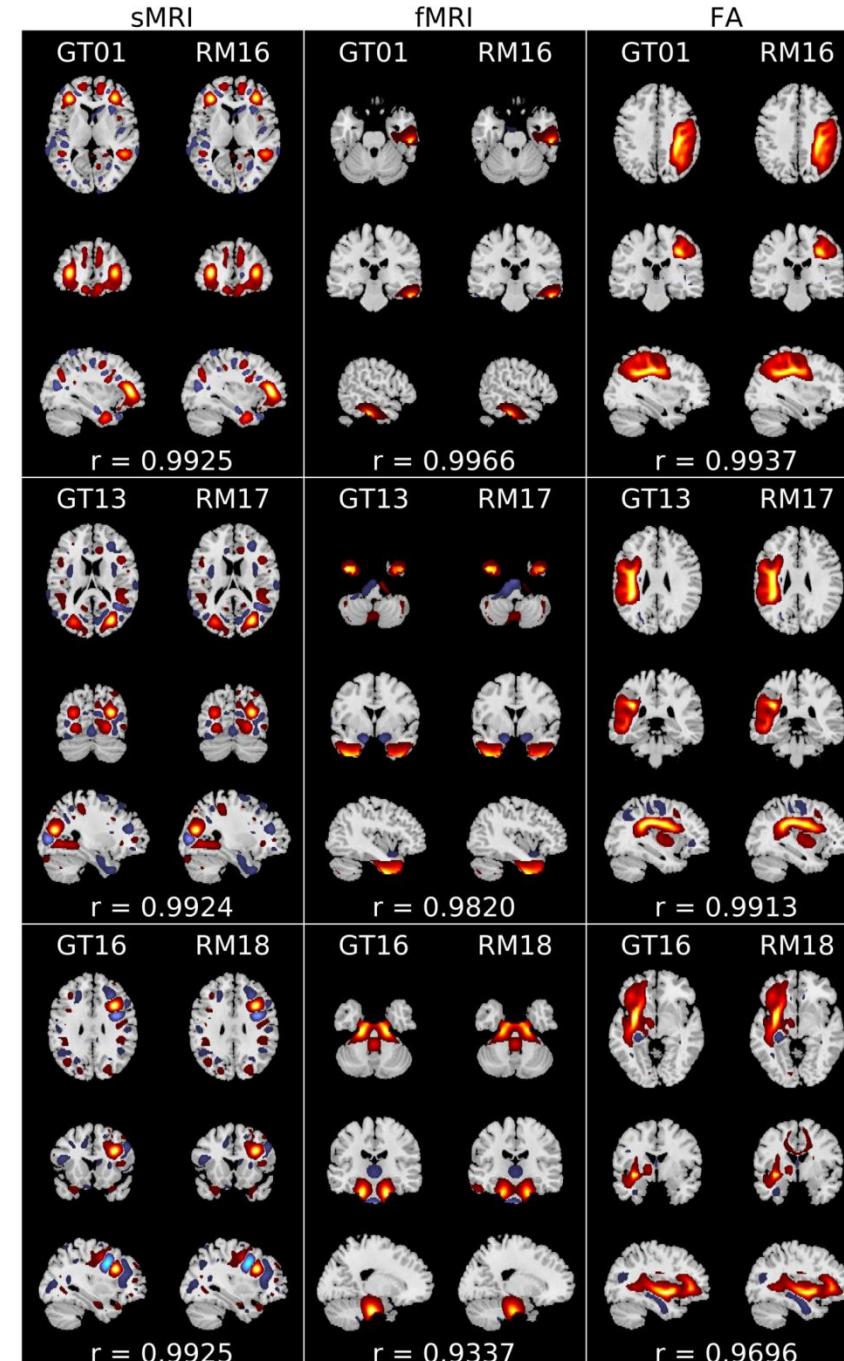
- M = 16 datasets
- C = 75 hidden units into K = 75 sixteen-dimensional subspaces
- N = 66000 examples sampled from a Multivariate Laplace Distribution
- Each run a new, unique (V × C) rectangular mixing matrix A (V = 250)
- Initialized with ten different random row-orthogonal W0



Greedy Combinatorial Optimizer

- ISA & MISA: local minima due to incorrect assignment of hidden units.
- Greedy combinatorial optimizer moves the solution out of the local minimum.

- M = 16 datasets
- sMRI: V ≈ 300K voxels, fMRI: V ≈ 67K voxels, FA: V ≈ 15K voxels
- Mixing matrices A_m are the "real" part of the datasets
- condition numbers: 1.52, 4.59, 1.63
- C = 20 hidden units into K = 20 three-dimensional subspaces
- N = 600 examples sampled from a Gaussian copula
- Additive Gaussian sensor noise: SNR = 3dB

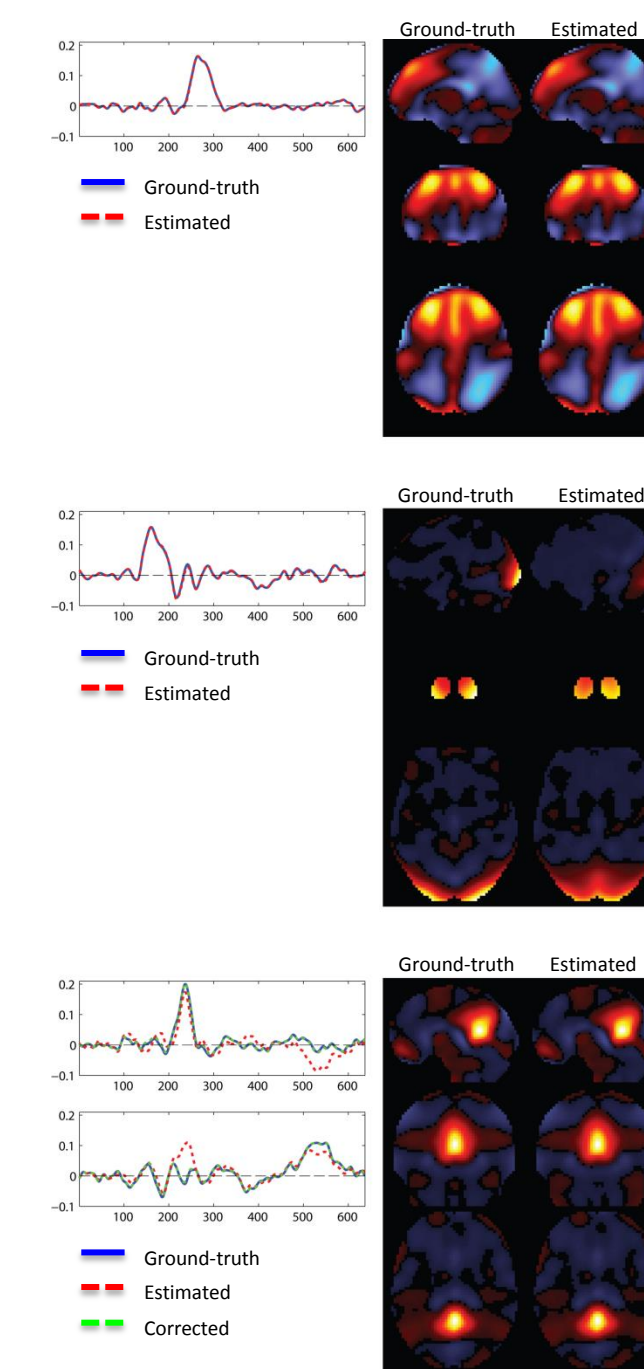


IVA

Excellent performance on realistic data settings.

MISA with rectangular, orthogonal mixing:

- 2 Datasets, hybrid simulation
- Simulated Components (1001 subjects):
- 4 in dataset 1 (EEG), 3 subspaces
- 6 in dataset 2 (fMRI), 4 subspaces
- Orthogonal Mixing Matrices:
- 630 × 4 (EEG) and 66000 × 6 (fMRI)



MISA + modified autoencoder (RE) yields good performance despite small training sets.
ISA & MISA + GP: Greedy combinatorial optimizer significantly improves performance.

What's Next?

- Explore deep non-linear models before subspace formation to identify optimal modality-specific depth.
- Learn the strictly sparse Subspace Assignment Matrix \mathbf{P} automatically.
- Modality-specific architectures such as RNNs with hidden independent subspaces for modalities with sequential data

References:

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- [2] J.-F. Cardoso (1998). "Multidimensional independent component analysis," in Proc IEEE ICASSP 1998, vol. 4, Seattle, WA, pp. 1941-1944.
- [3] A. Hyvärinen and U. Köster (2006). "FastISA: A fast fixed-point algorithm for independent

subspace analysis," in Proc ESANN 2006, Bruges, Belgium, pp. 371-376.

[4] T. Kim, T. Eltoft, and T.-W. Lee (2006). Independent vector analysis: An extension of ICA to multivariate components. In Proc ICA 2006, LNCS (Vol. 3889, pp. 165-172). Charleston, SC

[5] R. Silva, S. Plis, T. Adalı, and V. Calhoun (2014). "Multidataset independent subspace analysis extends independent vector analysis," in Proc IEEE ICIP 2014, Paris, France, pp. 2864-2868.

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[6] R. Silva, S. Plis, J. Sui, M. Pattichis, T. Adalı, and V. Calhoun (2016). "Blind source separation for unimodal and multimodal brain networks: A unifying framework for subspace modeling," IEEE J Sel Topics Signal Process, 10 (7), 1134-1149.